

### Reinforcement learning and its application in particle accelerators

Andrea Santamaría García

12/09/2022 - Conceptual Advances in Deep Learning

#### Machine learning in the search for new fundamental **physics**

Georgia Karagiorgi ⊠, Gregor Kasieczka ⊠, Scott Kravitz ⊠, Benjamin Nachman ⊠ & David Shih ⊠

Nature Reviews Physics 4, 399-412 (2022) Cite this article

924 Accesses | 11 Altmetric | Metrics

#### **Abstract**

Compelling experimental evidence suggests the existence of new physics be established and tested standard model of particle physics. Various current an experiments are searching for signatures of new physics. Despite the variety

#### Pervasive machine learning in physics

Nature Reviews Physics 4, 353 (2022) | Cite this article

1325 Accesses | 6 Altmetric | Metrics

No longer restricted to data analysis, machine learning is now increasingly being used in theory, experiment and simulation  $-$  a sign that data-intensive science is starting to encompass all traditional aspects of research.

#### **Machine Learning Pins Down Cosmological Parameters**

August 19, 2022 · Physics 15, s111

Cosmological constraints can be improved by applying machine learning to a combination of data from two leading probes of the large-scale structure of the Universe.

#### ARTIFICIAL INTELLIGENCE (AI)

Computers mimic human behaviour

- First chatbots
- Robotics
- Expert systems
- Natural language processing
- Fuzzy logic
- Explainable AI



#### MACHINE LEARNING (ML)

Computers learn without being explicitly programmed to do so and improve with experience Multi-layered neural networks perform

Collection of **data-driven** methods / algorithms

Data + Algorithm

Focused on **prediction** / **optimization / control** based on properties learned from data

Tries to **generalize** to unseen scenarios

#### DEEP LEARNING (DL)

certain tasks with high accuracy



- Speech/handwriting recognition
- Language translation
- Recommendation engines

Narrow AI

Computer vision







#### **Deep Learning Networks**

- § Convolutional Neural Networks
- § Recurrent Neural Networks
- § Long Short-Term Memory **Networks**
- § Autoencoders
- § Deep Boltzmann Machine
- § Deep Belief Networks

#### **Bayesian Algorithms**

- § Naive Bayes
- § Gaussian Naive Bayes
- § Bayesian Network
- § Bayesian Belief Network
- § Bayesian optimization

**Regularization, dimensionality reduction, ensemble, evolutionary algorithms, computer vision, recommender systems, …**

#### Reinforcement learning more than machine learning



**Psychology** (classical conditioning) **Neuroscience** (reward system) **Economics** (game theory) **Mathematics** (operations research) **Engineering** (optimal control, planning)

### Reinforcement learning

understanding how the human brain learns makes deci





#### The RL problem

#### **Reward hypothesis**

all goals can be described by the maximization of expected cumulative sum of a received scalar signal "Reward is enough"



an agent must learn through trial-and-error interactions with a dynamic environment



#### How to cumulate reward?

Model

agent's representation of the environment

Agent Which behaviors perform well in this environment?

**Policy** agent's behaviour function<br>(how the agent picks its actions)

Estimate the utility of taking actions in particular states of the environment (evaluation of the policy)

## Value function  $how good each state$  and/or action are

- $\triangleright$  **Prediction**: evaluate the future given a policy
- $\triangleright$  **Control**: optimize the future (find the best policy)

### Challenges in RL

#### Trade-off between exploitation and exploration

- Actions may have long-term consequences
- Reward might be delayed (does not happen immediately)

should the agent sacrifice immediate reward to gain more long term reward?

The agent needs to:

- **► Exploit** what it has already experienced in order to obtain reward now
- **Explore** the environment to select better actions in the future by sacrificing known reward now

…and both cannot be pursued exclusively without failing at the task



Must:

- § Be able to **sense the state** of its environment to some extent
- Be able to **take actions** that affect that state
- **Have a goal** or goals relating to the state of the environment

#### **Markov Decision Processes**

Sensation

"Free-will

**Motivation** 

Include this 3 elements without trivializing any of them

### Markov Decision Process (MDP)

Mathematical framework for modelling sequential decision making

A Markov Decision Process is a 5-tuple:

$$
(\mathcal{S}, \mathcal{A}, \mathcal{P}_{SS}^a, \mathcal{R}_S^a, \gamma) \quad \text{ } \mathcal{S} \text{ = finite set of states}
$$



**State** information used to determine what happens next

A state transition can be:

- Deterministic  $s_{t+1} = f(\mathcal{H}_t)$
- Stochastic  $s_{t+1}{\thicksim}\mathbb{P}(s_{t+1}|\tau_t)$

**Trajectory** sequence of states and

 $\tau = (s_0, a_0, s_1, a_1, s_2, a_2, ...)$ 

**Environment state (S<sup>e</sup>)**: environment's internal representation, usually not visible to the agent

**Agent state**  $(S^a)$ **: agent's internal representation,** used by the RL algorithm to pick the next action

**Observation (O)**: partial description of a state, which may omit information

### Markov Decision Process (MDP)

Mathematical framework for modelling sequential decision making

A Markov Decision Process is a 5-tuple:

$$
(\mathcal{S}, \mathcal{A}, \mathcal{P}_{SS}^a, \mathcal{R}_S^a, \gamma) \quad \text{ } s \text{ = finite set of states}
$$



information used to determine what happens next

A state transition can be:

- Deterministic  $s_{t+1} = f(\mathcal{H}_t)$ **Stochastic**  $s_{t+1} \sim \mathbb{P}(s_{t+1} | \tau_t)$
- 

**Trajectory** sequence of states and

 $\tau = (s_0, a_0, s_1, a_1, s_2, a_2, ...)$ 

**Markov state / property** A state is Markov if and only if:

$$
\mathbb{P}[s_{t+1}|s_t] = \mathbb{P}[s_{t+1}|s_{1,\dots,t}]
$$

- The state is a sufficient statistic of the future
- The future is independent of the past, given the present
- Once the state is known, the history may be discarded

state transitions of an MDP satisfy the Markov property

#### Fully observable environments  $\mathcal{O}_t = \mathcal{S}_t^a = \mathcal{S}_t^e$

- § Agent directly observes environment state
- § Necessary condition to formalize an RL problem with an MDP

## Partially observable environments  $\delta_t^a \neq \delta_t^e$

Agent constructs its own state representation:

- Complete trajectory:
- $\blacksquare$  Beliefs of environment state:
- Recurrent neural networks:

$$
\begin{aligned} \mathcal{S}_t^a &= \tau_t \\ \mathcal{S}_t^a &= \left( \mathbb{P}[\mathcal{S}_t^e = s_1], \dots, \mathbb{P}[\mathcal{S}_t^e = s_n] \right) \\ \mathcal{S}_t^a &= \sigma(w_0 \mathcal{O}_t + w_s \mathcal{S}_{t-1}^a) \end{aligned}
$$

 $\rightarrow$  Partially observable MDP

### Markov Decision Process (MDP)

Mathematical framework for modelling sequential decision making

A Markov Decision Process is a 5-tuple: 
$$
(\mathcal{S}, \mathcal{A}, \mathcal{P}_{ss}^a, \mathcal{R}_s^a, \gamma)
$$

#### State transition model / probability **Predicts the next state** (dynamics of the environment)

$$
\mathcal{P}_{SS'}^a = \mathbb{P}[\mathcal{S}_{t+1} = s' | \mathcal{S}_t = s, \mathcal{A} = a] \text{ Probability of ending in state s' aftertaking action a while being in state s}
$$



Transition probabilities from all states and successor states

### Non-deterministic environment

Taking the same action in the same state on two different occasions may result in different next states

 $\epsilon$   $\epsilon$  $- \rightarrow$ 



#### Markov Decision Process (MDP)

Mathematical framework for modelling sequential decision making

A Markov Decision Process is a 5-tuple: 
$$
(\mathcal{S}, \mathcal{A}, \mathcal{P}_{ss}^a, \mathcal{R}_s^a, \gamma)
$$



The goal is to maximize the return

- The discount factor  $\gamma \in [0, 1)$  avoids infinite returns (sum converges)
- It values immediate reward over delayed reward (human-like)
- It deals with uncertainty about the future (no perfect model of env.)



- Policy  $\pi$  completely defines how the agent will behave
- It's a distribution over actions given a certain state



**Deterministic**:  $a=\pi(s)$ 

**Stochastic**: 
$$
\pi(a|s) = \mathbb{P}[\mathcal{A}_t = a|\mathcal{S}_t = s]
$$

Probability of taking a specific action by being in a specific state **Categorical** (discrete action spaces)

Given an MDP  $\langle S, A, P, R, \gamma \rangle$  and a policy  $\pi$ :

$$
\mathcal{P}_{s,s'}^{\pi} = \sum_{a \in \mathcal{A}} \pi(a|s) \mathcal{P}_{s,s'}^{a} \qquad \mathcal{R}_{s}^{\pi} = \sum_{a \in \mathcal{A}} \pi(a|s) \mathcal{R}_{s}^{a}
$$

### Value function Estimation of expected

future reward

#### **A way to compare policies**

- Used to choose between states depending on how much reward we expect to get
- Depends on the agent's behavior (policy)

#### State-value function

Expected return starting from state s and following policy  $\pi$ (evaluates the policy)

$$
\mathcal{V}_{\overline{\mathcal{D}}}(s) = \mathbb{E}_{\pi}[G_t | S_t = s]
$$

Action-value function

Expected return starting from state  $s$ , taking action  $a$ , and following policy  $\pi$ 

$$
Q_{\pi}(s, a) = \mathbb{E}_{\pi}[G_t \mid \mathcal{S}_t = s, \mathcal{A}_t = a]
$$

"Q function"

### Bellman optimality equation

The state-value function can be decomposed into:

- **•** immediate reward  $\mathcal{R}_{t+1}$
- **•** discounted value of next state  $\gamma v(S_{t+1})$

$$
\mathcal{V}(s) = \mathbb{E}[G_t | S_t = s]
$$
\n
$$
= \mathbb{E}[\mathcal{R}_{t+1} + \gamma \mathcal{R}_{t+2} + \gamma^2 \mathcal{R}_{t+3} ... | S_t = s]
$$
\n
$$
= \mathbb{E}[\mathcal{R}_{t+1} + \gamma (\mathcal{R}_{t+2} + \gamma \mathcal{R}_{t+3} ...)| S_t = s]
$$
\n
$$
= \mathbb{E}[\mathcal{R}_{t+1} + \gamma G_{t+1} | S_t = s]
$$
\n
$$
= \mathbb{E}[\mathcal{R}_{t+1} + \gamma G_{t+1} | S_t = s]
$$
\n
$$
= \mathbb{E}[\mathcal{R}_{t+1} + \gamma V(S_{t+1}) | S_t = s]
$$
\n
$$
\mathcal{V}(s) = \mathcal{R}_s + \gamma \sum_{s' \in S} \mathcal{P}_{s,s'} \mathcal{V}(s')
$$

### Bellman expectation equation

Considering the policy  $\pi$  we get:

$$
\mathcal{V}(s) = \sum_{a \in \mathcal{A}} \pi(a|s) \left( \mathcal{R}_s^a + \gamma \sum_{s \in \mathcal{S}} \mathcal{P}_{s,s}^a, \mathcal{V}(s') \right)
$$

Direct solution only for small MRPs

 $\triangleright$  System of S simultaneous linear equations with S unknowns

Other ways of solving it:

- $\triangleright$  Iteratively (dynamic programming)
- $\triangleright$  Sampling (Monte-Carlo evaluation)
- $\triangleright$  Approximation (temporal-difference learning)

### Example: gridworld

The agent needs to get from state **0** to state **15** to get out of the maze



#### Actions  $\mathcal{A} = (\uparrow, \downarrow, \leftarrow, \rightarrow)$

#### Deterministic env:  $\mathcal{P}^a_{S,S'}=1$

no discount  $\gamma$ 







### Example: gridworld

#### Value function

$$
\mathcal{V}(s) = \sum_{a \in \mathcal{A}} \pi(a|s) \left( \mathcal{R}_s^a + \gamma \sum_{s \in \mathcal{S}} \mathcal{P}_{s,s}^a, \mathcal{V}(s')
$$

Solving simultaneously linear set of equations:  $\triangleright$  environment's dynamics are completely known

```
0.5*v0 - 0.25*v1 - 0.25*v4 + 1.0 = 0-0.25*V0 + 0.5*V1 - 0.25*V5 + 1.0 = 00.25*V3 - 0.25*V7 + 1.0 = 0-0.25*V0 + 0.75*V4 - 0.25*V5 - 0.25*V8 + 1.0 = 0-0.25*v1 - 0.25*v4 + 0.75*v5 - 0.25*v6 + 1.0 = 0-0.25*V10 - 0.25*V5 + 0.75*V6 - 0.25*V7 + 1.0 = 0-0.25*v3 - 0.25*v6 + 0.5*v7 + 1.0 = 0-0.25*V12 - 0.25*V4 + 0.5*V8 + 1.0 = 00.5*V10 - 0.25*V14 - 0.25*V6 + 1.0 = 00.25*V12 - 0.25*V8 + 1.0 = 0-0.25*V10 + 0.5*V14 + 0.5 = 0
```
11 variables, 11 equations



how much value this policy has?

#### Example: gridworld



**26** Andrea Santamaria Garcia – Reinforcement Learning

how much value this po

### Dynamic programming algorithms turn the Bellman eq.

- § **Prediction**: what's the value for a specific policy? ✅
- § **Control**: which policy gives as much reward as possible?  $\rightarrow$  the policy with more value!



For any MDP:

• There exists an optimal policy  $\pi_*$  that is better or equal to all other policies  $\pi_* \geq \pi \,\forall \pi$ 

into update rules

• All optimal policies achieve the optimal value function  $\mathcal{V}_{\pi_*} = \mathcal{V}_*(s)$  and  $Q_{\pi_*} = Q_*(s, a)$ 

So…do I have to calculate the value of every policy and compare them?

 $|{\mathcal{A}}|$   $|{\mathcal{S}}|$  deterministic policies in an MDP

 $4^{11} \approx 4$  million policies for simple gridworld example

#### Bellman optimality equations

$$
\mathcal{V}_{\pi*}(s) = \mathbb{E}_{\pi*}[G_t | S_t = s] = \max_{\pi} \mathcal{V}_{\pi}(s) \quad \forall \ s \in S
$$

$$
\mathcal{Q}_{\pi*}(s) = \max_{\pi} \mathcal{Q}_{\pi}(s) \quad \forall \ s \in S, a \in \mathcal{A}
$$

 ${\mathcal P}_{_{S,S}}\big({\mathcal V}_{*}({s}')$ 

By replacing the optimal policy on the Bellman equations we get:

 $\pi_*$  assigns probability 1 to the action that receives the highest value

Optimal value functions

maximum value over every next possible state

$$
Q_*(s, a) = \mathcal{R}_s^a + \gamma \sum_{s' \in \mathcal{S}} \mathcal{P}_{s, s'}^a \max_{a'} Q_*(s', a')
$$

$$
\triangleright
$$
 Nonlinear(max), no closed-form solution

 $\triangleright$  Dynamic programming solutions only applicable if the dynamics of the system  $\mathcal P$ are known

 $v_*(s) = \max \left( R_s + \gamma \right)$ 

 $\overline{a}$ 

#### Determining an optimal policy

$$
\boldsymbol{\mathcal{V}}_{*}(\boldsymbol{s}) = \max_{a} \left( \mathcal{R}_{s} + \gamma \sum_{s' \in \mathcal{S}} \mathcal{P}_{s,s'} \, \mathcal{V}_{*}(s') \right)
$$

maximum over all actions



For any state we look at each available action and take the one that maximizes the argument

$$
\pi_*(s) = \underset{a}{\text{argmax}} \left( \mathcal{R}_s + \gamma \sum_{s' \in \mathcal{S}} \mathcal{P}_{s,s'} \, \mathcal{V}_*(s') \right)
$$
\n
$$
\underset{\text{particular action that}}{\text{particular action that}}
$$
\n
$$
\underset{\text{(greedy action)}}{\text{and } \text{matrix}}
$$



$$
\boldsymbol{\pi}_*(\boldsymbol{s}) = \operatorname*{argmax}_{a} Q_*
$$

#### Policy improvement & iteration

Let's consider a value function  $\mathcal{V}_{\pi}$  that is non-optimal, and we select an action that is greedy with respect to it:

$$
\boldsymbol{\pi}'(\boldsymbol{s}) = \underset{a}{\text{argmax}} \left( \mathcal{R}_{\boldsymbol{s}} + \gamma \sum_{\boldsymbol{s}' \in \boldsymbol{\mathcal{S}}} \mathcal{P}_{\boldsymbol{s},\boldsymbol{s}'} \, \mathcal{V}_{\boldsymbol{\pi}}(\boldsymbol{s}') \right)
$$

- § If the action has a higher value, the policy is better
- $\nu_*$  is the unique solution to the Bellman optimality eq.
- **•** If this greedy operation does not change  $\nu$ , then it converged to the optimal policy because it satisfies the Bellman optimality eq.



 $\pi_1 \rightarrow \mathcal{V}_{\pi 1} \rightarrow \pi_2$ 

improve

### Dynamic programming algorithms turn the Bellman eq.

into update rules



when we don't know  $P$ 

### Off-policy learning

**On-policy:** improve and evaluate the policy being used to select actions **Off-policy**: improve and evaluate a different policy from the one used to select actions

- $\triangleright$  Learn a target policy  $\pi$  (optimal policy) while...
- $\triangleright$  ... selecting actions from behavior policy *b* (exploratory policy)

Provides another strategy for continuous exploration (experiences a larger # of states)

### Temporal difference learning

- Learning method specialized for multi-step **prediction learning**
- TD learning is learning a prediction from another, later learned prediction  $\triangleright$  learning a guess from a guess (you don't know the true  $\nu$ )

 $V(s) \leftarrow V(s) + \alpha [\mathcal{R} + \gamma \mathcal{V}(s') - \mathcal{V}(s)]$ 

- $D$  Difference between both predictions  $=$  temporal difference
- No  $P$  model needed (unlike in dynamic programming)
	- § Allows you to estimate the value function before the episode is finished
	- Making long-term predictions is exponentially complex
		- $\triangleright$  Memory scales with the #steps of the prediction
	- TD model = standard model of reward systems in the brain

Q-learning Off-policy TD control

 $Q(s, a) \leftarrow Q(s, a) + \alpha [\mathcal{R} + \gamma \max Q(s', a) - Q(s, a)]$ 

Converges to the optimal value function as long as the agent continues to explore sampling the state-action space

**32** Andrea Santamaria Garcia – Reinforcement Learning

### Overview of RL methods

#### **Tabular solution methods**

- $\triangleright$  Iterative (dynamic programming)
- $\triangleright$  Sample-based (Monte-Carlo evaluation)
- $\triangleright$  Temporal-difference learning
- § Used to solve finite MDPs
- § Value functions are stored as arrays (tables)
- Methods can often find exact solutions

In real-life situations, we cannot store the values of each possible state in an array, especially in continuous problems

 $\triangleright$  Autonomous driving: array per possible image the camera sees?

#### **Approximate solution methods**

- **►** Value-based ► Policy gradient
	-
- Ø Policy-based Ø Actor-critic
- § Approximate value by function parametrized by a weight vector --> **neural networks (learning!)**
- § Applicable to partially observable problems

### Approximate solution methods

#### Value-based

contains a value function, policy is implicit

§ Sample efficient

#### DQN, NAF

- § Computationally fast
- Unstable (bias, don't know true  $\nu$ )

#### Policy-based

does not store the value function, only the policy





The agent simply relies on some trial-and-error experience for action selection

- The environment is initially unknown
- The agent interacts with the environment
- The agent improves its policy
	- all algorithms from previous slide

### Model-free Model-based

Predictive model: "what will happen if I take this action?"

- The environment is known
- The agent performs internal computations with its model without external interaction
- The agent improves its policy



#### Particle accelerators …

…are major tools for basic and applied research, industry & medicine worldwide

#### …make fundamental discoveries in particle physics



Technological innovation is needed to keep up with the challenging goals!

### When to apply machine learning?



#### Future accelerators trends and challenges and this is not considering user's needs!



#### What can machine learning do for us?

*Very fast predictions by evaluating an already trained model*



#### Coherent Synchrotron Radiation (CSR) **Motivation**



#### CSR self interaction Influencing the micro-bunching instability





#### RF voltage modulation with manual control



Mitigation via Dynamic RF Amplitude Modulation

### Applying reinforcement learning

#### **Action**

 $\hat{V}(t) = \hat{V}_{0} + A_{mod} \sin(2\pi f_{mod} + \varphi_{mod})$ 

#### **Observable (state definition)**

**Charge distribution** Input: (256x256) matrix + (5x1) feature vector

#### **Reward**

 $R = \mu_{CSR} - w \sigma_{CSR}$  where *w* is a weight Could we improve the reward definition?

#### **Observable (state definition)**

**CSR signal**

Input: (8x1) feature vector **Easier to measure & process**



Images courtesy of T. Boltz





as state definition

#### Evolution of the actions with time (PPO)



Images courtesy of T. Boltz **1** step = 0.25 synchrotron periods (chosen small enough for the agent to be able to react to the changing micro-structure dynamics)

#### State-of-the-art detectors Real-time, high-repetition data acquisition



#### **Fast feedback for real-time optimization** In practice: we need hardware!



# Thank you for your attention! What questions do you have for me?

- Sutton & Barto book
- § https://arxiv.org/pdf/cs/9605103.pdf
- **Reinforcement learning lectures by David Silver**
- § https://spinningup.openai.com/en/latest/
- Coursera RL specialization

**Let's connect!** andrea.santamaria@kit.edu / @ansantam

#### Reinforcement learning



Andrea Santamaria Garcia – Reinforcement Learning **50**

#### How fast can neural networks run?



Images courtesy of E. Bründermann, M. Caselle, L. Scomparin W. Wang, M. Caselle, et al IEEE TNS, https://doi.org/10.1109/TN

#### Observation vector based on the CSR  $\blacksquare$  signal



- $\mu_{CSR}$  is the normalized mean of the CSR power signal in the last time period.
- $\sigma_{\text{CSR}}$  is the normalized standard deviation of the CSR power signal in the last time period.
- $1/m_{trend}$  is a slow trend of the CSR power signal
	- $a_{f_{main}}$  is the amplitude of the main frequency in the Fourier transformed CSR signal.
	- $f_{main}$  is the main frequency in the Fourier transformed CSR signal.
	- $\varphi_{f_{main}}$  is the phase of the main frequency in the Fourier transformed CSR signal.
	- $\Delta\theta_{RF}$  is the relative phase between the CSR signal and the applied RF signal (amplitude modulation).
	- $\bullet$   $c_{term}$  models the termination condition (difference between the last reward and the one 10 steps prior).
- **52** Andrea Santamaria Garcia Reinforcement Learning