(Probing ultralight dark matter with cold atoms) Implications of ultralight spin-0 dark matter

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Mostly based on work \w: Hook (2018) Abhishek Banerjee & Joshua Eby, 2210.05690; Hyungjin Kim, 2205.12988; Banerjee, Kim, Matsedonski, GP, Safranova (20) ...

DISCRETE 2022 8th Symposium on Prospects in the Physics of Discrete Symmetries Kongresshaus Baden-Baden November 7-11, 2022

• Intro, ultralight dark matter, challenges, indirect test (begin by demotivating my talk)

• Interesting models that address the challenges:

(i) Z_n QCD axion (ii) relaxed-relaxion

The importance of looking at scalar-effect, variation of constants, as you'll see CP plays crucial role, appropriate for the conference

Summary

Ultralight spin-0 dark matter?

Models of ultralight spin-0 dark matter (ULDM) are problematic:

They face typically 2 major problems -

(i) quality (sensitivity to UV/Planck suppressed operators)

(ii) naturalness (quantum sensitivity to UV scale)

Let us demonstrate it for elementary scalar with linear ULDM coupling, then for axions

$$\mathscr{L}_{\mathrm{Pl}} \in d_{m_e} \frac{\phi}{M_{\mathrm{Pl}}} m_e \bar{e}e + d_g \frac{\phi}{2gM_{\mathrm{Pl}}} \beta_g GG$$

Quality problem, 5th force vs EP violation, electron coupling



EP: Planck suppressed operators are excluded for $m_{\phi} \lesssim 10^{-6} \text{ eV}$ **5th force:** *operators are excluded for* $10^{-19} \lesssim m_{\phi} \lesssim 10^{-13} \text{ eV}$

Quality problem, 5th force vs EP violation, gluon



EP: Planck suppressed operators are excluded for $m_{\phi} \lesssim 10^{-5} \,\text{eV}$ **5th force:** *operators are excluded for* $m_{\phi} \lesssim 10^{-3} \,\text{eV}$

Naturalness problem ULDM scalars

• For this action there's also an issue of naturalness: $d_{m_e} < 4\pi m_{\phi}/\Lambda_e \times M_{\rm Pl}/m_e$ With $\Lambda_e \gtrsim m_e$ (for mirror model) => $d_{m_e} \lesssim 10^{6,0} \times \frac{m_{\phi}}{10^{-10} \,\mathrm{eV}} \times \frac{m_e, \mathrm{TeV}}{\Lambda_e}$ $\mathscr{L}_{\text{Pl}} \in d_{m_e} \frac{\phi}{M_{\text{Pl}}} m_e \bar{e} e + d_g \frac{\phi}{2gM_{\text{Pl}}} \beta_g G G$ 10^{6} d_{m_e} 10^{3} 10^{0} natural 10^{-3} **EP** tests natural 10^{-6} 10^{-21} 10^{-15} 10^{-18} 10^{-6} 10^{-12} 10^{-9} m_{ϕ} [eV

Quality and naturalness of axions

• Example of a quality problem for the QCD axion:

$$V = \Lambda_{\rm QCD}^4 \cos(a/f + \bar{\theta}) + \frac{\Phi^n}{M_{\rm Pl}^n} (\Phi^{\dagger} \Phi)^2 \implies \Lambda_{\rm QCD}^4 \sin \delta\theta \sim \epsilon^N f^4 \implies_{f \to 10^{10} \,\rm GeV} \left(\frac{\Lambda_{\rm QCD}}{10^{10} \,\rm GeV}\right)^4 10^{-10} \sim \left(\frac{10^{10} \,\rm GeV}{M_{\rm Pl}}\right)^n$$

where with *n*<7 operators, $\delta\theta > 10^{-10}$ and the strong CP problem is not solve!

This may be solved if one impose a (gauged) discrete symmetry, respected by gravity

• Even more general axion-like-particles are not immune:

$$\frac{\Phi^n}{M_{\rm Pl}^n} (\Phi^{\dagger} \Phi)^2 \quad \Rightarrow \quad \delta m_{\rm ALP} \sim \epsilon^{\frac{n}{2}} f \sim 10^{-4n} \times \left(\frac{f}{10^{10} \,{\rm GeV}}\right)^{\frac{n}{2}} \times 10^{10} \,{\rm GeV} =_{f=10^{10} \,{\rm GeV}} 10^{19-4n} \,{\rm eV}$$

natural eV ULDM requires n>4 operators

How serious is the strong CP problem

- In the SM the CKM phase is order 1 but $\bar{\theta} = \theta \arg \left[\det \left(Y_u Y_d \right) \right] \lesssim 10^{-10}$
- Is this a problem? Not necessarily, different spurions at tree level they are orthogonal, as exploited in Nelson-Barr type of models
- At 7 loops the EDM receives log-div contributions but it is tiny, and the finite contribution predicts $\bar{\theta} \sim 10^{-16}$ so it doesn't look like a serious problem at the moment, similar to the flavor problem ...
- In fact in Nelson-Barr the two CP phases are related but not in axion models ...

So what's next?

Briefly describe 2 models that avoid the above issues:

Z_n QCD axion model

Hook (2018) See also: Di Luzio, Gavela, Quilez & Ringwald (21)

Relaxed-(QCD)-relaxion

Relaxion idea: Graham, Kaplan & Rajendran (15) QCD-relaxion: Abhishek Banerjee & Joshua Eby, 2210.05690 Relaxed-relaxion: Banerjee, Kim, Matsedonski, GP, Safranova (20)

Axion searches with clocks

Kim & GP, 2205.12988

Magical Z_n QCD axion model

• The model based on *N* copies of the SM:

N

$$\mathscr{L} = \sum_{k=1}^{N} \mathscr{L}_{SM}^{k} + \Phi \sum_{k} Q_{k} Q_{k}^{c} \exp(2\pi i k/N), \ \langle \Phi \rangle = (f_{a} + \rho) \exp(i a/f_{a})/\sqrt{2}$$

• Under the U(1) and Z_N sym': $\mathscr{L}^i_{SM} \to \mathscr{L}^{i+1}_{SM}, \quad Q^{(c)}_i \to Q^{(c)}_{i+1}, \quad \Phi \to e^{2\pi i/N}\Phi \text{ and } Q_i \to e^{i\theta}Q_i, \quad \Phi \to e^{-i\theta}\Phi$

• Resulting with the following change to the QCD axion potential:

$$V(a) \approx -\Lambda_{\rm QCD}^4 \cos\left(\frac{a}{f} + \bar{\theta}\right) \Rightarrow -\left(\frac{m_u}{m_d}\right)^N \Lambda_{\rm QCD}^4 \cos\left(\frac{Na}{f} + \bar{\theta}\right)$$

• It achieves: (i) high quality; (ii) allow to go above the QCD line: $\frac{1}{f} \gg \frac{m_a}{\Lambda_{\text{QCD}}^2}$

(Z_n) QCD axion parameter space



The relaxion mechanism in a nutshell

Graham, Kaplan & Rajendran (15)

Relaxion mechanism (inflation based, slow rolling)

Graham, Kaplan & Rajendran (15)

(*i*) Add an ALP (relaxion) Higgs dependent mass:





Graham, Kaplan & Rajendran (15)

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(*i*) Add an ALP (relaxion) Higgs dependent mass:

 $\underbrace{\mu^2(\phi)}_{\left(\Lambda^2 - g\Lambda\phi\right)H^{\dagger}H} \cdot$

(*ii*) ϕ roles till μ^2 changes sign $\Rightarrow \langle H \rangle \neq 0 \Rightarrow$ stops rolling.



Successful if $\mu^2(\phi_{\text{stop}}) \ll \Lambda^2$

However the model suffers from a quality problem and fails to solve the strong CP problem Flacke, Frugiuele, Fuchs, Gupta & GP (16)

Davidi, Gupta, GP, Redigolo & Shalit (17)

High quality (classical) solution to the QCD relaxion problem

Banerjee, Eby & GP, last month

• The relaxion is based on two breaking of the shift symmetry

- The Rolling potential and the backreaction potential
- As seen the stopping condition is when the derivative of the Rolling potential is equal to the one of the backreaction potential, where QCD axion require the the axion settles at the minimum of its potential => $a/f_a \approx \pi/2$
- This is incompatible unless one is giving up on classical evolution, which my force us to think about the measure problem & eternal inflation

Nelson & Prescod-Weinstein (17) Gupta (18) Chatrchyan & Servant (22)

Combine ingredients to avoid the QCD relaxion CP problem

Banerjee, Eby & GP, last month

- Assume Z_{4N} sym' QCD relaxion model, say Z_4 and make the backreaction dominated by a single sector, k, which is not the SM.
- As we showed, the relaxion will stop the evolution at $\bar{\theta}_k \sim \pi/2$
- Consider for instance having the SM at the *N*th site and the site with the dominant backreaction on the site after:

$$V(\bar{\theta}) \sim -\Lambda_{\rm QCD'}^{\prime 4} \cos(\bar{\theta} + a/f + \pi/2) \iff \mathscr{L}_k = \left(\bar{\theta} + a/f_a + \pi/2\right) \frac{1}{32\pi^2} G'\tilde{G}' \implies (a/f_a)_{\rm relax} \approx -\bar{\theta}$$

• If this is just the sector after the SM then the SM will have

$$\mathscr{L}_{\text{SM}} = \left(\bar{\theta} + a/f_a\right) \frac{1}{32\pi^2} G\tilde{G}$$
, solving the strong CP problem.

• Let's highlight two interesting effect the first is just related to the fact that the QCD axion coupled quadratically to masses:

Oscillations of energy levels induced by QCD-axion-like DM

Kim & GP, last month

- Consider axion model $\ (\alpha_s/8) (a/f) G\tilde{G}$ coupling, usually searched by magnetometers
- However, spectrum depends on $\theta^2 = (a(t)/f)^2$: $m_{\pi}^2(\theta) = B\sqrt{m_u^2 + m_d^2 + 2m_u m_d \cos \theta}$ Brower, Chandrasekharanc, Negele & Wiese (03)

$$\operatorname{MeV} \times \theta^2 \bar{n}n \Rightarrow \frac{\delta f}{f} \sim \frac{\delta m_N}{m_N} \sim 10^{-16} \times \cos(2m_a) \times \left(\frac{10^{-15} \,\mathrm{eV}}{m_\phi} \frac{10^9 \,\mathrm{GeV}}{f}\right)^2 \quad \mathrm{vs} \quad m_N \frac{a}{f} \bar{n} \gamma^5 n \Rightarrow \left(f \gtrsim 10^9 \,\mathrm{GeV}\right)_{\mathrm{SN}}$$

It's exciting as clocks (& EP tests) are much more precise than magnetometers They can sense oscillation of energy level due to change of mass of the electron or QCD masses to precision of better than 1:10¹⁸!

Oscillations of energy levels induced by QCD-axion-like DM

• Consider axion model $\langle w(\alpha_s/8)(a/f) G\tilde{G}$ coupling, usually searched by magnetometers

$$\begin{split} \mathrm{MeV} \times \theta^2 \bar{n}n \Rightarrow \frac{\delta f}{f} \sim \frac{\delta m_N}{m_N} \sim 10^{-16} \times \cos(2m_a) \times \left(\frac{10^{-15} \,\mathrm{eV} \, 10^9 \,\mathrm{GeV}}{m_\phi} \right)^2 & \mathrm{vs} \quad m_N \frac{a}{f} \bar{n} \gamma^5 n \Rightarrow \left(f \gtrsim 10^9 \,\mathrm{GeV}\right)_{\mathrm{SN}} \\ & \int 0^{-10} \,\mathrm{GeV}_{\mathrm{SN}} & \int 0^{-10}$$

Pheno #2

• The 2nd is due to the fact that the min' of relaxion potential deviates from $\pi/2$



Pheno

Let me highlight two interesting effect the first is just related to the fact that the QCD axion coupled quadratically to masses: see next page

• The 2nd is due to the fact that the min' of relaxion potential deviates from pi/2.

The QCD axion also induces a scalar interaction with the nucleon in the presence of a CP-violating phase of the form of

$$g_{\phi NN} \simeq 1.3 imes 10^{-2} \, rac{m_N}{f} \delta_{ heta} \, . \ rac{9 imes 10^{-24}}{f_{11}} \lesssim g_{\phi NN} \lesssim rac{4 imes 10^{-23}}{f_{11}} \, ,$$

where, $f_{11} = f/(10^{11} \text{ GeV})$ and we have used m_N ~ 1 GeV. The strongest bound on $g_{\phi N N}$ comes from the experiments looking for the existence of fifth force and/or violation of equivalence principle (EP). The bound from EP violation searches, for the axion mass around 10^{-6} eV , is $g_{\phi NN}$? 10^{-21}

There's also a bound for axion-proton pseudoscalar and axion-nucleon scalar coupling which will be probed by Ariadne

$$\frac{4 \times 10^{-35}}{f_{11}^2} \lesssim |g_p^a g_{\phi NN}| \lesssim \frac{2 \times 10^{-34}}{f_{11}^2} \,. \tag{25}$$

Pheno

Finally it could be probed by combination of scalar oscillation as well as pseudo scalar ...

- Ultralight dark matter (ULDM) of spin-0 particles are challenging
- Strong CP + hierarchy problem, why the QCD relaxion doesn't work
- Hook's Z_n high quality ultra light QCD axion model
- A high quality Z_{4n} QCD relaxion model via the concept of relaxed relaxion
- Exciting phenomenology, possibly involving breaking of CP, can be probed with clocks due to their extreme precision

Backups

The model requirements and parameters

• We need to make the N+1 th site to dominate the backreaction we do it by

breaking the sym' choosing
$$\gamma \equiv v/v' \sim 0.1 - 0.001$$
 and $\epsilon_b \equiv \frac{y_u \Lambda_{\text{QCD}}^3}{y'_u \Lambda'_{\text{QCD}'}^3} \lesssim \gamma$

• The leading deviation from $\bar{\theta}_{N-1} = \pi/2$ is coming from two sources: the fact that $\delta \neq 0 \Rightarrow \bar{\theta} \gtrsim \delta \sim 10^{-11} \sqrt{\frac{\gamma}{\epsilon_b}} \qquad \left[\Delta v^2/v^2 = g\Lambda f/v^2 = g\Lambda^3 f/v^2 \Lambda^2 \sim y_u \Lambda_{QCD}^3/\Lambda^2 v \equiv \mu_{br}^2/\Lambda^2\right] \equiv \delta^2$

and that the other contributions push toward $\bar{\theta}_N = \pi/2$

• We can't switch the two off (nor we want) in particular: suppressing tunneling (+ quantum): $\Delta V \sim \Lambda_{\text{back}}^4 \delta^3 \equiv \left(m'_u \Lambda_{\text{QCD'}}^{\prime 3} \right)^4 \delta^3 \gg H_I^4$

• Ensuring inflation domination $H_I^2 \gg \Lambda^4 / M_{\text{Pl}}^2 \Rightarrow \Lambda_{\text{back}}^4 (\mu_{\text{back}}^2 / \Lambda^2)^3 \ll \Lambda^8 / M_{\text{Pl}}^4$

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Relaxion and cosmology

• Must not disturb inflation $H^2 > \Lambda^4 / M_{Mpl}^2$

• Dominated by classical evolution $H < \dot{\phi}/H \sim V'/H^2 \leq v^4/fH^2 \Rightarrow \Lambda < f < v^4/H^3$

• Combining the two $\Lambda \leq M^{\frac{3}{7}}v^{\frac{4}{7}} \sim 10^8 \,\mathrm{GeV}$

• There is also an interesting relation between the cutoff and the number of e-folds

$$\Delta \phi \sim F \implies N_{\rm ef} \sim F/\dot{\phi} \times H \sim FH^2/V' \sim F^2 H^2/\Lambda^4 \gtrsim F^2/M_{\rm Pl}^2$$

$$\sim (\Lambda/v)^8 f^2/M_{\rm Pl}^2 \gtrsim \Lambda^{10}/v^8 M_{\rm Pl}^2 \sim \left(\frac{\Lambda}{100\,{\rm TeV}}\right)^{10}$$

Relaxed relaxion & some pheno

Relaxion's naive parameters (similar to ALP, backreaction domination)

Naively: mixing angle in terms of mass $\sin \theta_{h\phi} \sim \frac{m_{\phi}}{v_{\rm EW}} \frac{\mu_b}{v_{\rm EW}}$

Maximum mixing angle
$$(\sin \theta_{h\phi})_{max} \sim \frac{m_{\phi}}{v_{EW}}$$
Naturalness
boundMinimum mixing angle $(\sin \theta_{h\phi})_{min} \sim \frac{m_{\phi}^2 \Lambda_{min}}{v_{EW}^3}$ Naturalness
bound

The relaxion's naive parameter space



The log crisis

• Lesson 1 - finding NP requires diverse approach, searches across frontier

• Lesson 2 - experimentally, worth checking where many decades are covered:



Less naive treatment, the relaxed relaxion

$$V(\phi,h) = \left(\Lambda^2 - \Lambda^2 \frac{\phi}{F}\right) |H|^2 - \frac{\Lambda^4}{F} \phi - \mu_b^2 |H|^2 \cos \frac{\phi}{f} \qquad v^2(\phi) = \begin{cases} 0 \text{ when } \phi < f_{\text{eff}} \\ > 0 \text{ when } \phi > f_{\text{eff}} \end{cases}$$

Relaxion stopping point determines the EW scale

$$\frac{\Lambda^4}{F} \sim \frac{\mu_{\rm b}^2 v_{\rm EW}^2}{f}$$

Higgs mass change for
$$\Delta \phi = 2\pi f$$
 $\frac{\Delta v^2}{v^2} \sim \frac{\Lambda^2}{F} \frac{f}{v^2} \sim \frac{\mu_b^2}{\Lambda^2} \equiv \delta^2 \ll 1$

$$V_{\rm br} = -\mu_{\rm b}^2 |H|^2 \cos \frac{\phi}{f} \qquad \Longrightarrow \qquad \begin{array}{c} {\rm Potential \ height \ grows} \\ {\rm incrementally} \end{array}$$

Stopping condition, fine resolution

Banerjee, Kim, Matsedonski, GP, Safranova (20)



Stopping condition, fine resolution

Banerjee, Kim, Matsedonski, GP, Safranova (20)



Relaxed mass => natural violation of naturalness bound

Banerjee, Kim, Matsedonski, GP, Safranova (20)

Max. Mixing angle:
$$\sin \theta_{h\phi}^{\max} = \left(\frac{m_{\phi}}{v_{EW}}\right)^{\frac{2}{3}} \gg \left(\frac{m_{\phi}}{v_{EW}}\right)_{\text{naturalness}}$$



Quality problem, 5th force vs EP violation, electron coupling



EP: Planck suppressed operators are excluded for $m_{\phi} \lesssim 10^{-6} \text{ eV}$ **5th force:** *operators are excluded for* $10^{-19} \lesssim m_{\phi} \lesssim 10^{-13} \text{ eV}$

Quality problem, 5th force vs EP violation, gluon



EP: Planck suppressed operators are excluded for $m_{\phi} \lesssim 10^{-5} \,\text{eV}$ **5th force:** *operators are excluded for* $m_{\phi} \lesssim 10^{-3} \,\text{eV}$

QCD low energy (2 gen ignoring eta')

At low energies:

$$\mathcal{C} \supset \frac{\theta g_s^2}{32\pi^2} G\tilde{G} + qMq^c, \qquad M = \begin{pmatrix} m_u & 0\\ 0 & m_d \end{pmatrix}$$



 $\langle qq^c
angle
eq 0,$ Breaks SU(2) L x R to diagonal

Chiral Goldstone action

$$U = e^{i\frac{\Pi^a}{\sqrt{2}f_\pi}\sigma^a},$$

$$rac{|SU(2)_L \; SU(2)_R \; U(1)_B \; U(1)_A}{U \; \square \; \square \; 2} \quad U \propto q q^c$$

$$\mathcal{L} = f_{\pi}^2 \operatorname{Tr} \partial_{\mu} U \partial^{\mu} U^{\dagger} + a f_{\pi}^3 \operatorname{Tr} M U + h.c.,$$

Axial sym transformation

 $u \to e^{i\alpha}u, \qquad u^c \to e^{i\alpha}u^c,$



 $u \to e^{i\alpha}u, \qquad d \to e^{i\alpha}d, \qquad \theta \to \theta - 2\alpha.$

 $U \to e^{i\alpha} U, \qquad \qquad M \to e^{-i\alpha} M.$

Removing the GGdual coupling, phase freedom

$$U = e^{i\pi^{a}\tau^{a}/f_{\pi}} = \cos\frac{|\vec{\pi}|}{f_{\pi}} + i\frac{\pi^{a}}{|\vec{\pi}|}\tau^{a}\sin\frac{|\vec{\pi}|}{f_{\pi}}.$$

$$u \rightarrow e^{i\phi_{u}}u$$

$$d \rightarrow e^{i\phi_{d}}d, \qquad \phi_{u} + \phi_{d} = \theta.$$

$$U_{0} = \begin{pmatrix} e^{i\phi_{u}} & 0\\ 0 & e^{i\phi_{d}} \end{pmatrix}.$$

$$V = -B_0 \operatorname{Tr}[(MU_0)U + (MU_0)^{\dagger}U^{\dagger}] = -B_0 \left[4A \cos \frac{|\vec{\pi}|}{f_{\pi}} - 4D \frac{\pi^3}{|\vec{\pi}|} \sin \frac{|\vec{\pi}|}{f_{\pi}} \right].$$

$$D = \frac{1}{2} \operatorname{Tr} \left[\tau^3 \begin{pmatrix} m_u \sin \phi_u & 0\\ 0 & m_d \sin \phi_d \end{pmatrix} \right] = \frac{1}{2} (m_u \sin \phi_u - m_d \sin \phi_d) = 0$$

QCD parameter space

$$\sin \phi_{u} = \frac{m_{d} \sin \theta}{[m_{u}^{2} + m_{d}^{2} + 2m_{u}m_{d} \cos \theta]^{1/2}}$$

$$\sin \phi_{d} = \frac{m_{u} \sin \theta}{[m_{u}^{2} + m_{d}^{2} + 2m_{u}m_{d} \cos \theta]^{1/2}}$$

$$\cos \phi_{u} = \frac{m_{u} + m_{d} \cos \theta}{[m_{u}^{2} + m_{d}^{2} + 2m_{u}m_{d} \cos \theta]^{1/2}}$$

$$\cos \phi_{d} = \frac{m_{d} + m_{u} \cos \theta}{[m_{u}^{2} + m_{d}^{2} + 2m_{u}m_{d} \cos \theta]^{1/2}}.$$

$$A = \frac{1}{2} \operatorname{Tr} \begin{pmatrix} m_u \cos \phi_u & 0\\ 0 & m_d \cos \phi_d \end{pmatrix} = \frac{1}{2} (m_u \cos \phi_u + m_d \cos \phi_d)$$

The QCD line

$$m_a \sim \frac{1}{f} \times \Lambda_{\text{QCD}}^2$$
 or $m_a \sim g_{\text{gluon}} \times \Lambda_{\text{cutoff, shiftsym}}^2$

$$m_a \gtrsim g_{\text{gluon}} \times \Lambda^2_{\text{cutoff, shiftsym}}$$
 or $1/f \lesssim m_a/\Lambda^2_{\text{QCD}}$

It is not hard to go naturally below the QCD line but it is very hard to go above it.

The QCD line



• Most minimal model would be just a free massive scalar :

$$\mathscr{L} \in m_{\phi}^2 \phi^2, \, \rho_{\mathrm{Eq}}^{\mathrm{DM}} \sim \mathrm{eV}^4 \sim m_{\phi}^2 \phi_{\mathrm{Eq}}^2 = m_{\phi}^2 \phi_{\mathrm{init}}^2 (\mathrm{eV}/T_{\mathrm{osc}})^3$$
$$T_{\mathrm{os}} \sim \sqrt{M_{\mathrm{Pl}} m_{\phi}} \implies \phi_{\mathrm{init}} \sim M_{\mathrm{Pl}} \left(\frac{10^{-27} \, \mathrm{eV}}{m_{\phi}}\right)^{\frac{1}{4}}$$

(can add a few more bounds, SR, isogurvature but still large parameter space, reasonable field excursion)

Iust remind you that if we add Planck suppressed operators then we did find bounds ...

Also, in the presence of these coupling if it's too light there will be naturalness issues …

The relaxion DM dynamical missalignment

Banerjee, Kim & GP (18)

♦ Basic idea is similar to axion DM:



Basic idea is similar to axion DM (but avoiding missalignment problem):
 After reheating the wiggles disappear (sym' restoration):



• Basic idea is similar to axion DM (but avoiding missalignment problem):

After reheating the wiggles disappear: and the relaxion roles a bit.



• Basic idea is similar to axion DM (but avoiding missalignment problem):

After reheating the wiggles disappear: and the relaxion roles a bit.



When the universe cools the electroweak symmetry is broken, brings back the wiggles.



When the universe cools the electroweak symmetry is broken, brings back the wiggles.



When the universe cools the electroweak symmetry is broken, brings back the wiggles.



When the universe cools the electroweak symmetry is broken, brings back the wiggles.



• Basic idea is similar to axion DM (but avoiding missalignment problem):



relaxion DM+GW

DM window



The black solid line encompass the DM relaxion parameter space. The colored regions inside the viable DM space can be probed via GWs in μ Ares (green) or SKA (blue/turquoise). The light shading and solid lines indicate points that can be probed for a subrange of reappearance temperatures, whereas the darker shaded parts enclosed by dotted lines are accessible for all valid T_{ra} .

Equivalence principle (EP) tests, prelim

• Consider the following effective action for scalar DM: $\mathscr{L}_{\phi} \in d_{m_e} \frac{\phi}{M_{\text{Pl}}} m_e \bar{e}e + d_g \frac{\phi}{2gM_{\text{Pl}}} \beta_g GG$

• The leading action in the non-relativistic limit, say, of the electron is

$$\mathscr{L}_e^{\mathrm{NR}} = m_e(\phi) + \frac{1}{2}m_e v^2 = m_e^0 + d_{m_e}\frac{\phi}{M_{\mathrm{Pl}}} \quad \Rightarrow \quad a = d_{m_e}\frac{\phi'}{M_{\mathrm{Pl}}}$$

Inside an atom we can rewrite it as:

$$\mathscr{L}_{\rm atm}^{\rm NR} = M_{\rm Nuc}(\phi) + Nm_e(\phi) + B \implies M_{\rm atm}a = \phi' \left(\partial_{\phi} M_{\rm Nuc}(\phi) + N\partial_{\phi} m_e(\phi)\right) \implies a = \phi' \partial_{\phi} \ln M_{\rm atm} \equiv \sqrt{G}_N \phi' \alpha_{\rm atm}$$

which can be readily generalised to any system.

• For a test particle at distances such that $m_{\phi}R \ll 1$ and say $R \gtrsim R_{\text{Earth}}$ have $\phi' \propto 1/R^2$ and

the acceleration is given by $a = G_N M_{\text{test}} \alpha_{\text{test}} M_{\text{Earth}} \alpha_{\text{Earth}} / R^2$

Damour & Donoghue (10)

Equivalence principle (EP) tests

- We would compare two bodies, *A* and *B*, to search for a differential acceleration effect via the EotWash parameter $\frac{\delta a_{AB}}{a} = \alpha_{\text{Earth}}(\alpha_A - \alpha_B)$
- Or if we switch on one coupling d_i it is useful to define the corresponding individual "diatonic charge" $d_i Q_i \equiv \alpha_i$
- The experiment test is very simple, let's search for masses smaller than the inverse size of the Earth then we can use two test bodies on a satellite that are free falling with the satellite and just track them. That's exactly what the Microscope mission is doing some 700km above earth
- After >5 yrs of running they've achieve precision of better than $\eta_{\rm EP} < 10^{-14}$, which can be translated to the following bounds on generic scalar models

Equivalence principle (EP) tests

• For variety of coupling it can be expressed as:

EP bounds :
$$\left(\frac{\delta a_{\text{test}}}{a}\right) < \eta_{\text{EP}} \sim 10^{-14} \iff \left(d_i^{(1)}d_j^{(1)}\right) \Delta Q_i^{\text{test}}Q_j^{\text{Earth}}$$

$$\vec{Q}^{\mathbf{a}} \approx F^{\mathbf{a}} \left(3\ 10^{-4} - 4\ r_I + 8\ r_Z, 3\ 10^{-4} - 3\ r_I, 0.9, 0.09 - \frac{0.04}{A^{1/3}} - 2 \times 10^6 r_I^2 - r_Z, 0.002\ r_I \right)$$

Where $\vec{X} \equiv X_{e,m_e,g,\hat{m},\delta m}$, with $\hat{m} \equiv (m_d + m_u)/2$, $\delta m \equiv (m_d - m_u)$, $10^4 r_{I;Z} \equiv 1 - 2Z/A$; $Z(Z - 1)/A^{4/3}$, & $F^{\mathbf{a}} = 931 A^{\mathbf{a}}/(m^{\mathbf{a}}/\text{MeV})$ with $A^{\mathbf{a}}$ being the atomic number of the atom \mathbf{a}

$$\Delta \vec{Q}^{\text{Mic}} \simeq 10^{-3} (-1.94, 0.03, 0.8, -2.61, -0.19)$$

Tretiak, et al.; Oswald, et al (22)

Equivalence principle (EP) tests

Banerjee, GP, Safronova, Savoray & Shalit (to appear)



Where one can find models that avoid the strongest EP bounds and for a pure dilaton the EP bound can be avoided
Tretiak, et al.; Oswald, et al.(22)

Direct dark matter searches, sensitivity

How do we search for ULDM directly?

Take for example the Lagrangian $\mathscr{L}_{\phi} \in d_{m_e} \frac{\phi}{M_{\text{Pl}}} m_e \bar{e}e + d_g \frac{\phi}{2gM_{\text{Pl}}} \beta_g GG$ and focus first about

the electron coupling?

• The most sensitive way is with clocks, because $\phi \sim \frac{\sqrt{2\rho_{\rm DM}}}{m_{\phi}} \cos(m_{\phi}t)$ then the electron

mass oscillates with time => energy levels oscillates with time: $E_n \sim m_e \alpha^2 1/2n^2$

• For instance:
$$\Delta E_{21} \sim m_e \alpha^2 1/2 \times 3/4 \times \left[1 + d_{m_e} \frac{\sqrt{2\rho_{\rm DM}}}{m_\phi M_{\rm Pl}} \left(\sim 10^{-15} \times \frac{d_{m_e}}{10^{-3}} \frac{10^{-15} \,\mathrm{eV}}{m_\phi} \right) \times \cos(m_\phi t) \right]$$

Direct dark matter searches via clocks

• Which implies that clocks can win over EP for precision of roughly 1:10¹⁵ for about 1 Hz

DM mass

• How the clock works: for this school it's just creating a state which is a superposition of the two states and thus oscillates with time and picking up the above phase: $\exp^{i\Delta E(m_e(t))t}$

• However, to see the effect you need to compare it to another system that would not have

the above precise dependence ...

Enhanced sensitivity

• The most robust coupling is to the gluons:

Mixing with the Higgs, dilaton and even QCD axion have coupling to the gluons • How to be sensitive to the coupling to QCD?

 Could be via reduced mass, or via g-factor, magnetic moment-spin interactions-hyperfine or vibrational model in molecules, or the queen of all nuclear clock , ²²⁹Th

• It is super sensitive because $E_{nu-clock} \sim E_{nu} - E_{QED} \sim 8 \text{ eV} \ll E_{nu} \sim \text{MeV}$

$$\frac{\Delta E}{E} = \frac{E_{\rm nu}(t) - E_{\rm QED}}{E_{\rm nu-clock}} \quad \Rightarrow \quad \frac{\Delta E_{\rm nu}(t)}{E_{\rm nu-clock}} \sim \frac{E_{\rm nu}}{E_{\rm nu-clock}} \times d_g \frac{m_N}{M_{\rm Pl}} \cos(m_\phi t) \sim 10^5 d_g \frac{m_N}{M_{\rm Pl}} \cos(m_\phi t)$$