

Phenomenology of Flavoured Dark Matter in Dark Minimal Flavour Violation

KSETA Plenary Workshop, Durbach

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 - Constraints from Relic Abundance of Dark Matter
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Dark Matter Evidence

- 1933: Virial theorem $2T = -U$ applied to coma cluster.

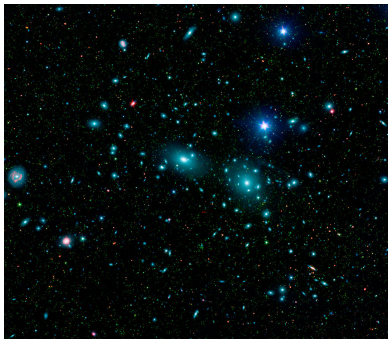


Figure : Coma cluster.

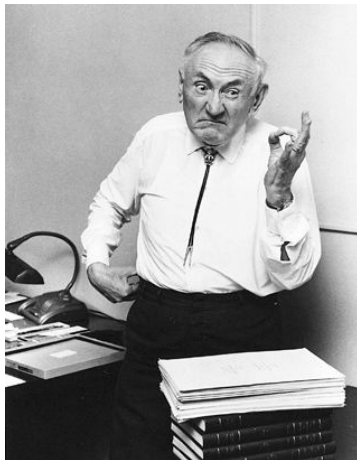


Figure : Fritz Zwicky.

Dark Matter Evidence

- 1970's: Rotation curves of stars in galaxies.



Figure : Vera Rubin.

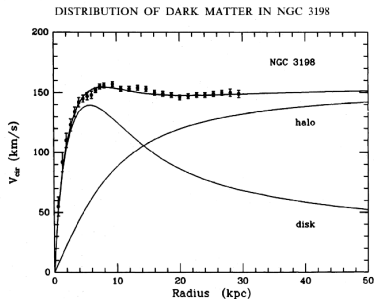


Figure : Rotation curve data vs. predictions.

Dark Matter Evidence

- After recombination baryonic structure formation profits from preexisting dense DM regions
⇒ galaxy formation possible in age of the Universe.

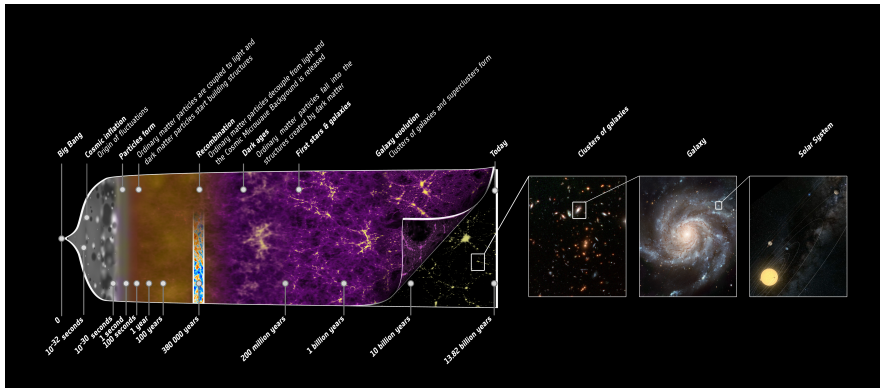


Figure : History of the Universe.

Dark Matter Evidence

- Gravitational lensing effects → Bullet Cluster. Misalignment of visible and gravitational mass distribution.

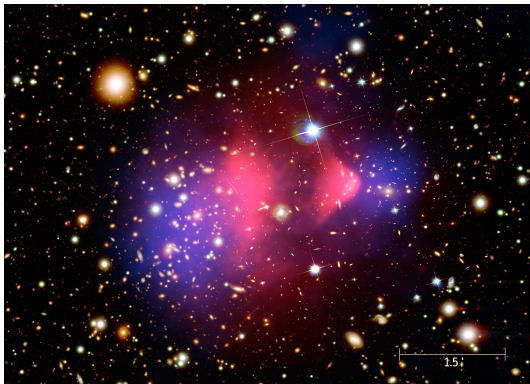


Figure : Bullet cluster. Visible matter distribution (red) and dark matter distribution (blue).

Dark Matter Evidence

- Imprints in Cosmic Microwave Background (CMB).

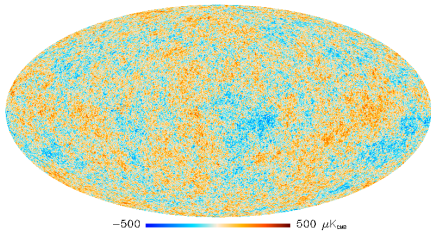


Figure : Temperature fluctuations in CMB (Planck 2013).

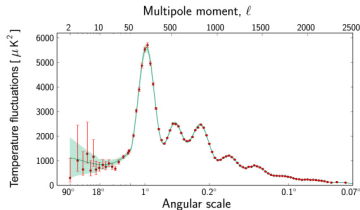


Figure : CMB power spectrum (Planck 2013).

Approaches to identify Dark Matter

- Extension of SM motivated by a new idea solving several problems (e.g. SUSY, Axions).
- Study of all kind of higher dimensional effective SM-DM interactions in Effective Field Theory (EFT).
- **Simplified models:** Study phenomenology of specific interactions with limited number of parameters.

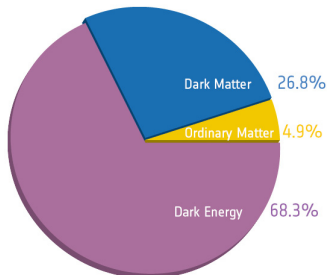


Figure : Energy distribution of the Universe (Planck 2015).

The Flavour Gate to Dark Matter

Assume an analogy to the SM fermions \rightarrow dark flavour triplet $\begin{pmatrix} \chi_u \\ \chi_c \\ \chi_t \end{pmatrix}$.

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Flavoured Dark Matter coupling to SM right-handed up-quark triplet:

- DM flavour triplet χ_j , Dirac fermion, SM gauge singlet.
- Heavy scalar mediator ϕ , carrying colour and hypercharge.
- Lagrangian has unbroken \mathbb{Z}_3 symmetry and hence yields stability of DM χ (for $m_\phi > m_\chi$).

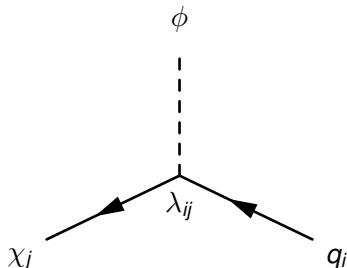


Figure : New physics interaction (basic vertex).

[Agrawal, Blanke, Gemmler '14]

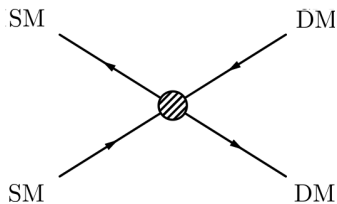
Minimal Flavour Violation:

- Standard approach.
- Structure of λ_{ij} simple and completely determined by SM Yukawa couplings.
- Limited number of free parameters left in model.
- Easier to analyze limited phenomenology.

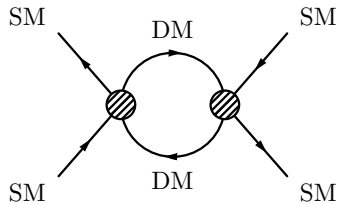
Dark Minimal Flavour Violation:

- Novel approach.
- Structure of λ_{ij} left general and as a new source of flavour and CP violating effects.
- Extended number of free parameters from coupling: 3 “couplings” $D_{\lambda,ij}$, 3 “mixing angles” θ_{ij} , 3 “phases” δ_{ij} .
- More complicated but also more interesting phenomenology.

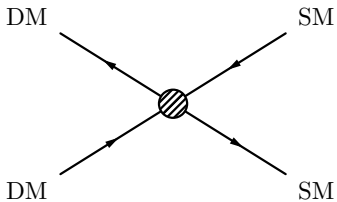
How to Detect Flavoured Dark Matter?



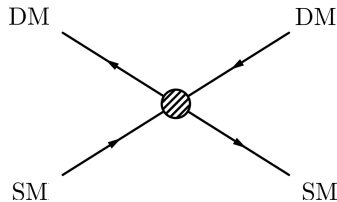
collider searches



precision flavour data



indirect detection / freeze-out



direct detection

Constraints from Colliders

- Study the process
 $pp \rightarrow \phi\phi^\dagger \rightarrow q\bar{q}\chi\bar{\chi}$.
- Depending on decay product of ϕ we detect either a top-signature or a jet (+ \cancel{E}_T).
- Inspiration from SUSY searches at LHC [ATLAS collaboration '14].
 \Rightarrow Upper bounds on CS of both $t\bar{t}$ and dijet signals.
- Those constraints translate to lower bound on mediator mass and upper bound on “couplings”.

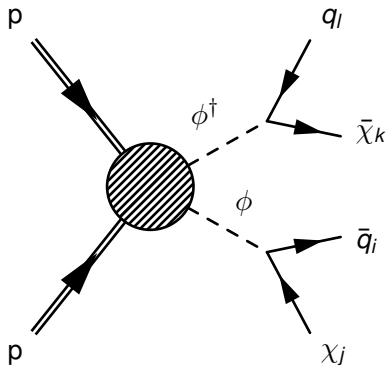


Figure : Studied LHC DM production processes.

Constraints from Flavour Precision Data

- No mesons with top-quark are possible, the only constraints come from D-mesons.

⇒ not too strong

- The NP contribution has to be smaller than experimental bounds [UTfit collaboration '14].

- Mixing angles are associated with CP violation phases.

⇒ get constrained

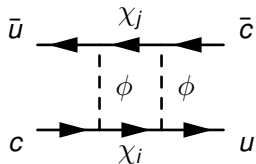


Figure : NP contr. to neutral D-meson mixing.

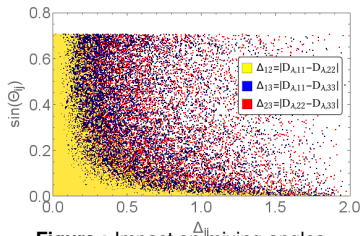


Figure : Impact on mixing angles.

DM Constraints from Observed Relic Abundance

- Assume DM abundance as a thermal relic.
 - ⇒ SM matter and DM used to be in thermal equilibrium in early universe.
 - ⇒ Same order of magnitude for energy content.
- Freeze-out: annihilation rate VS expansion.
 - ⇒ Remaining relic DM depends on speed of annihilation, i.e. on the cross section

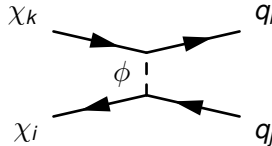


Figure : Annihilation of DM flavours.

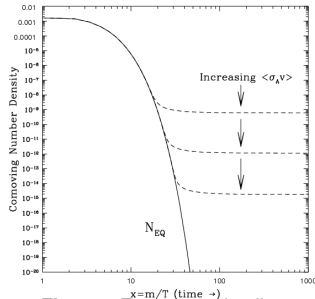


Figure : Freeze-out timeline.

- Annihilation cross section needs to have just the right value (in tolerance interval)
[Steigman, Dasgupta, Beacom '12]
to produce the observed relic DM.

$$\langle \sigma v \rangle_{eff} \approx \lambda^4 \frac{m_\chi^2}{m_\phi^4}$$

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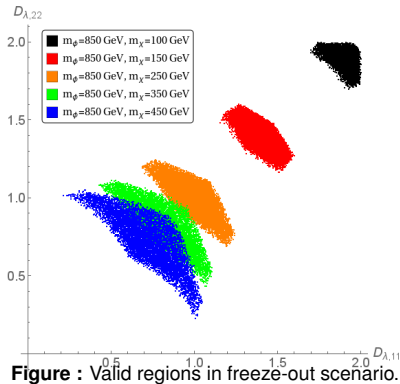


Figure : Valid regions in freeze-out scenario.

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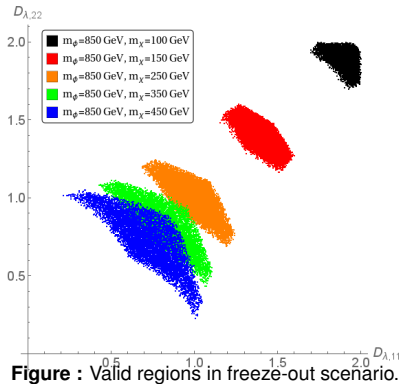


Figure : Valid regions in freeze-out scenario.

- Actual form of CS more complicated and dependent on several criteria.

Constraints from Direct Detection Experiments

- Foremost liquid Xenon experiments.
- Current best bounds from LUX data [LUX collaboration '16].
- Several future experiments in pursuit.



Figure : Xenon chamber of LUX experiment.

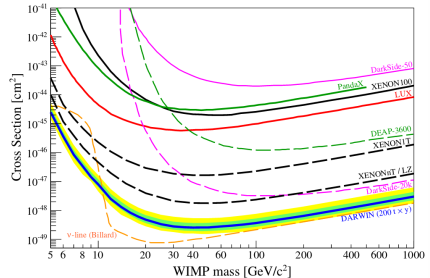
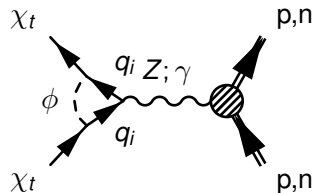
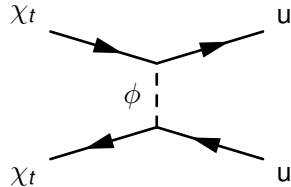
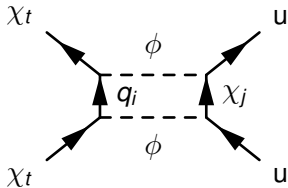


Figure : Bounds of current and future direct detection experiments.

Constraints from Direct Detection Experiments

Many contributions to total WIMP-nucleon cross section:

$$\sigma_n^{SI} = \frac{\mu_n^2}{\pi A^2} |Zf_p + (A - Z)f_n|^2.$$



Constraints from Direct Detection Experiments



Figure : Cancellation of tree-level and neutron Z-penguin contributions (symbolic).

- Cancellation forces mixing angle.
- Xenon has several stable isotopes.
⇒ Simultaneous suppression.
- Future bounds exclude high couplings.

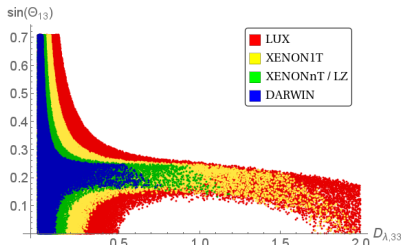


Figure : Valid mixing angle vs coupling.

Results of Combined Analysis

- Interplay of different constraints.
 - For given m_χ and m_ϕ relic abundance constraints will determine coupling strength.
 - Upper bound of possible coupling strength from direct detection constraints
- ⇒ Lower bound on DM mass from the combination (in dependence of mediator mass)

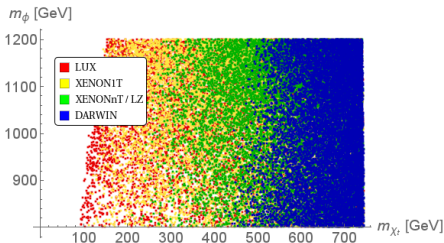


Figure : Valid regions for different strengths of direct detection constraints.

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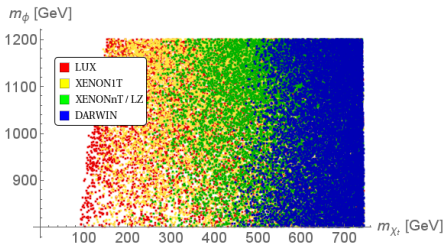


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Many more interesting details and other effects.

- Simplified model of flavoured dark matter.
- Leave coupling general (Dark Minimal Flavour Violation).
- Demanding phenomenologically interesting DM mass in combination with constraints also has impact on other parameters.
- Interesting interplay of constraints.
- Future direct detection experiments have large impact on parameter-space.

Thank you!

Thank you!

Questions?



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The Flavour Gate to Dark Matter

[Agrawal, Blanke, Gemmler '14]

Assume an analogy to the SM fermions \rightarrow dark flavour triplet χ_i .

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Flavoured Dark Matter coupling to SM right-handed up-quark triplet:

$$\mathcal{L}_{\text{NP,int}} = -\lambda_{ij} \bar{u}_{Ri} \chi_j \phi + h.c.$$

$$\mathcal{L}_{\text{NP,mass}} = -m_\phi \phi^\dagger \phi - m_\chi \bar{\chi} \chi$$

- DM flavour triplet χ_j , Dirac fermion, SM gauge singlet.
- Heavy scalar mediator ϕ , carrying colour and hypercharge.
- Lagrangian has unbroken \mathbb{Z}_3 symmetry and hence yields stability of DM χ (for $m_\phi > m_\chi$).

Dark Minimal Flavour Violation

[Agrawal, Blanke, Gemmler '14]

Flavour Symmetry

$$U(3)_u \times U(3)_d \times U(3)_q \times U(3)_\chi$$

is only broken by SM Yukawa couplings and the **DM-quark coupling** λ_{ij} (Dark Minimal Flavour Violation).

⇒ Beyond Minimal Flavour Violation.

⇒ only DM mass splitting comes from RG running:

$$m_{ij} = m_\chi (\mathbb{1} + \eta \lambda^\dagger \lambda + \dots)_{ij} = m_\chi (1 + \eta (D_{\lambda,ij})^2 + \dots) \delta_{ij}.$$

- η depends on the full theory → has to be a parameter of the simplified model.
- flavour with lowest mass is our DM candidate.
→ we choose the “top-flavour”. [Kilic, Klimek, Yu '15]

Dark Minimal Flavour Violation (DMFV): λ_{ij} is a general 3×3 coupling matrix \rightarrow 9 real parameters and 9 complex phases.

- Can be split up as (bilinear diagonalization):

$$\lambda = U^\lambda D_\lambda V^\lambda$$

with unitary matrices U^λ , V^λ and diagonal real matrix D_λ .

- Use redundancy to eliminate 3 phases in U^λ .
- Use flavour symmetry in dark sector $U(3)_\chi$ to get rid of V^λ

After using all the symmetries at our disposal λ has 9 parameters left and can be parametrized as:

$$\lambda = U_{23}^\lambda U_{13}^\lambda U_{12}^\lambda D_\lambda$$

[ATLAS collaboration '14]

- Study the process
 $pp \rightarrow \phi\phi^\dagger \rightarrow q\bar{q}\chi\bar{\chi}$.
- Depending on decay product of ϕ we detect either a top-signature or a jet (+ \cancel{E}_T).
- Inspiration from SUSY searches at LHC
 \Rightarrow Upper bounds on CS of both $t\bar{t}$ and dijet signals.

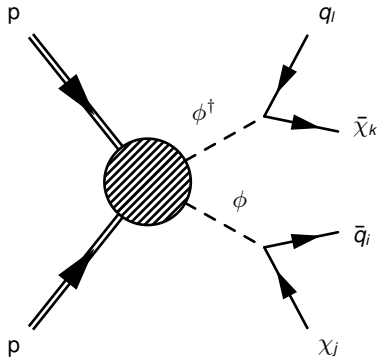
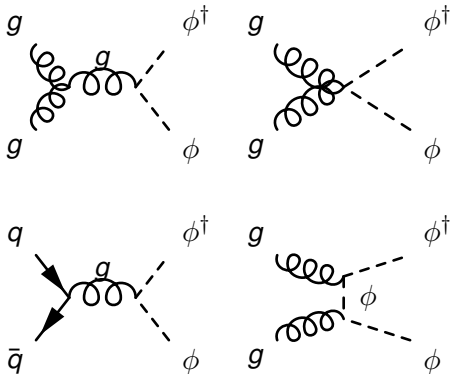


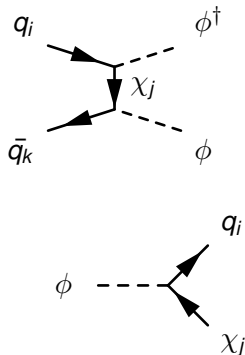
Figure : Studied LHC DM production processes.

Constraints from SUSY Searches at LHC

Involved QCD processes



Involved NP processes



References

- $D_{\lambda,33}$ increased
→ BR of decay goes up.
- $D_{\lambda,11}, D_{\lambda,22}$ increased
→ BR of decay goes down.
- **BUT:** For high $D_{\lambda,11} = D_{\lambda,22}$ we observe increasing excluded areas.

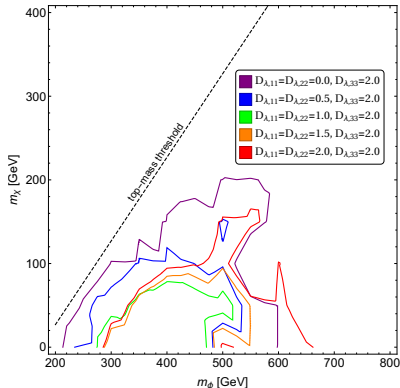


Figure : Exclusion plot for $t\bar{t}$ final state, mixing angles set to zero.

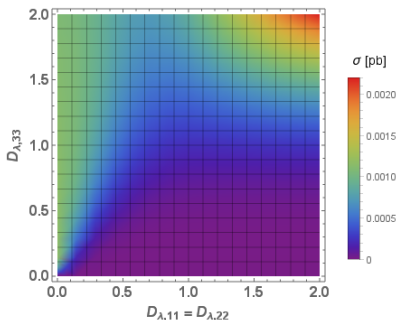


Figure : Cross section of $t\bar{t}$ final state for $m_\phi = 850$ GeV and $m_\chi = 50$ GeV, mixing angles set to zero.

Explanation: NP production

- Major contribution to total production (for high $D_{\lambda,11}$, $D_{\lambda,22}$)
- This effect can make up for drop in BR
- $D_{\lambda,33}$ not relevant, since the protons do not contain top
- Very high couplings can lead to serious exclusion areas.

Constraints from dijet + \cancel{E}_T Searches at LHC

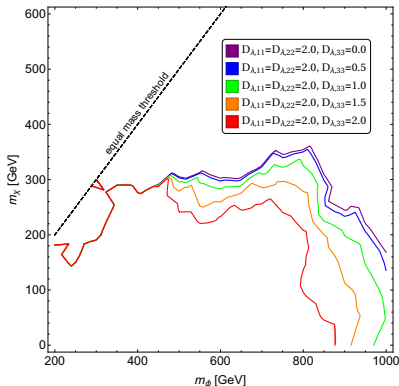


Figure : Exclusion plot for dijet final state, mixing angles set to zero.

- Stronger exclusion bounds on model.
- The phenomenologically interesting region is $m_\chi \leq 1$ TeV.
- Too large couplings $D_{\lambda,ii}$ would exclude nearly all of parameter space.
- Most serious constraints come from dijet final state.

⇒ Safe parameter-space:

$$m_\phi \geq 850 \text{ GeV}$$

$$2.0 \geq D_{\lambda,33} \geq D_{\lambda,22}, D_{\lambda,11}$$

- Mixing angles shift influences between couplings $D_{\lambda,ii}$.
⇒ For big splitting in the couplings, mixing angles can cause big shifts in cross sections.
 - For our choice of m_ϕ bounds from $t\bar{t}$ final state cause no constraints.
 - Worst allowed case for dijet final state, in our safe parameter-space, is $D_{\lambda,11} = D_{\lambda,22} = D_{\lambda,33} = 2.0$
⇒ Unchanged by mixing angles.
- ⇒ Mixing angles can cause no problem with this choice of safe parameter-space.

[UTfit collaboration '14]

- No mesons with top-quark are possible, the only constraints come from D-mesons.
 ⇒ not too strong
- The NP contribution has to be smaller than experimental bounds.

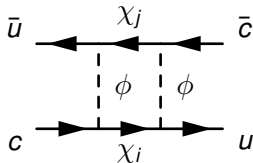


Figure : NP contr. to neutral D-meson mixing.

$$\begin{aligned}
 M_{12}^{D, NP} &= \frac{1}{2m_D} \langle \bar{D}^0 | \mathcal{H}_{eff}^{\Delta C=2, new} | D^0 \rangle^* \\
 &= \frac{1}{384\pi^2 m_\phi^2} \sum_{i,j} \lambda_{uj}^* \lambda_{cj} \lambda_{ui}^* \lambda_{ci} \cdot L(x_i, x_j) \cdot \eta_D \cdot m_D f_D^2 \hat{B}_D.
 \end{aligned}$$

Flavour Constraints from Neutral Meson Mixing

$$\left((\lambda\lambda^\dagger)_{cu} \right)^2 = \left((U_\lambda D_\lambda D_\lambda^\dagger U_\lambda^\dagger)_{cu} \right)^2$$

- For degeneracy

$D_{\lambda,11} = D_{\lambda,22} = D_{\lambda,33}$ the mixing matrices U_{ij}^λ will drop out.

- The higher the splitting

$\Delta_{ij} = D_{\lambda,ii} - D_{\lambda,jj}$, the more we will see the constraints on the mixing angle θ_{ij} .

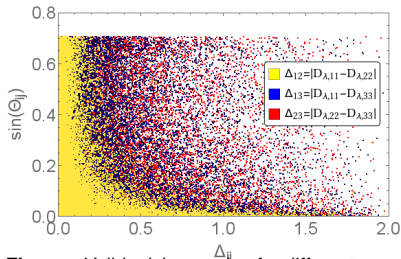


Figure : Valid mixing angles for different coupling splittings. $m_\phi = 850$ GeV and $m_\chi = 250$ GeV.

\Rightarrow Most significant constraints on θ_{12} , other mixings nearly unconstrained.

[Steigman, Dasgupta, Beacom '12]

- Assume DM abundance as a thermal relic, $T_f \propto \frac{m_\chi}{20}$
- Annihilation CS has to be just large enough to produce the correct relic density (we allow for a 10% tolerance interval):

$$\langle \sigma v \rangle_{\text{eff,exp}} = 2.2 \times 10^{-26} \text{cm}^3/\text{s}.$$

\Rightarrow cuts out valid area for $D_{\lambda,ii}$ depending on m_ϕ and m_χ

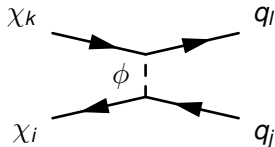


Figure : Annihilation of DM flavours.

$$\langle \sigma v \rangle_{\text{eff}} = \frac{1}{9} \times \frac{3}{256\pi} \sum_{i,j=1,2,3} \sum_{k,l=u,c,t} \lambda_{ki} \lambda_{ki}^* \lambda_{lj} \lambda_{lj}^* \frac{\sqrt{(4m_\chi^2 - (m_k - m_l)^2)(4m_\chi^2 - (m_k + m_l)^2)}}{\left(m_\phi^2 + m_\chi^2 - \frac{m_k^2}{2} - \frac{m_l^2}{2}\right)^2}.$$

- Depending on the mass splitting of the different DM flavours several freeze-out scenarios are possible.

$$m_{ij} = m_\chi (1 + \eta (D_{\lambda,ij})^2 + \dots) \delta_{ij}.$$

- For a DM mass below the top-quark mass this decay channel drops out.

⇒ CS formula and hence impact on parameters can be quite different

- Extreme example: only χ_t present at freeze-out with DM mass below top mass threshold:

$$\langle \sigma v \rangle_{eff} = \frac{3}{256\pi} \sum_{k,l=u,c} \lambda_{k3} \lambda_{k3}^* \lambda_{l3} \lambda_{l3}^* \frac{4m_\chi^2}{(m_\phi^2 + m_\chi^2)^2}.$$

Quasi-Degenerate Freeze-Out (QDF) Szenario

- All DM flavours are present at the freeze-out.
- We require the mass splitting to be less than 1% (significantly smaller than T_f) for this to happen.
- η is free parameter \rightarrow choose it favourable: -0.01.
- This guarantees top-flavoured DM (see direct detection section for motivation).
- Constraint cuts out valid area for $D_{\lambda,ii}$ depending on m_ϕ and m_χ .
- Lower bound on m_χ due to upper limits for $D_{\lambda,ii}$, depending on m_ϕ .

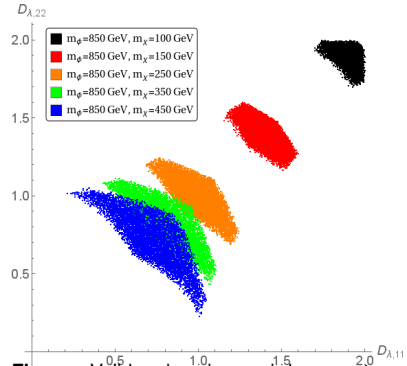


Figure : Valid regions in quasi-degenerate freeze-out scenario.

Single Flavour Freeze-Out (SFF) Szenario

- Only m_χ present at freeze-out.
- We require the mass splitting to be more than 10% (significantly bigger than T_f) for this to happen.
- η is free parameter \rightarrow choose it favourable: -0.075.
- This guarantees top-flavoured DM (see direct detection section for motivation).
- Constraint cuts out valid area of parameters depending on m_ϕ and m_χ , with significant effect on mixing angles.
- In addition to lower bound, we also find an upper bound on m_χ due to upper and lower (from mass splitting condition) limits for $D_{\lambda,ii}$, depending on m_ϕ .

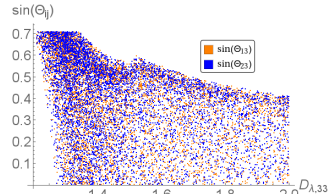


Figure : Valid regions in single flavour freeze-out scenario for $m_\phi = 850$ GeV and $m_\chi = 210$ GeV.

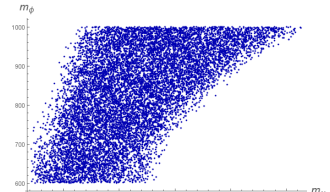
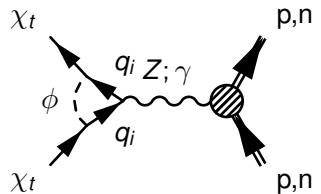
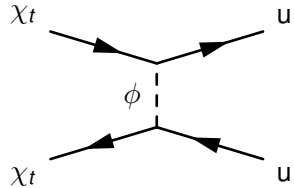
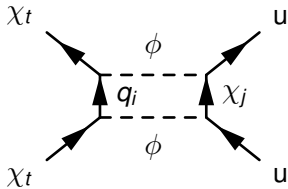


Figure : Mass bounds in single flavour freeze-out scenario.

DM Bounds from Direct Detection Experiments

Many contributions to total WIMP-nucleon cross section:

$$\sigma_n^{SI} = \frac{\mu_n^2}{\pi A^2} |Zf_p + (A - Z)f_n|^2.$$



$$f_p^{tree} = 2f_n^{tree} = \frac{|\lambda_{ut}|^2}{4m_\phi^2}.$$

$$f_p^{box} = 2f_n^{box} = \sum_{i,j} \frac{|\lambda_{ui}|^2 |\lambda_{jt}|^2}{32\pi^2 m_\phi^2} F\left(\frac{m_{q_i}^2}{m_\phi^2}, \frac{m_{\chi_j}^2}{m_\phi^2}\right).$$

$$f_p^{photon} = - \sum_i \frac{|\lambda_{it}|^2 e^2}{48\pi^2 m_\phi^2} \left(\frac{3}{2} + \log\left(\frac{m_{q_i}^2}{m_\phi^2}\right) \right).$$

$$f_p^Z = - \sum_i \frac{3|\lambda_{it}|^2 e^2 \left(\frac{1}{2} - 2\sin^2(\Theta_W)\right)}{32\pi^2 \sin^2(\Theta_W) \cos^2(\Theta_W) m_Z^2} \frac{m_{q_i}^2}{m_\phi^2} \left(1 + \log\left(\frac{m_{q_i}^2}{m_\phi^2}\right) \right).$$

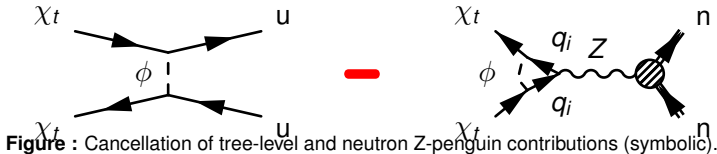
$$f_n^Z = - \sum_i \frac{3|\lambda_{it}|^2 e^2 \left(-\frac{1}{2}\right)}{32\pi^2 \sin^2(\Theta_W) \cos^2(\Theta_W) m_Z^2} \frac{m_{q_i}^2}{m_\phi^2} \left(1 + \log\left(\frac{m_{q_i}^2}{m_\phi^2}\right) \right).$$

DM Bounds from Direct Detection Experiments

[LUX collaboration '15]

- All contributions have to combine to a WIMP-nucleon cross-section below the LUX bounds.
- All contributions are positive, only the Z-penguin with the neutron is negative \Rightarrow saves the day.
- Largest contribution comes from tree-level process. Largest negative term is hence interference term of tree-level and neutron Z-penguin.
- Most important terms, have to nearly cancel each other:

$$A_I \cdot D_{\lambda,33}^4 \cdot \sin(\theta_{13})^4 - A_{II} \cdot D_{\lambda,33}^4 \cdot \sin(\theta_{13})^2 \cdot \cos(\theta_{13})^2 \cdot \cos(\theta_{23})^2$$



- Tree level and neutron Z-penguin have to nearly cancel each other.
⇒ serious constraints on θ_{13}
- For higher couplings the cancellation gets more complicated.
- For too large couplings the cancellation is no longer possible at all
→ excluded.
- Top-flavoured DM is the natural choice:
⇒ Tree-level contribution small
⇒ Neutron Z-penguin contribution large.

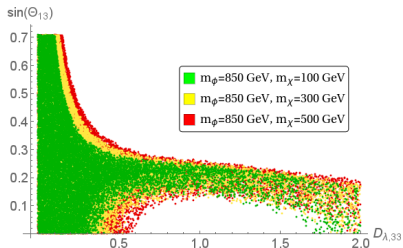


Figure : Valid mixing angle Θ_{13} vs $D_{\lambda,33}$.

Combined Analysis of Constraints (QDF)

Combined application of both flavour, relic abundance and direct detection constraint in quasi-degenerate freeze-out scenario.

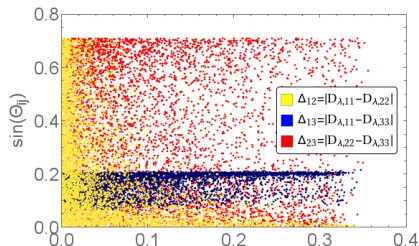


Figure : Valid regions for $m_\phi = 850$ GeV and $m_\chi = 150$ GeV (QDF).

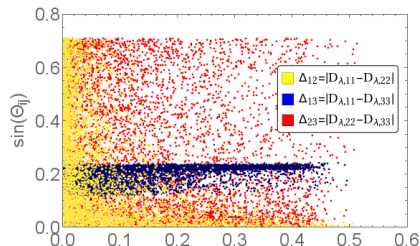
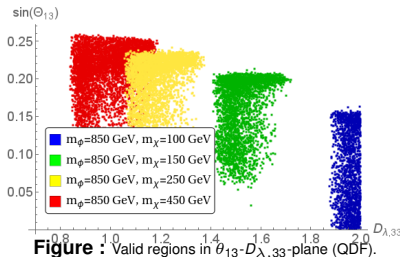


Figure : Valid region for $m_\phi = 850$ GeV and $m_\chi = 250$ GeV (QDF).

- A combination of relic abundance and direct detection constraints confine θ_{13} to a narrow interval.
- The bounds on the DM mass become more serious, since the parameters do not only have to fulfill relic abundance constraints.
- The combined analysis clearly prefers top-flavoured DM.



Combined Analysis of Constraints (SFF)

Combined application of both flavour, relic abundance and direct detection constraint in single flavour freeze-out scenario.

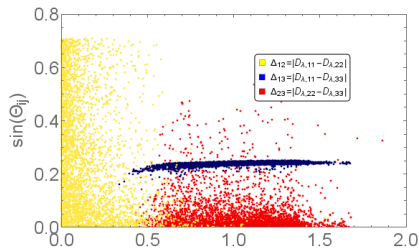


Figure : Valid region for $m_\phi = 850$ GeV and $m_\chi = 225$ GeV (SFF).

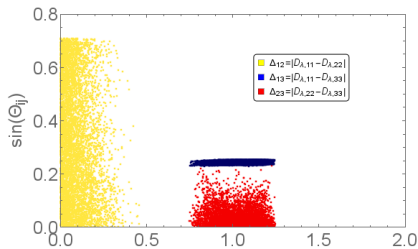


Figure : Valid regions for $m_\phi = 850$ GeV and $m_\chi = 250$ GeV (SFF).

Combined Analysis of Constraints (SFF)

- A combination of relic abundance and direct detection constraints confine θ_{13} to a narrow interval (even more serious than in QDF).
- Especially in SFF the combination of all constraints extremely limits the chance of finding a valid configuration of all parameters for $m_{\chi_t} \leq m_{top}$.
- The combined analysis clearly prefers top-flavoured DM.

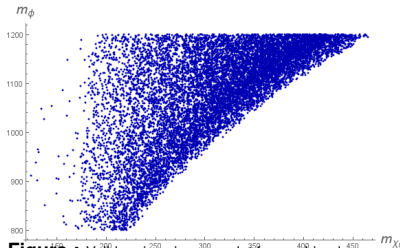


Figure : Valid regions in mass plot for combined constraints (SFF).

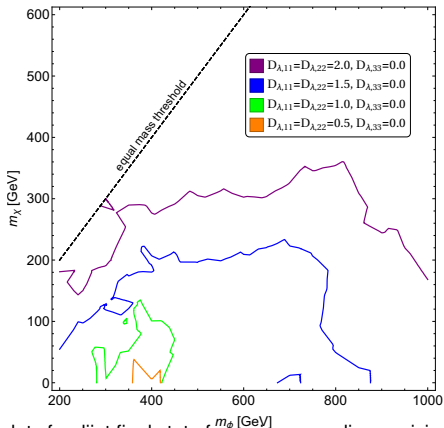


Figure : Exclusion plots for dijet final state for various couplings, mixing angles set to zero.

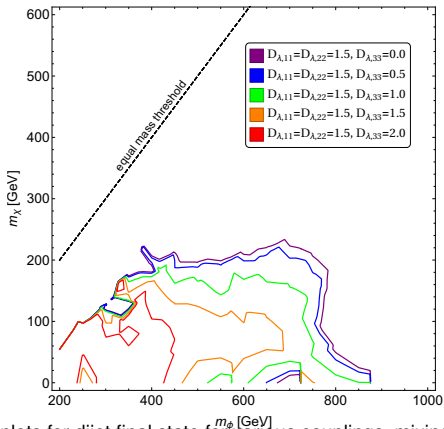


Figure : Exclusion plots for dijet final state for various couplings, mixing angles set to zero.

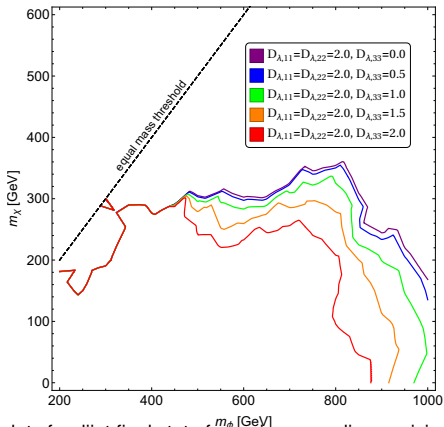


Figure : Exclusion plots for dijet final state for various couplings, mixing angles set to zero.

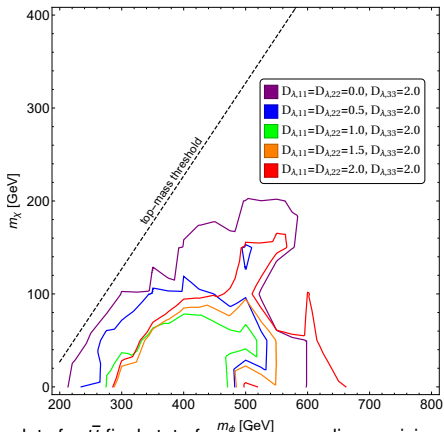


Figure : Exclusion plots for $t\bar{t}$ final state for various couplings, mixing angles set to zero.

Backup Material 5a

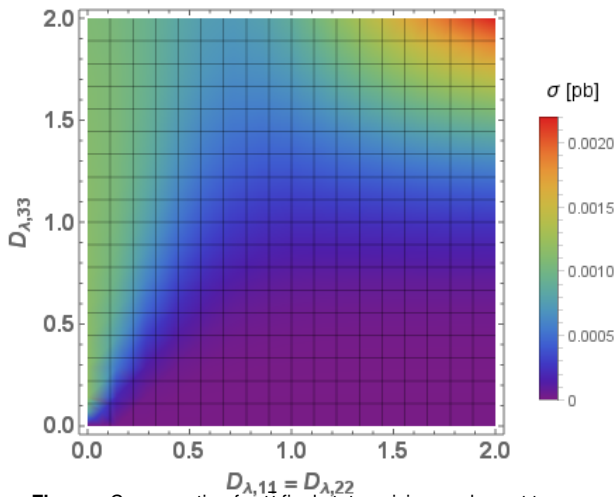


Figure : Cross section for $t\bar{t}$ final state, mixing angles set to zero.

Backup Material 5b

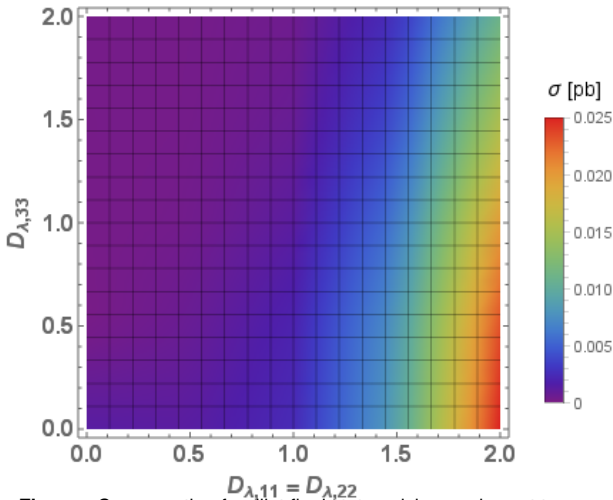


Figure : Cross section for dijet final state, mixing angles set to zero.

relative number of valid points

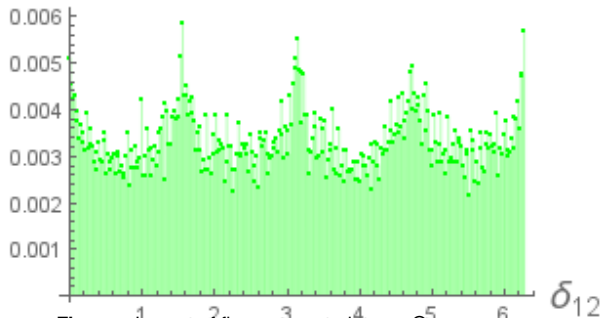


Figure : Impact of flavour constraints on Θ_{12} .

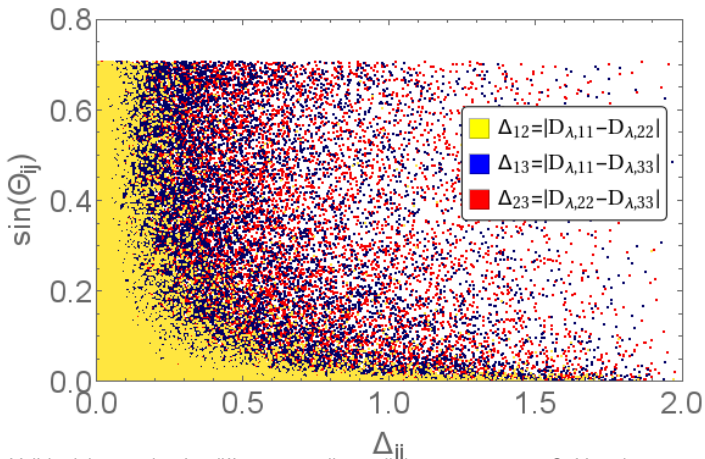


Figure : Valid mixing angles for different coupling splittings. $m_\phi = 850$ GeV and $m_\chi = 250$ GeV.

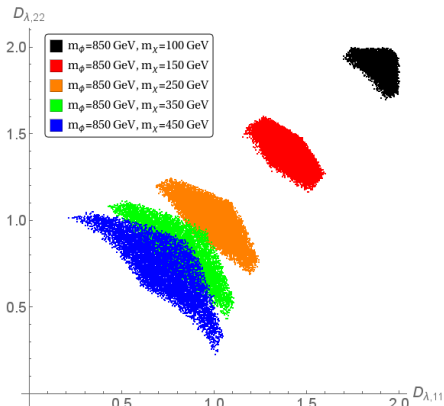


Figure : Valid regions in quasi-degenerate freeze-out scenario in $D_{\lambda,11} - D_{\lambda,22}$ -plane for various DM masses.

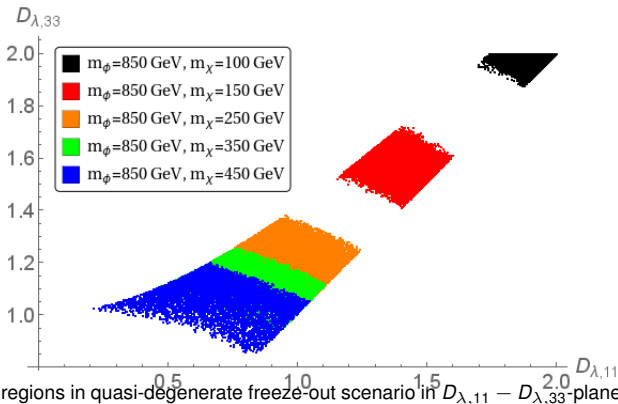


Figure : Valid regions in quasi-degenerate freeze-out scenario in $D_{\lambda,11} - D_{\lambda,33}$ plane for various DM masses.

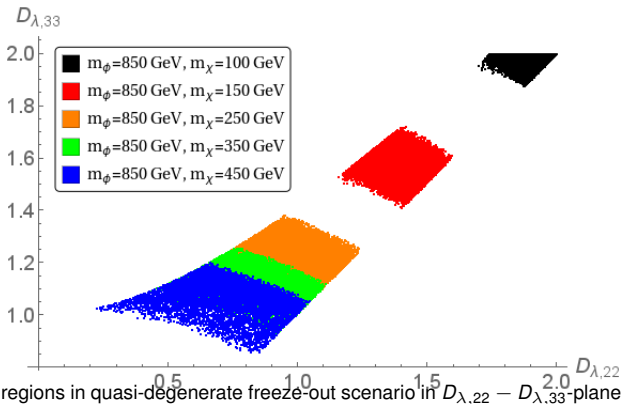


Figure : Valid regions in quasi-degenerate freeze-out scenario in $D_{\lambda,22} - D_{\lambda,33}$ plane for various DM masses.

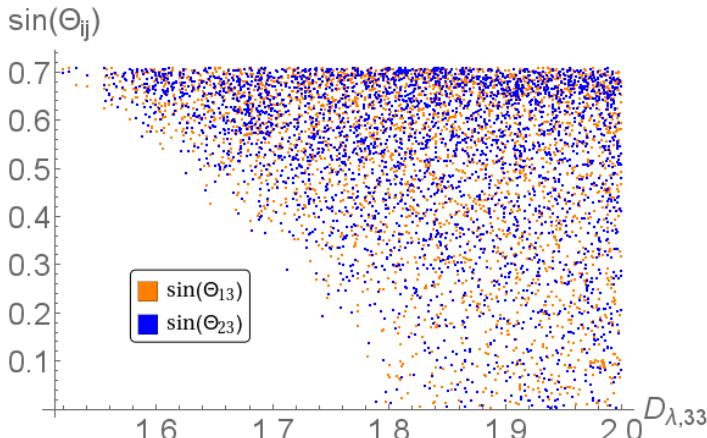


Figure : Valid regions in single-flavour freeze-out scenario in $D_{\lambda,33} - \sin(\Theta_{ij})$ -plane for $m_\phi = 850$ GeV and $m_\chi = 150$ GeV.

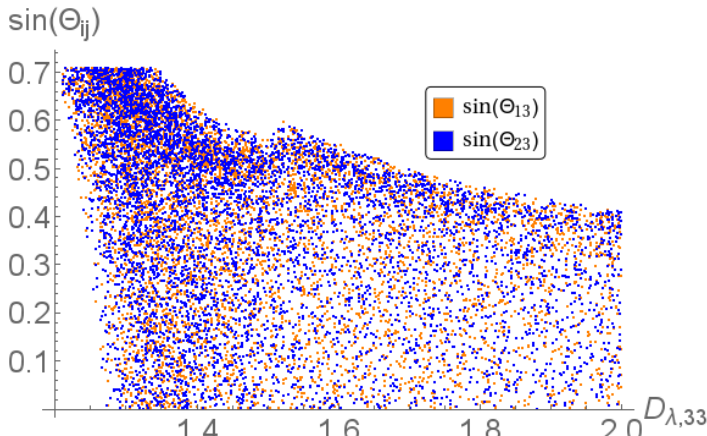


Figure : Valid regions in single-flavour freeze-out scenario in $D_{\lambda,33} - \sin(\Theta_{ij})$ -plane for $m_\phi = 850$ GeV and $m_\chi = 210$ GeV.

Backup Material 13

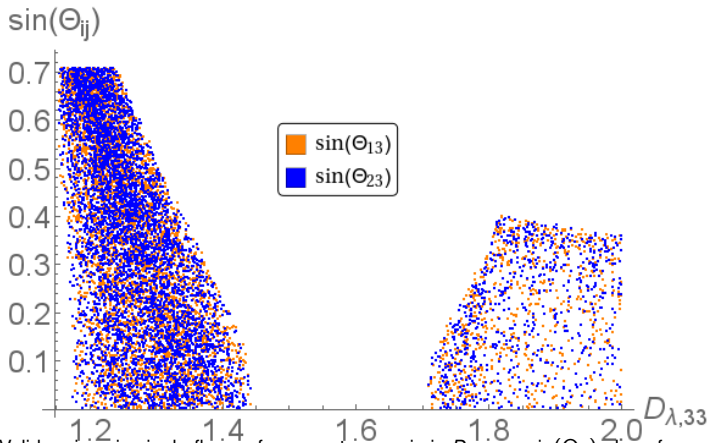
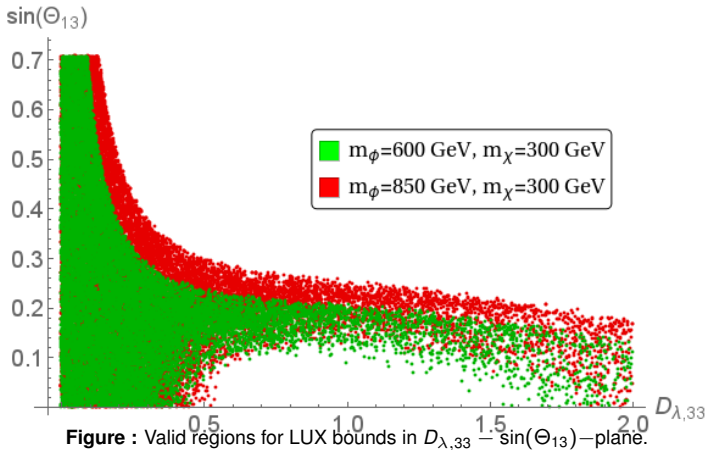
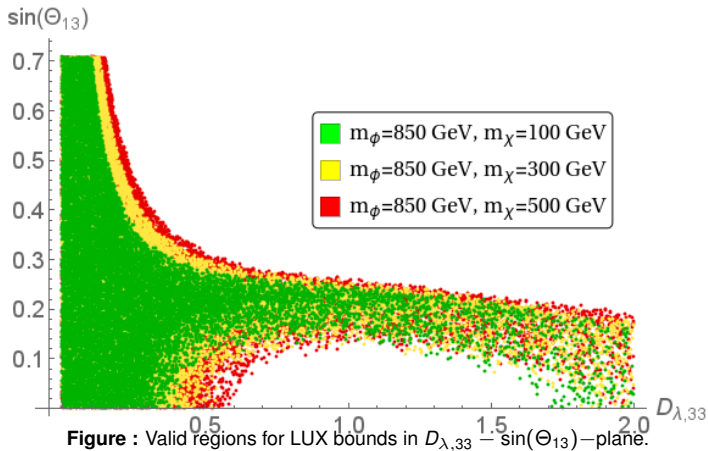


Figure : Valid regions in single-flavour freeze-out scenario in $D_{\lambda,33} - \sin(\Theta_{ij})$ -plane for $m_\phi = 850$ GeV and $m_\chi = 230$ GeV.





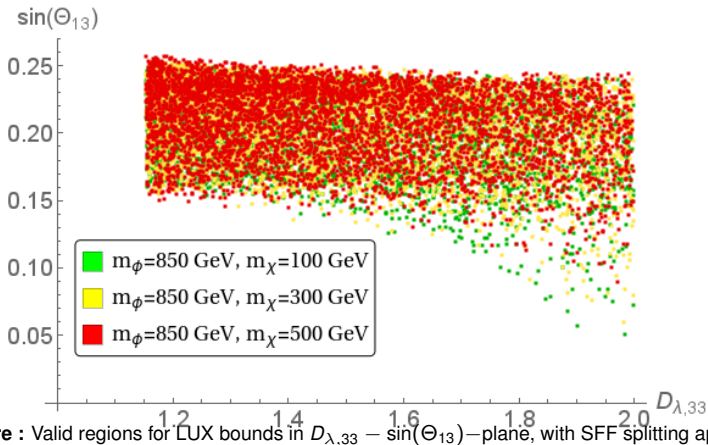


Figure : Valid regions for LUX bounds in $D_{\lambda,33}$ - $\sin(\Theta_{13})$ -plane, with SFF splitting applied.

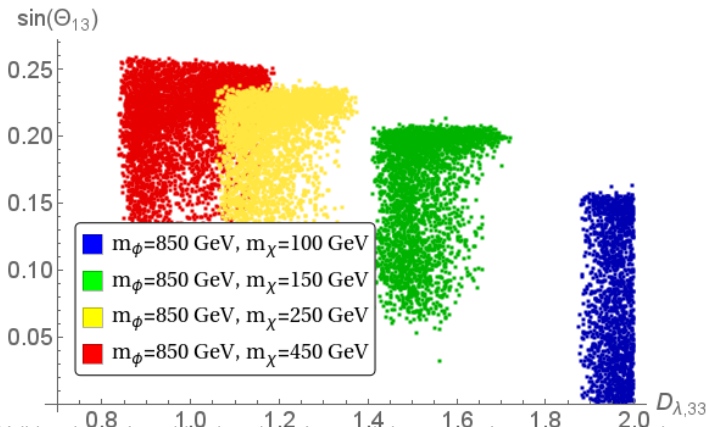


Figure : Valid regions of combined analysis for quasi-degenerate freeze-out scenario in $D_{\lambda,33} - \sin(\Theta_{13})$ -plane for different DM masses.

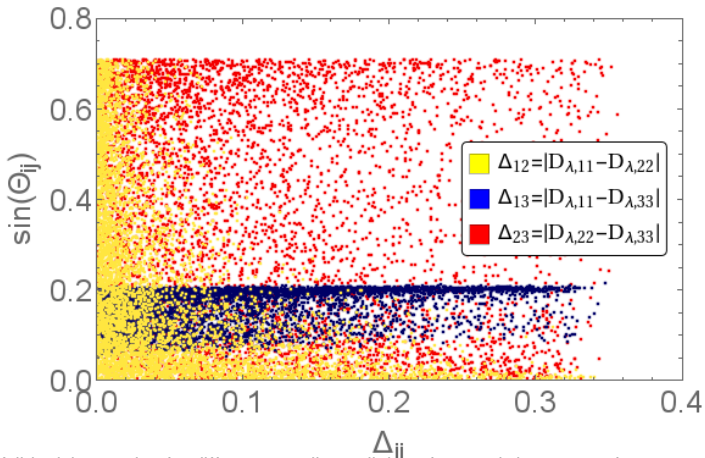


Figure : Valid mixing angles for different coupling splittings for quasi-degenerate freeze-out scenario.
 $m_\phi = 850$ GeV and $m_\chi = 150$ GeV.

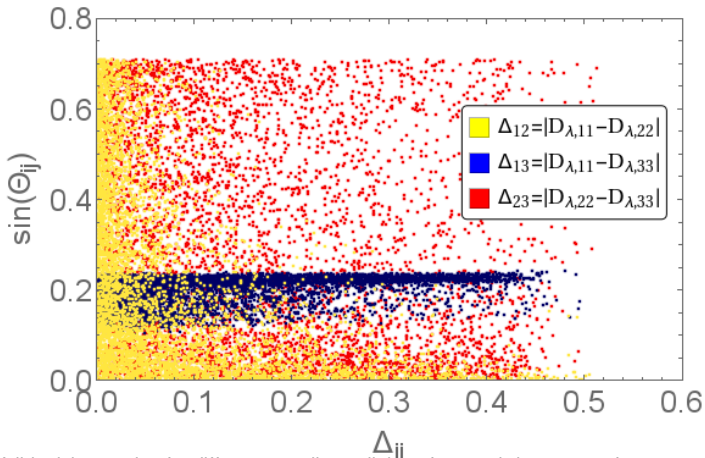


Figure : Valid mixing angles for different coupling splittings for quasi-degenerate freeze-out scenario.
 $m_\phi = 850$ GeV and $m_\chi = 250$ GeV.

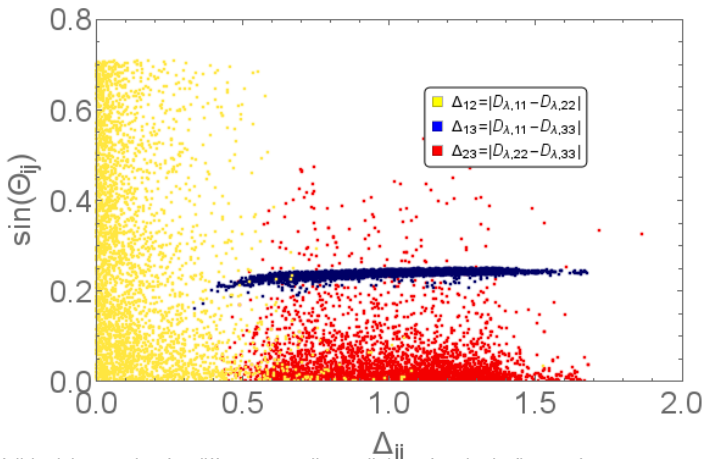


Figure : Valid mixing angles for different coupling splittings for single-flavour freeze-out scenario.
 $m_\phi = 850$ GeV and $m_\chi = 225$ GeV.

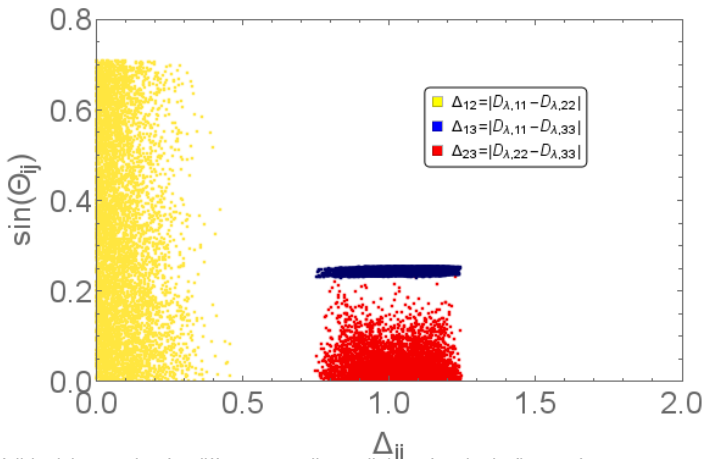


Figure : Valid mixing angles for different coupling splittings for single-flavour freeze-out scenario.
 $m_\phi = 850$ GeV and $m_\chi = 250$ GeV.

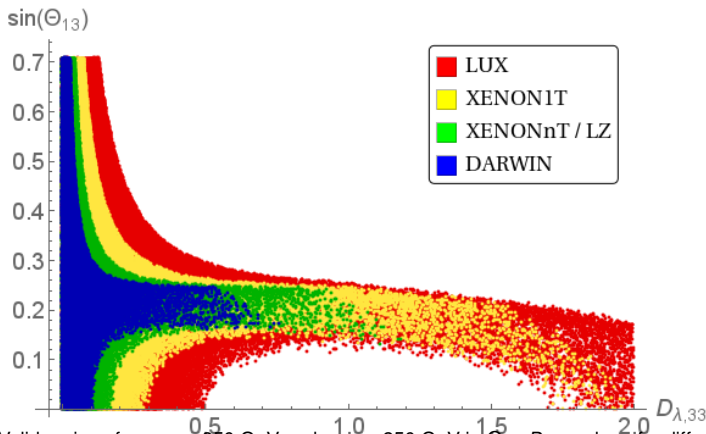


Figure : Valid regions for $m_\phi = 850$ GeV and $m_\chi = 250$ GeV in Θ_{13} - $D_{\lambda,33}$ -plane for different strengths of direct detection constraints in QDF.

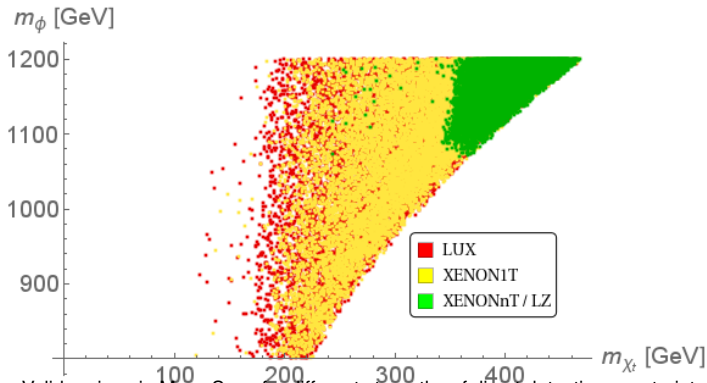


Figure : Valid regions in Mass Scan for different strengths of direct detection constraints in SFF.

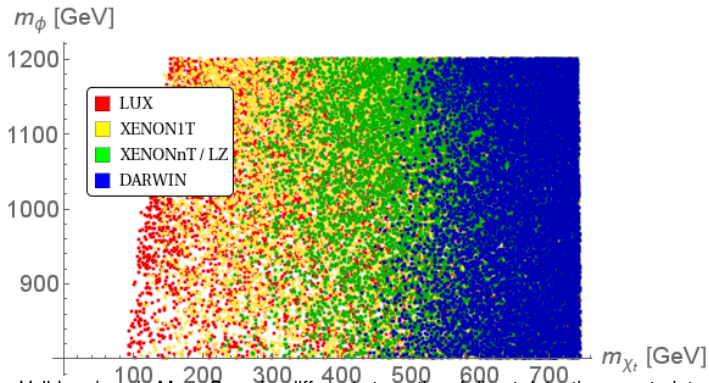


Figure : Valid regions in Mass Scan for different strengths of direct detection constraints in QDF.