

Reinforcement learning and its application in particle accelerators

Andrea Santamaría García

12/09/2022 - Conceptual Advances in Deep Learning

Machine learning in the search for new fundamental physics

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Nature Reviews Physics 4, 399-412 (2022) | Cite this article

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Abstract

Compelling experimental evidence suggests the existence of new physics be established and tested standard model of particle physics. Various current ar experiments are searching for signatures of new physics. Despite the variety

Pervasive machine learning in physics

Nature Reviews Physics 4, 353 (2022) | Cite this article

1325 Accesses | 6 Altmetric | Metrics

No longer restricted to data analysis, machine learning is now increasingly being used in theory, experiment and simulation – a sign that data-intensive science is starting to encompass all traditional aspects of research.

Machine Learning Pins Down Cosmological Parameters

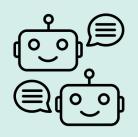
August 19, 2022 • *Physics* 15, s111

Cosmological constraints can be improved by applying machine learning to a combination of data from two leading probes of the large-scale structure of the Universe.

ARTIFICIAL INTELLIGENCE (AI)

Computers mimic human behaviour

- First chatbots
- Robotics
- Expert systems
- Natural language processing
- Fuzzy logic
- Explainable AI



MACHINE LEARNING (ML)

Algorithm

Computers learn without being explicitly programmed to do so and improve with experience

Collection of **data-driven** methods / algorithms Focused on **prediction** / **optimization** / **control** based on properties learned from data

Tries to generalize to unseen scenarios

Data

DEEP LEARNING (DL)

Multi-layered neural networks perform certain tasks with high accuracy

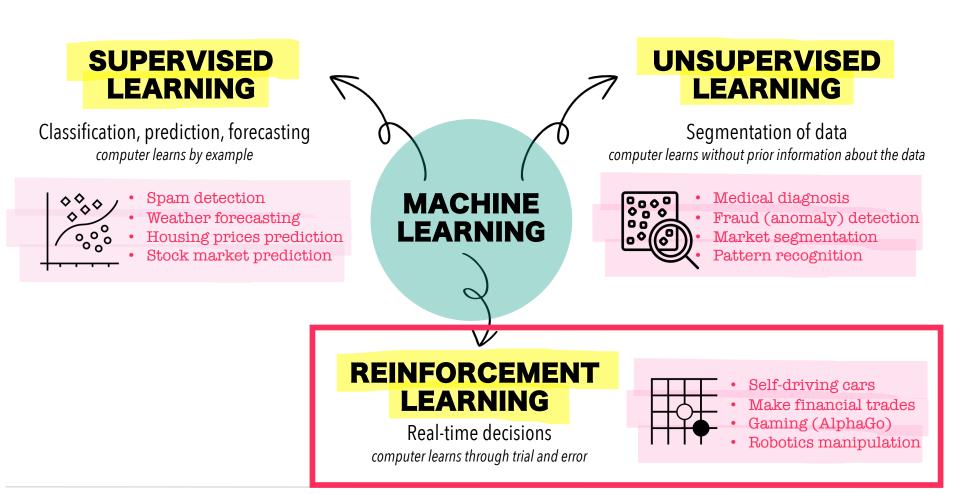


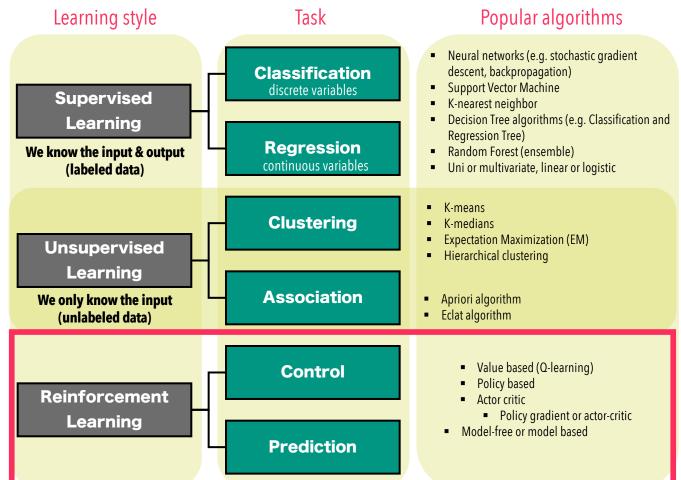
- Speech/handwriting recognition
- Language translation
- Recommendation engines

Narrow Al

• Computer vision







Deep Learning NetworksConvolutional Neural Networks

- Recurrent Neural Networks
- Long Short-Term Memory Networks
- Autoencoders
- Deep Boltzmann Machine
- Deep Belief Networks

Bayesian Algorithms

- Naive Bayes
- Gaussian Naive Bayes
- Bayesian Network
- Bayesian Belief Network
- Bayesian optimization

Regularization, dimensionality reduction, ensemble, evolutionary algorithms, computer vision, recommender systems, ...

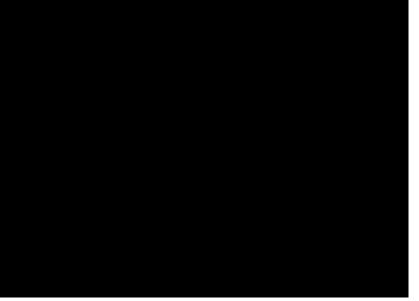
Machine Learning

Reinforcement learning more than machine learning



Psychology (classical conditioning)
Neuroscience (reward system)
Economics (game theory)
Mathematics (operations research)
Engineering (optimal control, planning)

Reinforcement learning understanding how the human brain learns makes decisions



https://www.deepmind.com/publications/playing-atari-withdeep-reinforcement-learning



The RL problem

Reward hypothesis

all goals can be described by the maximization of expected cumulative sum of a received scalar signal

<u>"Reward is enough"</u>

Reward

scalar feedback signal \mathcal{R}_t that indicates how well the agent is doing at step t

Goal

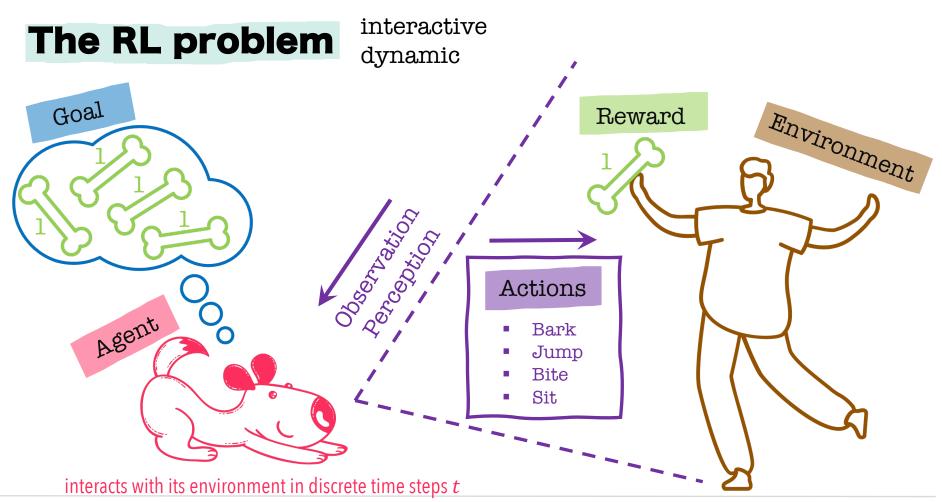
maximization of cumulative reward through selected actions

Agent

executes action \rightarrow receives observation

 \rightarrow receives scalar reward

an agent must learn through trial-and-error interactions with a dynamic environment



How to cumulate reward?

Agent Model

agent's representation of the environment

Which behaviors perform well in this environment?

Policy agent's behaviour function (how the agent picks its actions)

Estimate the utility of taking actions in particular states of the environment (evaluation of the policy)

Value function

how good each state and/or action are

Prediction: evaluate the future given a policy
 Control: optimize the future (find the best policy)

Challenges in RL

Trade-off between exploitation and exploration

- Actions may have long-term consequences
- Reward might be delayed (does not happen immediately)

should the agent sacrifice immediate reward to gain more long term reward?

The agent needs to:

Exploit what it has already experienced in order to obtain reward now
 Explore the environment to select better actions in the future by

sacrificing known reward now

..and both cannot be pursued exclusively without failing at the task



Must:

- Be able to sense the state of its environment to some extent s
- Be able to **take actions** that affect that state
- **Have a goal** or goals relating to the state of the environment

Markov Decision Processes

Sensation

"Free-Will

Motivation

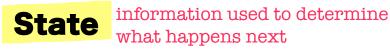
Include this 3 elements without trivializing any of them

Markov Decision Process (MDP)

Mathematical framework for modelling sequential decision making

A Markov Decision Process is a 5-tuple:

$$(\mathcal{S}, \mathcal{A}, \mathcal{P}^a_{ss}, \mathcal{R}^a_s, \gamma)$$
 \mathcal{S} = finite set of states



A state transition can be:

- Deterministic $S_{t+1} = f(\mathcal{H}_t)$ Stochastic $S_{t+1} \sim \mathbb{P}(S_{t+1}|\tau_t)$

Trajectory

sequence of states and actions until time t

 $\tau = (s_0, a_0, s_1, a_1, s_2, a_2, \dots)$

Environment state (S^e): environment's internal representation, usually not visible to the agent

Agent state (S^{α}): agent's internal representation, used by the RL algorithm to pick the next action

Observation (*O*):partial description of a state, which may omit information

Markov Decision Process (MDP)

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A Markov Decision Process is a 5-tuple:

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 \mathcal{S} = finite set of



information used to determine what happens next

A state transition can be:

- Deterministic $S_{t+1} = f(\mathcal{H}_t)$ Stochastic $S_{t+1} \sim \mathbb{P}(S_{t+1}|\tau_t)$

Trajectory

sequence of states and actions until time t

 $\tau = (s_0, a_0, s_1, a_1, s_2, a_2, \dots)$

Markov state / property A state is Markov if and only if:

$$\mathbb{P}[s_{t+1}|s_t] = \mathbb{P}[s_{t+1}|s_{1,\dots,t}]$$

states

- The state is a sufficient statistic of the future
- The future is independent of the past, given the present
- Once the state is known, the history may be discarded

state transitions of an MDP satisfy the Markov property

Fully observable environments $O_t = S_t^a = S_t^e$

- Agent directly observes environment state
- Necessary condition to formalize an RL problem with an MDP

Partially observable environments $S_t^a \neq S_t^e$

 $\mathcal{S}_{t}^{a} = \tau_{t}$

Agent constructs its own state representation:

- Complete trajectory:
- Beliefs of environment state:
- Recurrent neural networks:

$$S_t^a = (\mathbb{P}[S_t^e = s_1], \dots, \mathbb{P}[S_t^e = s_n])$$

$$S_t^a = \sigma(w_0\mathcal{O}_t + w_s\mathcal{S}_{t-1}^a)$$

 \rightarrow Partially observable MDP

Markov Decision Process (MDP)

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A Markov Decision Process is a 5-tuple:
$$(\mathcal{S}, \mathcal{A}, \mathcal{P}^a_{ss'}, \mathcal{R}^a_s, \gamma)$$

State transition model / probability

Predicts the next state (dynamics of the environment)

$$\mathcal{P}^{a}_{ss'} = \mathbb{P}[\mathcal{S}_{t+1} = s' | \mathcal{S}_{t} = s, \mathcal{A} = a] \quad \stackrel{\text{Probability of ending in state } s' \text{ after taking action } a \text{ while being action } a \text{ after taking action } a \text{ after t$$

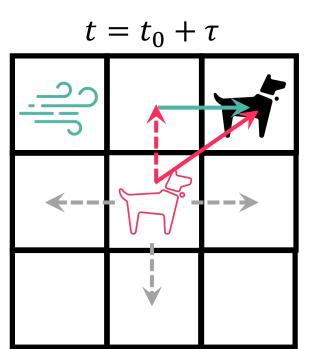


Transition probabilities from all states and successor states

Non-deterministic environment

Taking the same action in the same state on two different occasions may result in different next states

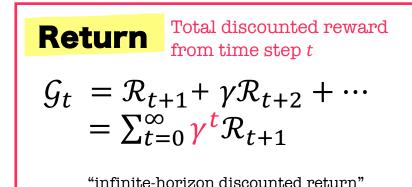
 $t = t_0$ **-**--



Markov Decision Process (MDP)

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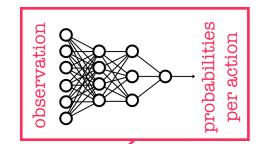


The goal is to maximize the return

- The discount factor $\gamma \in [0, 1)$ avoids infinite returns (sum converges)
- It values immediate reward over delayed reward (human-like)
- It deals with uncertainty about the future (no perfect model of env.)



- Policy π completely defines how the agent will behave
- It's a distribution over actions given a certain state



Deterministic: $a = \pi(s)$

Stochastic:
$$\pi(a|s) = \mathbb{P}[\mathcal{A}_t = a|\mathcal{S}_t = s]$$

Probability of taking a specific action by being in a specific state

Categorical (discrete action spaces) **Gaussian** (continuous action spaces)

Given an MDP $\langle S, \mathcal{A}, \mathcal{P}, \mathcal{R}, \gamma \rangle$ and a policy π :

$$\mathcal{P}^{\pi}_{s,s'} = \sum_{a \in \mathcal{A}} \pi(a|s) \, \mathcal{P}^{a}_{s,s'} \qquad \mathcal{R}^{\pi}_{s} = \sum_{a \in \mathcal{A}} \pi(a|s) \, \mathcal{R}^{a}_{s}$$

Value function

Estimation of expected future reward

A way to compare policies

- Used to choose between states depending on how much reward we expect to get
- Depends on the agent's behavior (policy)

State-value function

Expected return starting from state s and following policy π (evaluates the policy)

$$\mathcal{V}_{\pi}(s) = \mathbb{E}_{\pi}[\mathcal{G}_t \mid \mathcal{S}_t = s]$$

Action-value function Expected return st taking action a, an

Expected return starting from state s , taking action a , and following policy π

$$Q_{\pi}(s,a) = \mathbb{E}_{\pi}[\mathcal{G}_t \mid \mathcal{S}_t = s, \mathcal{A}_t = a]$$

"Q function"

Bellman optimality equation

The state-value function can be decomposed into:

- immediate reward \mathcal{R}_{t+1}
- discounted value of next state $\gamma v(S_{t+1})$

$$\mathcal{V}(s) = \mathbb{E}[\mathcal{G}_{t} \mid \mathcal{S}_{t} = s]$$

$$= \mathbb{E}[\mathcal{R}_{t+1} + \gamma \, \mathcal{R}_{t+2} + \gamma^{2} \, \mathcal{R}_{t+3} \dots \mid \mathcal{S}_{t} = s]$$

$$= \mathbb{E}[\mathcal{R}_{t+1} + \gamma \, (\mathcal{R}_{t+2} + \gamma \, \mathcal{R}_{t+3} \dots) \mid \mathcal{S}_{t} = s]$$

$$= \mathbb{E}[\mathcal{R}_{t+1} + \gamma \, \mathcal{G}_{t+1} \mid \mathcal{S}_{t} = s]$$

$$= \mathbb{E}[\mathcal{R}_{t+1} + \gamma \, \mathcal{V}(\mathcal{S}_{t+1}) \mid \mathcal{S}_{t} = s]$$

$$= \mathbb{E}[\mathcal{R}_{t+1} + \gamma \, \mathcal{V}(\mathcal{S}_{t+1}) \mid \mathcal{S}_{t} = s]$$

$$\mathcal{V}(s) = \mathcal{R}_{s} + \gamma \sum_{s' \in \mathcal{S}} \mathcal{P}_{s,s'} \, \mathcal{V}(s')$$

Bellman expectation equation

Considering the policy π we get:

$$\mathcal{V}(s) = \sum_{a \in \mathcal{A}} \pi \left(a | s \right) \left(\mathcal{R}_{s}^{a} + \gamma \sum_{s' \in \mathcal{S}} \mathcal{P}_{s,s'}^{a} \, \mathcal{V}(s') \right)$$

Direct solution only for small MRPs

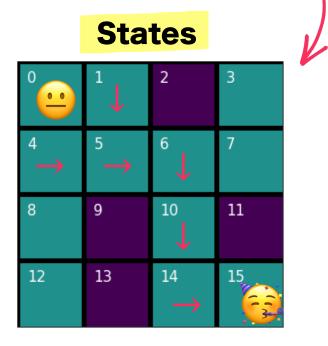
System of *S* simultaneous linear equations with *S* unknowns

Other ways of solving it:

- Iteratively (dynamic programming)
- Sampling (Monte-Carlo evaluation)
- > Approximation (temporal-difference learning)

Example: gridworld

The agent needs to get from state **0** to state **15** to get out of the maze

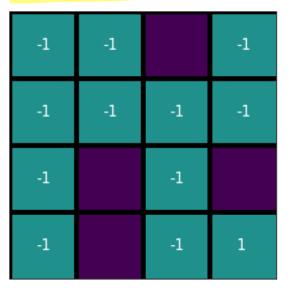


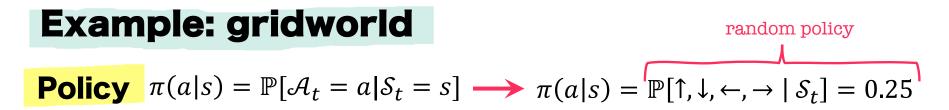
Actions $\mathcal{A} = (\uparrow, \downarrow, \leftarrow, \rightarrow)$

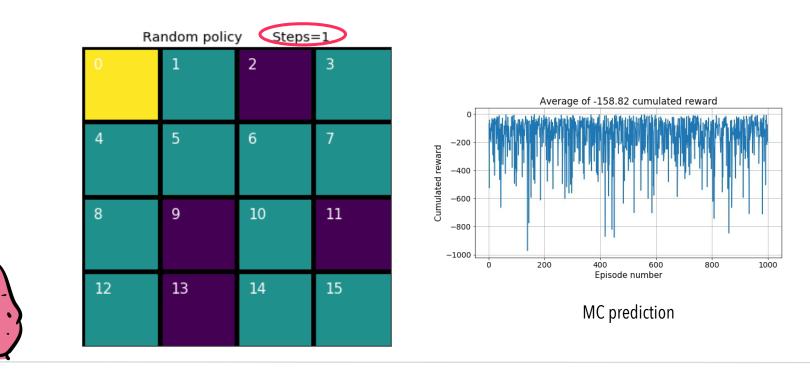
Deterministic env: $\mathcal{P}^{a}_{s,s'} = 1$

Rewards

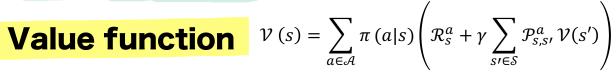
no discount γ







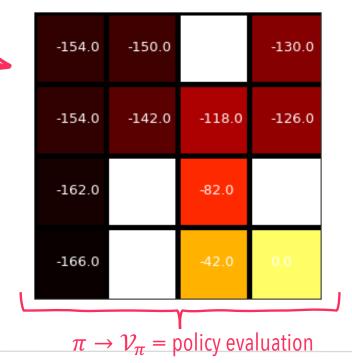
Example: gridworld



Solving simultaneously linear set of equations: environment's dynamics are completely known

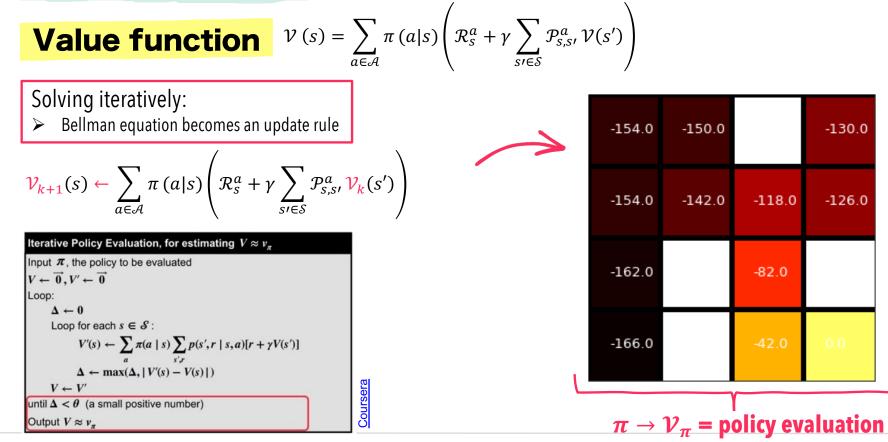
```
0.5*v0 - 0.25*v1 - 0.25*v4 + 1.0 = 0
-0.25*v0 + 0.5*v1 - 0.25*v5 + 1.0 = 0
0.25*v3 - 0.25*v7 + 1.0 = 0
-0.25*v0 + 0.75*v4 - 0.25*v5 - 0.25*v8 + 1.0 = 0
-0.25*v1 - 0.25*v4 + 0.75*v5 - 0.25*v6 + 1.0 = 0
-0.25*v10 - 0.25*v5 + 0.75*v6 - 0.25*v7 + 1.0 = 0
-0.25*v3 - 0.25*v6 + 0.5*v7 + 1.0 = 0
-0.25*v12 - 0.25*v4 + 0.5*v8 + 1.0 = 0
0.5*v10 - 0.25*v14 - 0.25*v6 + 1.0 = 0
0.25*v12 - 0.25*v8 + 1.0 = 0
-0.25*v10 + 0.5*v14 + 0.5 = 0
```

11 variables, 11 equations



how much value this policy has?

Example: gridworld



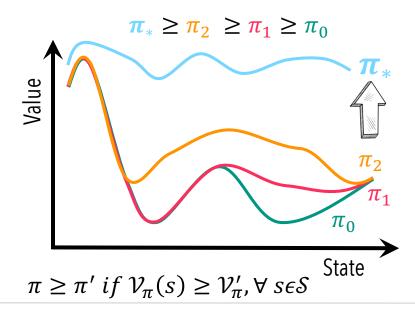
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how much value this policy has?

Dynamic programming algorithms

Prediction: what's the value for a specific policy?

Control: which policy gives as much reward as possible?
 → the policy with more value!



For any MDP:

 There exists an <u>optimal policy</u> π_∗ that is better or equal to all other policies π_∗ ≥ π ∀π

turn the Bellman eq.

into update rules

• All optimal policies achieve the optimal value function $\mathcal{V}_{\pi_*} = \mathcal{V}_*(s)$ and $Q_{\pi_*} = Q_*(s, a)$

So...do I have to calculate the value of every policy and compare them?

 $|\mathcal{A}|^{|\mathcal{S}|}$ deterministic policies in an MDP

 $4^{11} \approx 4$ million policies for simple gridworld example

Bellman optimality equations

$$\mathcal{V}_{\pi*}(s) = \mathbb{E}_{\pi*}[\mathcal{G}_t \mid \mathcal{S}_t = s] = \max_{\pi} \mathcal{V}_{\pi}(s) \quad \forall s \in \mathcal{S}$$
$$\mathcal{Q}_{\pi*}(s) = \max_{\pi} \mathcal{Q}_{\pi}(s) \quad \forall s \in \mathcal{S}, a \in \mathcal{S}$$

By replacing the optimal policy on the Bellman equations we get:

 π_* assigns probability 1 to the action that receives the highest value

Optimal value functions

maximum value over every next possible state

$$Q_*(s, a) = \mathcal{R}_s^a + \gamma \sum_{s' \in \mathcal{S}} \mathcal{P}_{s,s'}^a \max_{a'} Q_*(s', a')$$

 $\boldsymbol{\mathcal{V}}_{*}(\boldsymbol{s}) = \max_{\boldsymbol{a}} \left(\mathcal{R}_{\boldsymbol{s}} + \gamma \sum_{\boldsymbol{t} = \boldsymbol{c}} \mathcal{P}_{\boldsymbol{s}, \boldsymbol{s}} \left(\mathcal{V}_{*}(\boldsymbol{s}') \right) \right)$

Nonlinear (max), no closed-form solution

Dynamic programming solutions only applicable if the dynamics of the system *P* are known

Determining an optimal policy

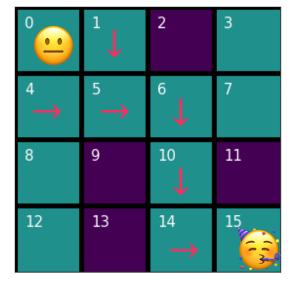
$$\boldsymbol{\mathcal{V}}_*(\boldsymbol{s}) = \max_{\boldsymbol{a}} \left(\mathcal{R}_{\boldsymbol{s}} + \gamma \sum_{\boldsymbol{s}' \in \mathcal{S}} \mathcal{P}_{\boldsymbol{s}, \boldsymbol{s}'} \, \mathcal{V}_*(\boldsymbol{s}') \right)$$

maximum over all actions



For any state we look at each available action and take the one that maximizes the argument

$$\pi_*(s) = \underset{a}{\operatorname{argmax}} \left(\mathcal{R}_s + \gamma \sum_{s' \in \mathcal{S}} \mathcal{P}_{s,s'} \mathcal{V}_*(s') \right)$$
particular action that
achieves that maximum
(greedy action)



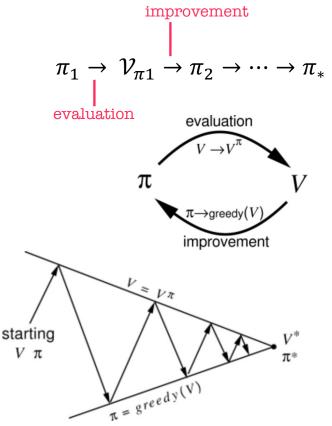
$$\pi_*(s) = \operatorname*{argmax}_a \mathcal{Q}_*$$

Policy improvement & iteration

Let's consider a value function \mathcal{V}_{π} that is non-optimal, and we select an action that is greedy with respect to it:

$$\boldsymbol{\pi}'(\boldsymbol{s}) = \underset{\boldsymbol{a}}{\operatorname{argmax}} \left(\mathcal{R}_{\boldsymbol{s}} + \gamma \sum_{\boldsymbol{s}' \in \mathcal{S}} \mathcal{P}_{\boldsymbol{s}, \boldsymbol{s}'} \, \mathcal{V}_{\boldsymbol{\pi}}(\boldsymbol{s}') \right)$$

- If the action has a higher value, the policy is better
- \mathcal{V}_* is the unique solution to the Bellman optimality eq.
- If this greedy operation does not change V, then it converged to the optimal policy because it satisfies the Bellman optimality eq.



Dynamic programming algorithms

turn the Bellman eq. into update rules

PredictionExpectation equationIterative policy evaluationTemporal differenceControlExpectation equation + greedy policyPolicy iterationSarsaControlOptimality equationValue iterationO-learning	Problem	Bellman equation	Algorithm	Sample-based version
	Prediction	Expectation equation	Iterative policy evaluation	Temporal difference
Control Optimality equation Value iteration O-learning	Control	Expectation equation + greedy policy	Policy iteration	Sarsa
	Control	Optimality equation	Value iteration	Q-learning

when we don't know ${\mathcal P}$

Off-policy learning

On-policy: improve and evaluate the policy being used to select actions **Off-policy**: improve and evaluate a different policy from the one used to select actions

- > Learn a target policy π (optimal policy) while...
- ...selecting actions from behavior policy b (exploratory policy)

Provides another strategy for continuous exploration (experiences a larger # of states)

Temporal difference learning

TD learning is learning a prediction from another, later learned prediction \blacktriangleright learning a guess from a guess (you don't know the true \mathcal{V})

 $\mathcal{V}(s) \leftarrow \mathcal{V}(s) + \alpha [\mathcal{R} + \gamma \mathcal{V}(s') - \mathcal{V}(s)]$

- Difference between both predictions = temporal difference
- No \mathcal{P} model needed (unlike in dynamic programming)
 - Allows you to estimate the value function before the episode is finished
 - Making long-term predictions is exponentially complex
 Memory scales with the #steps of the prediction

 - TD model = standard model of reward systems in the brain

Off-policy TD control

 $Q(s,a) \leftarrow Q(s,a) + \alpha[\mathcal{R} + \gamma \max Q(s',a) - Q(s,a)]$

Converges to the optimal value function as long as the agent continues to explore sampling the state-action space

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Q-learning

Overview of RL methods

Tabular solution methods

- Iterative (dynamic programming)
- Sample-based (Monte-Carlo evaluation)
- > Temporal-difference learning

- Used to solve finite MDPs
- Value functions are stored as arrays (tables)
- Methods can often find exact solutions

In real-life situations, we cannot store the values of each possible state in an array, especially in continuous problems

Autonomous driving: array per possible image the camera sees?

Approximate solution methods

- Value-based > Policy gradient
- Policy-based > Actor-critic

- Approximate value by function parametrized by a weight vector --> neural networks (learning!)
- Applicable to partially observable problems

Approximate solution methods

Value-based

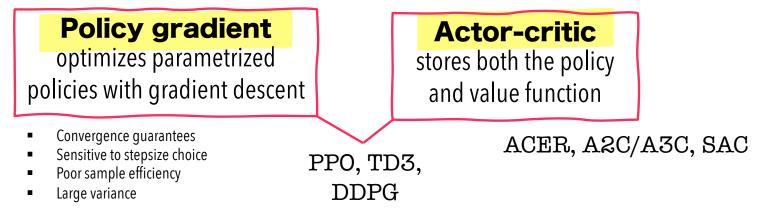
contains a value function, policy is implicit

Sample efficient

- DQN, NAF
- Computationally fast
- Unstable (bias, don't know true V)

Policy-based

does not store the value function, only the policy



	Description	Policy	Action space	State space	Operator
DQN	Deep Q Network	Off-policy	Discrete	Continuous	Q-value
DDPG	Deep Deterministic Policy Gradient	Off-policy	Continuous	Continuous	Q-value
A3C	Asynchronous Advantage Actor- Critic Algorithm	On-policy	Continuous	Continuous	Advantage
TRPO	Trust Region Policy Optimization	On-policy	Continuous	Continuous	Advantage
PPO	Proximal Policy Optimization	On-policy	Continuous	Continuous	Advantage
TD3	Twin Delayed Deep Deterministic Policy Gradient	Off-policy	Continuous	Continuous	Q-value
SAC	Soft Actor Critic	Off-policy	Continuous	Continuous	Advantage

Model-free

The agent simply relies on some trial-and-error experience for action selection

- The environment is initially unknown
- The agent interacts with the environment
- The agent improves its policy
 - ➡ all algorithms from previous slide

Model-based

Predictive model: "what will happen if I take this action?"

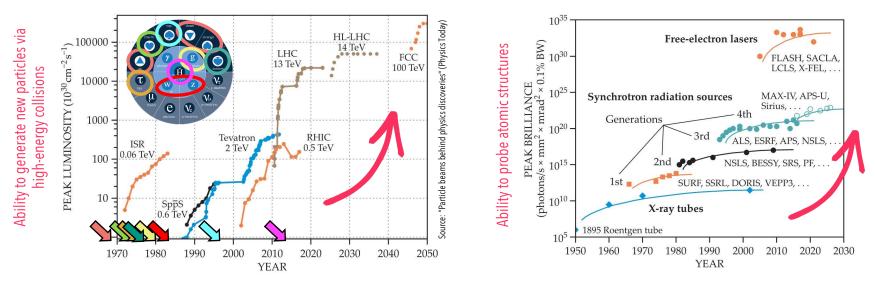
- The environment is known
- The agent performs internal computations with its model without external interaction
- The agent improves its policy



Particle accelerators …

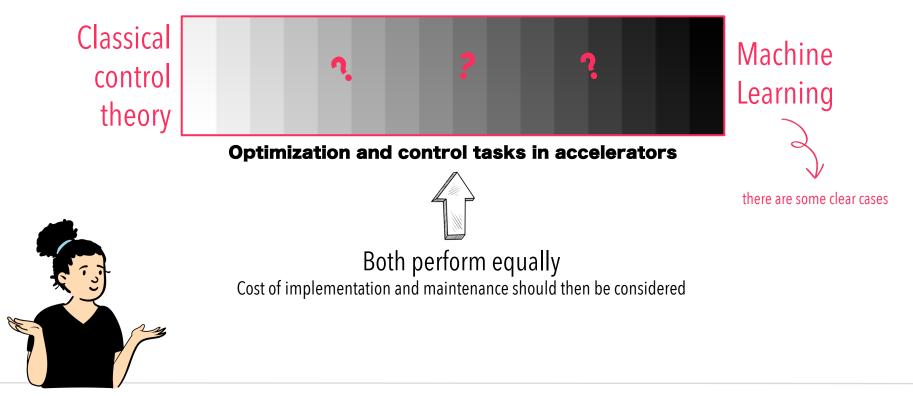
...are major tools for basic and applied research, industry & medicine worldwide

...make fundamental discoveries in particle physics



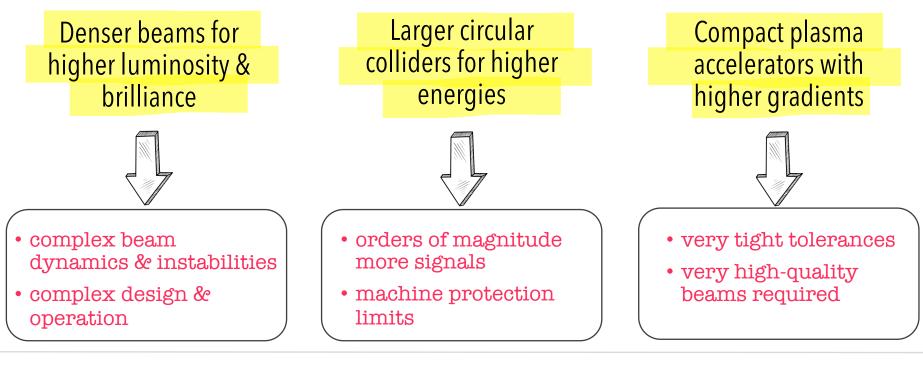
Technological innovation is needed to keep up with the challenging goals!

When to apply machine learning?



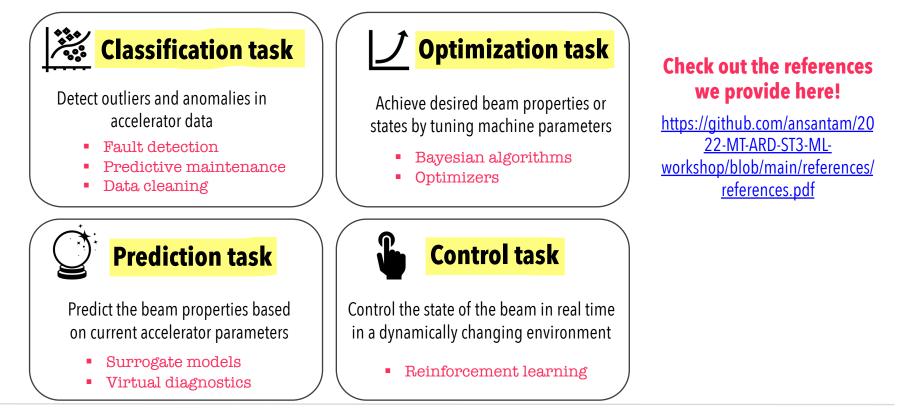
Future accelerators trends and challenges

and this is not considering user's needs!

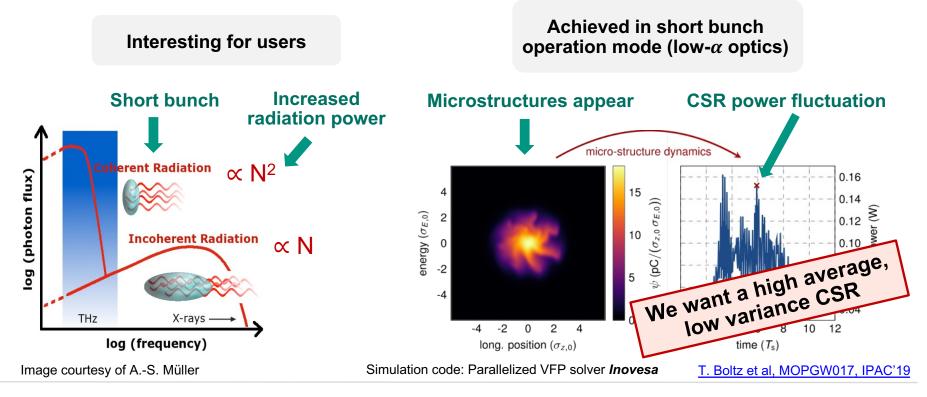


What can machine learning do for us?

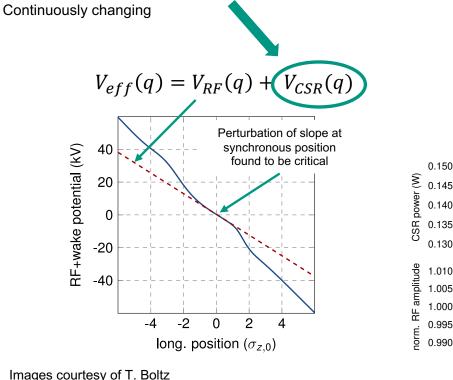
Very fast predictions by evaluating an already trained model



Motivation Coherent Synchrotron Radiation (CSR)



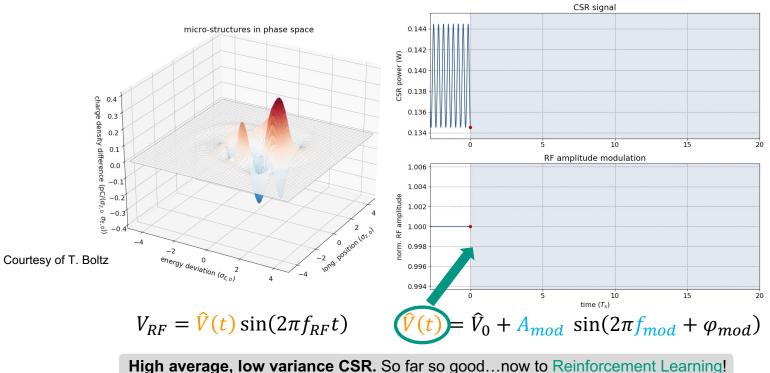
Influencing the micro-bunching instability CSR self interaction



Compensate the effect of the CSR perturbation by modulating the RF voltage (amplitude) $V_{RF} = \hat{V}(t) \sin(2\pi f_{RF}t)$ $\hat{V}(t) = \hat{V}_0 + A_{mod} \sin(2\pi f_{mod} + \varphi_{mod})$ Initial damping, but quickly out of sync...we need Constant modulation dynamic control! 10 0 5

time (T_s)

RF voltage modulation with manual control



Mitigation via Dynamic RF Amplitude Modulation

Applying reinforcement learning

Action

 $\widehat{V}(t) = \widehat{V}_0 + A_{mod} \sin(2\pi f_{mod} + \varphi_{mod})$

Observable (state definition)

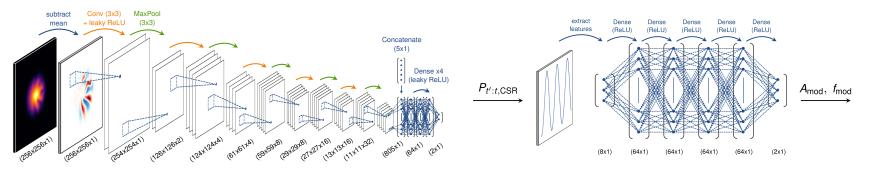
Charge distribution Input: (256x256) matrix + (5x1) feature vector

Reward

R = μ_{CSR} - $w \sigma_{CSR}$ where w is a weight Could we improve the reward definition?

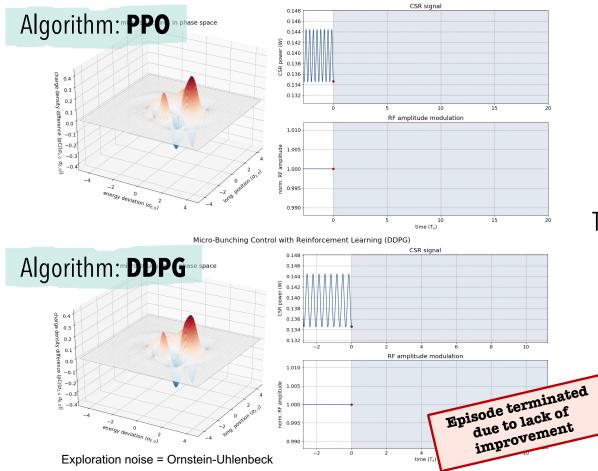
Observable (state definition)

CSR signal Input: (8x1) feature vector Easier to measure & process



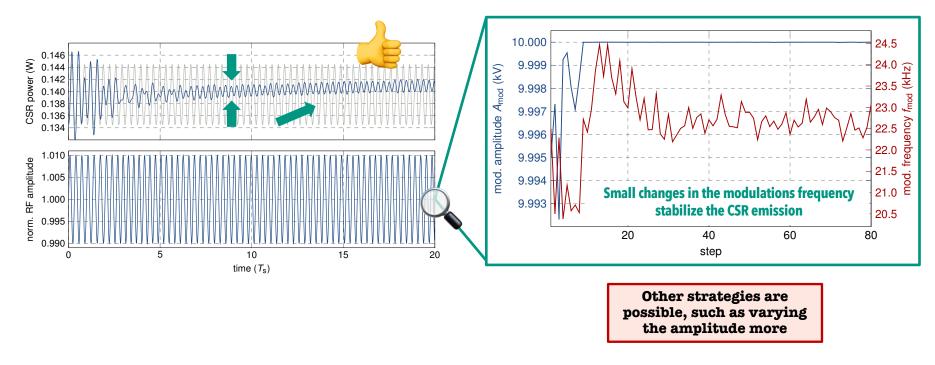
Images courtesy of T. Boltz

Micro-Bunching Control with Reinforcement Learning (PPO)



Tests in simulation with CSR signal as state definition

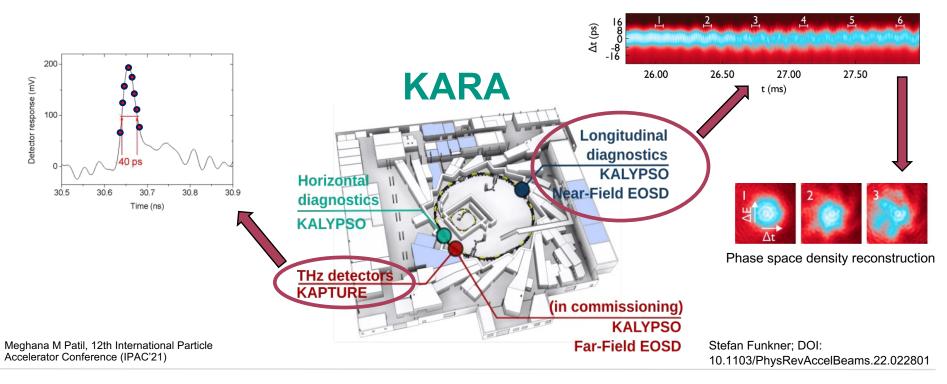
Evolution of the actions with time (PPO)



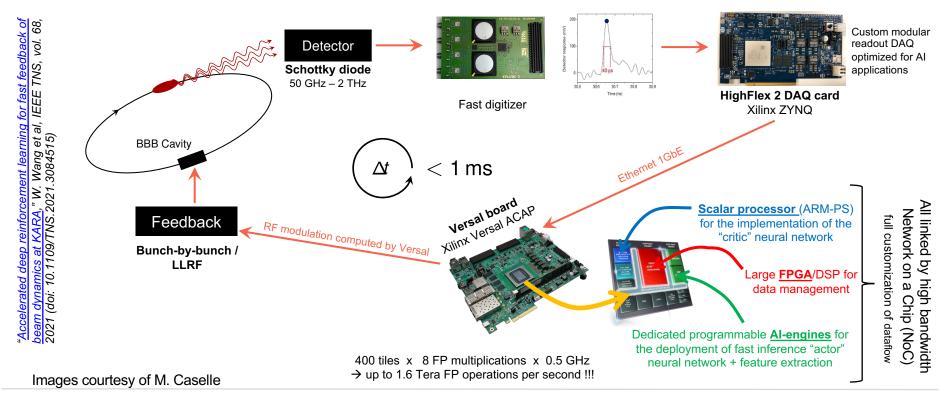
Images courtesy of T. Boltz

1 step = 0.25 synchrotron periods (chosen small enough for the agent to be able to react to the changing micro-structure dynamics)

Real-time, high-repetition data acquisition State-of-the-art detectors



In practice: we need hardware! Fast feedback for real-time optimization

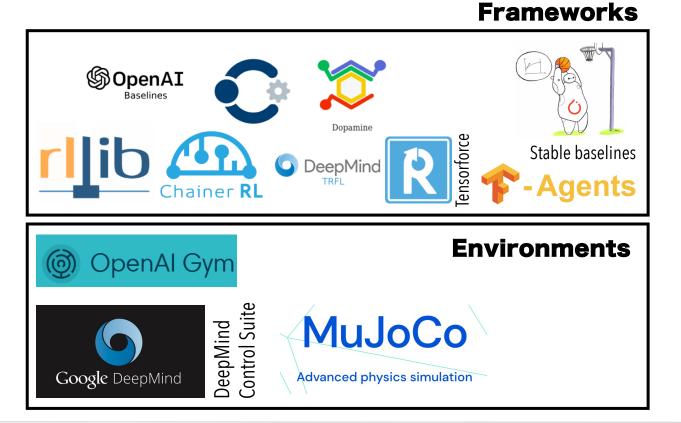


Thank you for your attention! What questions do you have for me?

- <u>Sutton & Barto book</u>
- https://arxiv.org/pdf/cs/9605103.pdf
- <u>Reinforcement learning lectures by David Silver</u>
- https://spinningup.openai.com/en/latest/
- <u>Coursera RL specialization</u>

Let's connect! andrea.santamaria@kit.edu / @ansantam

Reinforcement learning

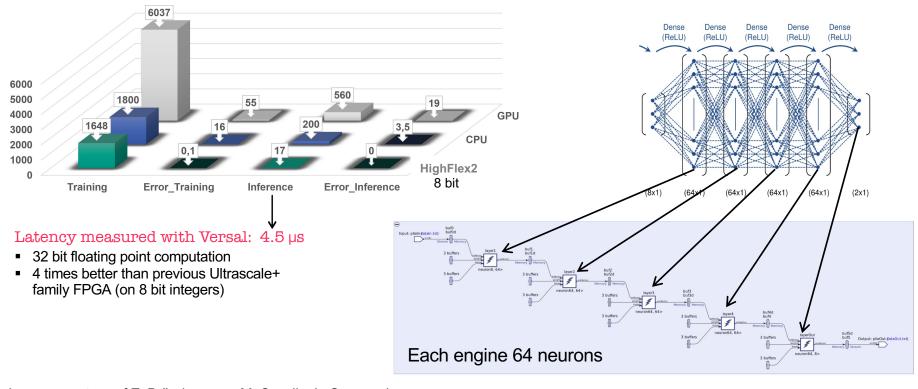


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https://neptune.ai/blog/the-best-tools-for-reinforcement-learning-in-python

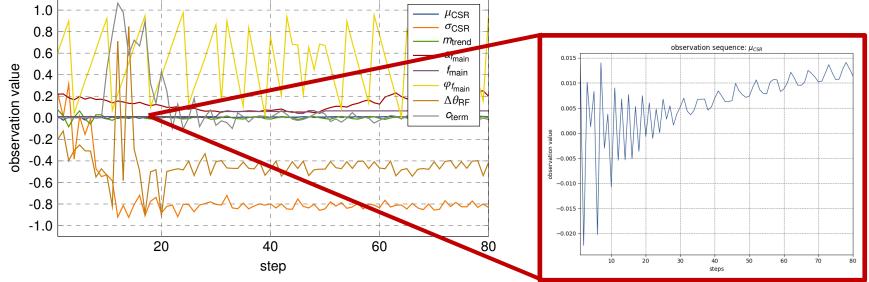
How fast can neural networks run?



Images courtesy of E. Bründermann, M. Caselle, L. Scomparin W. Wang, M. Caselle, et al IEEE TNS, https://doi.org/10.1109/TNS.2021.3084515 (2021)

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Observation vector based on the CSR signal



- μ_{CSR} is the normalized mean of the CSR power signal in the last time period.
- σ_{CSR} is the normalized standard deviation of the CSR power signal in the last time period.
- *m*_{trend} is a slow trend of the CSR power signal
- $a_{f_{main}}$ is the amplitude of the main frequency in the Fourier transformed CSR signal.
- f_{main} is the main frequency in the Fourier transformed CSR signal.
- $\varphi_{f_{main}}$ is the phase of the main frequency in the Fourier transformed CSR signal.
- $\Delta \theta_{RF}$ is the relative phase between the CSR signal and the applied RF signal (amplitude modulation).
- c_{term} models the termination condition (difference between the last reward and the one 10 steps prior).
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