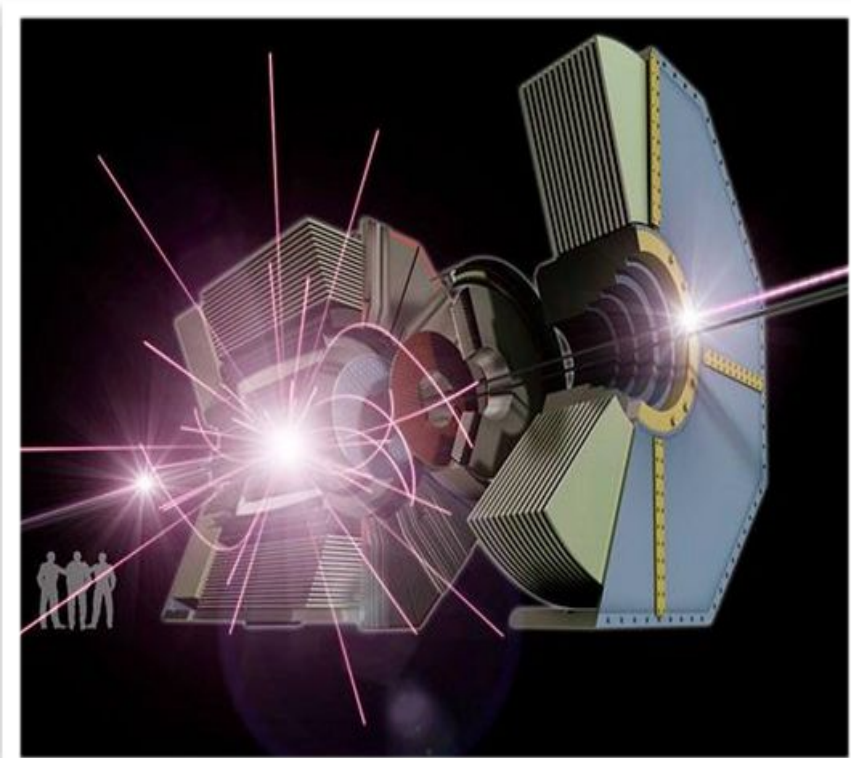
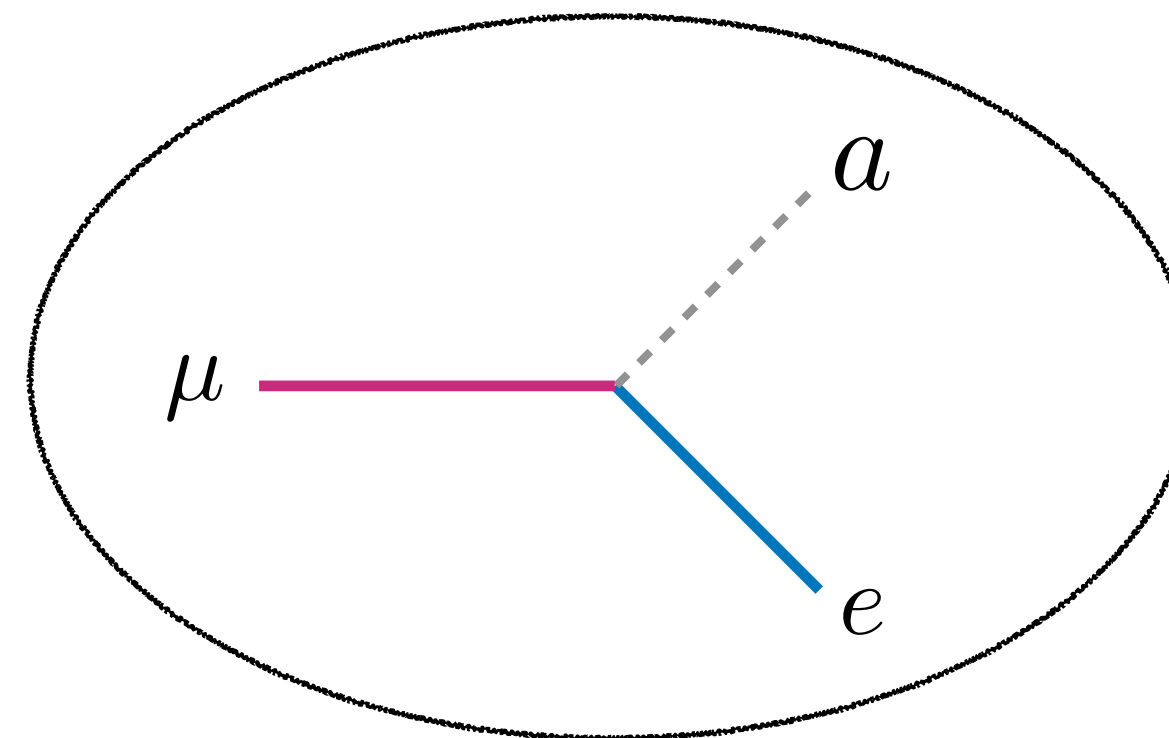


Flavor Probes of Axion Dark Matter

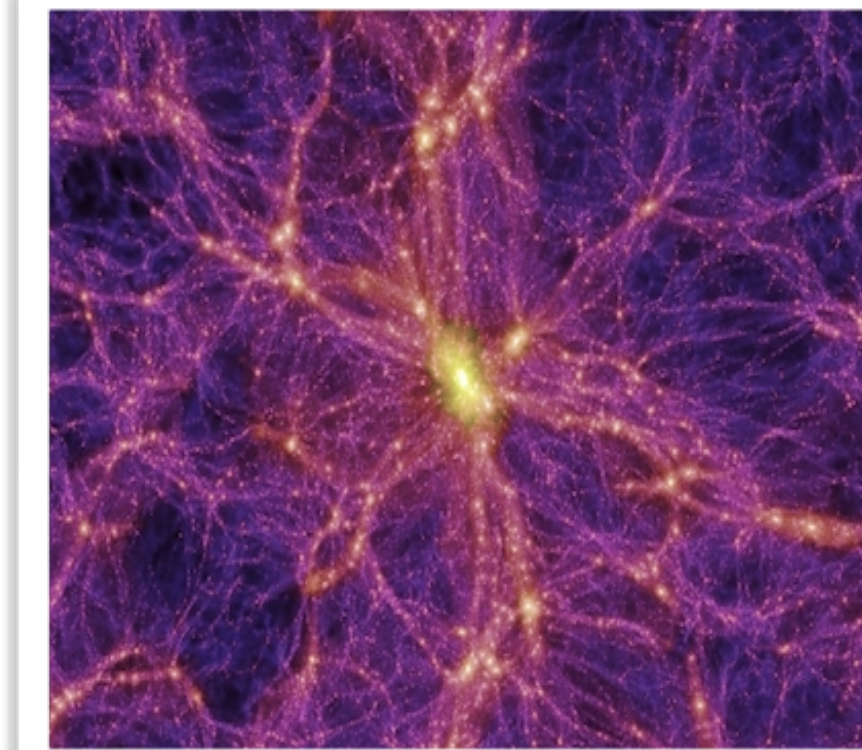
Robert Ziegler



Flavor Factories

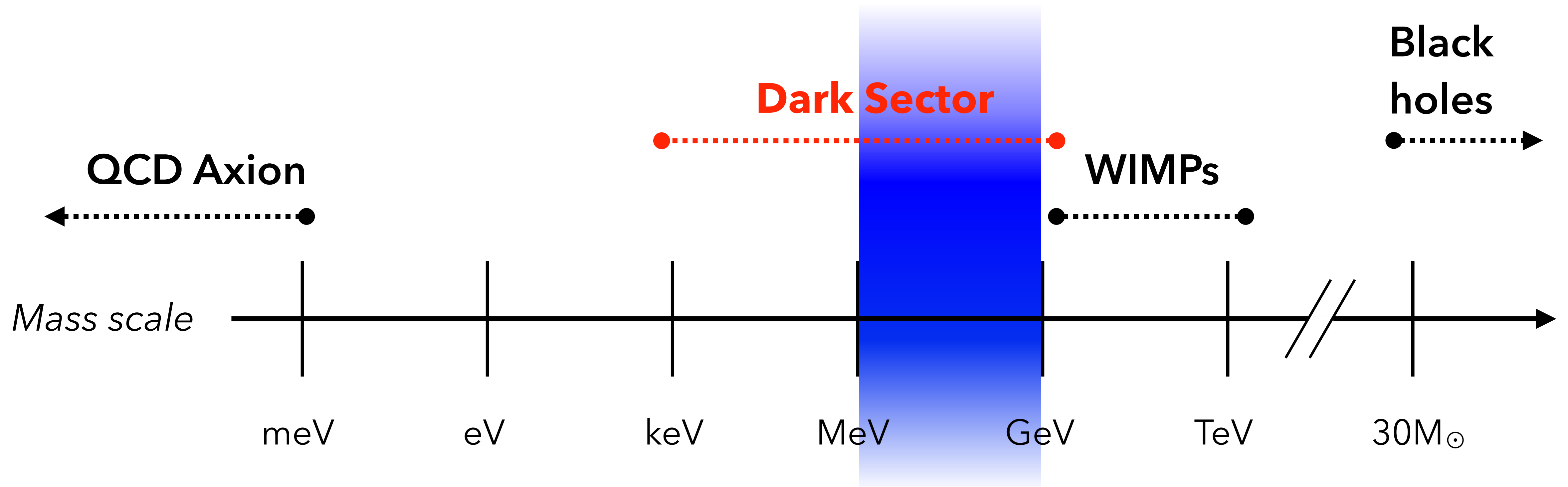


Supernovae



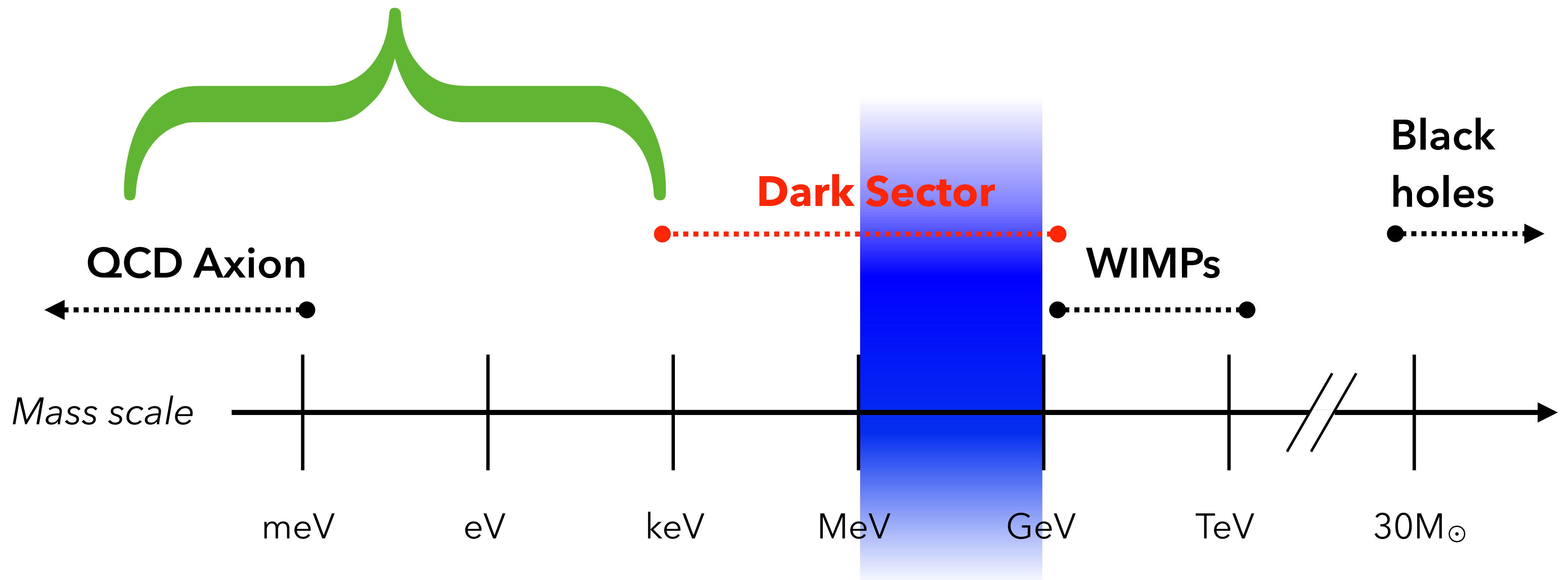
Early Universe

B factories can explore the Dark Sector



B factories can explore the Dark Sector

...and (QCD) Axion Dark Matter!

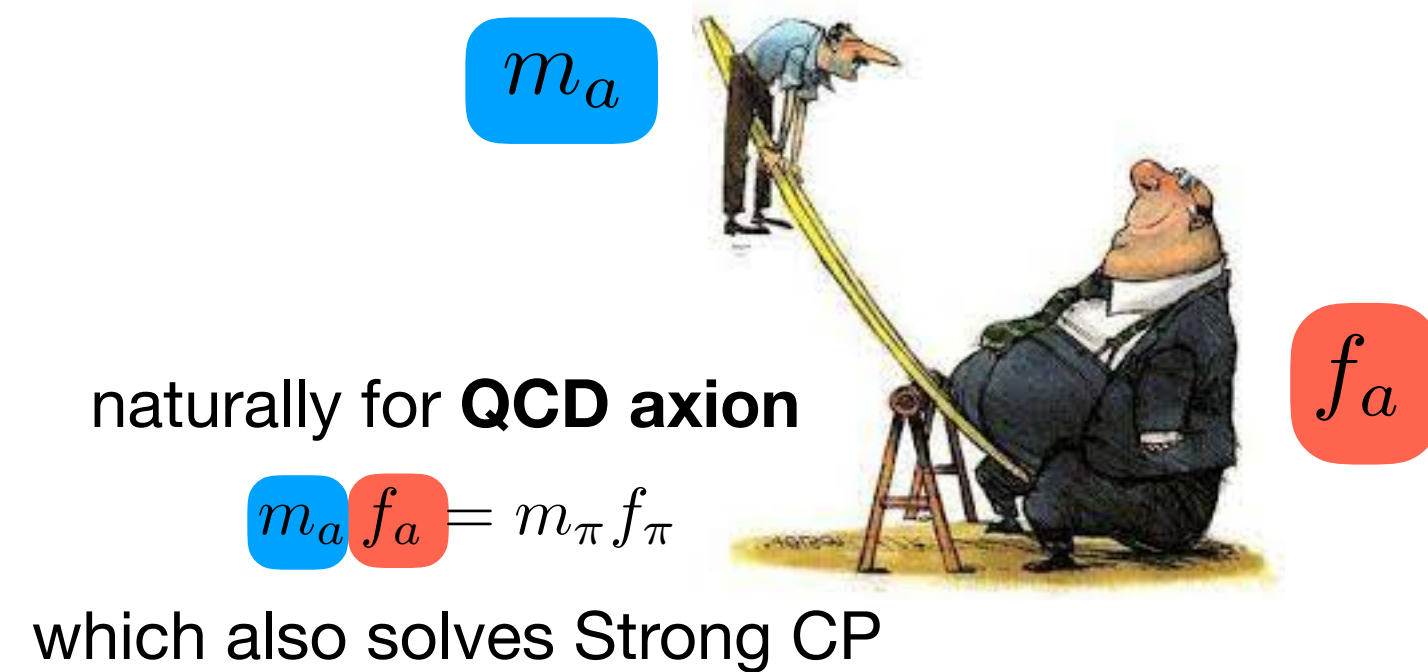


Axion Dark Matter

- ✿ Axions are excellent DM candidates

Pseudo-Goldstone bosons of PQ symmetry **broken at high scales**

↓
light



↓
decoupled

➔ **stable** on cosmological scales

$$1/\Gamma(a \rightarrow \gamma\gamma) \simeq 10^{12} \text{yrs} \left(\frac{f_a}{10^9 \text{GeV}} \right)^2 \left(\frac{\text{keV}}{m_a} \right)^3$$

- ✿ Produced in early universe via misalignment, decays of topological defects, thermal freeze-out, thermal freeze-in, ...

see talk by
J. Jaeckel

Flavor-violating Axions

- ✿ Often ignored, but general axion couplings are flavor-violating!

$$\mathcal{L}_{\text{eff}} = \frac{a}{f_a} \frac{\alpha_s}{8\pi} G\tilde{G} + C_{a\gamma} \frac{a}{f_a} \frac{\alpha_{\text{em}}}{8\pi} F\tilde{F} + \frac{\partial_\mu a}{2f_a} \bar{f}_i \gamma^\mu (C_{ij}^V + C_{ij}^A \gamma_5) f_j$$

proliferates parameters, but enriches phenomenology

- ✿ Allows for axion production from decays of SM particles

e.g. $\mu \rightarrow e a$ $\tau \rightarrow e a$ $K \rightarrow \pi a$ $\Lambda \rightarrow n a$ $B \rightarrow \rho a$...

in precision flavor factories, SN1987A and early universe

↓
direct searches

↓
star cooling

↓
freeze-in

Theoretical Motivation

❖ Two possible sources of flavor-violating axion couplings

1) Tree-level misalignment of PQ charges and Yukawas $[Y_d Y_d^\dagger, \text{PQ}_q] \neq 0$

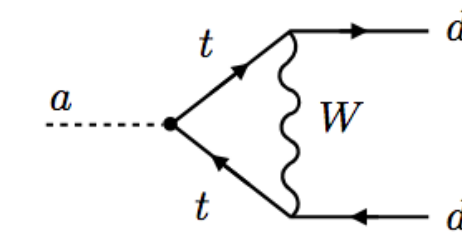
➔ present in non-universal DFSZ models: couplings given by Yukawa misalignment

➔ predictive scenario when PQ = flavor symmetry addressing Yukawa hierarchies

e.g. PQ = FN: $C_{sd} \sim V_{us} \sim 0.2$

Calibbi, Goertz, Redigolo, RZ, Zupan '16; Ema et al '16; Wilczek '82

2) SM flavor violation from RG running Bauer et al '21



$$C_{sd} \sim \frac{y_t^2 V_{td} V_{ts} C_{tt}}{16\pi^2} \log \sim 10^{-5}$$

for light axions flavor constraints weaker than star cooling constraints from diagonal couplings 2201.07805

Axion Production in Flavor Factories

- ✿ Test flavor-violating couplings with **SM decays + missing energy**
look like meson/lepton decays with neutrino pair, but 2-body

Quarks

SM background **tiny**

$$\text{BR}(K \rightarrow \pi \nu \bar{\nu}) \sim 10^{-10}$$

Leptons

SM background **huge**

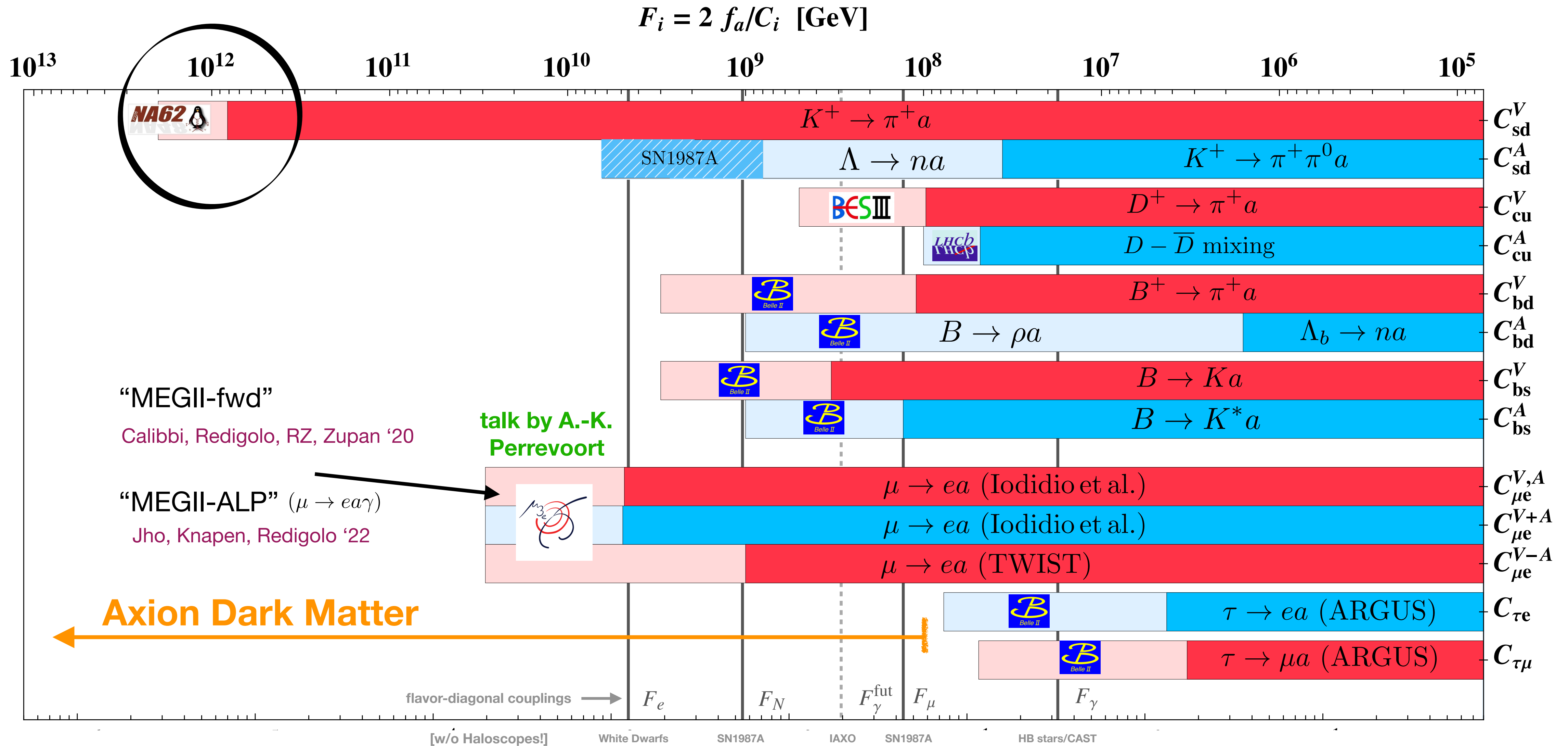
$$\text{BR}(\mu \rightarrow e \nu \bar{\nu}) = 1 \quad [\text{but can profit from polarization}]$$

Experimental analyses of 2-body meson decays are rare \longrightarrow recast
e.g. no bound on $D \rightarrow \pi a, B \rightarrow K^* a, B \rightarrow \rho a$ no BaBar/Belle bound on $B \rightarrow K a, B \rightarrow \pi a$

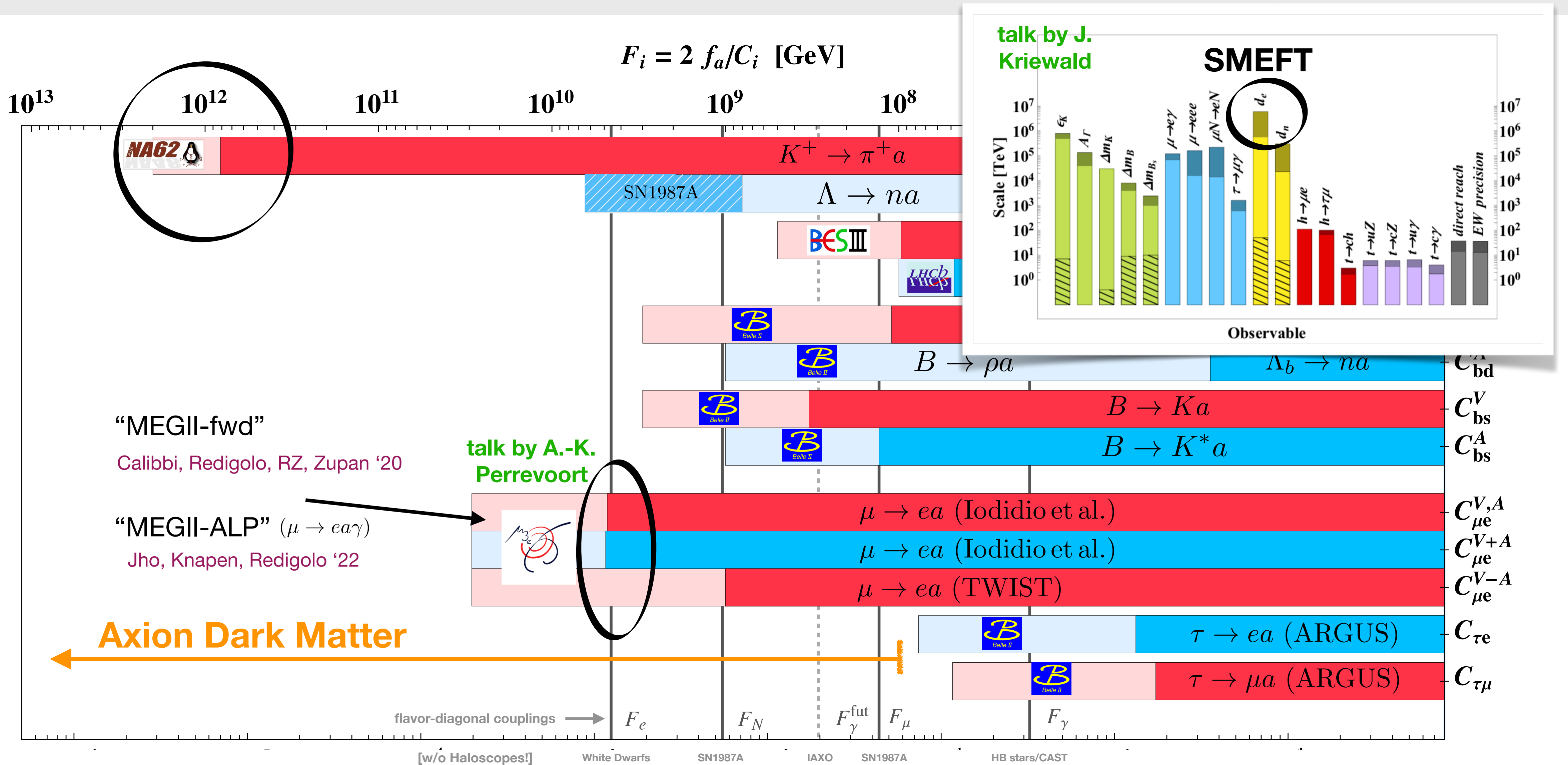
- ✿ 2-body decays probe **LARGE NP scales** [and typically more constraining than meson mixing]

| | | | | | | |
|---|--|--------------------------------|----------|---|--|----------------------------------|
| $\frac{\partial_\mu a}{f_a} \bar{b} \gamma^\mu s$ | $B \rightarrow K a$ \longrightarrow | $f_a \gtrsim 10^5 \text{ TeV}$ | \vdots | $\frac{1}{\Lambda^2} (\bar{b} \gamma^\mu s) (\bar{\nu} \gamma_\mu \nu)$ | $B \rightarrow K \nu \bar{\nu}$ \longrightarrow | $\Lambda \gtrsim 10 \text{ TeV}$ |
| | $B_s - \text{mixing}$ \longrightarrow | $f_a \gtrsim 200 \text{ TeV}$ | | | | |

Summary of present and future Constraints



Summary of present and future Constraints



Constraints from SN1987A

Best handle on axial-vector coupling to s-d from hyperon decays

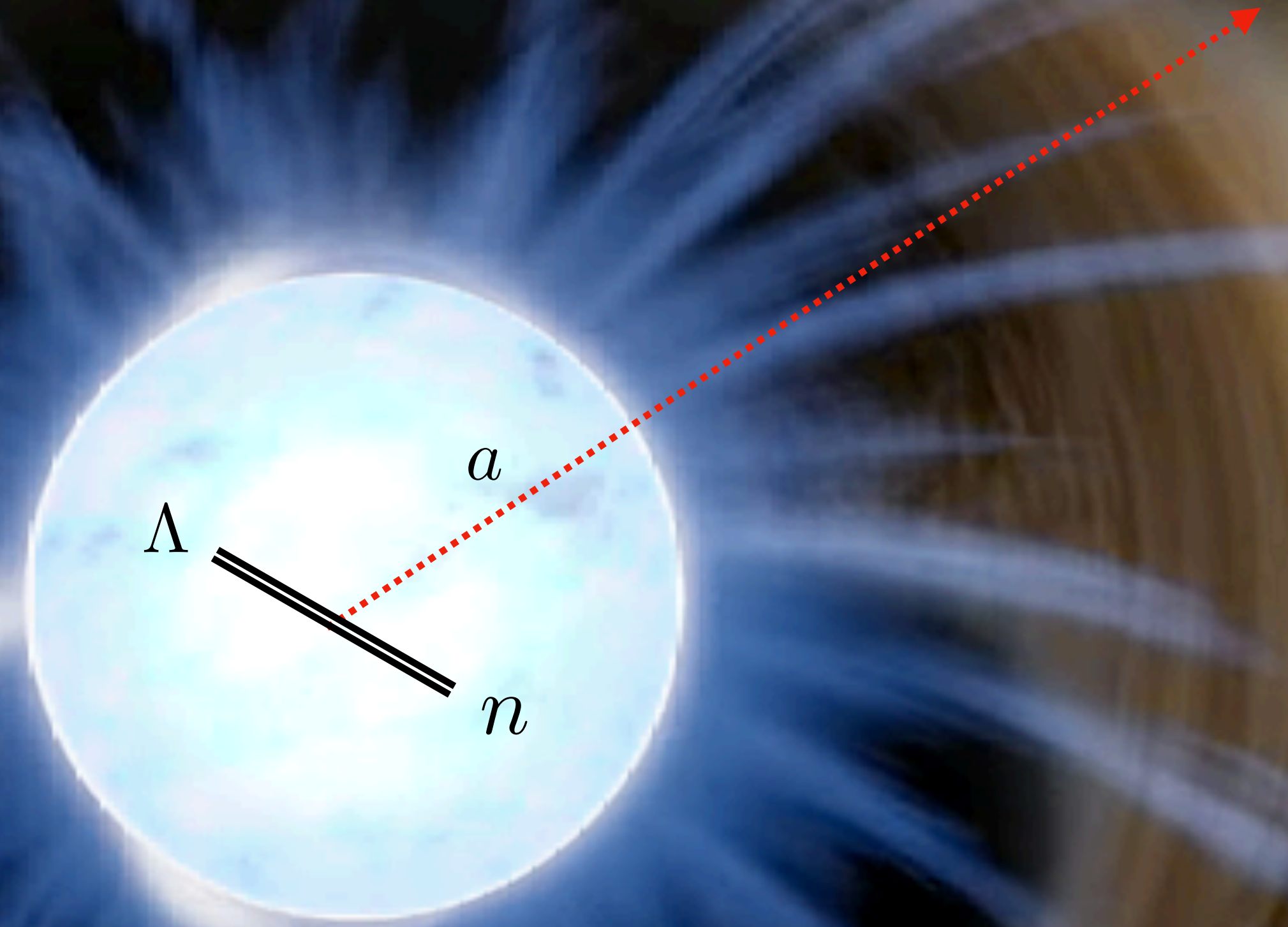
Many hyperons in hot proto-neutron star formed during core-collapse supernovae [$T \approx 40$ MeV]

Hyperon decays to axions provide extra cooling which would have shorten observed neutrino pulse of SN1987A: limits energy loss rate

$$L_a \simeq \int_{\text{PNS}} n_n (m_\Lambda - m_n) \Gamma(\Lambda \rightarrow na) e^{-\frac{m_\Lambda - m_n}{T}} dV \leq 10^{52} \text{ erg/s}$$

Gives best bound on invisible hyperon decays:
[can do same for LFV muon decays, but weaker than lab bound]

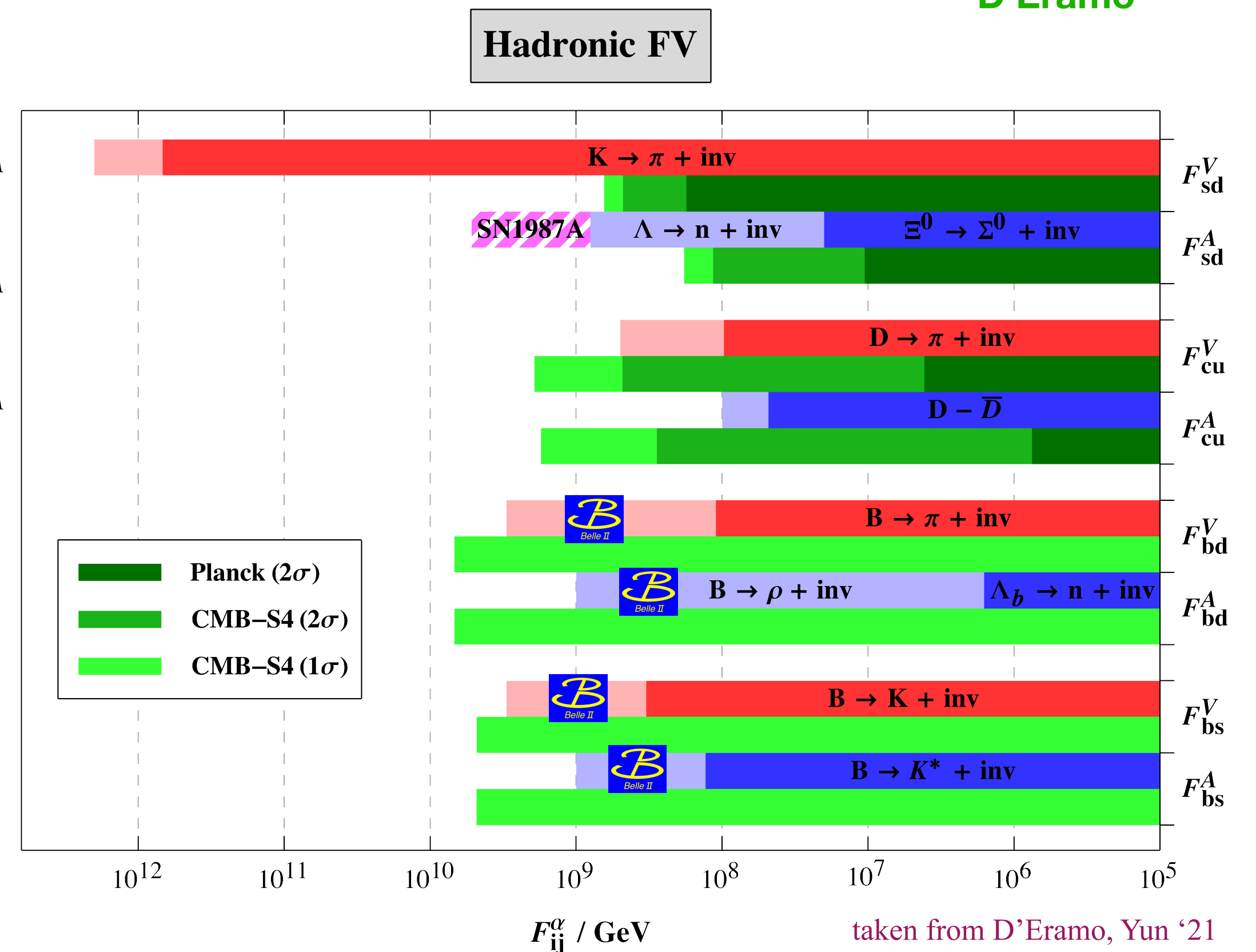
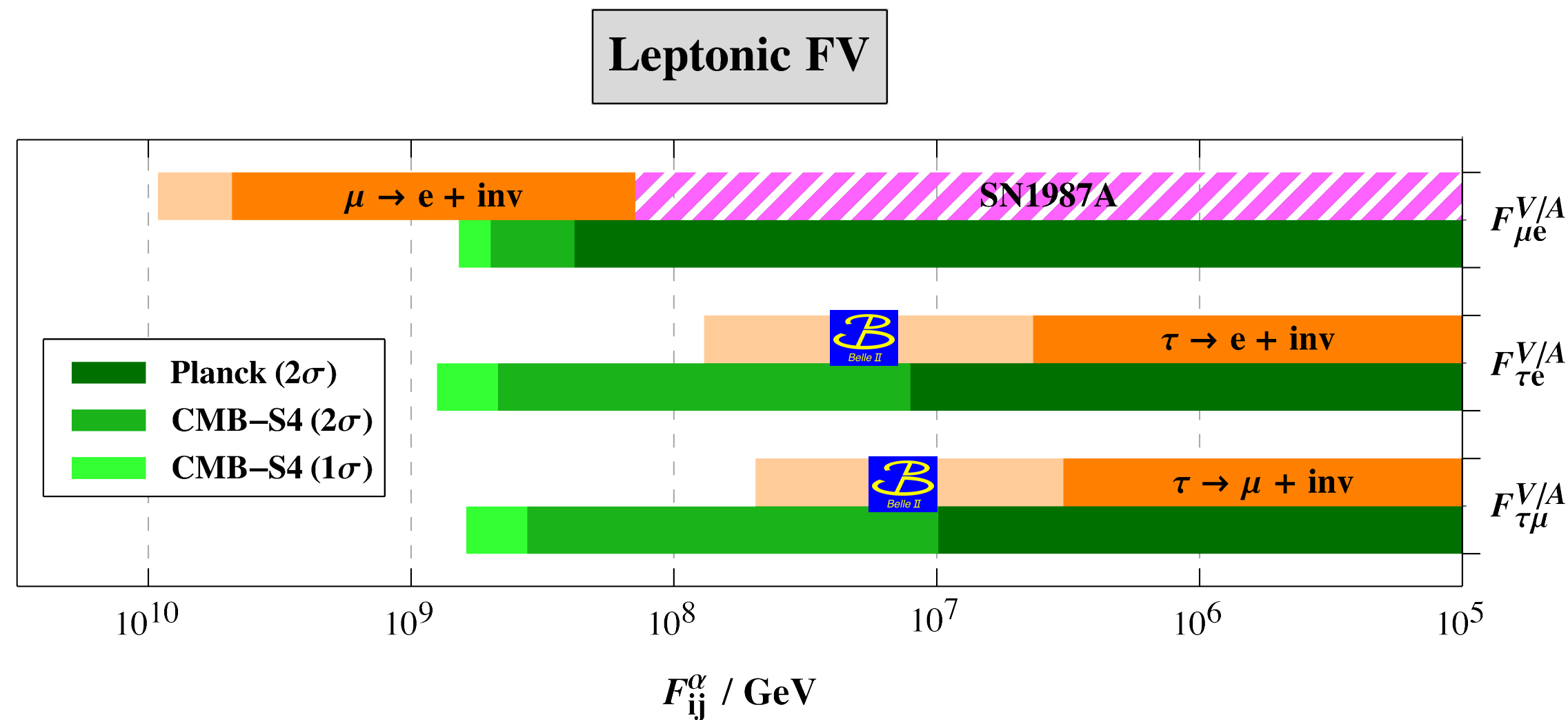
$$\text{BR}(\Lambda \rightarrow na) \lesssim 5.0 \times 10^{-9}$$



Constraints from Cosmology

- Flavor-violating SM decays produce hot axions in early universe
very light axions constrained by bounds on Dark Radiation from CMB

talk by F. D'Eramo



➔ Belle-II will compete with future CMB telescopes

Axion Dark Matter from SM Decays

- ✿ Use flavor-violating decays as main production of axion Dark Matter

LFV: 2209.03371, with P. Panci, D. Redigolo, T. Schwetz

abundance fixes decay rate: **get explicit targets for exp. searches**

DM Abundance

$$\Omega_a h^2 \propto m_a \Gamma(\ell_i \rightarrow \ell_j a) \propto m_a \frac{C_{ij}^2}{f_a^2} = 0.12$$

gives viable axion mass window

$$m_a^{\min} < m_a < m_a^{\max}$$

lab constraints &
Warm Dark Matter

kinematic
threshold

DM Stability

$$\Gamma(a \rightarrow \gamma\gamma) \propto \frac{m_a^3}{f_a^2} \left| E + N + C_{ii} \frac{m_a^2}{12m_{\ell_i}^2} \right|^2 \lesssim \frac{1}{10^{28} \text{sec}}$$

X-ray telescopes

need anomaly-free PQ and light axion/
heavy lepton/small diagonal coupling

Explicit LFV Scenarios

- Give leptons traceless PQ charges (two generations for simplicity)

$$\text{PQ}_e = \begin{pmatrix} 1 & & \\ & -1 & \\ & & 0 \end{pmatrix} \xrightarrow[\text{in 1-2 plane}]{\text{rotation}} C_{e_i e_j}^V = C_{e_i e_j}^A = \begin{pmatrix} s_\alpha & c_\alpha & 0 \\ c_\alpha & -s_\alpha & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

- Axion relic abundance dominantly arises from LFV decays (for small T_R)

$$\Omega h^2|_{\mu \rightarrow ea} \approx 0.19 \left(\frac{m_a}{20 \text{ keV}} \right) \left(\frac{10^9 \text{ GeV}}{f_a / \cos \alpha} \right)^2$$

IR freeze-in from LFV decays

IR freeze-in of $\mu\gamma \rightarrow ea$

UV freeze-in of $\mu h \rightarrow ea$

Misalignment reduced by

$$\left. \begin{array}{l} \alpha_{\text{em}} \\ \frac{m_\mu T_R}{3\pi^3 v^2} \\ \frac{T_R}{T_{\text{osc}}^{\text{std}}} \end{array} \right\} \times \Omega h^2|_{\mu \rightarrow ea} \quad (\text{matter domination})$$

- DM lifetime

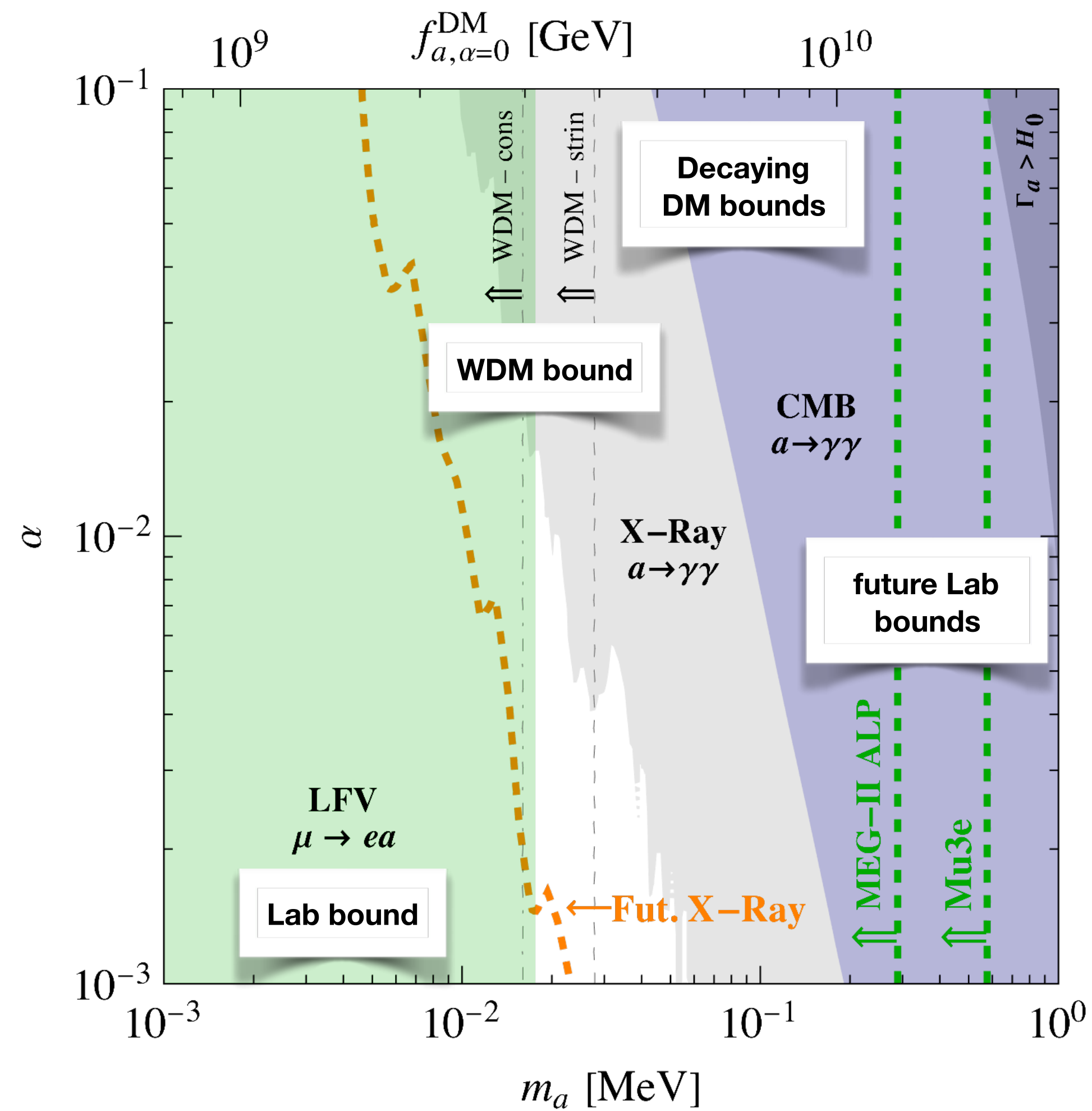
$$\tau_a = 10^{20} \text{ sec} \left(\frac{60 \text{ keV}}{m_a} \right)^7 \left(\frac{f_a / \sin \alpha}{10^9 \text{ GeV}} \right)^2$$

Warm DM bound:

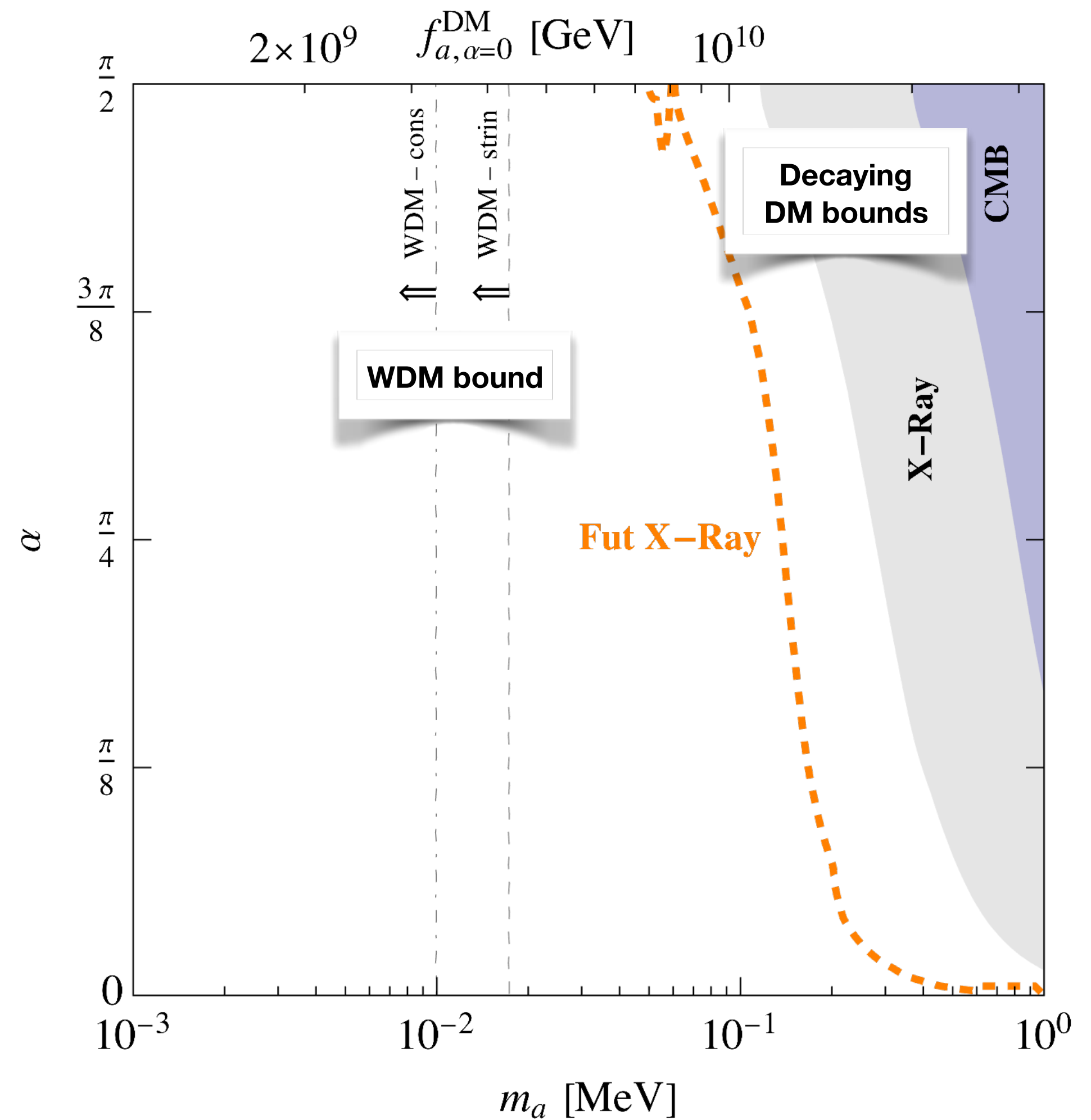
$$m_a \gtrsim 20 \text{ keV}$$

Results

μe -Scenario



$\tau\mu$ -Scenario



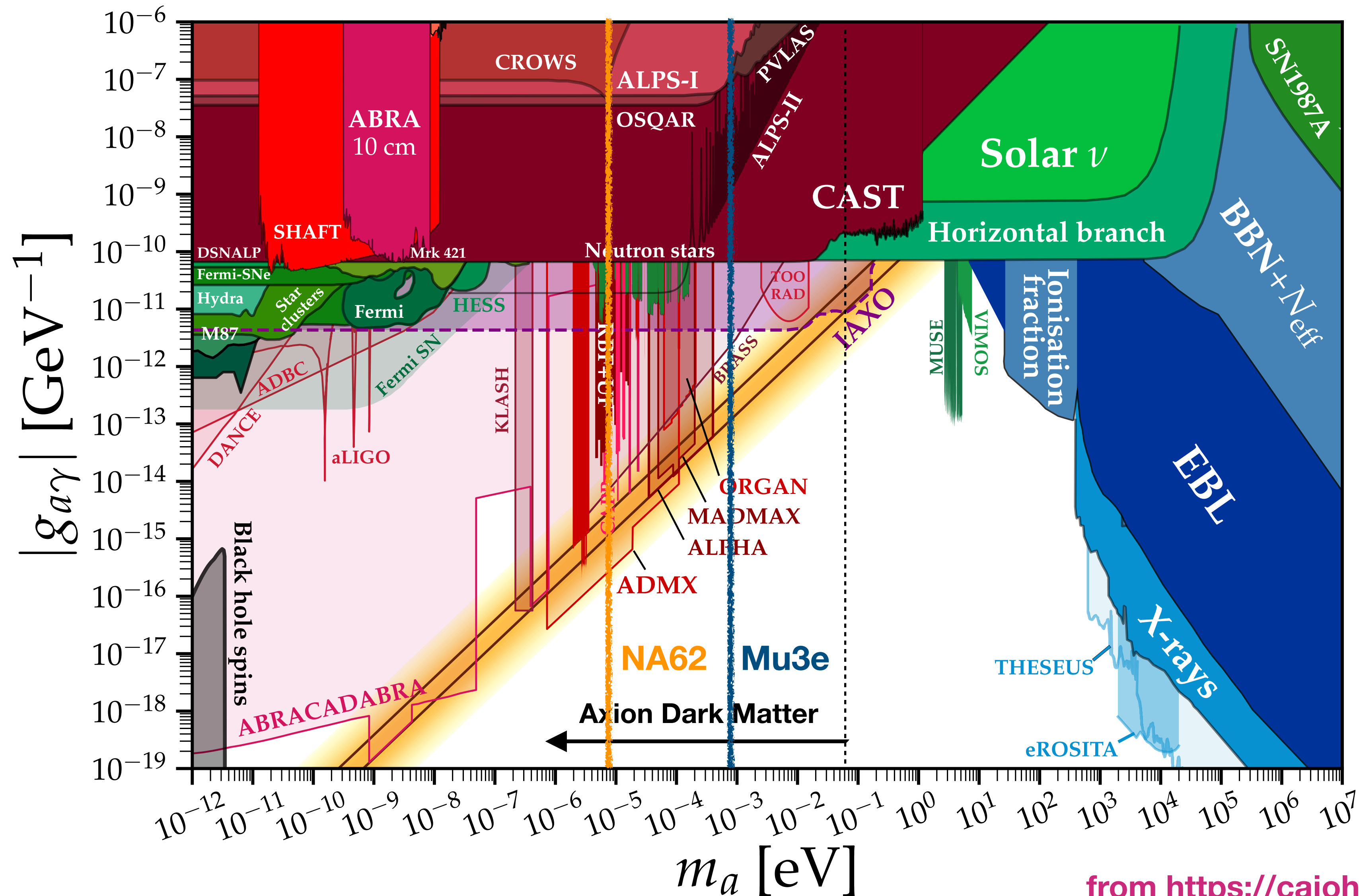
Summary

DM Axions with flavor-violating couplings can be produced by SM decays

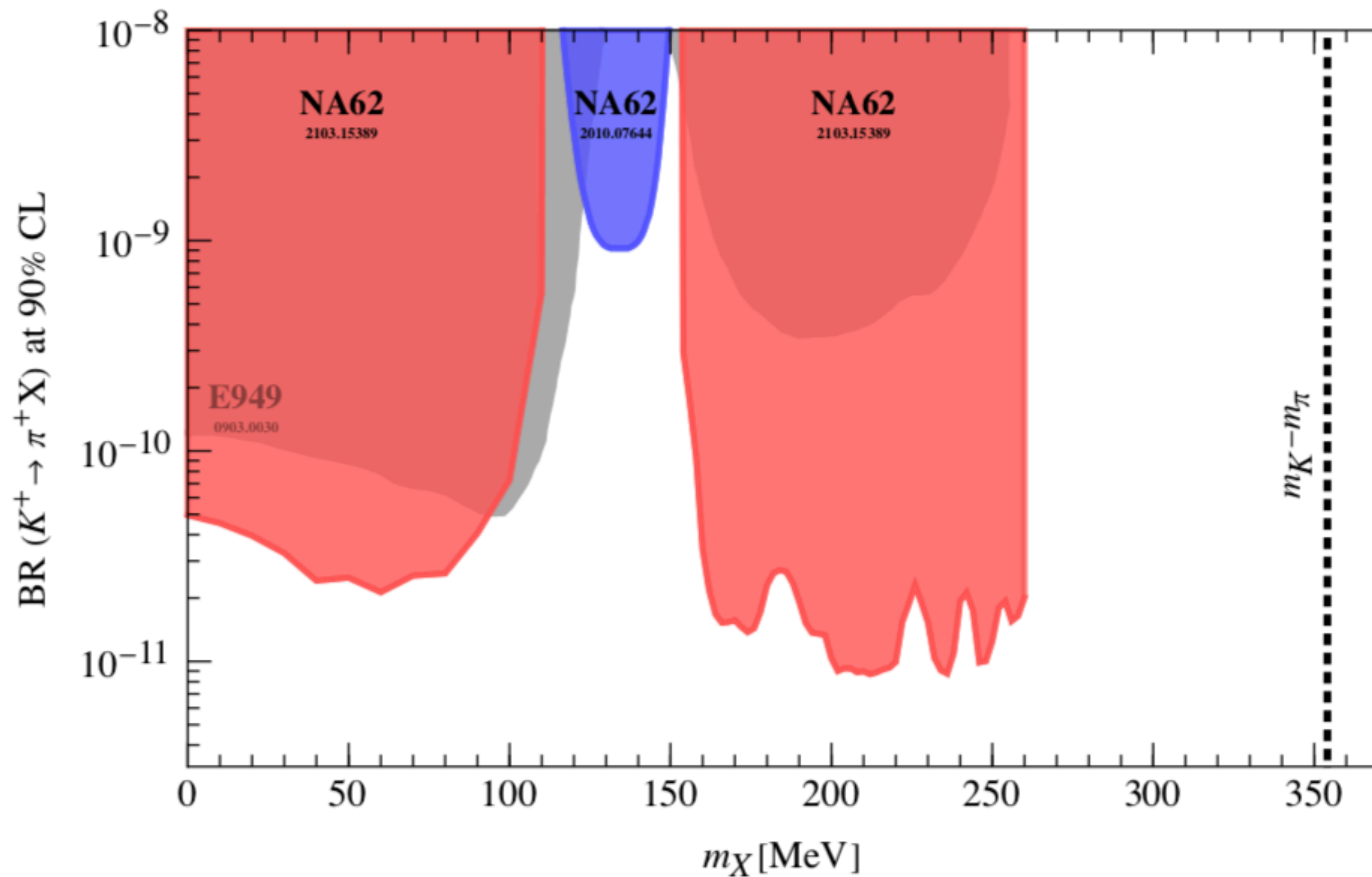
- ★ **in precision flavor experiments**, probing decay constants up to 10^{12} GeV (NA62) or 10^{10} GeV (Mu3e) or 10^8 GeV (B-factories)
- ★ **in SN1987A** from decays of moderately heavy flavors, contributing to energy loss and providing strongest bounds on hyperons decays
- ★ **in the early universe**, giving observed DM abundance via freeze-in: very simple class of DM models that can be tested at flavor factories such as Mu3e and MEG-II [quark case in progress]

Backup

Flavor Constraints in the Axion Plane

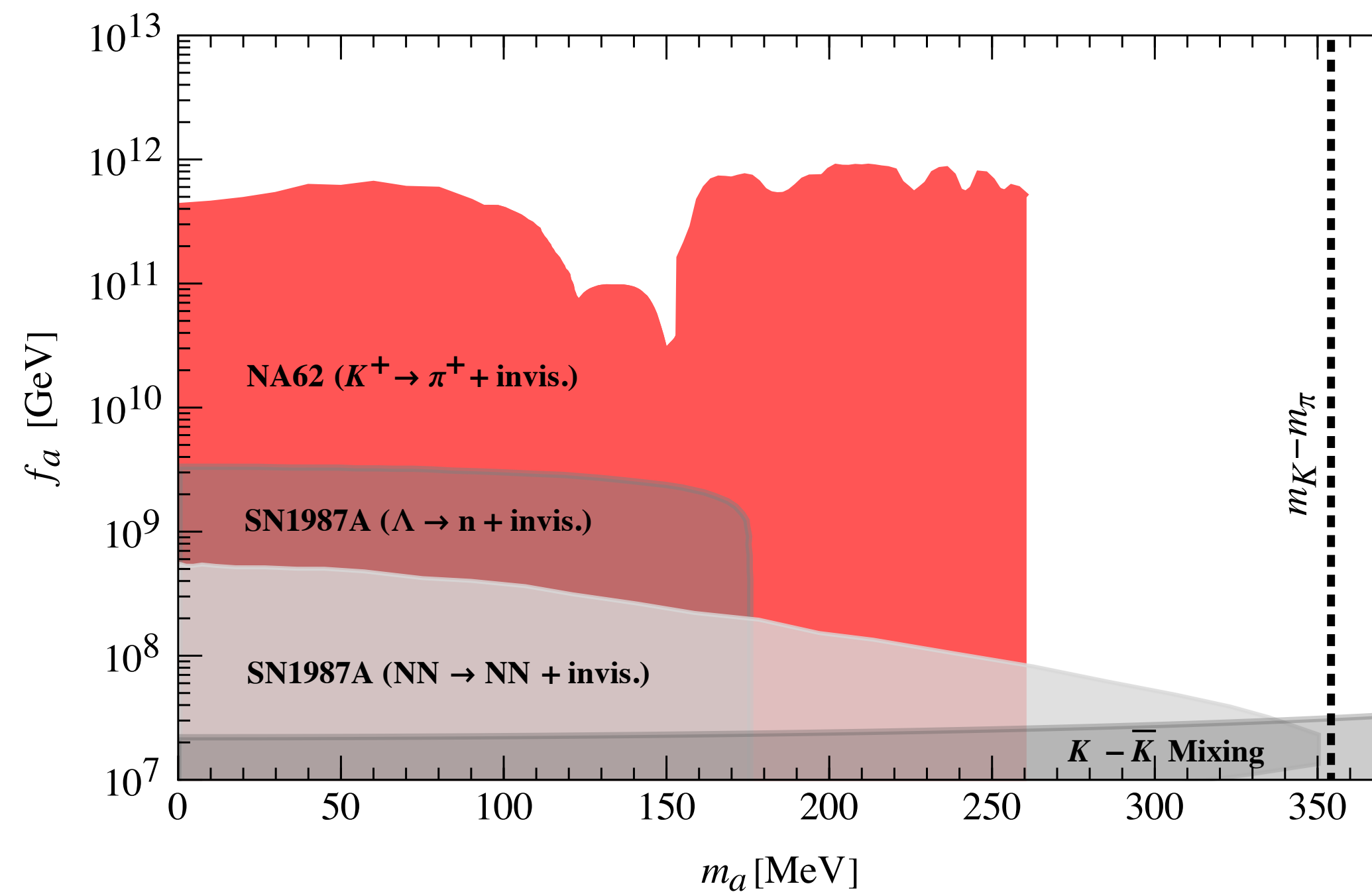


Bounds from NA62



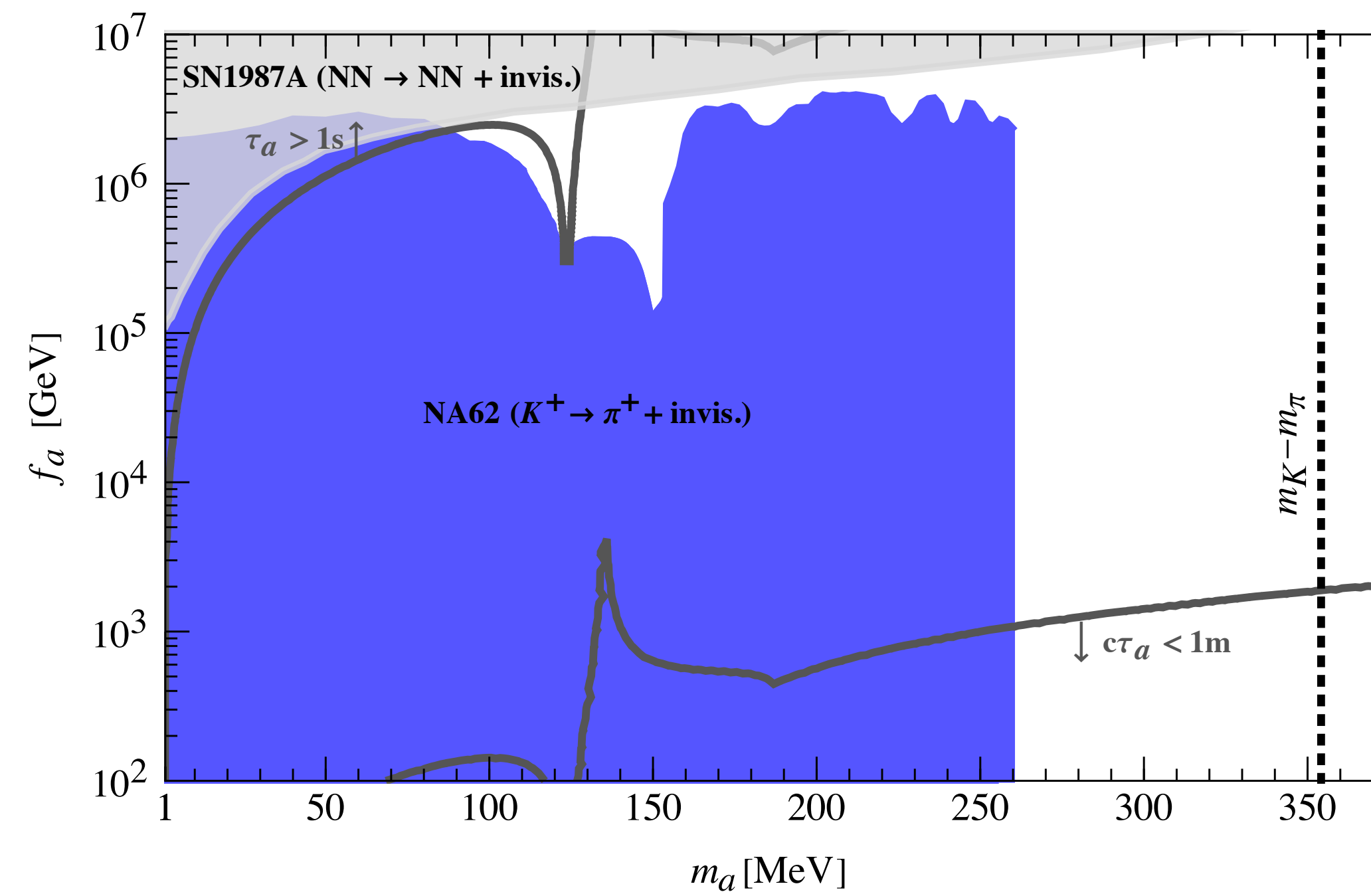
Flavor Anarchy vs. MFV

Flavor Anarchy



all axion UV couplings = 1

Minimal Flavor Violation



all flavor-diagonal UV couplings = 1

Lepton Sector Bounds

| Present best limits | | | | |
|-------------------------------|------------------------|----------------------------|-----------------------|-------------------------------|
| Process | BR Limit | Decay constant | Bound (GeV) | Experiment |
| Star cooling | – | F_{ee}^A | 4.6×10^9 | WDs [44] |
| | – | $F_{\mu\mu}^A$ | 1.3×10^8 | SN1987A $_{\mu\mu}$ [45, 46] |
| | 4×10^{-3} | $F_{\mu e}$ | 1.4×10^8 | SN1987A $_{\mu e}$ (Sec. 6.1) |
| $\mu \rightarrow e a$ | $2.6 \times 10^{-6*}$ | $F_{\mu e}$ (V or A) | 4.8×10^9 | Jodidio et al. [9] |
| $\mu \rightarrow e a$ | $2.5 \times 10^{-6*}$ | $F_{\mu e}$ ($V + A$) | 4.9×10^9 | Jodidio et al. [9] |
| $\mu \rightarrow e a$ | $5.8 \times 10^{-5*}$ | $F_{\mu e}$ ($V - A$) | 1.0×10^9 | TWIST [10] |
| $\mu \rightarrow e a \gamma$ | $1.1 \times 10^{-9*}$ | $F_{\mu e}$ | $5.1 \times 10^{8\#}$ | Crystal Box [47] |
| $\tau \rightarrow e a$ | $2.7 \times 10^{-3**}$ | $F_{\tau e}$ | 4.3×10^6 | ARGUS [43] |
| $\tau \rightarrow \mu a$ | $4.5 \times 10^{-3**}$ | $F_{\tau\mu}$ | 3.3×10^6 | ARGUS [43] |
| Expected future sensitivities | | | | |
| Process | BR Sens. | Decay constant | Sens. (GeV) | Experiment |
| $\mu \rightarrow e a$ | $7.2 \times 10^{-7*}$ | $F_{\mu e}$ (V or A) | 9.2×10^9 | MEGII-fwd* |
| $\mu \rightarrow e a$ | $7.2 \times 10^{-8*}$ | $F_{\mu e}$ (V or A) | 2.9×10^{10} | MEGII-fwd** |
| $\mu \rightarrow e a$ | $7.3 \times 10^{-8*}$ | $F_{\mu e}$ (V or A) | 2.9×10^{10} | Mu3e [42] |
| $\tau \rightarrow e a$ | $8.3 \times 10^{-6**}$ | $F_{\tau e}$ | 7.7×10^7 | Belle II |
| $\tau \rightarrow \mu a$ | $2.0 \times 10^{-5**}$ | $F_{\tau\mu}$ | 4.9×10^7 | Belle II |

Constraints from Meson Decays

- Experimental bounds often old or non-existent

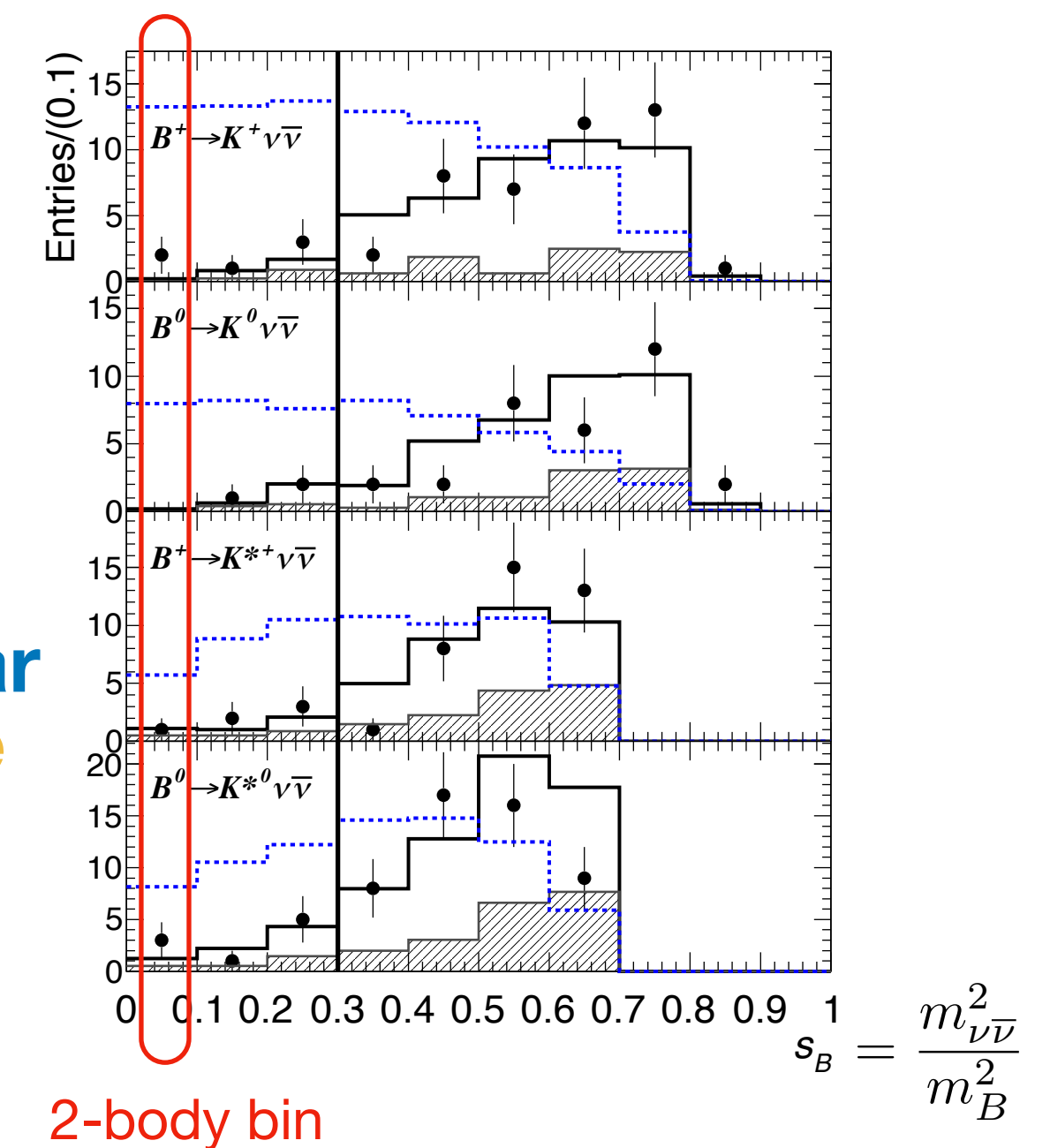
e.g. no bound in PDG on $D^+ \rightarrow \pi^+ a$, $B \rightarrow K^* a$, $B \rightarrow \rho a$

- Need to recast data for SM decays in 2-body region

Martin Camalich, Pospelov, Vuong, RZ, Zupan '20

| | | $K \rightarrow \pi a$ | $D \rightarrow \pi a$ | $B \rightarrow \pi a$ | $B \rightarrow K a$ |
|--------------------|--|---|---------------------------|---------------------------|---------------------------|
| Decay | | sd | cu | bd | bs |
| $\propto C_{ij}^V$ | $\text{BR}(P_1 \rightarrow P_2 + a)_{\text{exp}}$ | 7.3×10^{-11} [85] | no analysis | 4.9×10^{-5} [86] | 4.9×10^{-5} [86] |
| | $\text{BR}(P_1 \rightarrow P_2 + a)_{\text{recast}}$ | no need | 8.0×10^{-6} [87] | 2.3×10^{-5} [88] | 7.1×10^{-6} [89] |
| | $\text{BR}(P_1 \rightarrow P_2 + \nu\bar{\nu})_{\text{exp}}$ | $1.47_{-0.89}^{+1.30} \times 10^{-10}$ [85] | no analysis | 0.8×10^{-5} [90] | 1.6×10^{-5} [90] |
| $\propto C_{ij}^A$ | $\text{BR}(P_1 \rightarrow V_2 + a)_{\text{exp}}$ | 3.8×10^{-5} [91] | no analysis | no analysis | no analysis |
| | $\text{BR}(P_1 \rightarrow V_2 + a)_{\text{recast}}$ | no need | no data | no data | 5.3×10^{-5} [89] |
| | $\text{BR}(P_1 \rightarrow V_2 + \nu\bar{\nu})_{\text{exp}}$ | 4.3×10^{-5} [91] | no analysis | 2.8×10^{-5} [90] | 2.7×10^{-5} [90] |
| | | $K \rightarrow \pi\pi a$ | $D \rightarrow \pi\pi a$ | $B \rightarrow \rho a$ | $B \rightarrow K^* a$ |

BaBar
Belle



e.g. recast **CLEO** data on $D \rightarrow \tau\nu$, $\tau \rightarrow \pi\nu$ to get bound on $D^+ \rightarrow \pi^+ a$

Kamenik, Smith '11