

# Supervised and Reinforced Jet-Parton Assignment for Particle Physics Analyses

Martin Erdmann, Benjamin Fischer, [Dennis Noll](#)

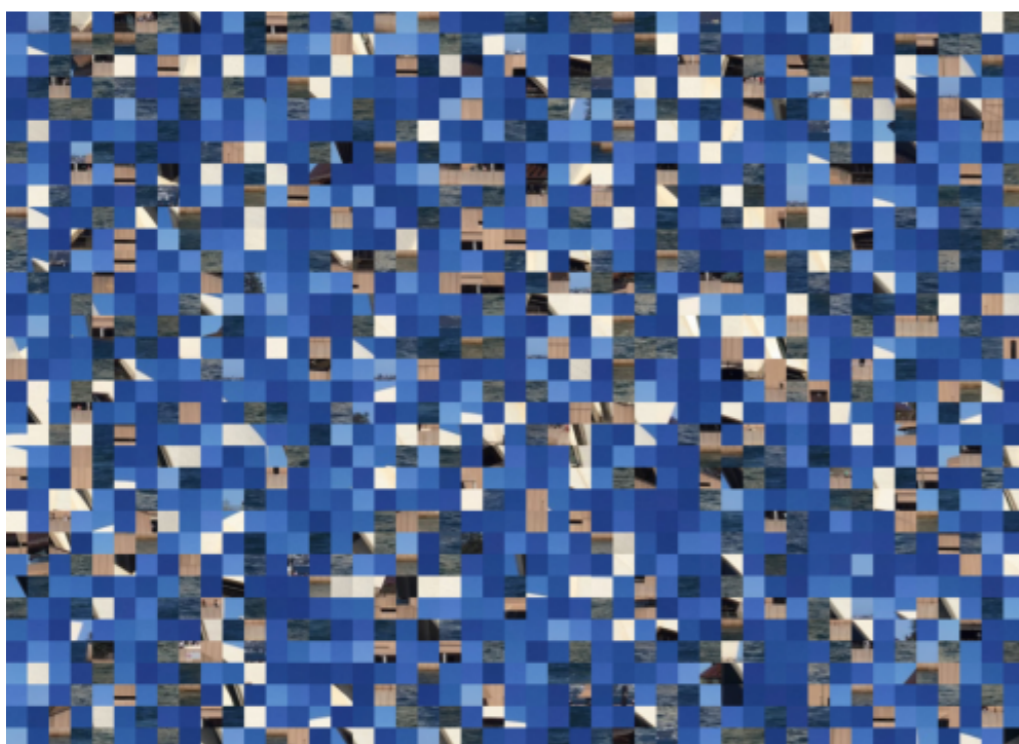
Conceptual Advances Workshop

13.09.22

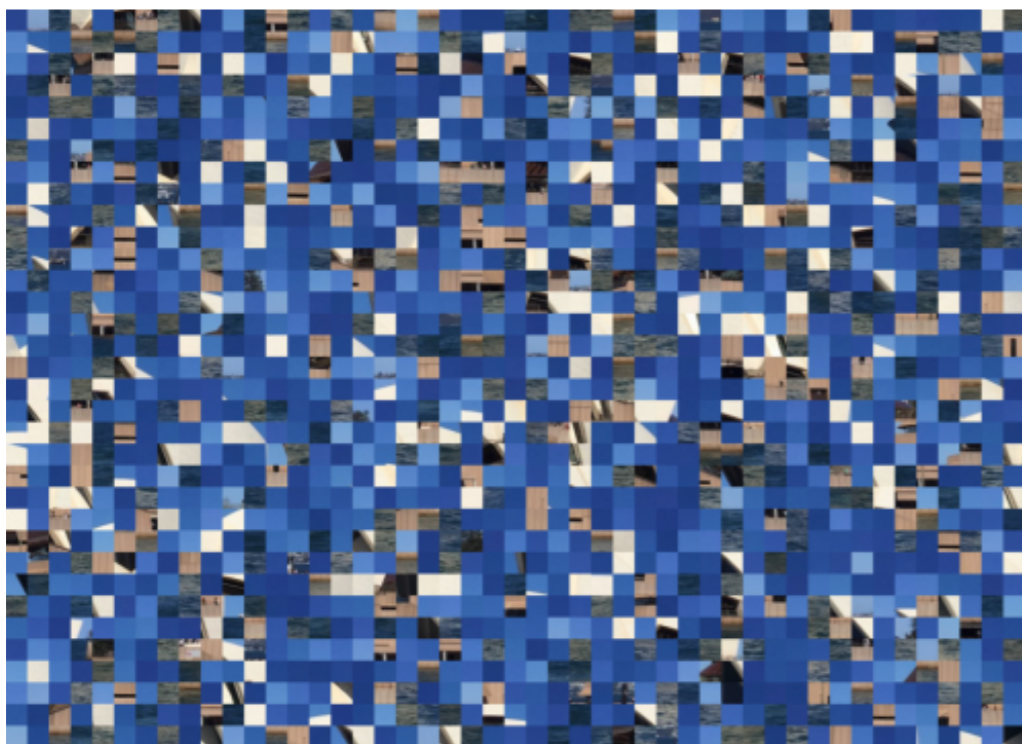


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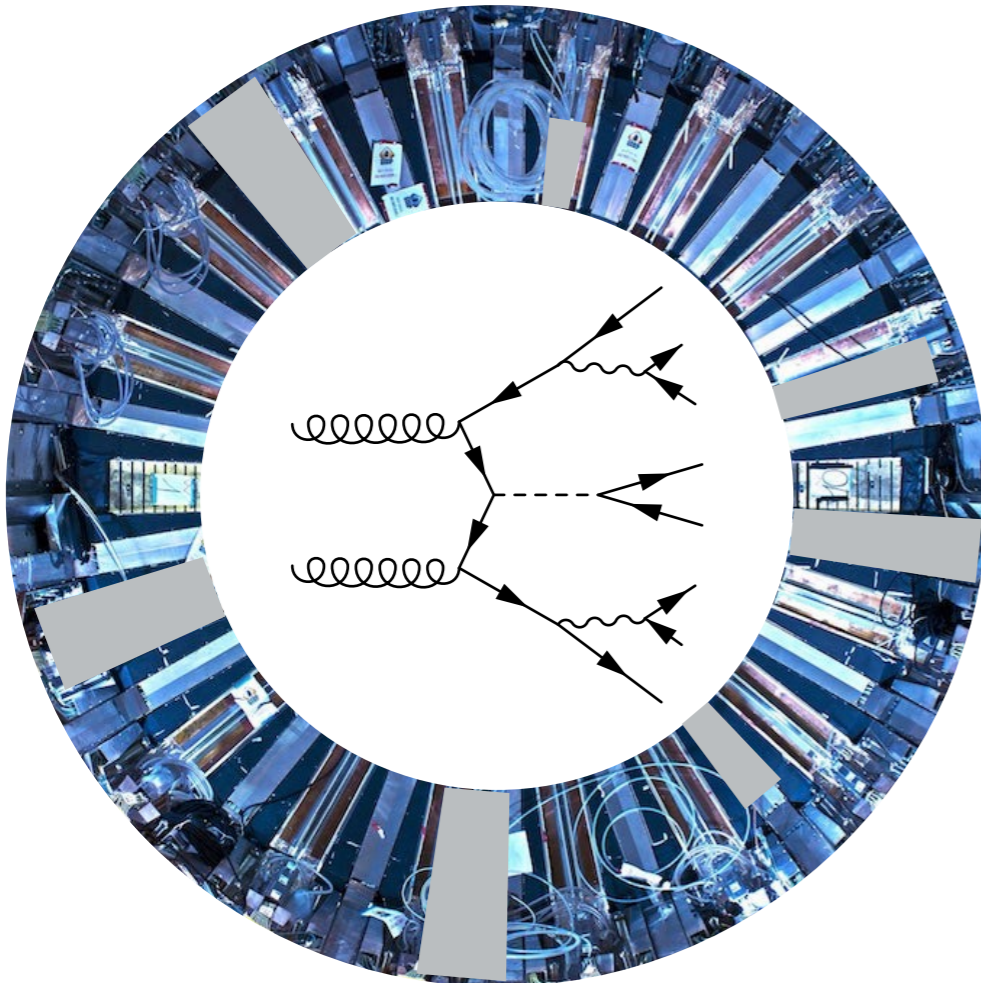
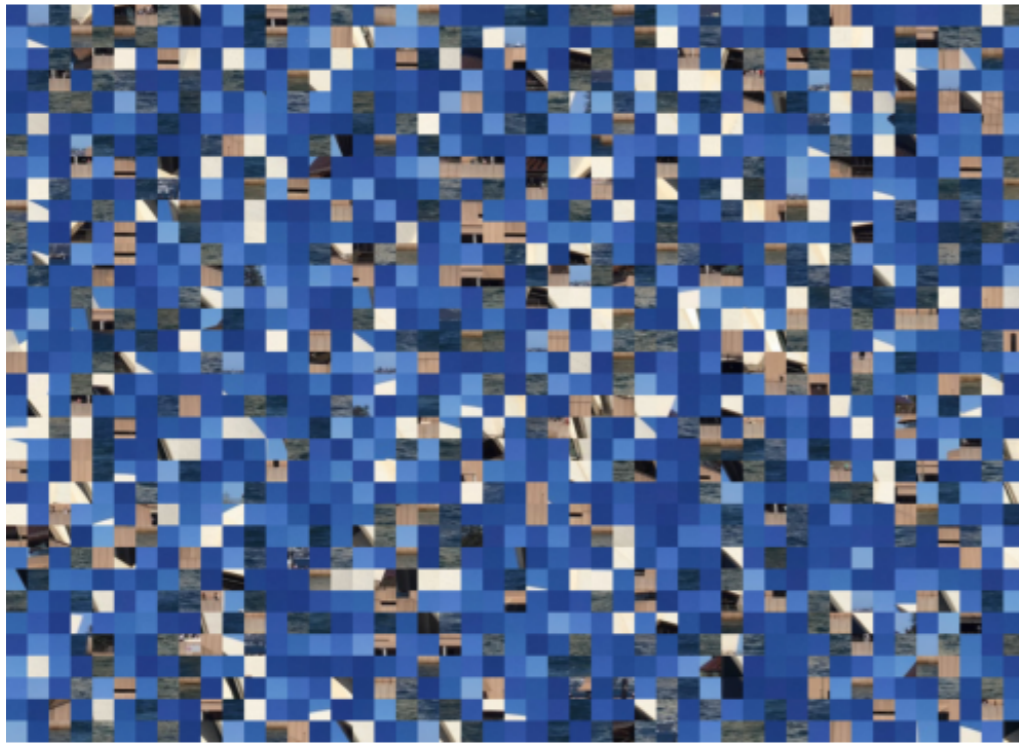
# 2 Motivation



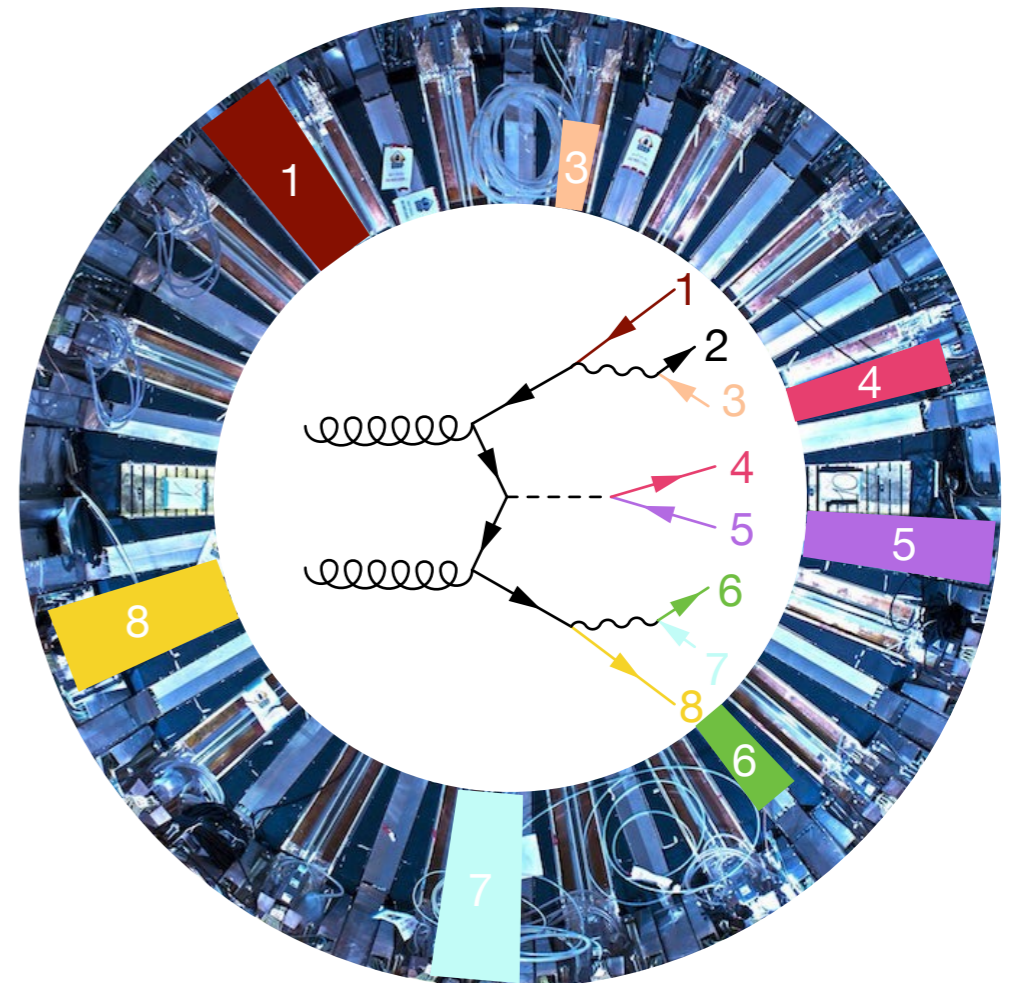
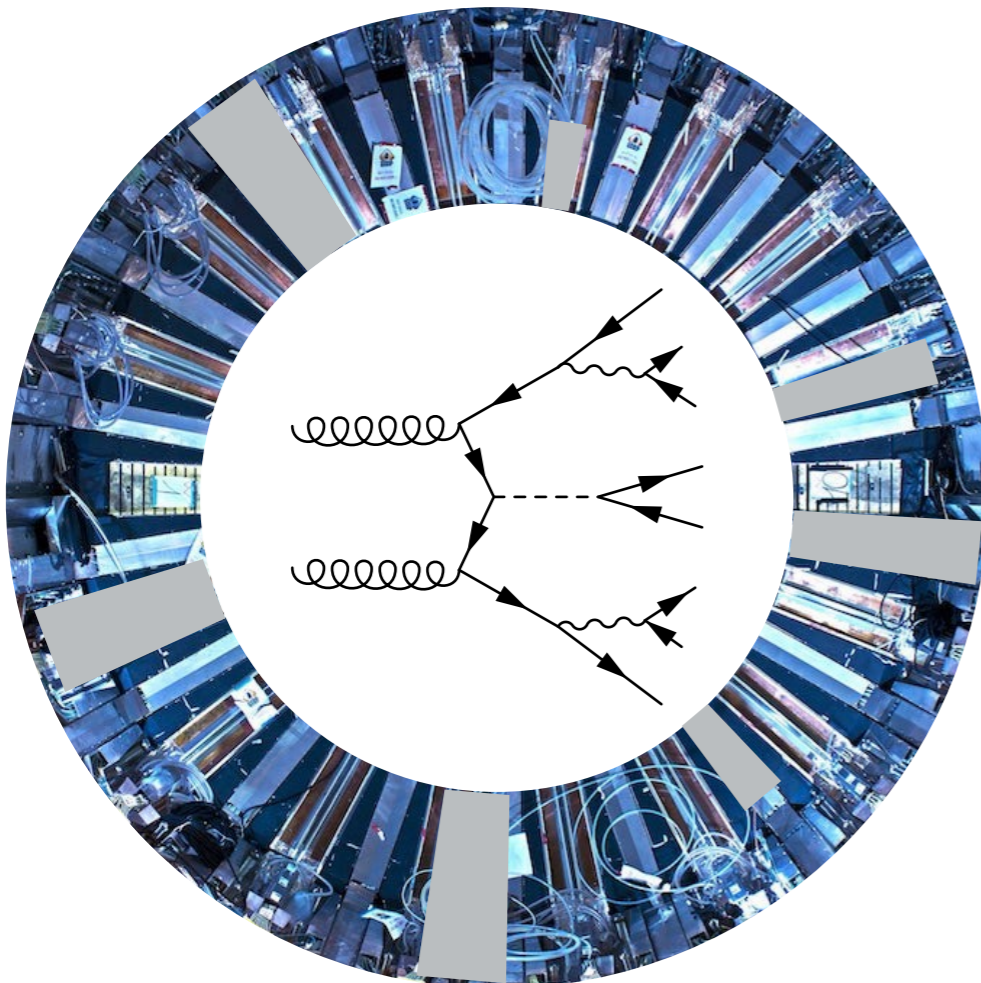
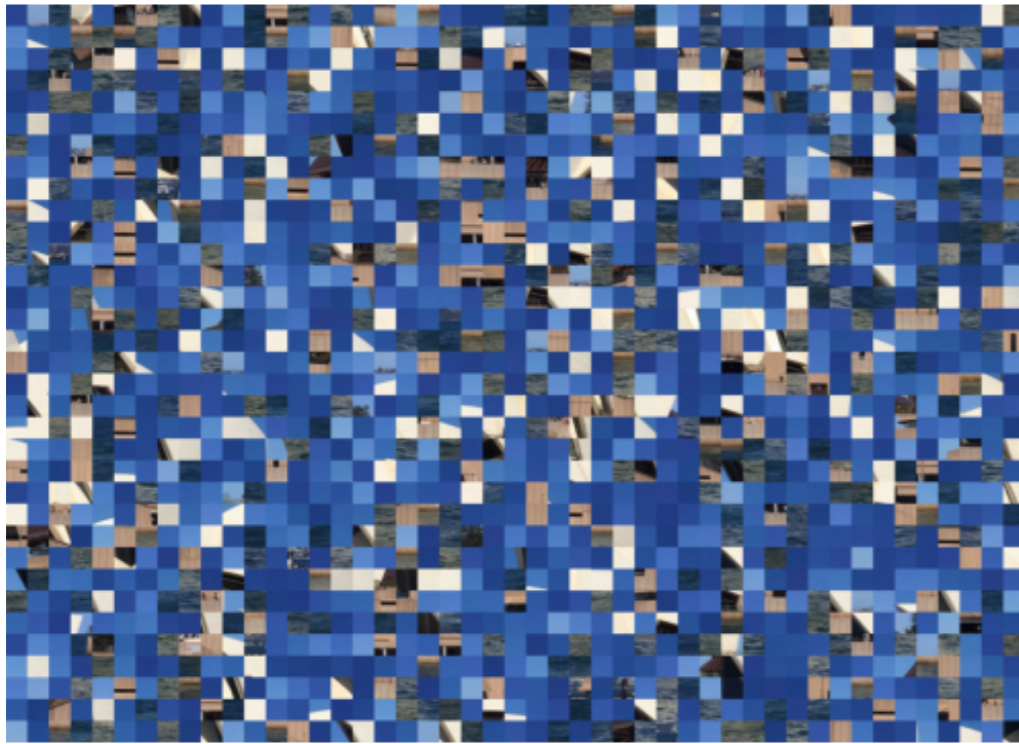
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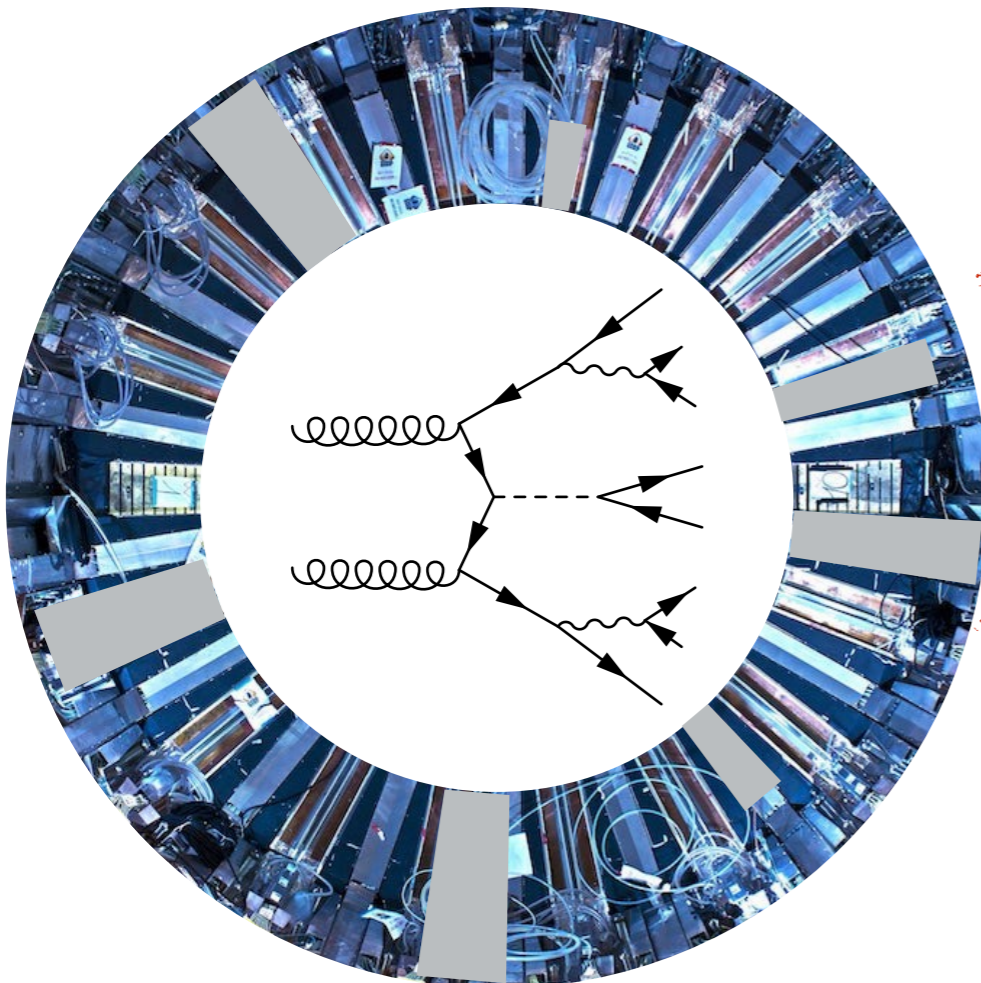
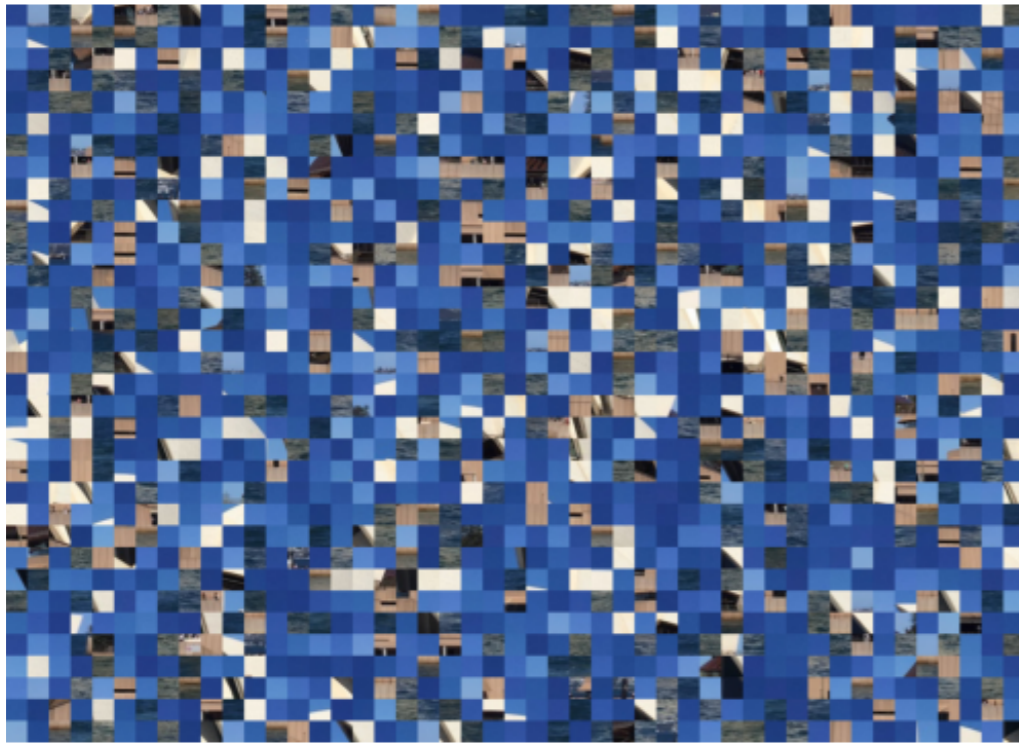


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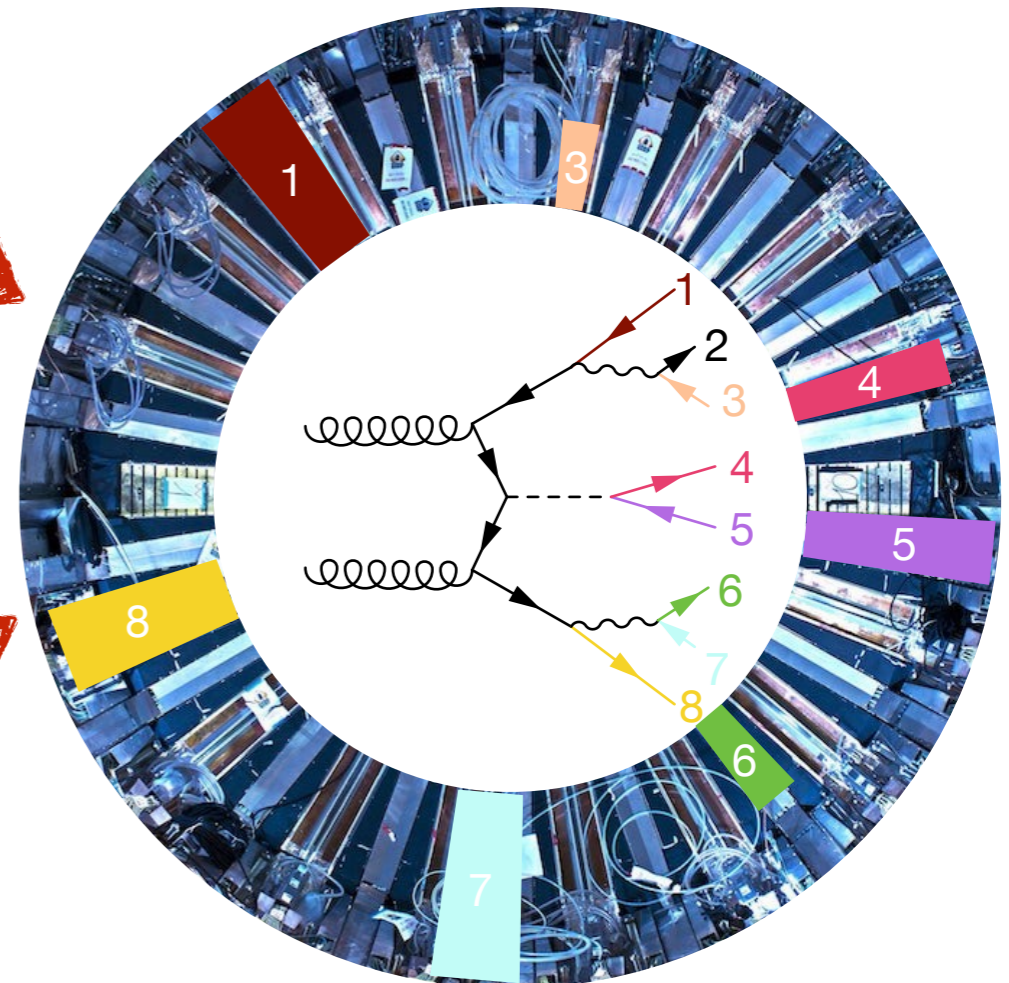




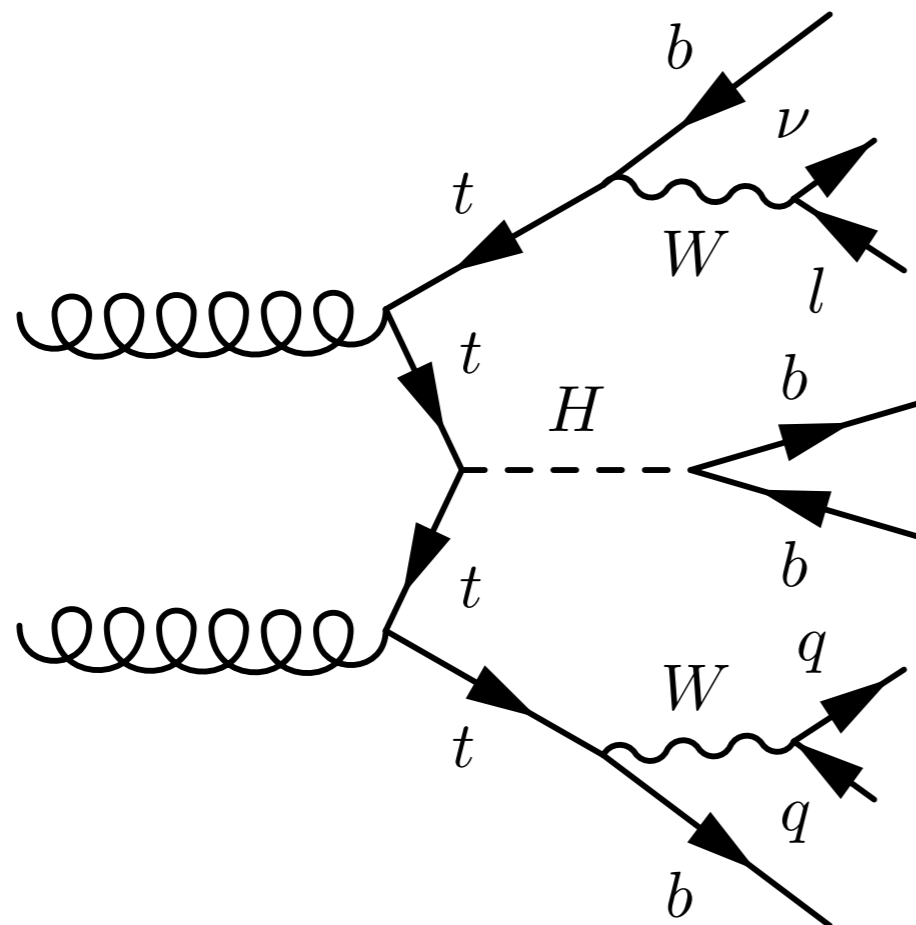
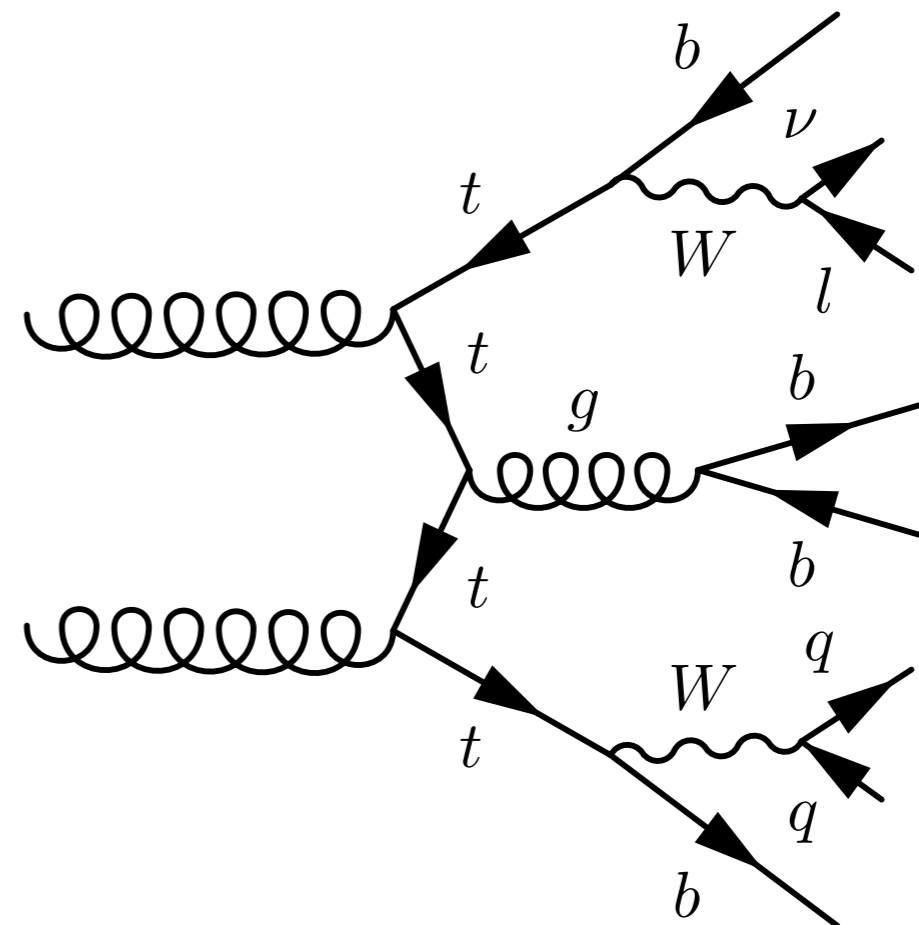
**Supervised**  
(Slides 5-7)



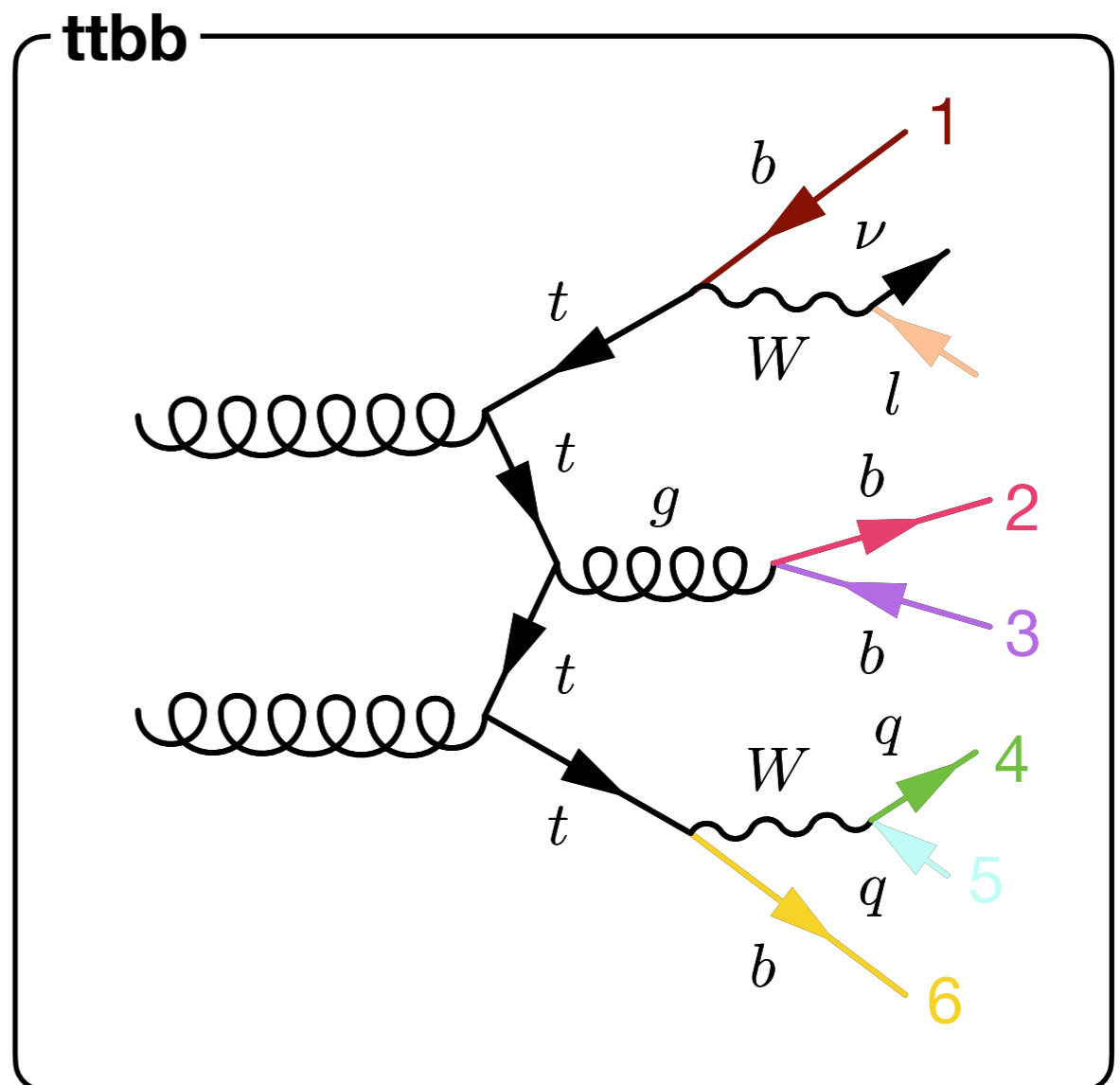
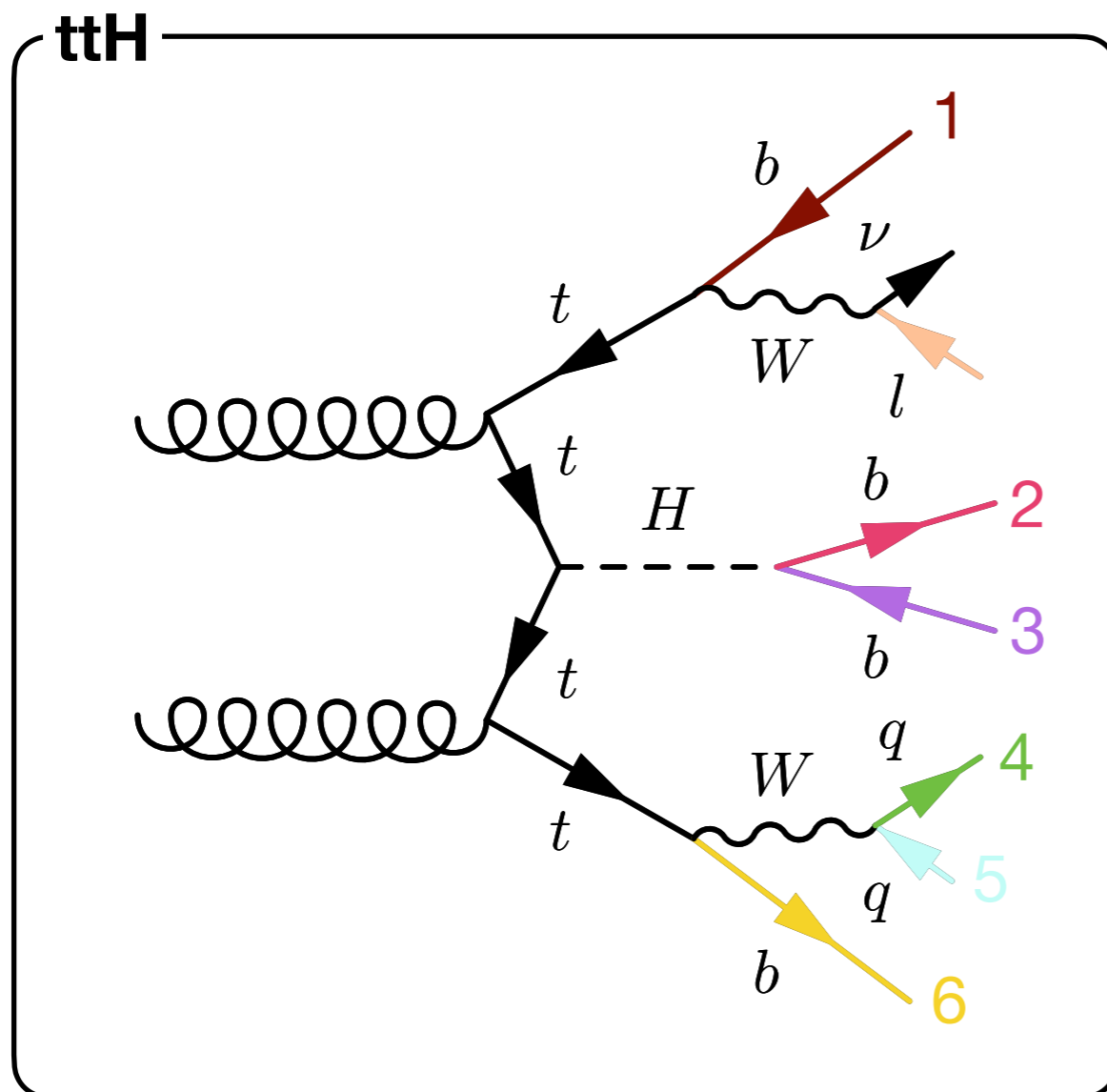
**Reinforced**  
(Slides 8-12)



- Classification of ttH vs ttbb ([1812.09722](#)):
  - Two processes with same final state
  - Jet Parton Assignment (JPA) crucial:
    - Without JPA: **Complex**
    - **With JPA: Easy** (e.g.  $m_{bb}$  from slot 2 and 3)

**ttH**

**ttbb**


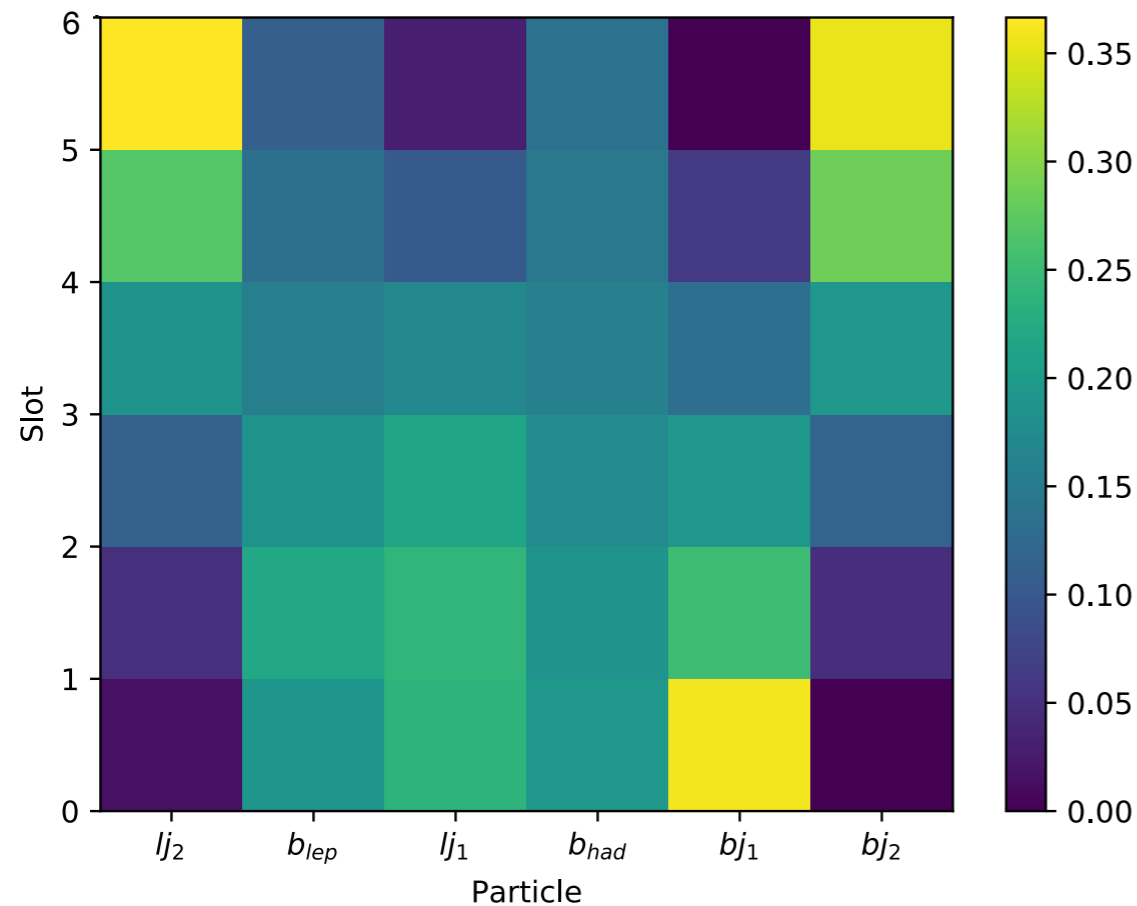
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## Particle Based

- Assign with one variable (pT)
- Pro: Fast & works with many part.
- Con: High ambiguity



## Permutation Methods

- Evaluate all different assignments
- Pro: Accurate
- Con: Scaling of permutations
  - ( $6! = 720$ ;  $10! > 3\text{Mio}$ )

Method	Probability of assigning all particles correctly
$\chi^2$	37 %
DNN	52 %

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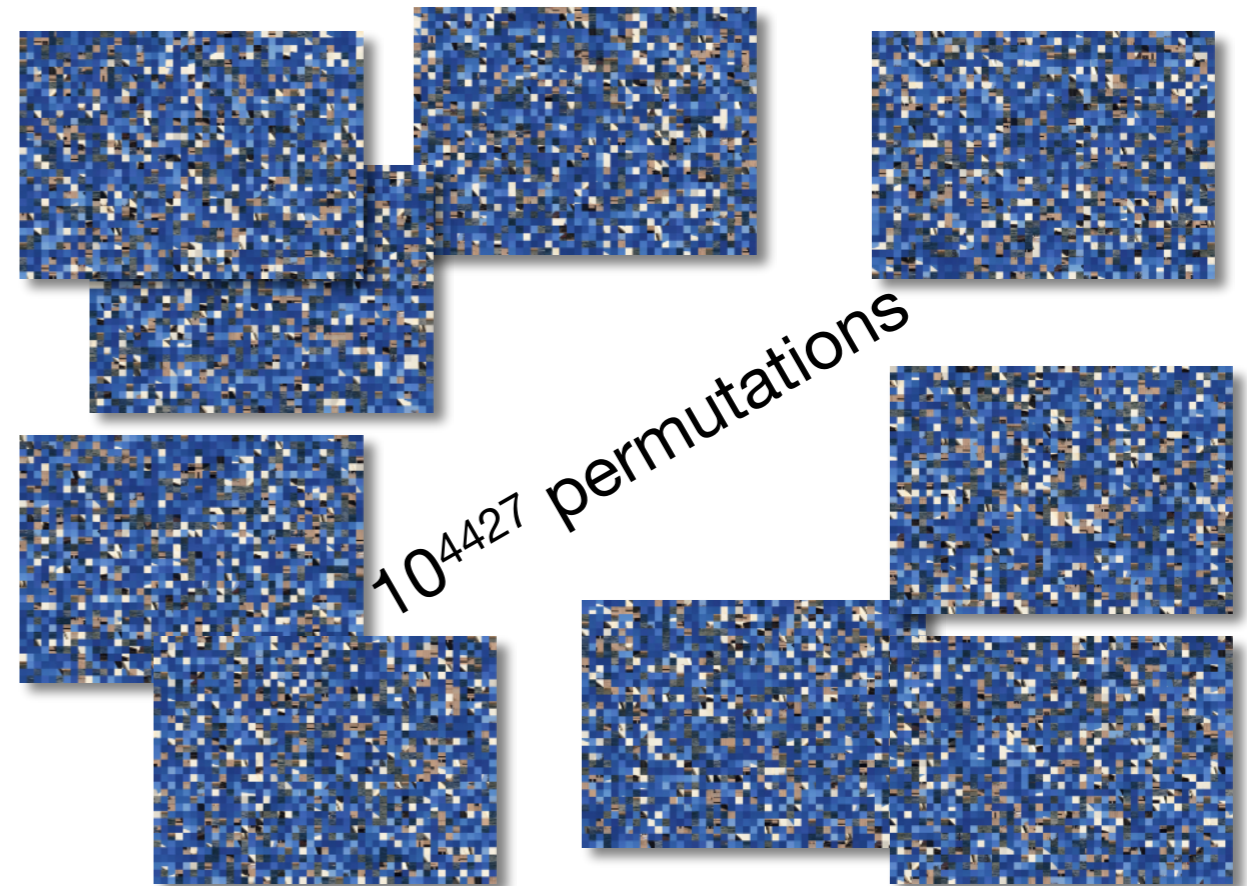
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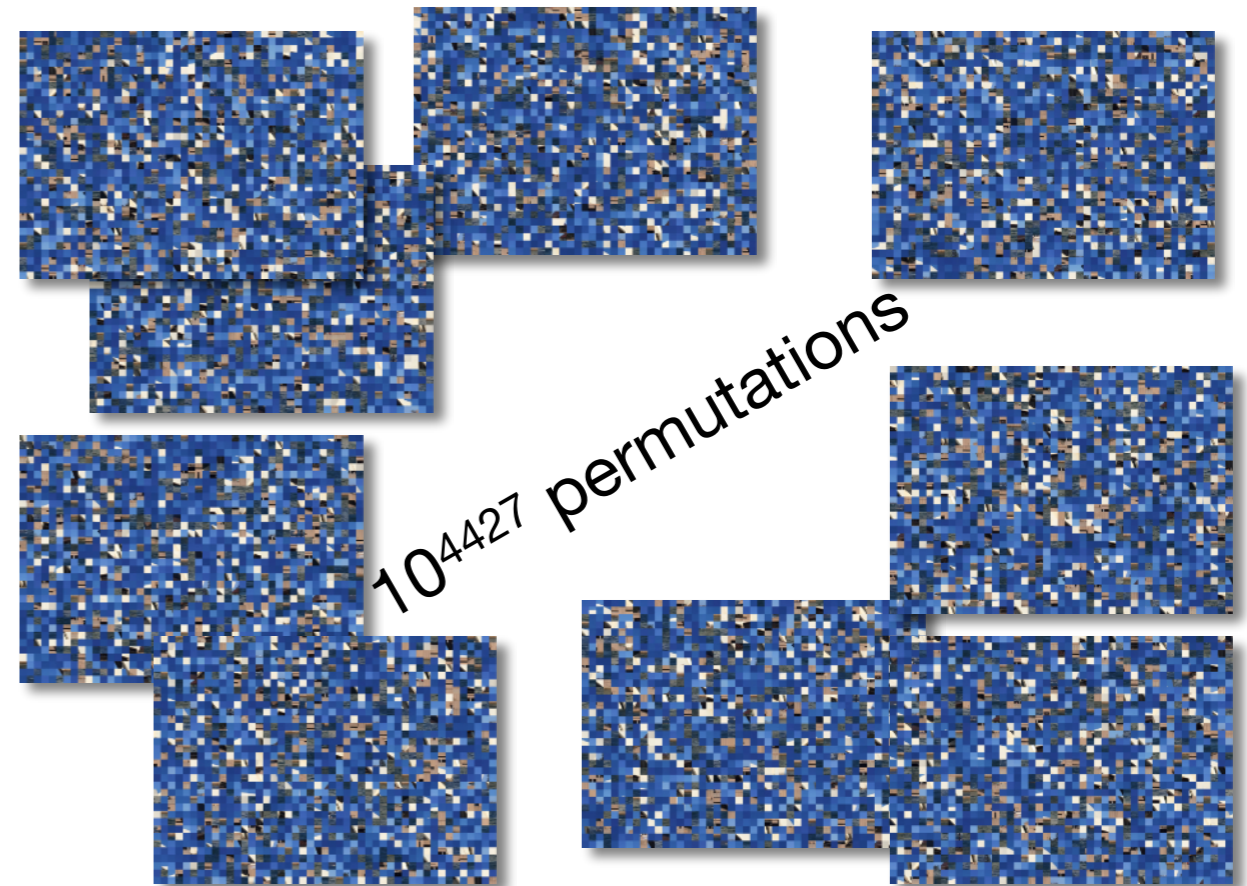
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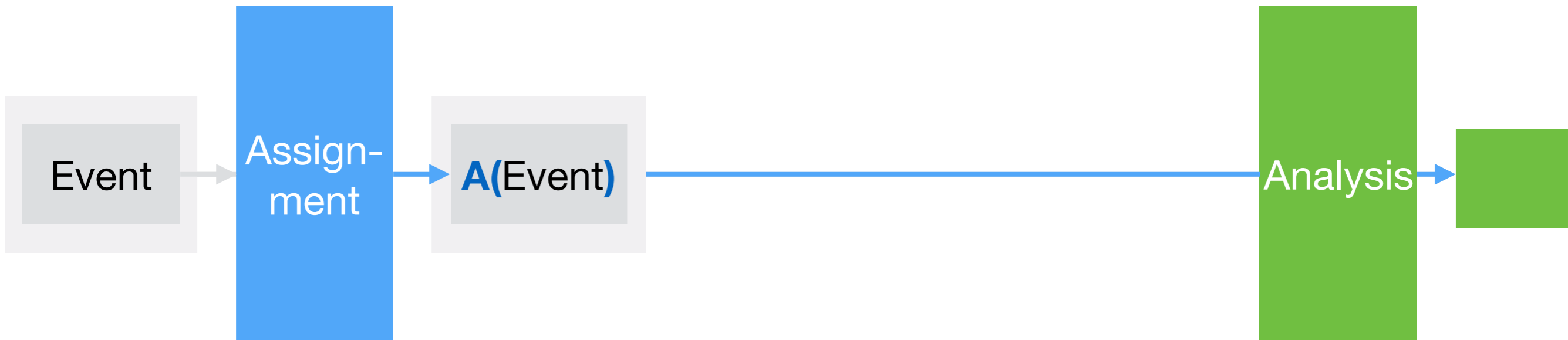


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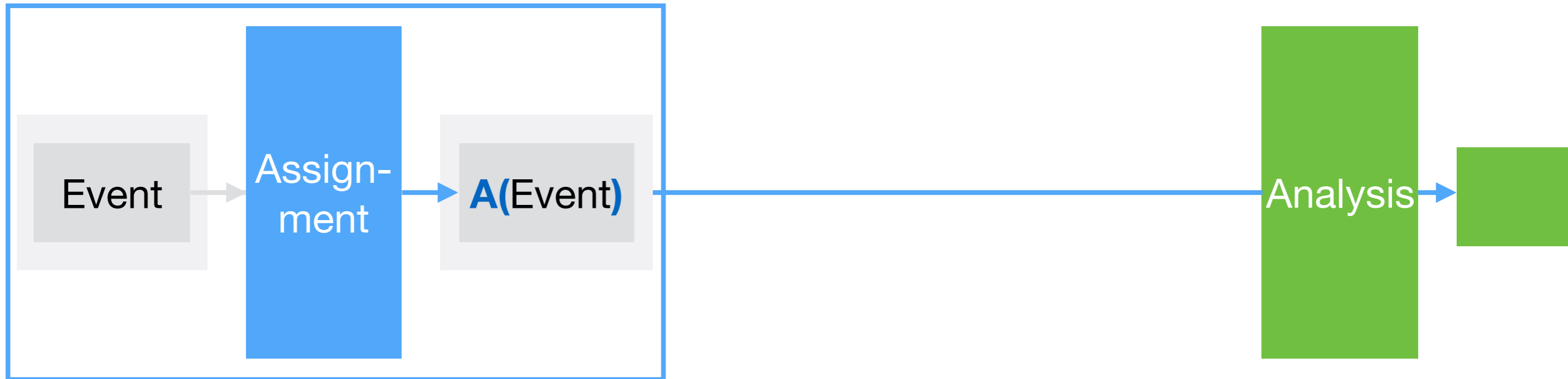
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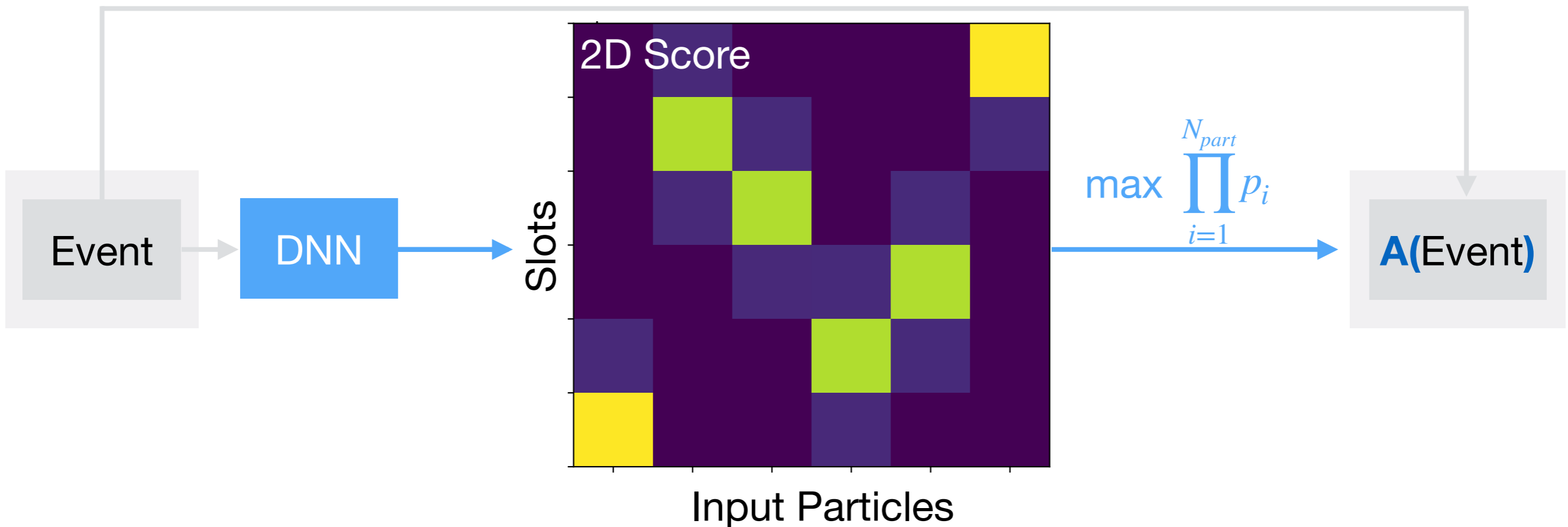
- Take the best out of the existing approaches:
  - Fast as particle based
  - Accurate as permutation method



- Evaluation:
  - Input  $p_T$  sorted Event
  - **Assignment** network assigns particles **A(Event)** (trainable)
  - **Analysis** evaluates assigned events **S(A(Event))** (trainable)

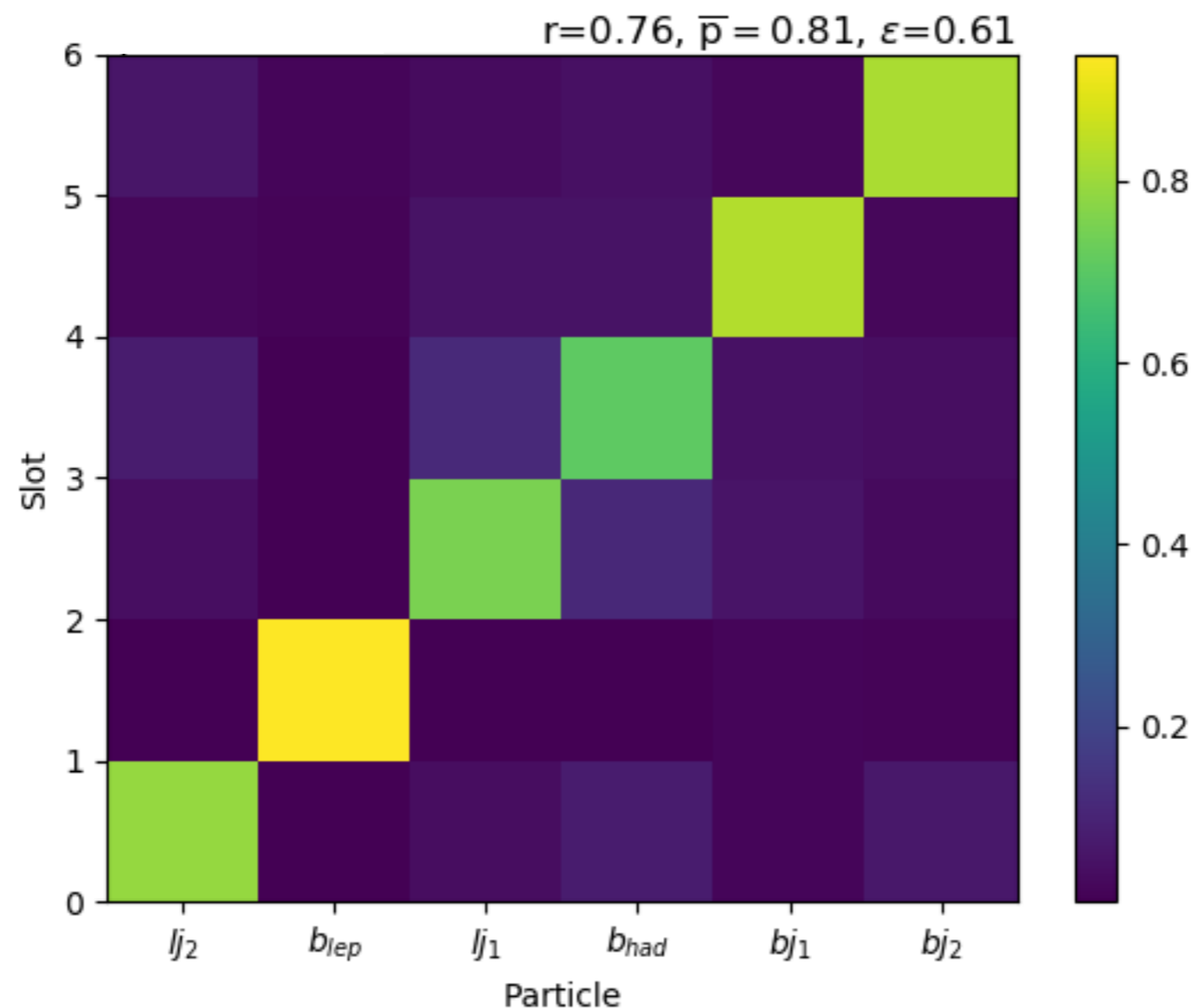


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- Multi-classification DNN:
  - Produces 2D Score
  - Bipartite graph:
    - Particle  $\leftrightarrow$  Slot
- Assignment:
  - Maximise joint score
  - Uses Munkres algorithm

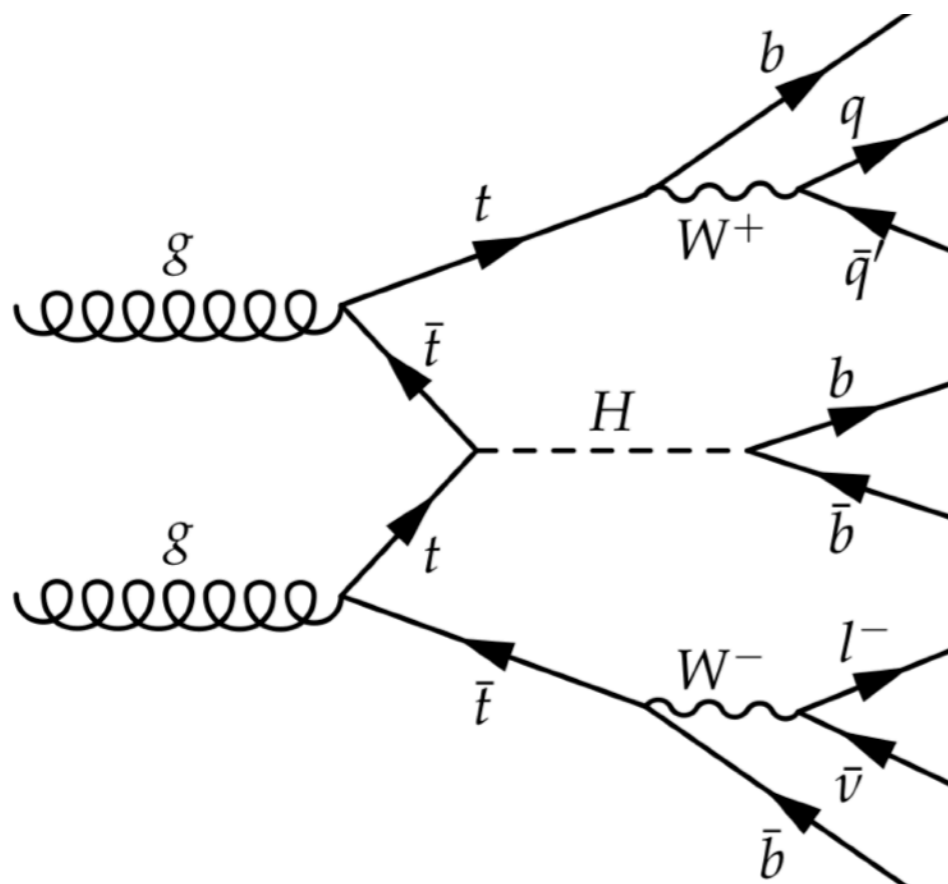
- Supervised training with fixed Particle  $\leftrightarrow$  Slot
- Correct assignment can be learned
- Probability to correctly identify complete ttH final state is  $\epsilon = 61\%$
- Better than state-of-the-art parton assignment methods ( $\epsilon = 52\%$ , 1706.01117)





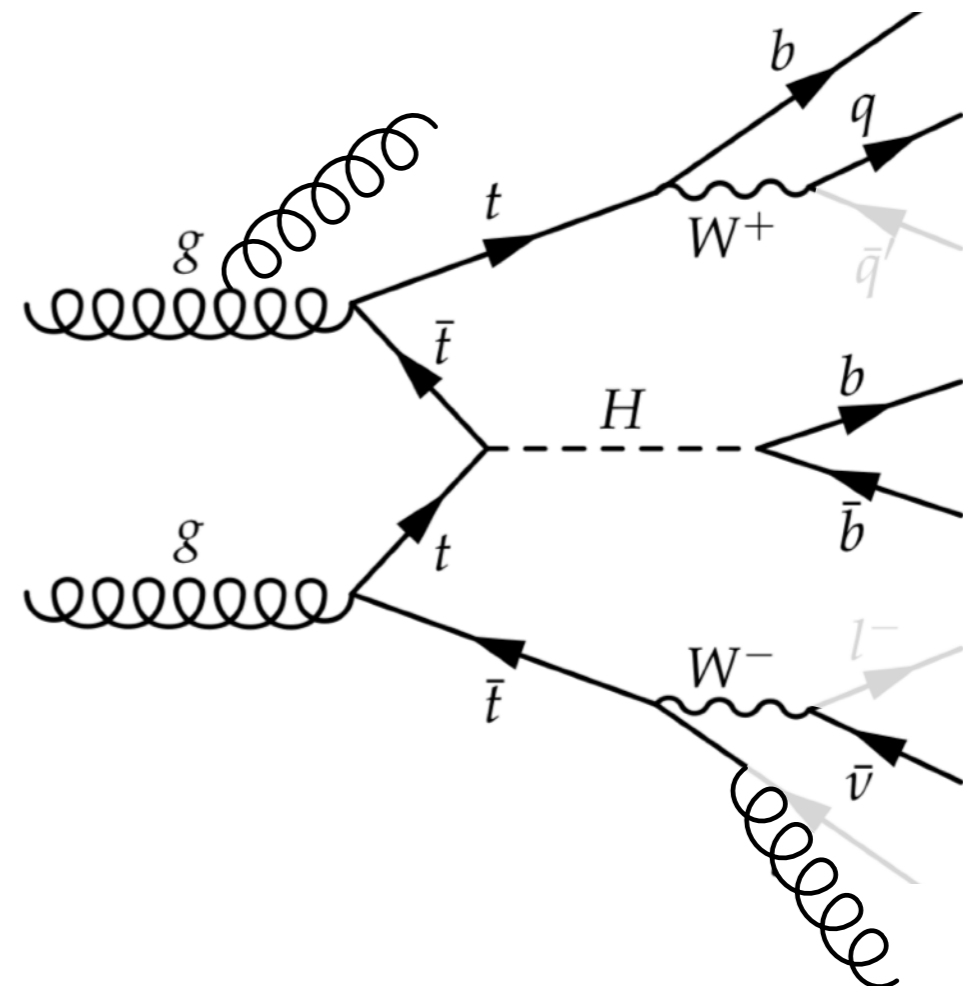
### Textbook example

- Particle nature fully known
- One slot for one particle
- Supervised training works

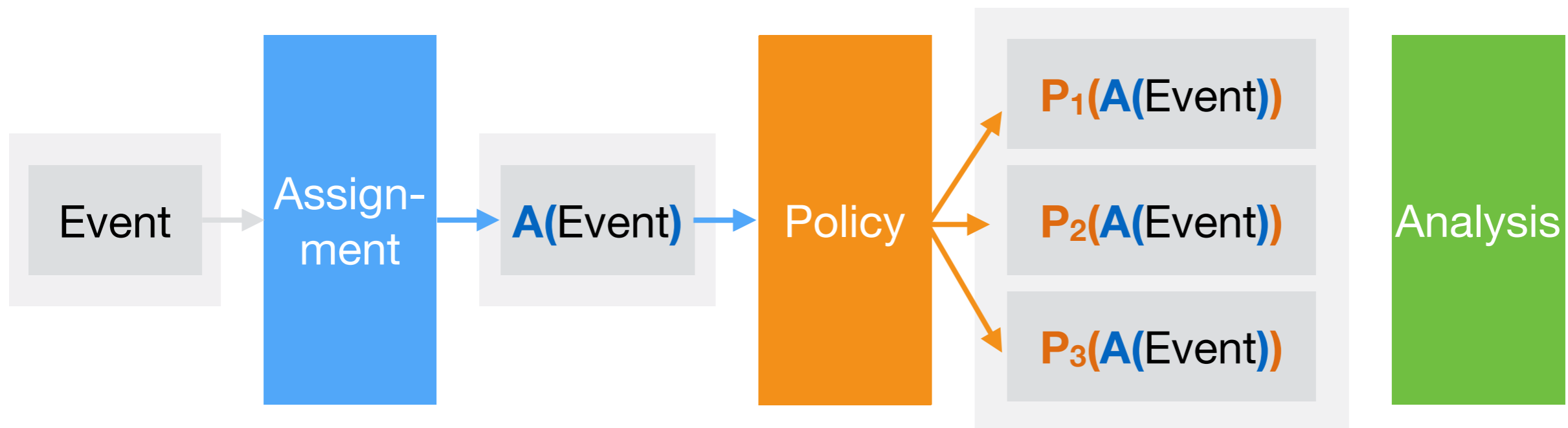


### Real World

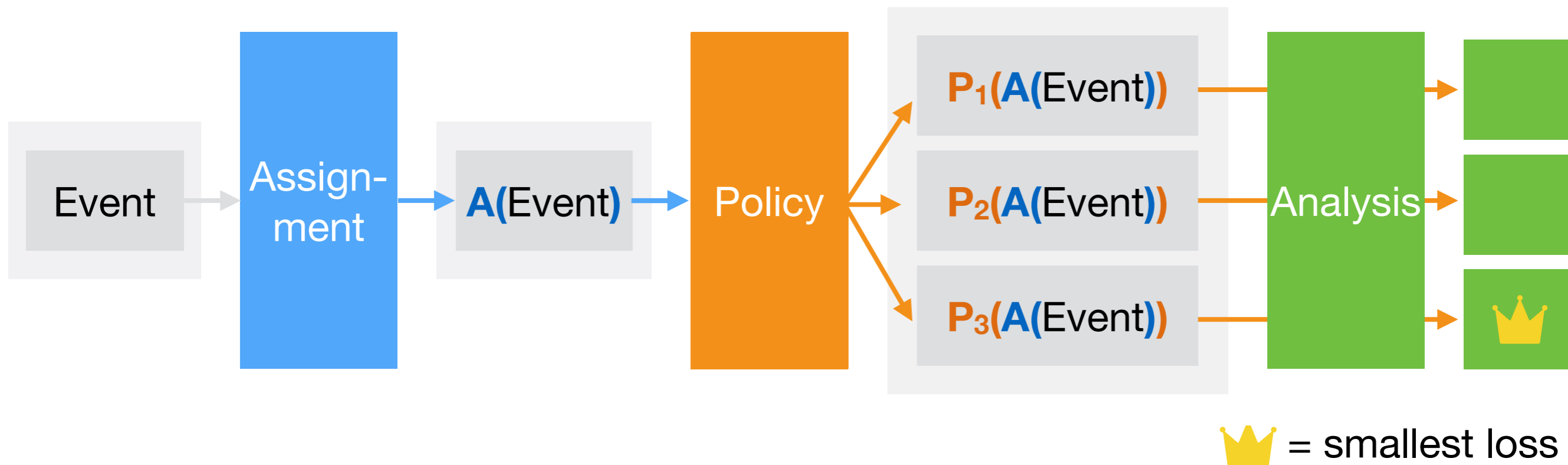
- Particle nature often not known
- Different particles in every event
- Need autonomy to adapt



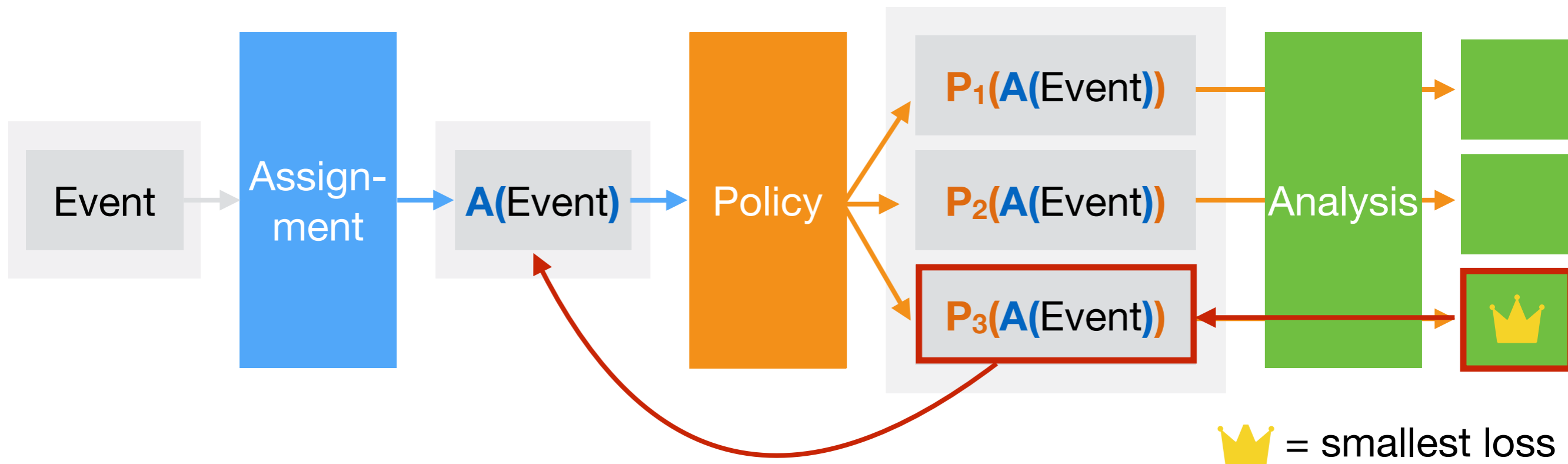
- Training objective: Find order of inputs, which is best suited for analysis
  - Assignment network assigns particles  $A(\text{Event})$
  - Policy suggests new orderings  $P_1(A(\text{Event}))$ ,  $P_2(A(\text{Event}))$ ,  $P_3(A(\text{Event}))$ , ...
  - Analysis evaluates assigned (and permuted) events



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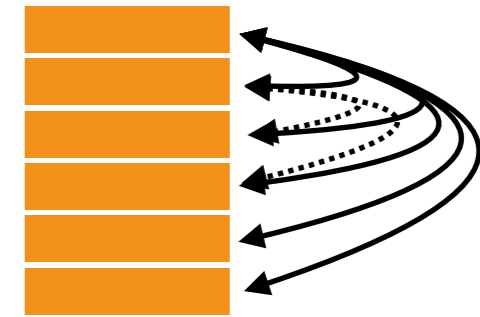
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- Step 1: Train assignment  $A_{\text{new}} \leftarrow P_3(A)$  (Policy Gradients)
- Step 2: Train analysis with  $A_{\text{new}}(\text{Event})$

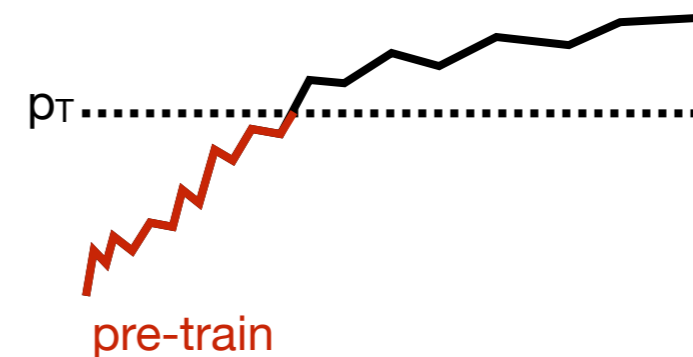
## Permutation Policy

- Ensures that all permutations can be probed along the training
- All pair-wise swaps [ $\mathcal{O}(n^2)$ ]:
  - $N_{pool}(6) = 15$



## Training

- Epoch wise Schedule:
  - 1 Epoch Assignment
  - 1 Epoch Analysis
- Pre-training ( $p_T$  as baseline):
  - Done for assignment and analysis
- Use three best permutations (weighted)



1

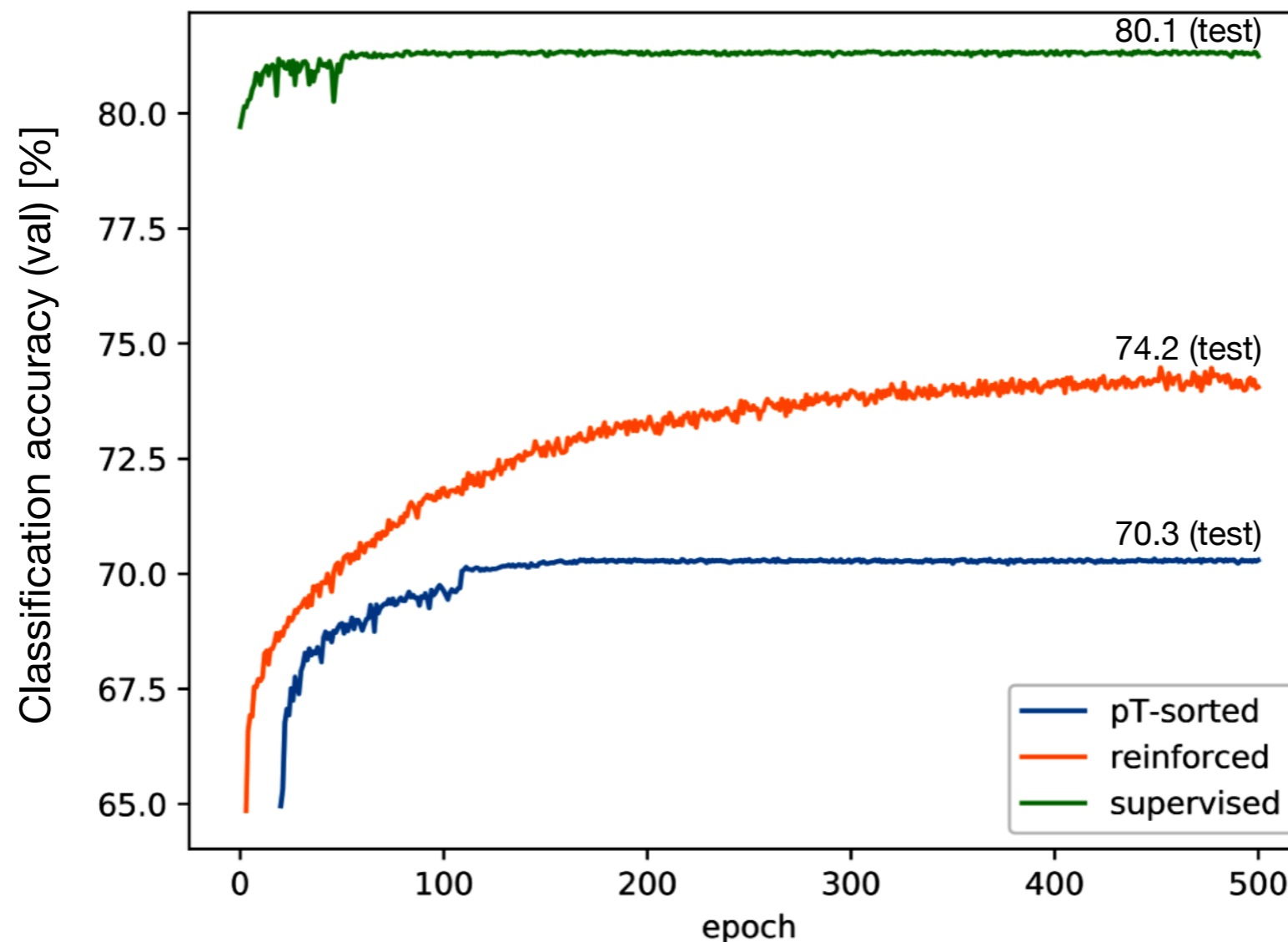


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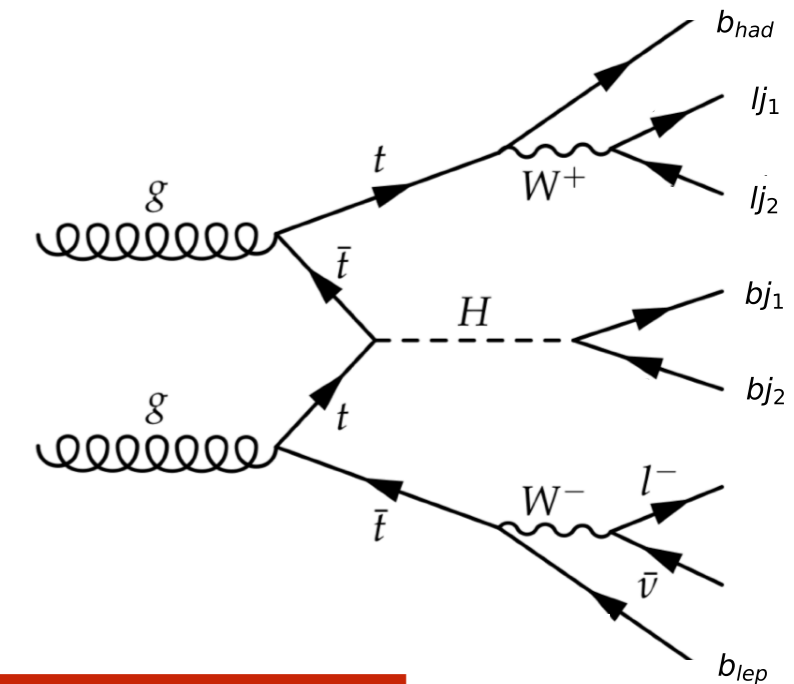


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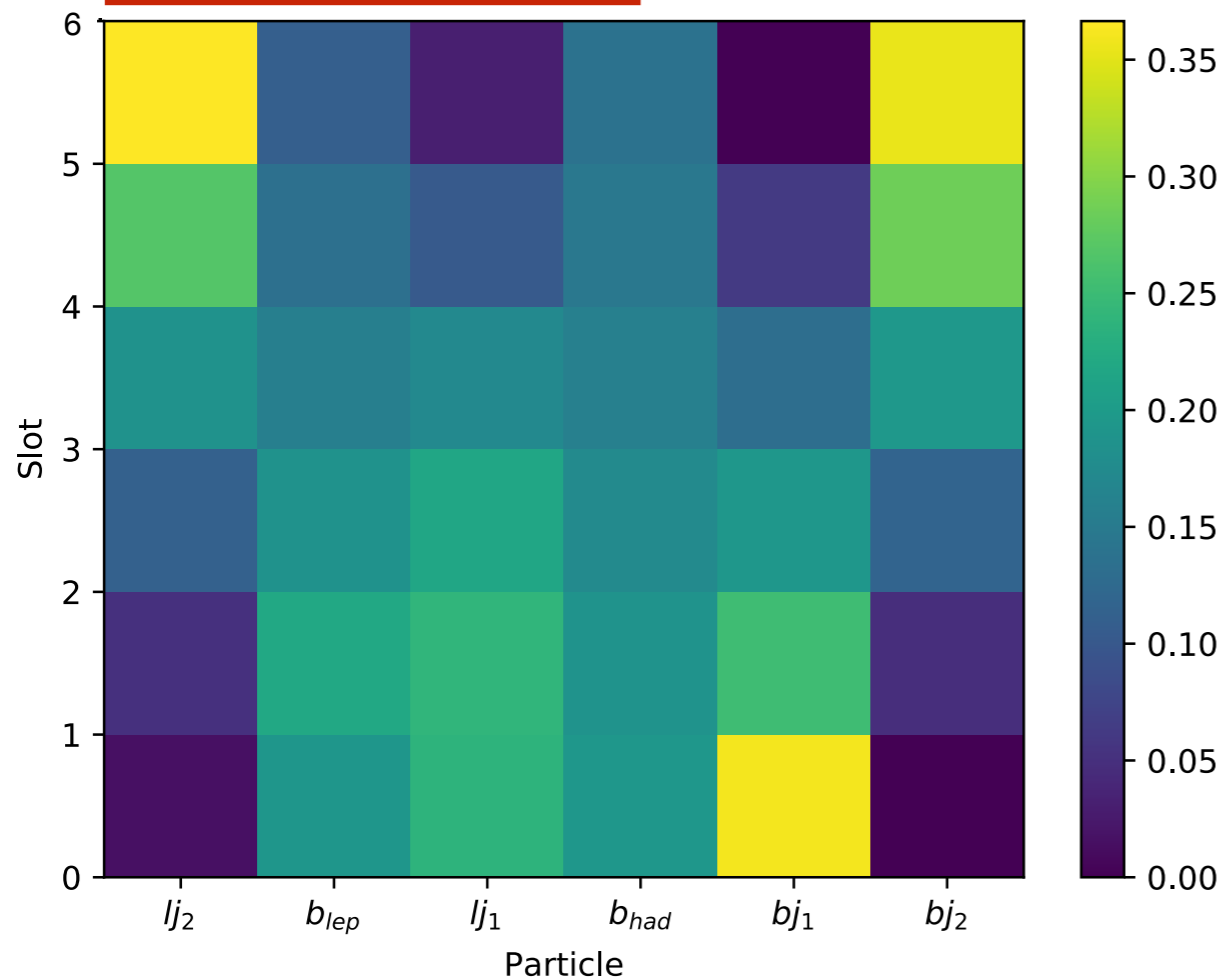
- Evaluate three methods for jet-parton assignment with same analysis network:
  - Standard:  $p_T$  - sorted
  - New (supervised): pre-trained **with** generator information
  - New (reinforced): autonomously trained **without** generator information



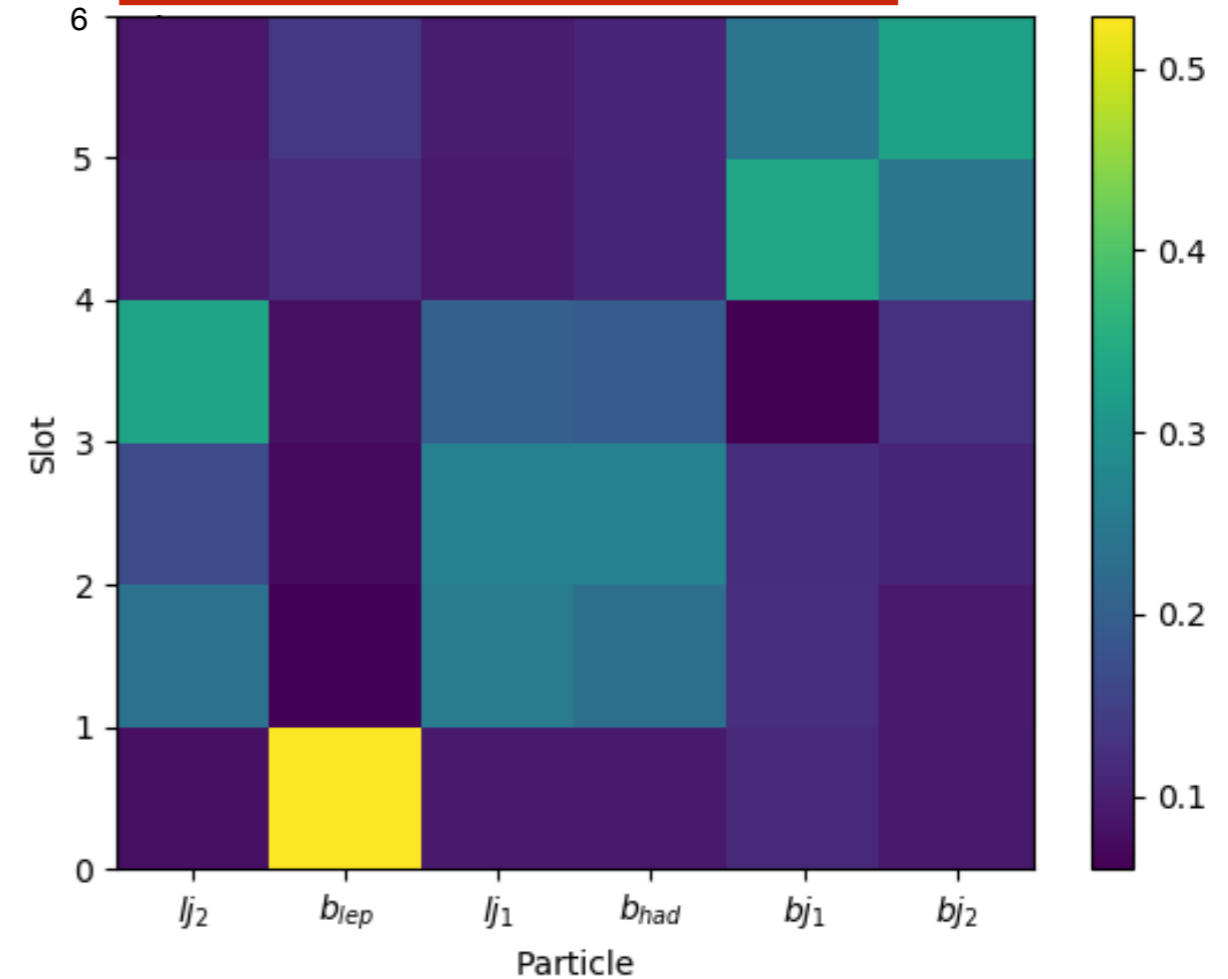
- Assignment network autonomously learns structure:
  - Direct neighbours grouped (e.g.  $b_{j1}$ ,  $b_{j2}$ )
  - Do not confuse distinguishable particles (e.g.  $l_{j2}$ ,  $b_{j2}$ )
  - Identifies branches of Feynman graph (e.g.  $b_{lep}$ )



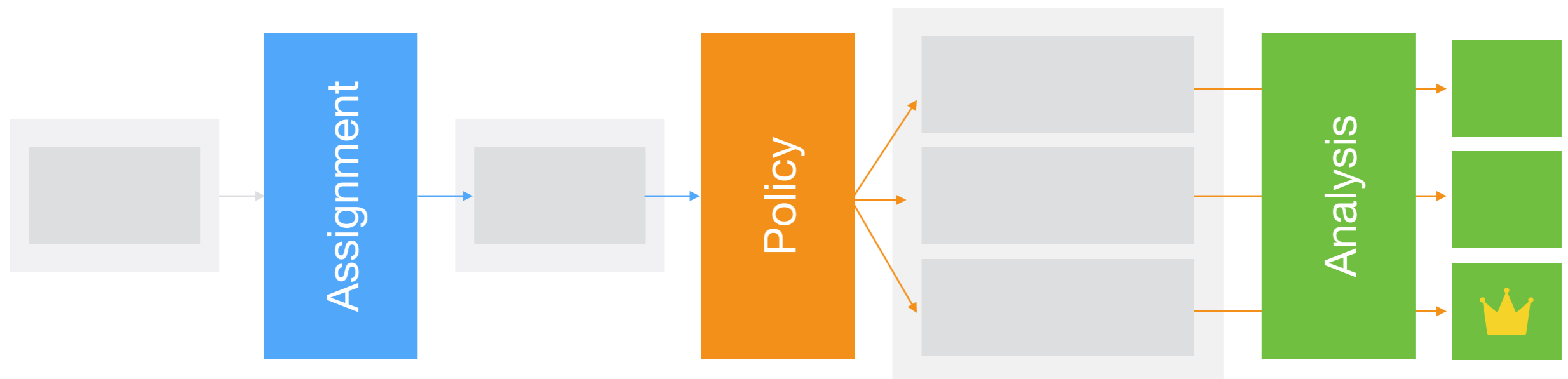
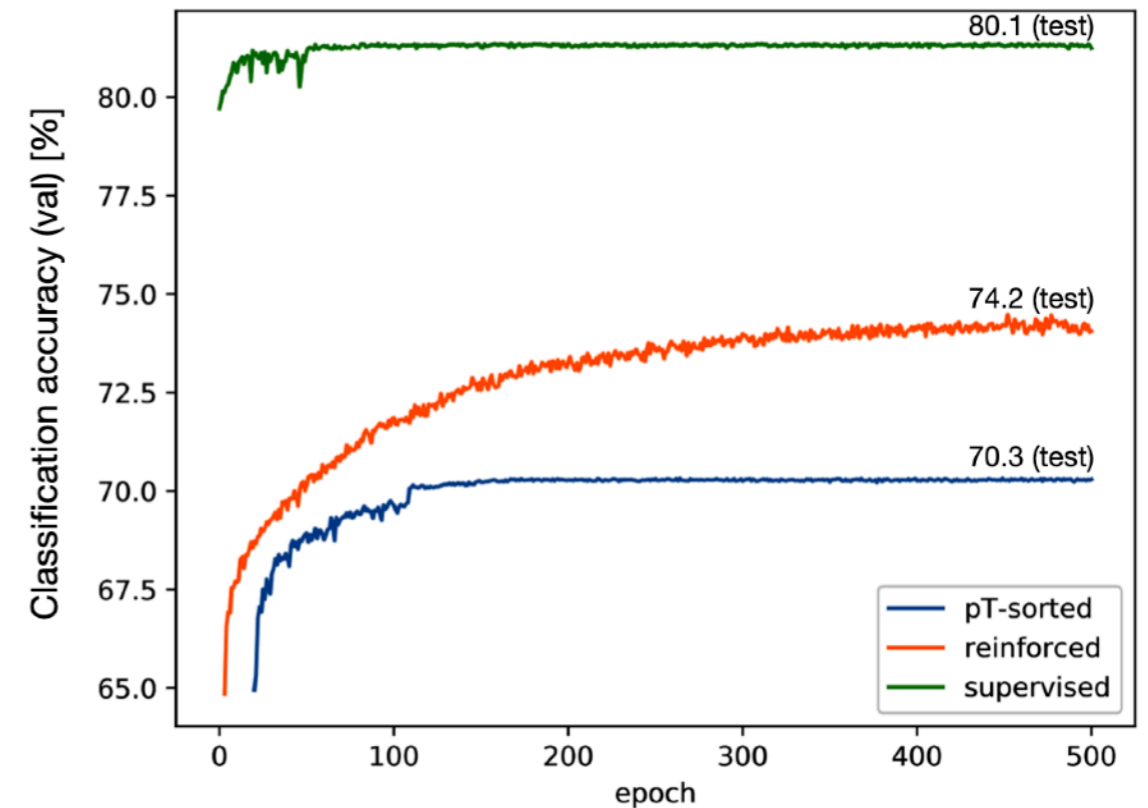
$p_T$  - assignment



reinforced - assignment



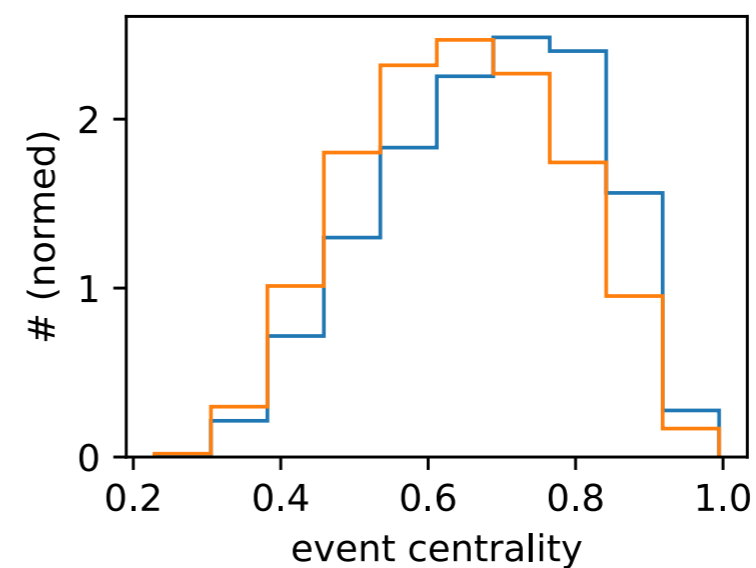
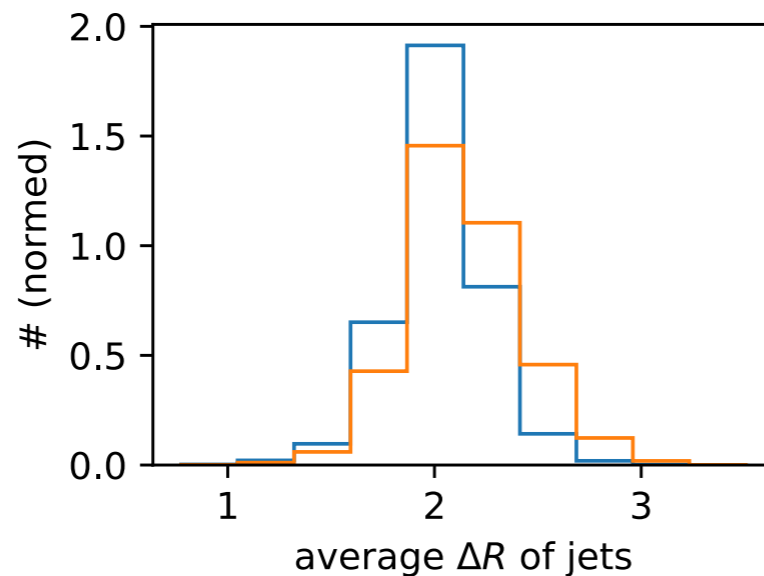
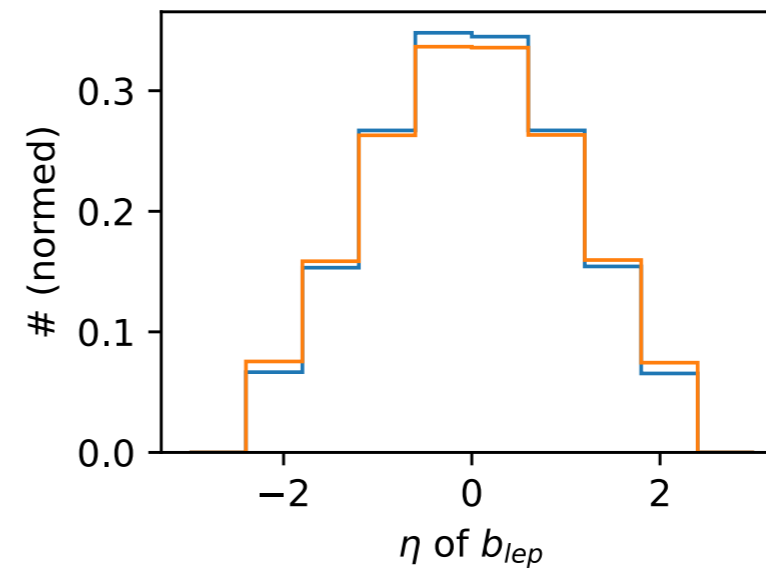
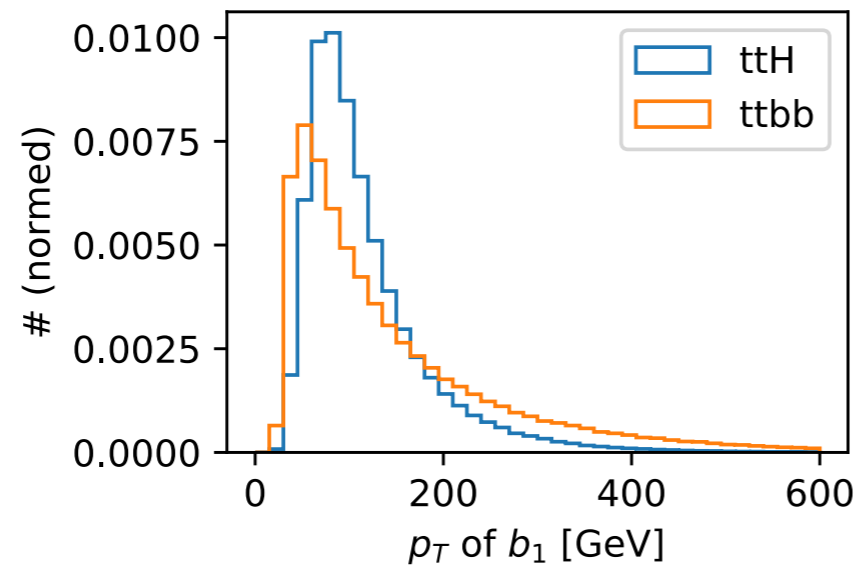
- A new method for jet-parton assignment
  - Supervised training if generator information is known
  - Reinforced training autonomously learns assignment based on the analysis



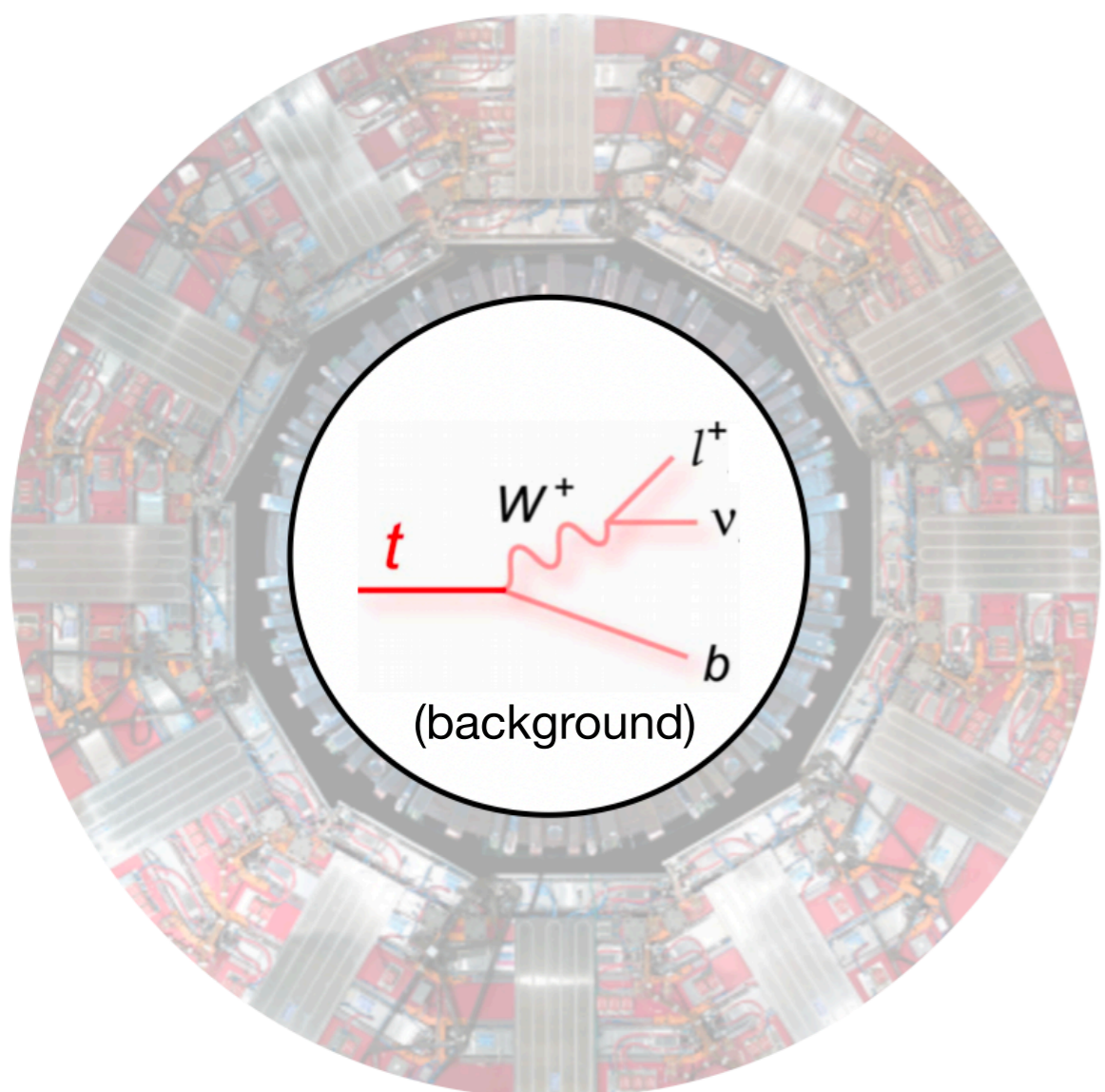


Backup

- Simulations Pythia + Delphes ( $10^6$  events - 50% ttH, 50% ttbb)
- Input variables:
  - Low-level: 4-vector of 8 particles
  - High-level: 26 variables (see backup)



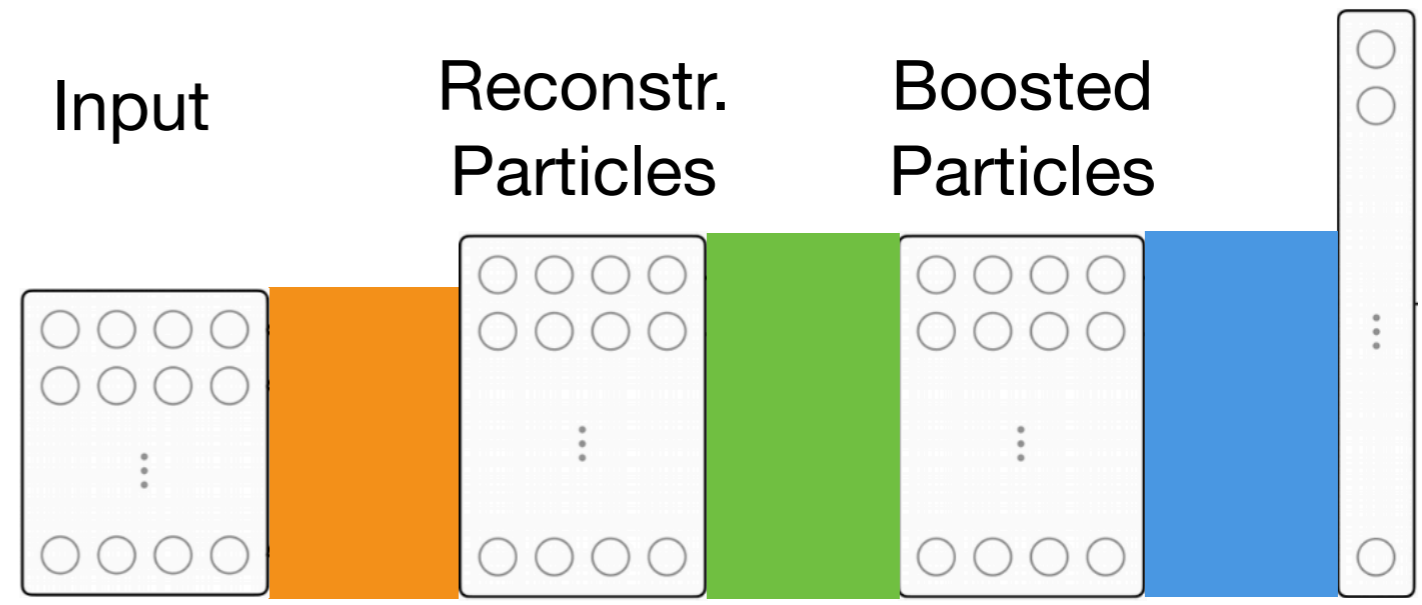
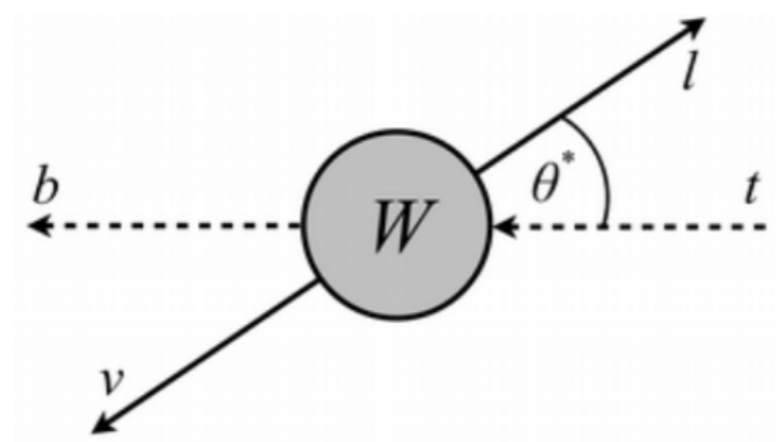
- Assignment Network:
  - Feed forward
    - 5 ELu Layers
      - 500 Nodes
    - Batch Normalization
- Analysis Network:
  - Lorentz-Boost Network (1812.09722)
  - Together with Feed forward:
    - 2 Elu Layers
      - 128 Nodes



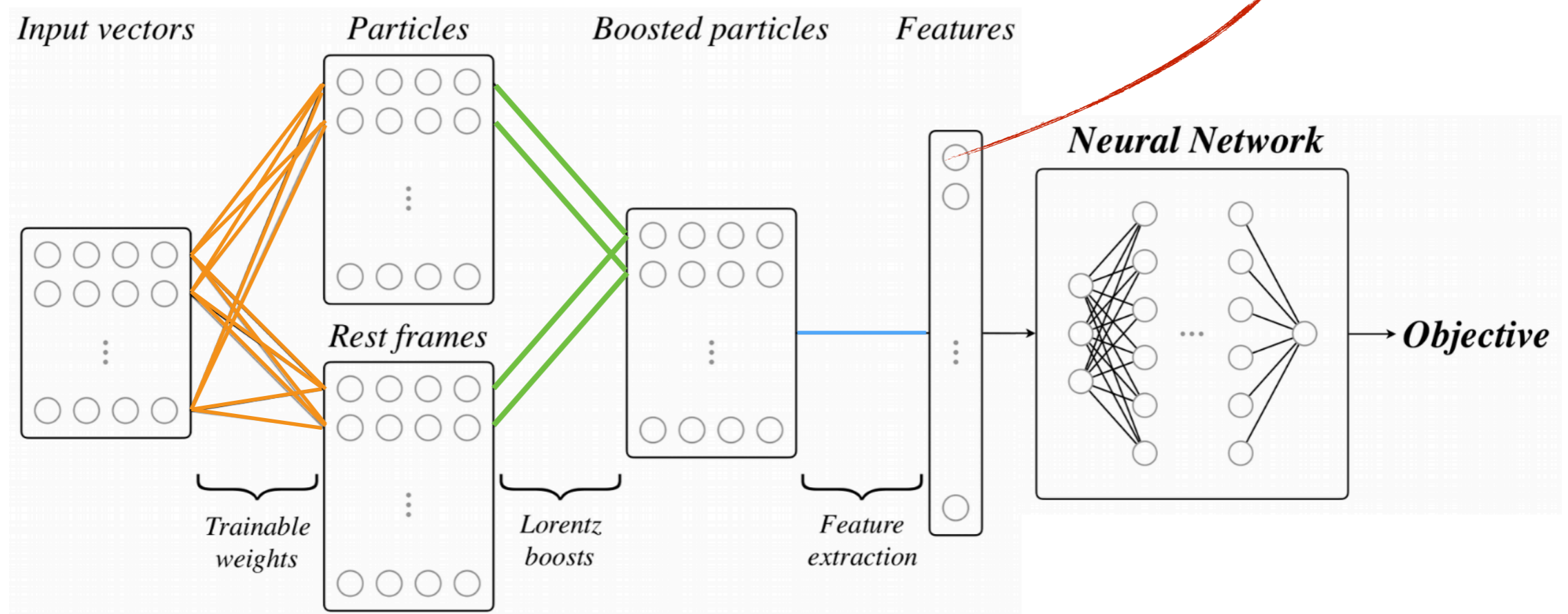
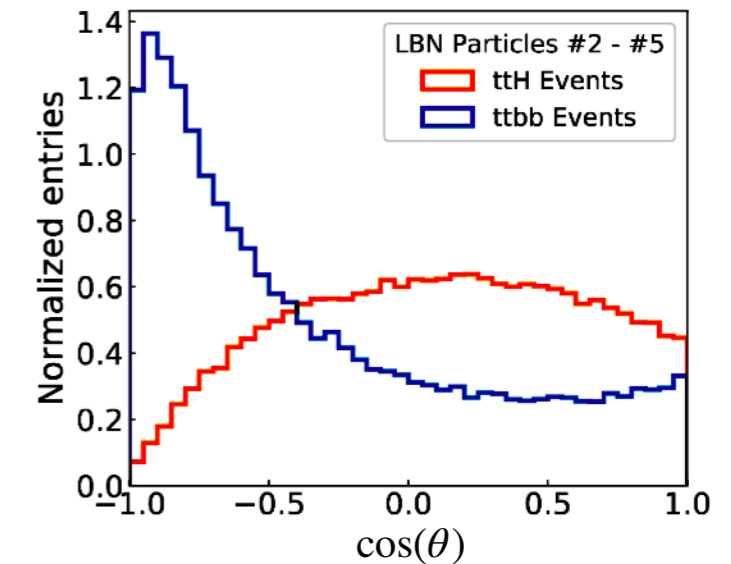
Calculate  $\theta^*$  :

- Reconstruct  $W$
- Reconstruct  $t$
- Boost lepton in  $W$  System =  $l_W$
- Boost  $W$  in  $t$  system =  $W_t$
- Calculate angle  $\angle(l_W, W_t)$

Features



- Autonomously build high level variables:
  - **Reconstruction**: learnable weights
  - **Boost**: Gamma Matrix
  - **Features**: Single particle + Pairwise
- Lorentz symmetry within neural network



- Optimally solving the assignment problem Particle  $\leftrightarrow$  Slot
- Example:

	40	60	15
Jobs (slots)	25	30	45
	55	30	25
	Workers (particle)		

Assignment cost

Optimal choice

- Achieves a complexity of  $O(n^3)$  compared to all different permutations  $O(n!)$
- Involves 5 steps - different complexity:
  1. Row reduction -  $O(n^2)$
  2. Column reduction -  $O(n^2)$
  3. Test for optimal assignment -  $O(n^3)$
  4. If needed: Shift zeros -  $O(n^3)$
  5. Making the final assignment -  $O(n)$

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**Algorithm 1** Reinforced Training

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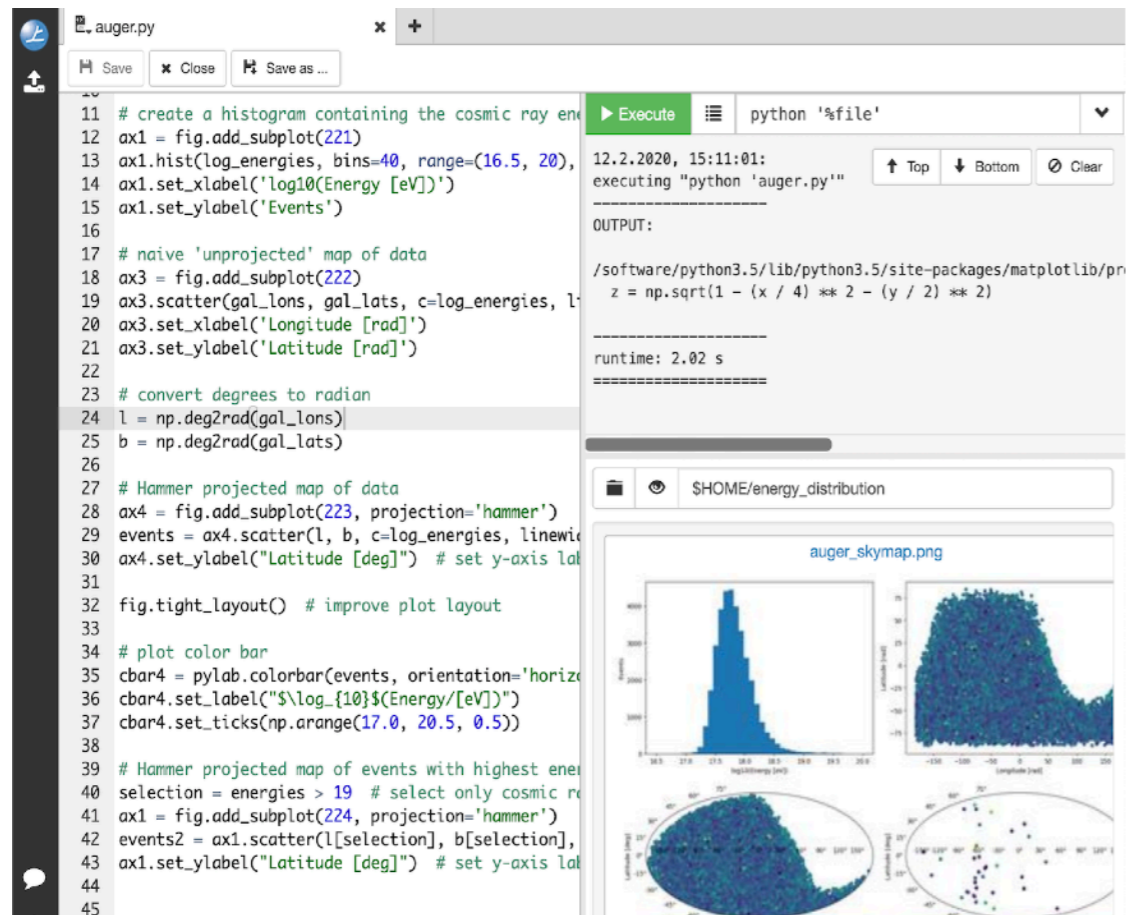
**Input:** Events ( $\mathbf{e}$ ), Permutations ( $\mathbb{P}$ ),  
Analysis ( $A_0$ ), Sorting model ( $S_0$ )

- 1: **for**  $i \leftarrow 0$  to epochs **do**
  - 2:      $\hat{P} \leftarrow \operatorname{argmax}_{P_n \in \mathbb{P}} A_i(P_n(S_i(\mathbf{e})))$
  - 3:      $T \leftarrow \hat{P}(S_i)$
  - 4:     train  $S_{i+1}$  to approximate  $T$
  - 5:     train  $A_{i+1}$  with  $S_{i+1}(\mathbf{e})$
-

# VISPA

## Software

- Full development environment (editor, file browser, ...)
- Runs in your web browser



## Hardware

- 200 CPU Cores
- 30 GPU Cards (300 TFlops)
- (ITC RWTH: 1500 TFlops)



- Accessible via <https://vispa.physik.rwth-aachen.de/>



- Event shape variables: sphericity, transverse sphericity, aplanarity, centrality
- First five Fox-Wolfram moments
- Cosine of spatial angular difference  $\theta^*$  between the charged lepton in the W boson restframe and the W boson direction when boosted into the rest frame of its corresponding top quark. In the hadronic branch, the down-type quark is used owing to its increased spin analyzing power
- minimum, maximum and average of  $\Delta R$  of jet pairs
- minimum, maximum and average  $|\Delta\eta|$  of jet pairs.
- minimum and maximum of the distance in  $\Delta R$  of jet-lepton pairs
- minimum, maximum and average  $|\Delta\eta|$  of jet-lepton pairs
- sum of the transverse momenta of all jets
- transverse momentum and the mass of the jet pair with the smallest  $\Delta R$
- transverse momentum and the mass of the jet pair whose combined mass is closest to the Higgs boson mass  $m_H=125\text{GeV}$