(Probing ultralight dark matter with cold atoms) Implications of ultralight spin-0 dark matter

#### Gilad Perez, Weizmann Inst.

Mostly based on work \w: Hook (2018) Abhishek Banerjee & Joshua Eby, [2210.05690;](https://arxiv.org/abs/2210.05690) Hyungjin Kim, [2205.12988](https://arxiv.org/abs/2205.12988); Banerjee, Kim, Matsedonski, GP, Safranova (20) …



Intro, ultralight dark matter, challenges, indirect test (begin by demotivating my talk)

Interesting models that address the challenges:

(i)  $Z_n$  QCD axion (ii) relaxed-relaxion

The importance of looking at scalar-effect, variation of constants, as you'll see CP plays crucial role, appropriate for the conference

Summary

# Ultralight spin-0 dark matter?

Models of ultralight spin-0 dark matter (ULDM) are problematic:

 They face typically 2 major problems - (i) quality (sensitivity to UV/Planck suppressed operators) (ii) naturalness (quantum sensitivity to UV scale)

Let us demonstrate it for elementary scalar with linear ULDM coupling, then for axions

$$
\mathcal{L}_{\text{Pl}} \in d_{m_e} \frac{\phi}{M_{\text{Pl}}} m_e \bar{e}e + d_g \frac{\phi}{2gM_{\text{Pl}}} \beta_g GG
$$

# Quality problem, 5th force vs EP violation, electron coupling



EP: Planck suppressed operators are excluded for  $m_\phi \lesssim 10^{-6}$  eV 5th force: *operators are excluded for*  $10^{-19} \lesssim m_\phi \lesssim 10^{-13} \, {\rm eV}$ 

# Quality problem, 5th force vs EP violation, gluon



EP: Planck suppressed operators are excluded for  $m_\phi \lesssim 10^{-5}\, \text{eV}$ **5th force:** *operators are excluded for* $m_{\phi} \lesssim 10^{-3}$  **eV** 

#### Naturalness problem ULDM scalars

For this action there's also an issue of naturalness:  $d_{m_e} < 4\pi m_{\phi}/\Lambda_e \times M_{\rm Pl}/m_e$ *mϕ me*, TeV With  $\Lambda_e \gtrsim m_e$  (for mirror model) =>  $d_{m_e} \lesssim 10^{6.0} \times$  $\times$  $10^{-10}$  eV  $\Lambda_e$ *ϕ ϕ*  $\mathscr{L}_{\text{Pl}} \in d_{m_e}$  $m_e\bar{e}e + d_g$ *βgGG*  $M_{\rm Pl}$  $2gM_{\rm Pl}$  $10^{6}$ Tel.  $d_{m_e}$ ∼ $10^3$  *me* Λ*<sup>e</sup>* ∼Λ*<sup>e</sup>*  $10<sup>0</sup>$ natural  $10^{-3}$ EP tests natural $10^{-6}$  $^{0}$  10<sup>-21</sup>  $10^{-15}$  $10^{-6}$  $10^{-18}$  $10^{-12}$  $10^{-9}$  $m_{\phi}$  [eV

# Quality and naturalness of axions

Example of a quality problem for the QCD axion:

$$
V = \Lambda_{\text{QCD}}^4 \cos(a/f + \bar{\theta}) + \frac{\Phi^n}{M_{\text{Pl}}^n} (\Phi^{\dagger} \Phi)^2 \Rightarrow \Lambda_{\text{QCD}}^4 \sin \delta\theta \sim \epsilon^N f^4 \Rightarrow_{f \to 10^{10} \text{GeV}} \left( \frac{\Lambda_{\text{QCD}}}{10^{10} \text{GeV}} \right)^4 10^{-10} \sim \left( \frac{10^{10} \text{GeV}}{M_{\text{Pl}}} \right)^n
$$

where with  $n$ <7 operators,  $\delta\theta > 10^{-10}$  and the strong CP problem is not solve!

This may be solved if one impose a (gauged) discrete symmetry, respected by gravity

Even more general axion-like-particles are not immune:

$$
\frac{\Phi^n}{M_{\text{Pl}}^n} (\Phi^{\dagger} \Phi)^2 \quad \Rightarrow \quad \delta m_{\text{ALP}} \sim \epsilon^{\frac{n}{2}} f \sim 10^{-4n} \times \left(\frac{f}{10^{10} \text{GeV}}\right)^{\frac{n}{2}} \times 10^{10} \text{GeV} =_{f=10^{10} \text{GeV}} 10^{19-4n} \text{eV}
$$

natural eV ULDM requires *n>*4 operators

# How serious is the strong CP problem

- In the SM the CKM phase is order 1 but  $\bar{\theta} = \theta \arg \left[ \det \left( Y_u Y_d \right) \right] \lesssim 10^{-10}$
- Is this a problem? Not necessarily, different spurions at tree level they are orthogonal, as exploited in Nelson-Barr type of models
- At 7 loops the EDM receives log-div contributions but it is tiny, and the finite contribution predicts  $\bar{\theta} \sim 10^{-16}$  so it doesn't look like a serious problem at the moment, similar to the flavor problem …
- In fact in Nelson-Barr the two CP phases are related but not in axion models …

So what's next?

Briefly describe 2 models that avoid the above issues:

# *Zn* QCD axion model

Hook (2018) See also: Di Luzio, Gavela, Quilez & Ringwald (21)

# Relaxed-(QCD)-relaxion

Relaxion idea: Graham, Kaplan & Rajendran (15) QCD-relaxion: Abhishek Banerjee & Joshua Eby, [2210.05690](https://arxiv.org/abs/2210.05690)  Relaxed-relaxion: Banerjee, Kim, Matsedonski, GP, Safranova (20)

# Axion searches with clocks

Kim & GP, [2205.12988](https://arxiv.org/abs/2205.12988)

# Magical *Zn* QCD axion model

The model based on *N* copies of the SM:

*N*

$$
\mathcal{L} = \sum_{k=1}^{N} \mathcal{L}_{\text{SM}}^{k} + \Phi \sum_{k} Q_{k} Q_{k}^{c} \exp(2\pi i k/N), \ \langle \Phi \rangle = (f_{a} + \rho) \exp(ia/f_{a})/\sqrt{2}
$$

Under the  $U(1)$  and  $Z_N$  sym':  $\mathscr{L}_{\text{SM}}^i \to \mathscr{L}_{\text{SM}}^{i+1}, \quad Q_i^{(c)} \to Q_{i+1}^{(c)}, \quad \Phi \to e^{2\pi i/N} \Phi \text{ and } Q_i \to e^{i\theta} Q_i, \quad \Phi \to e^{-i\theta} \Phi$ 

Resulting with the following change to the QCD axion potential:

$$
V(a) \approx -\Lambda_{\text{QCD}}^4 \cos\left(\frac{a}{f} + \bar{\theta}\right) \Rightarrow -\left(\frac{m_u}{m_d}\right)^N \Lambda_{\text{QCD}}^4 \cos\left(\frac{Na}{f} + \bar{\theta}\right)
$$

It achieves: (i) high quality; (ii) allow to go above the QCD line: 1 *f* ≫ *ma*  $\Lambda_\text{QCD}^2$ 

# (*Zn*)QCD axion parameter space



### The relaxion mechanism in a nutshell

Graham, Kaplan & Rajendran (15)

#### Relaxion mechanism (inflation based, slow rolling)

Graham, Kaplan & Rajendran (15)

(*i*) Add an ALP (relaxion) Higgs dependent mass: .





Graham, Kaplan & Rajendran (15)

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Graham, Kaplan & Rajendran (15)

(*i*) Add an ALP (relaxion) Higgs dependent mass: .  $\mu^2(\phi)$  $(\Lambda^2 - g\Lambda\phi) H^{\dagger}H$ (*ii*)  $\phi$  roles till  $\mu^2$  changes sign  $\Rightarrow \langle H \rangle \neq 0 \Rightarrow$  stops rolling.  $V(\phi)$  $\phi$  $\cancel{\phi}$  $\mathcal{L}$  to  $\mathcal{L}$  to  $\mathcal{L}$  to  $\mathcal{L}$  $V(H) = -\mu^2 H^{\dagger} H + \lambda (H^{\dagger} H)^2$  $\langle H \rangle = v \neq 0$ <br> $\langle H \rangle = v \neq 0$ <br>*m<sub>w,z</sub>*  $\neq 0$  $\bigwedge$  $\mu^2 > 0 \Rightarrow$  at present:  $|V(H)|$ *H*  $V(H)$ *H*  $\mu^2(\phi)=0$ evolution  $\frac{b_{a_{c_{k_{c_{a_{c_{k_{c}}}}}}}}}{\mu_{\beta}}$ *μ*<sup>2</sup> *<sup>b</sup>* <sup>|</sup>*H*<sup>|</sup> 2 cos(*ϕ*/*<sup>f</sup>* )

Successful if  $\mu^2(\phi_{\text{stop}}) \ll \Lambda^2$ 

# However the model suffers from a quality problem and fails to solve the strong CP problem Flacke, Frugiuele, Fuchs, Gupta & GP (16)

Davidi, Gupta, GP, Redigolo & Shalit (17)

# High quality (classical) solution to the QCD relaxion problem

Banerjee, Eby & GP, last month

The relaxion is based on two breaking of the shift symmetry

The Rolling potential and the backreaction potential

As seen the stopping condition is when the derivative of the Rolling potential is equal to the one of the backreaction potential, where QCD axion require the the axion settles at the minimum of its potential  $\Rightarrow a/f_a \approx \pi/2$ Banerjee, Kim, Matsedonski, GP, Safranova (20)

This is incompatible unless one is giving up on classical evolution, which my force us to think about the measure problem & eternal inflation

Nelson & Prescod-Weinstein (17) Gupta (18) Chatrchyan & Servant (22)

# Combine ingredients to avoid the QCD relaxion CP problem

Banerjee, Eby & GP, last month

- Assume *Z4N* sym' QCD relaxion model, say *Z4* and make the backreaction dominated by a single sector, *k,* which is not the SM.
- As we showed, the relaxion will stop the evolution at  $\bar{\theta}_k \sim \pi/2$
- Consider for instance having the SM at the *N*th site and the site with the  $\bigcirc$ dominant backreaction on the site after:

$$
V(\bar{\theta}) \sim -\Lambda_{\text{QCD'}}^4 \cos(\bar{\theta} + a/f + \pi/2) \iff \mathcal{L}_k = (\bar{\theta} + a/f_a + \pi/2) \frac{1}{32\pi^2} G' \tilde{G}' \implies (a/f_a)_{\text{relax}} \approx -\bar{\theta}
$$

 $\Theta$  If this is just the sector after the SM then the SM will have

$$
\mathcal{L}_{\text{SM}} = (\bar{\theta} + a/f_a) \frac{1}{32\pi^2} G\tilde{G}
$$
, solving the strong CP problem.

Let's highlight two interesting effect the first is just related to the fact that the QCD axion coupled quadratically to masses:

#### Oscillations of energy levels induced by QCD-axion-like DM  $\frac{1}{2}$  induced by  $\Omega$   $\Omega$  axion like  $\overline{\text{DM}}$ plinduced by QCD-axion-like Divi

Kim & GP, last month the GP, last month

- Consider axion model \w  $(\alpha_s/8)$   $(a/f)$   $G\tilde{G}$  coupling, usually searched by magnetometers
- However, spectrum depends on  $\theta^2 = (a(t)/f)^2 : m_\pi^2(\theta) = B$  $\overline{\phantom{a}}$  $m_u^2 + m_d^2 + 2m_u m_d \cos \theta$ Brower, Chandrasekharanc, Negele & Wiese (03)

$$
\text{MeV} \times \theta^2 \bar{n}n \Rightarrow \frac{\delta f}{f} \sim \frac{\delta m_N}{m_N} \sim 10^{-16} \times \cos(2m_a) \times \left(\frac{10^{-15} \text{eV}}{m_\phi} \frac{10^9 \text{GeV}}{f}\right)^2 \quad \text{vs} \quad m_N \frac{a}{f} \bar{n} \gamma^5 n \Rightarrow (f \ge 10^9 \text{GeV})_{\text{SN}}
$$

It's exciting as clocks (& EP tests) are much more precise than magnetometers  $\frac{1}{\sqrt{1-\frac{1$ dark matter (Duniverse Commission universe commission universe [10]. In the present universe commission universe commission universe commission universe commission universe commission universe commission universe commissio electron or QCD masses to precision of better than 1:10<sup>18</sup> !  $\frac{eVe}{\sqrt{a}}$ <br> $(a/fe)^2$ <br> $\frac{2m_a}{s}$ <br>**f** en They can sense oscillation of energy level due to change of mass of the

#### Oscillations of energy levels induced by QCD-axion-like DM

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$$
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$$
\n
$$
\frac{10^{-7}}{10^{-10}}
$$
\n
$$
\text{Kim} \& \text{GP (22)}
$$
\n
$$
\text{H/S1}
$$
\n
$$
\frac{\delta m_\pi^2}{m_\pi^2} \approx \frac{1}{4} \theta^2
$$
\n
$$
\frac{\delta m_N}{m_N} \simeq 0.13 \frac{\delta m_\pi}{m_\pi}
$$
\n
$$
\frac{\delta f_{\text{Th}}}{f_{\text{Th}}} \simeq 2 \times 10^5 \frac{\delta m_\pi^2}{m_\pi^2}
$$
\n
$$
\frac{10^{-22}}{10^{-24}} \frac{10^{-22}}{10^{-22}} \frac{10^{-20}}{10^{-20}} \frac{10^{-18}}{10^{-16}} \frac{\text{eV}}{10^{-16}} \frac{\text{eV}}{\text{SIN}} \frac{\text{SIN}}{\text{SIN}} \frac{f = M_{\text{Pl}}}{f_{\text{Pl}}}
$$
\n
$$
\frac{\text{eV}}{f_{\text{Pl}} \cdot f_{\text{Pl}}}} \approx 0.13 \frac{\delta m_\pi}{m_\pi}
$$
\n
$$
\frac{\delta f_{\text{Th}}}{f_{\text{Pl}}} \simeq 2 \times 10^5 \frac{\delta m_\pi^2}{m_\pi^2}
$$
\n
$$
\frac{10^{-22}}{10^{-24}} \frac{10^{-22}}{10^{-22}} \frac{10^{-20}}{10^{-20}} \frac{10^{-18}}{10^{-16}} \frac{10^{-16}}{10^{-14}} \frac{10^{-12}}{10^{-12}} \frac{10^{-10}}{10^{-16}} \frac{10^{-8}}{10^{-8}}
$$
\n
$$
m \text{ [eV]}
$$

#### Pheno #2

The 2nd is due to the fact that the min' of relaxion potential deviates from  $\pi/2$ 



#### the nucleon in the phase of a CP-violating phase of a  $T_{\rm eff}$  axion also induces a scalar interaction also induces a scalar interaction with  $T_{\rm eff}$

the form of

Let me highlight two interesting effect the first is just related to the fact that the QCD axion coupled quadratically to masses: see next page the form of th<br>The form of the form of th resung encer are morns past related to the current constraint on *<sup>|</sup>g<sup>a</sup>* range of *<sup>|</sup>g<sup>a</sup>*  $\mu$  and  $\mu$  *m i masses.* See heat page  $r^2$ the fact that the

The 2nd is due to the fact that the min' of relaxion potential deviates from pi/2.  $t_0$  the foot that the min' of notarious potential deviate  $\alpha$  to the fact that the min of relaxion potential deviates *md*)<sup>2</sup> ' 0*.*22 , we obtain *g*<sup>1</sup> *M*<sub>N</sub> *M*<sup>*N*</sup> *M*<sub>N</sub> 101 *m*<sup>*N*</sup> *f f .* (*II*.25) *f* 2 11 . *<sup>|</sup>g<sup>a</sup>*

The QCD axion also induces a scalar interaction with the nucleon in the presence of a CP-violating phase of the form of *m*<sub>d</sub> *m*  $\frac{1}{2}$  *m* alar interaction with the nucleon in the presence of a CP-violating phase of the form of

$$
g_{\phi NN} \simeq 1.3 \times 10^{-2} \, \frac{m_N}{f} \delta_\theta \, .
$$
 
$$
\frac{9 \times 10^{-24}}{f_{11}} \lesssim g_{\phi NN} \lesssim \frac{4 \times 10^{-23}}{f_{11}},
$$

where,  $f_{11} = f/(10^{11} \text{ GeV})$  and we have used m<sub>N</sub> ~ 1 GeV. The strongest bound on  $g_{\phi N}$  or comes from the experiments looking for the existence of the SM are used  $\lim_{N \to \infty}$  of  $V$ . The strongest bound on *g*<sub>*QNN</sub>*  $N$  comes from the experiments fooking for the existence of equivalence principle (EP). The bound from EP violation searches, for the axion mass aroun</sub> rathe cuistance of fifth force and/or violation of equivalence principle (EP). The bound from EP violation searches, for the axion mass around  $10^{-6}$  eV, is  $g_{\phi NN}$ ?  $10^{-21}$ higher powers of *<sup>f</sup> <sup>N</sup>* . Therefore within a factor of *<sup>O</sup>*(few) where,  $f_{11} = f/(10^{11} \text{ GeV})$  and we have used m<sub>N</sub> ~ 1 GeV. The strongest bound on  $g_{\phi N}$  N comes from the experiments lo

pseudoscalar and axion-nucleon scalar cou seudoscalar and axion-nucleon scalar coupling which will be probed by Ariadne There's also a bound for axion-proton pseudoscalar and axion-nucleon scalar coupling which will be probed by Ariadne B. Direct searches for a Z4*N*  $\alpha$   $\alpha$   $\alpha$   $\alpha$ cally send axion-pucleon scalar coupling which will be  $\frac{1}{2}$ 

$$
\frac{4 \times 10^{-35}}{f_{11}^2} \lesssim |g_p^a g_{\phi NN}| \lesssim \frac{2 \times 10^{-34}}{f_{11}^2} \, .
$$

current constraint on *<sup>|</sup>g<sup>a</sup>*

*<sup>e</sup> <sup>g</sup>NN <sup>|</sup>* . <sup>5</sup>*.*7⇥10<sup>32</sup> in the mass

### Pheno

Finally it could be probed by combination of scalar oscillation as well as pseudo scalar …

- Ultralight dark matter (ULDM) of spin-0 particles are challenging
- $\odot$  Strong CP + hierarchy problem, why the QCD relaxion doesn't work
- Hook's *Zn* high quality ultra light QCD axion model
- A high quality *Z4n* QCD relaxion model via the concept of relaxed relaxion
- Exciting phenomenology, possibly involving breaking of CP, can be probed with clocks due to their extreme precision

*Backups*

# The model requirements and parameters

We need to make the *N*+1'th site to dominate the backreaction we do it by

breaking the sym' choosing 
$$
\gamma \equiv v/v' \sim 0.1 - 0.001
$$
 and  $\epsilon_b \equiv \frac{y_u \Lambda_{QCD}^3}{y_u' \Lambda_{QCD'}^3} \lesssim \gamma$ 

The leading deviation from  $\bar{\theta}_{N-1} = \pi/2$  is coming from two sources: the fact that  $\delta \neq 0 \Rightarrow \bar{\theta} \geq \delta \sim 10^{-11} \sqrt{\frac{\gamma}{\epsilon}}$ *ϵb*  $\left[\Delta v^2/v^2 = g\Lambda f/v^2 = g\Lambda^3 f/v^2\Lambda^2 \sim \Lambda_{\rm br}^4/v^2\Lambda^2 \sim y_u\Lambda_{\rm QCD}^3/\Lambda^2 v \equiv \mu_{\rm br}^2/\Lambda^2\right] \equiv \delta^2$ 

and that the other contributions push toward  $\bar{\theta}$ *N*  $=$   $\pi/2$ 

 $\bullet$  We can't switch the two off (nor we want) in particular: suppressing tunneling (+ quantum):  $\Delta V \sim \Lambda_{\text{back}}^4 \delta^3 \equiv \left( m_u^{\prime} \Lambda_{\text{QCD}}^3 \right)$ 4  $\delta^3 \gg H_I^4$ 

Ensuring inflation domination  $H_I^2 \gg \Lambda^4 / M_{\rm Pl}^2 \Rightarrow \Lambda_{\rm back}^4 (\mu_{\rm back}^2 / \Lambda^2)$ <sup>3</sup> ≪ Λ<sup>8</sup>/Μ<sup>4</sup><sub>Pl</sub>

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# Relaxion and cosmology

Must not disturb inflation  $H^2 > \Lambda^4 / M_{\rm Mpl}^2$ 

 $\Theta$  Dominated by classical evolution  $H < \dot{\phi}/H \sim V'/H^2 \lesssim v^4/fH^2 \Rightarrow \Lambda < f < v^4/H^3$ 

$$
\bullet
$$
 Combining the two  $\Lambda \lesssim M^{\frac{3}{7}}v^{\frac{4}{7}} \sim 10^8 \,\text{GeV}$ 

There is also an interesting relation between the cutoff and the number of e-folds

$$
\Delta \phi \sim F \quad \Rightarrow \quad N_{\rm ef} \sim F/\dot{\phi} \times H \sim FH^2/V' \sim F^2H^2/\Lambda^4 \gtrsim F^2/M_{\rm Pl}^2
$$

$$
\sim (\Lambda/\nu)^8 f^2 / M_{\rm Pl}^2 \gtrsim \Lambda^{10} / \nu^8 M_{\rm Pl}^2 \sim \left(\frac{\Lambda}{100 \,\text{TeV}}\right)^{10}
$$

# Relaxed relaxion & some pheno

### Relaxion's naive parameters (similar to ALP, backreaction domination)

$$
m_{\phi}^2 \sim \partial_{\phi}^2 V_{br}(\phi, h) \sim \frac{\mu_b^2 v_{EW}^2}{f^2} \cos \frac{\phi_0}{f}
$$
\n
$$
\sim 1
$$
\nThe relaxation is light and mixes with the Higgs  
\n
$$
\sin \theta_{h\phi} \sim \partial_{\phi} \partial_h V_{br}(\phi, h) / v_{EW}^2 \sim \frac{\mu_b^2}{f v_{EW}} \sin \frac{\phi_0}{f}
$$
\n
$$
\sim 1
$$
\n
$$
\text{The relaxation is light}
$$
\n
$$
\text{and mixes with the Higgs}
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\n
$$
\text{and mixes with the Higgs}
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\n
$$
\text{and mixes with the Higgs}
$$
\n
$$
\text{and gives } \sin \theta_{h\phi} \sim \partial_{\phi} \partial_h V_{br}(\phi, h) / v_{EW}^2 \sim \frac{\mu_b^2}{f v_{EW}} \sin \frac{\phi_0}{f}
$$

Naively: mixing angle in terms of mass  $\hspace{1mm} \sin \theta_{h\phi} \sim$  $m_\phi$ *v*EW  $\mu_b$ *v*EW

Maximum mixing angle 
$$
(\sin \theta_{h\phi})_{\text{max}} \sim \frac{m_{\phi}}{v_{\text{EW}}}
$$
 Naturalness  
Minimum mixing angle  $(\sin \theta_{h\phi})_{\text{min}} \sim \frac{m_{\phi}^2 \Lambda_{\text{min}}}{v_{\text{EW}}^3}$ 

#### The relaxion's naive parameter space



# The log crisis

Lesson 1 - finding NP requires diverse approach, searches across frontier

Lesson 2 - experimentally, worth checking where many decades are covered:



### Less naive treatment, the relaxed relaxion

$$
V(\phi, h) = \left(\Lambda^2 - \Lambda^2 \frac{\phi}{F}\right) |H|^2 - \frac{\Lambda^4}{F} \phi - \mu_b^2 |H|^2 \cos \frac{\phi}{f} \qquad v^2(\phi) = \begin{cases} 0 & \text{when } \phi < f_{\text{eff}} \\ > 0 & \text{when } \phi > f_{\text{eff}} \end{cases}
$$

Relaxion stopping point determines the EW scale

$$
\frac{\Lambda^4}{F} \sim \frac{\mu_b^2 v_{\rm EW}^2}{f}
$$

Higgs mass change for 
$$
\Delta \phi = 2\pi f
$$
  $\frac{\Delta v^2}{v^2} \sim \frac{\Lambda^2}{F} \frac{f}{v^2} \sim \boxed{\frac{\mu_b^2}{\Lambda^2}} \equiv \delta^2 \ll 1$ 

$$
V_{\rm br} = -\mu_{\rm b}^2 |H|^2 \cos\frac{\phi}{f} \qquad \Longrightarrow \qquad \text{Potential height grows} \qquad
$$

### Stopping condition, fine resolution

Banerjee, Kim, Matsedonski, GP, Safranova (20)

$$
\left(V_{\phi}' = 0 \Rightarrow \sin \theta = \frac{v_{\text{EW}}^2}{v^2(\phi)} + \frac{v_{\text{EW}}^2}{\Lambda^2}\right) \quad \implies \quad \left(\frac{\phi_0}{f} \sim \frac{\pi}{2} \text{ upto resolution factors}\right)
$$



#### Stopping condition, fine resolution

Banerjee, Kim, Matsedonski, GP, Safranova (20)



#### Relaxed mass => natural violation of naturalness bound

Banerjee, Kim, Matsedonski, GP, Safranova (20)

Max. Mixing angle: 
$$
\sin \theta_{h\phi}^{\text{max}} = \left(\frac{m_{\phi}}{v_{EW}}\right)^{\frac{2}{3}} \gg \left(\frac{m_{\phi}}{v_{EW}}\right)_{\text{naturalness}}
$$



# Quality problem, 5th force vs EP violation, electron coupling



EP: Planck suppressed operators are excluded for  $m_\phi \lesssim 10^{-6}$  eV 5th force: *operators are excluded for*  $10^{-19} \lesssim m_\phi \lesssim 10^{-13} \, {\rm eV}$ 

# Quality problem, 5th force vs EP violation, gluon



EP: Planck suppressed operators are excluded for  $m_\phi \lesssim 10^{-5}\, \text{eV}$ **5th force:** *operators are excluded for* $m_{\phi} \lesssim 10^{-3}$  **eV** 

#### QCD low energy (2 gen ignoring eta')  $OCD$  low aposary  $(2 \cos \theta \sin \pi \sin \pi \sin \pi \sin^{2} \theta)$ **Predictions, and Ref. [5] provide good interest.**  $\bigcap_{i=1}^n \bigcap_{i=1}^n \bigcap_{i=1}^n$ QCD low energy (2 gen ignoring eta') <sup>2</sup> ✏*<sup>µ</sup>*⌫⇢*G*⇢. ✓ plays no roll in this subsection and will be ignored for now. This theory has an *SU*(3)

At low energies:

and spurions transform as

At low energies: 
$$
\mathcal{L} \supset \frac{\theta g_s^2}{32\pi^2} G\tilde{G} + qMq^c, \qquad M = \begin{pmatrix} ,m_u & 0 \\ 0 & m_d \end{pmatrix}
$$



 $\langle qq^c \rangle \neq 0$ , Breaks SU(2) L x R  $\langle qq^c \rangle \neq 0, \qquad$  Breaks SU(2) L x R to diagonal

# **Summer Chiral Goldstone action**

*<sup>a</sup>*

$$
U=e^{i\frac{\Pi^{a}}{\sqrt{2}f\pi}\sigma^{a}},
$$

*<sup>i</sup>* ⇧*<sup>a</sup>*

$$
\begin{array}{ccc} \bar{C} & \stackrel{-}{\leftarrow} & \stackrel{\vee}{\leftarrow} & \stackrel{J}{\leftarrow} & \stackrel{J}{\leftarrow}
$$

 $\mathbb{R}^n$  and  $\mathbb{R}^n$  and this symmetry, the corresponding pseudo-Goldstone boson,  $\mathbb{R}^n$ 

$$
\mathcal{L} = f_{\pi}^2 \operatorname{Tr} \partial_{\mu} U \partial^{\mu} U^{\dagger} + a f_{\pi}^3 \operatorname{Tr} MU + h.c.,
$$

#### Axial sym transformation  $t$  is thus, we wish to find a constant under which we can take the  $t$

 $u \rightarrow e^{i\alpha}u, \qquad u^c \rightarrow e^{i\alpha}u^c$ *,* (17) *<sup>u</sup>* ! *<sup>e</sup><sup>i</sup>*↵*u, u<sup>c</sup>* ! *<sup>e</sup><sup>i</sup>*↵*u<sup>c</sup>*  $u \rightarrow e u,$  $u \to e^{i\alpha}u, \qquad u^{\circ} \to e^{i\alpha}u^{\circ},$ as mentioned in the previous subsection, the *U*(1)<sup>A</sup> symmetry is not a good symmet



 $u \to e^{i\alpha}u$ ,  $d \to e^{i\alpha}d$ ,  $\theta \to \theta - 2\alpha$ .  $u \to e^{i\alpha}u$ ,  $d \to e^{i\alpha}d$ ,  $\theta \to \theta - 2\alpha$ .  $A$ s in the case of non-zero quark masses, broken symmetries are still useful in constraining how the intervals of  $\alpha$ *<sup>U</sup>* / *qq<sup>c</sup>* transforms. Thus there is an anomalous symmetry  $\dot{a}\alpha$  $u \to e^{i\alpha}u, \qquad d \to e^{i\alpha}d, \qquad \theta \to \theta - 2\alpha.$ 

 $U \to e^{i\alpha} U,$   $M \to e^{-i\alpha} M.$  $U \to e^{i\alpha} U, \qquad \qquad M \to e^{-i\alpha} M.$ Note that there are several important di↵erences between ✓ as a spurion and *M* as a spurion. A major di↵erence  $U \to e^{i\alpha} U, \qquad M \to e^{-i\alpha} M.$  $U \rightarrow e^{i\alpha}U,$   $M \rightarrow e^{-i\alpha}M.$ 

### Removing the GGdual coupling, phase freedom The pion mass . We first obtain a formula formula formula formula formula formula formula formula formula formula<br>The pion as a function of the pion as a function of the pion as a function of  $\alpha$  formula formula formula

$$
U = e^{i\pi^a \tau^a/f_\pi} = \cos\frac{|\vec{\pi}|}{f_\pi} + i\frac{\pi^a}{|\vec{\pi}|}\tau^a \sin\frac{|\vec{\pi}|}{f_\pi}.
$$
  
\n
$$
u \rightarrow e^{i\phi_u}u
$$
  
\n
$$
d \rightarrow e^{i\phi_d}d,
$$
  
\n
$$
U_0 = \begin{pmatrix} e^{i\phi_u} & 0 \\ 0 & e^{i\phi_d} \end{pmatrix}.
$$

$$
V = -B_0 \text{Tr}[(MU_0)U + (MU_0)^\dagger U^\dagger] = -B_0 \left[ 4A \cos \frac{|\vec{\pi}|}{f_\pi} - 4D \frac{\pi^3}{|\vec{\pi}|} \sin \frac{|\vec{\pi}|}{f_\pi} \right].
$$

$$
D = \frac{1}{2} \text{Tr} \left[ \tau^3 \begin{pmatrix} m_u \sin \phi_u & 0 \\ 0 & m_d \sin \phi_d \end{pmatrix} \right] = \frac{1}{2} (m_u \sin \phi_u - m_d \sin \phi_d) = 0
$$

#### **QCD** parameter space  $\frac{1}{2}$  $\mathbf{r}$  space **D** paramete **a** (*m<sup>u</sup>* sin *<sup>u</sup> m<sup>d</sup>* sin *d*)=0 (12)

$$
\sin \phi_u = \frac{m_d \sin \theta}{[m_u^2 + m_d^2 + 2m_u m_d \cos \theta]^{1/2}}
$$
\n
$$
\sin \phi_d = \frac{m_u \sin \theta}{[m_u^2 + m_d^2 + 2m_u m_d \cos \theta]^{1/2}}
$$
\n
$$
\cos \phi_u = \frac{m_u + m_d \cos \theta}{[m_u^2 + m_d^2 + 2m_u m_d \cos \theta]^{1/2}}
$$
\n
$$
\cos \phi_d = \frac{m_d + m_u \cos \theta}{[m_u^2 + m_d^2 + 2m_u m_d \cos \theta]^{1/2}}.
$$

$$
A = \frac{1}{2} \text{Tr} \begin{pmatrix} m_u \cos \phi_u & 0 \\ 0 & m_d \cos \phi_d \end{pmatrix} = \frac{1}{2} (m_u \cos \phi_u + m_d \cos \phi_d).
$$

# The QCD line

$$
m_a \sim \frac{1}{f} \times \Lambda_{\text{QCD}}^2
$$
 or  $m_a \sim g_{\text{gluon}} \times \Lambda_{\text{cutoff, shifting}}^2$ 

$$
m_a \gtrsim g_{\text{gluon}} \times \Lambda_{\text{cutoff, shiftingym}}^2
$$
 or  $1/f \lesssim m_a/\Lambda_{\text{QCD}}^2$ 

It is not hard to go naturally below the QCD line but it is very hard to go above it.

# The QCD line



Most minimal model would be just a free massive scalar :

$$
\mathcal{L} \in m_{\phi}^2 \phi^2, \rho_{\text{Eq}}^{\text{DM}} \sim \text{eV}^4 \sim m_{\phi}^2 \phi_{\text{Eq}}^2 = m_{\phi}^2 \phi_{\text{init}}^2 (\text{eV}/T_{\text{osc}})^3
$$

$$
T_{\text{os}} \sim \sqrt{M_{\text{Pl}} m_{\phi}} \implies \phi_{\text{init}} \sim M_{\text{Pl}} \left(\frac{10^{-27} \text{eV}}{m_{\phi}}\right)^{\frac{1}{4}}
$$

(can add a few more bounds, SR, isogurvature but still large parameter space, reasonable field excursion)

Just remind you that if we add Planck suppressed operators then we did find bounds …

Also, in the presence of these coupling if it's too light there will be naturalness issues …

# The relaxion DM dynamical missalignment

Banerjee, Kim & GP (18)

◆ Basic idea is similar to axion DM:



◆ Basic idea is similar to axion DM (but avoiding missalignment problem): After reheating the wiggles disappear (sym' restoration):



◆ Basic idea is similar to axion DM (but avoiding missalignment problem):

After reheating the wiggles disappear: and the relaxion roles a bit.



◆ Basic idea is similar to axion DM (but avoiding missalignment problem):

After reheating the wiggles disappear: and the relaxion roles a bit.



When the universe cools the electroweak symmetry is broken, brings back the wiggles.



When the universe cools the electroweak symmetry is broken, brings back the wiggles.



When the universe cools the electroweak symmetry is broken, brings back the wiggles.



When the universe cools the electroweak symmetry is broken, brings back the wiggles.



◆ Basic idea is similar to axion DM (but avoiding missalignment problem):



#### relaxion DM+GW

DM window



 $\frac{1}{2}$  GWs in  $\mu$ Ares (green) or SKA (blue/turquoise). The light shading and solid lines indicate points that can be probed for a subrange of  $\frac{1}{2}$  plane. The red and original plane in the region of the maint single shading and some most mass mateur points and our proceed for a subtange of compiled  $\frac{1}{2}$ . regions inside the viable dark matter space can be probed via gravitational waves in *µ*Ares (green) or SKA (blue/turquoise). The black solid line encompass the DM relaxion parameter space. The colored regions inside the viable DM space can be probed via reappearance temperatures, whereas the darker shaded parts enclosed by dotted lines are accessible for all valid *T*ra.

# Equivalence principle (EP) tests, prelim

Consider the following effective action for scalar DM:  $\mathcal{L}_{\phi} \in d_{m_e}$ *ϕ*  $M_{\rm Pl}$  $m_e\bar{e}e + d_g$ *ϕ*  $2gM_{\rm Pl}$ *βgGG*

The leading action in the non-relativistic limit, say, of the electron is

$$
\mathcal{L}_e^{\text{NR}} = m_e(\phi) + \frac{1}{2}m_e v^2 = m_e^0 + d_{m_e} \frac{\phi}{M_{\text{Pl}}} \Rightarrow a = d_{m_e} \frac{\phi'}{M_{\text{Pl}}}
$$

Inside an atom we can rewrite it as:

$$
\mathcal{L}_{\text{atm}}^{\text{NR}} = M_{\text{Nuc}}(\phi) + N m_e(\phi) + B \Rightarrow M_{\text{atm}} a = \phi' \left( \partial_{\phi} M_{\text{Nuc}}(\phi) + N \partial_{\phi} m_e(\phi) \right) \Rightarrow a = \phi' \partial_{\phi} \ln M_{\text{atm}} \equiv \sqrt{G_N} \phi' \alpha_{\text{atm}}
$$

which can be readily generalised to any system.

For a test particle at distances such that  $m_{\phi}R \ll 1$  and say  $R \gtrsim R_{\rm Earth}$  have  $\phi' \propto 1/R^2$  and

the acceleration is given by  $a = G_N M_{\text{test}} \alpha_{\text{test}} M_{\text{Earth}} \alpha_{\text{Earth}} / R^2$ 

Damour & Donoghue (10)

# Equivalence principle (EP) tests

- We would compare two bodies, *A* and *B*, to search for a differential acceleration effect via the EotWash parameter  $\frac{\delta a_{AB}}{A}$ *a*  $= \alpha_{\text{Earth}}(\alpha_A - \alpha_B)$
- Or if we switch on one coupling  $d_i$  it is useful to define the corresponding individual "diatonic charge"  $d_iQ_i \equiv \alpha_i$
- The experiment test is very simple, let's search for masses smaller than the inverse size of the Earth then we can use two test bodies on a satellite that are free falling with the satellite and just track them. That's exactly what the Microscope mission is doing some 700km above earth
- After >5 yrs of running they've achieve precision of better than  $\eta_{\rm EP}$  < 10<sup>-14</sup>, which can be translated to the following bounds on generic scalar models

# Equivalence principle (EP) tests

For variety of coupling it can be expressed as:

EP bounds: 
$$
\left(\frac{\delta a_{\text{test}}}{a}\right) < \eta_{\text{EP}} \sim 10^{-14} \Leftrightarrow \left(d_i^{(1)} d_j^{(1)}\right) \Delta Q_i^{\text{test}} Q_j^{\text{Earth}}
$$

$$
\overrightarrow{Q}^{\mathbf{a}} \approx F^{\mathbf{a}} \left( 3 \ 10^{-4} - 4 \ r_I + 8 \ r_Z, 3 \ 10^{-4} - 3 \ r_I, 0.9, 0.09 - \frac{0.04}{A^{1/3}} - 2 \times 10^6 r_I^2 - r_Z, 0.002 \ r_I \right)
$$

Where  $\vec{X} \equiv X_{e,m_e,g,\hat{m},\delta m}$ , with  $\hat{m} \equiv (m_d + m_u)/2$ ,  $\delta m \equiv (m_d - m_u)$ ,  $10^4$   $r_{I;Z} \equiv 1 - 2Z/A; Z(Z-1)/A^{4/3}$ , &  $F^{\bf a} = 931 A^{\bf a} / (m^{\bf a}/\text{MeV})$  with  $A^{\bf a}$ being the atomic number of the atom **a**

$$
\Delta \vec{Q}^{\text{Mic}} \simeq 10^{-3} (-1.94, 0.03, 0.8, -2.61, -0.19)
$$

Tretiak, et al.; Oswald, et al (22)

#### Equivalence principle (EP) tests EP-violating acceleration as discussed in [? ? ].

Banerjee, GP, Safronova, Savoray & Shalit (to appear)



Figure 11. Boundary 11. Boundary 11. Boundary 11. Boundary 11. Boundary and Ton a pure unation the LF-bound Can<br>The avoided deviation from Newtonian Gravity (figure searches) on  $d$  and  $d$  (22)  $d$ Where one can find models that avoid the strongest EP bounds and for a pure dilaton the EP bound can be avoided

Tretiak, et al.; Oswald, et al (22)

### Direct dark matter searches, sensitivity

How do we search for ULDM directly?

Take for example the Lagrangian  $\mathcal{L}_{\phi} \in d_{m_e} \frac{\gamma}{M_{\text{Pl}}} m_e \bar{e}e + d_g \frac{\gamma}{2 \rho M_{\text{Pl}}} \beta_g GG$  and focus first about the electron coupling? *ϕ*  $M_{\rm Pl}$  $m_e\bar{e}e + d_g$ *ϕ*  $2gM_{\rm Pl}$ *βgGG*

The most sensitive way is with clocks, because  $\phi \sim \frac{V + BM}{\cos(m_{\phi} t)}$  then the electron  $2\rho_{\rm DM}$ *m<sup>ϕ</sup>*  $cos(m_{\phi}t)$ 

mass oscillates with time => energy levels oscillates with time:  $E_n \sim m_e \alpha^2 1/2n^2$ 

For instance: 
$$
\Delta E_{21} \sim m_e \alpha^2 1/2 \times 3/4 \times \left[1 + d_{m_e} \frac{\sqrt{2\rho_{DM}}}{m_{\phi} M_{Pl}} \left(\sim 10^{-15} \times \frac{d_{m_e}}{10^{-3}} \frac{10^{-15} \text{ eV}}{m_{\phi}}\right) \times \cos(m_{\phi} t)\right]
$$

# Direct dark matter searches via clocks

Which implies that clocks can win over EP for precision of roughly 1:1015 for about 1 Hz

DM mass

How the clock works: for this school it's just creating a state which is a superposition of the two states and thus oscillates with time and picking up the above phase:  $exp^{i\Delta E(m_e(t))t}$ 

However, to see the effect you need to compare it to another system that would not have

the above precise dependence …

# Enhanced sensitivity

• The most robust coupling is to the gluons:

Mixing with the Higgs, dilaton and even QCD axion have coupling to the gluons How to be sensitive to the coupling to QCD?

Could be via reduced mass, or via g-factor, magnetic moment-spin interactions-hyperfine or vibrational model in molecules, or the queen of all nuclear clock , 229Th

It is super sensitive because  $E_{\text{nu-clock}} \sim E_{\text{nu}} - E_{\text{QED}} \sim 8 \text{ eV} \ll E_{\text{nu}} \sim \text{MeV}$ 

$$
\frac{\Delta E}{E} = \frac{E_{\text{nu}}(t) - E_{\text{QED}}}{E_{\text{nu-clock}}} \Rightarrow \frac{\Delta E_{\text{nu}}(t)}{E_{\text{nu-clock}}} \sim \frac{E_{\text{nu}}}{E_{\text{nu-clock}}} \times d_g \frac{m_N}{M_{\text{Pl}}} \cos(m_\phi t) \sim 10^5 d_g \frac{m_N}{M_{\text{Pl}}} \cos(m_\phi t)
$$