

# Heavy Higgs Searches in the MSSM with *CP* Violation

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Invisibles18 Workshop



# How does $CP$ Violation affect the MSSM Higgs Sector?

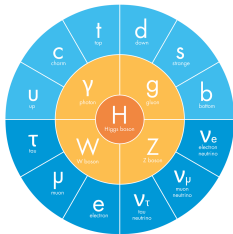
- 1 Introduction and Motivation
- 2 MSSM Higgs sector with  $CP$
- 3  $CP$  phase effects on Higgs production
- 4 Interference effects in MSSM Higgs searches
- 5 Summary

# Introduction and Motivation

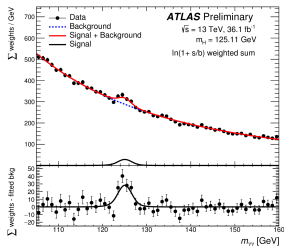
# Minimal Supersymmetric Standard Model

## Standard Model (SM)

FERMIONS (matter) | BOSONS (force carriers)  
● Quarks ● Leptons ● Gauge bosons ● Higgs boson



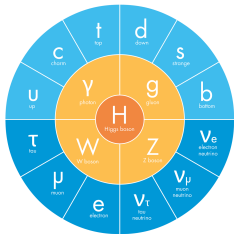
## A 125 GeV Higgs boson



# Minimal Supersymmetric Standard Model

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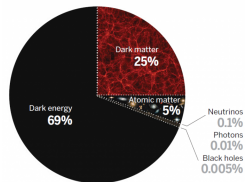
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## Baryon Asymmetry

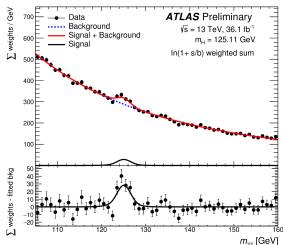
- ▶  $N_{\text{Matter}} > N_{\text{Antimatter}}$
- ▶  $\mathcal{CP}$  needed to generate asymmetry
- ▶ Insufficient  $\mathcal{CP}$  in the SM to explain observed asymmetry

## Dark Matter (DM)

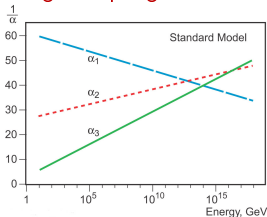


No DM candidate in the SM

## A 125 GeV Higgs boson



## Gauge coupling unification



## Hierarchy Problem



$$\Delta M_{H^0}^2 \propto \Lambda_{\text{NP}}^2$$

# Minimal Supersymmetric Standard Model

## Minimal Supersymmetric SM

- ▶  $Q|\text{Fermion}\rangle = |\text{Boson}\rangle$   
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- ▶ Particle content = SM particles + *superpartners*

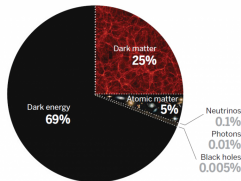
A 125 GeV Higgs boson

- ▶ MSSM predicts 3 neutral Higgs bosons
- ▶ Observed 125 GeV Higgs-state could belong to the MSSM

## Baryon Asymmetry

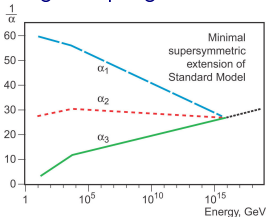
- ▶  $N_{\text{Matter}} > N_{\text{Antimatter}}$
- ▶  $CP$  needed to generate asymmetry
- ▶ Complex parameters in the MSSM provide additional  $CP$

## Dark Matter (DM)



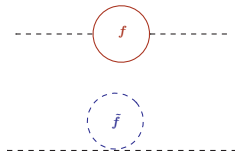
Lightest SUSY particle a DM candidate

## Gauge coupling unification



## Hierarchy Problem

[E. Fuchs, Disputation '15]



$$\Delta M_{H^0}^2 \propto \ln \left( \frac{m_{\tilde{f}}^2}{m_f^2} \right)$$

## Two-pronged approach for new physics at the LHC

Direct discovery  
↔ Multiplicity

Indirect discovery  
↔ Precision

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### Theoretical predictions

- ▶ Needed to interpret discovery from production ( $\sigma$ ) and decay (BR) of a particle
- ▶ Needed to extract information on possible new physics indirectly from data

### What this means for the MSSM Higgs sector

- ▶ Need precise knowledge of  $\sigma$  and BR for additional Higgs states
- ▶ Precise prediction + measurement of 125 GeV Higgs properties (couplings, production rates,  $p_T$  spectrum..) can characterize underlying dynamics of particles and quantify potential deviations from the SM predictions



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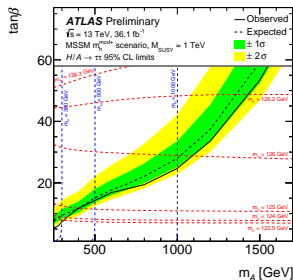
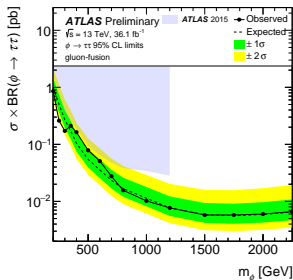
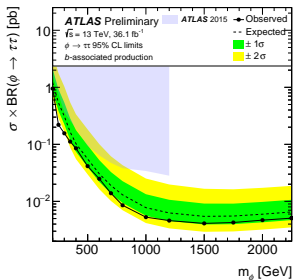
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## Interpretation of searches for additional scalars $\phi \in \{h, H, A\}$

- ▶ Standard Narrow Width Approximation (NWA):  $\sigma_{\text{prod}} \times \text{BR}$
- ▶ Production  $\{gg \rightarrow \phi, b\bar{b} \rightarrow \phi\} \times$  Decay  $\{\phi \rightarrow \tau^+ \tau^-, \mu^+ \mu^-, b\bar{b}\}$



[ATLAS-CO NF-2017-050, CMS-PAS-HIG-16-006]

Limitation: Neglects interference, especially important with **CP violation**

## Motivations

- ▶ BSM sources of  $CP$  needed to explain baryon asymmetry of the universe
- ▶ A  $CP$ -violating Higgs sector gives rise to richer phenomenology
- ▶ **No scenario with  $CP$  in the Higgs sector considered so far in the context of the LHC-HXSWG**

## What we need

- ▶ State of the art predictions of neutral Higgs masses, mixing,  $\sigma$  and BR taking into account  $CP$
- ▶ Framework for studying  $CP$  interference effects between neutral Higgs bosons
- ▶ Implementation into tools

## Goal

Re-interpretation of experimental limits on heavy Higgs boson searches in light of  $CP$

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# Higgs Sector of the MSSM with $CP$

## Two Higgs doublets

$$\mathcal{H}_1 = \begin{pmatrix} v_1 + \frac{1}{\sqrt{2}}(\phi_1^0 + i\chi_1^0) \\ \phi_1^- \end{pmatrix}, \quad \mathcal{H}_2 = e^{i\xi} \begin{pmatrix} \phi_2^+ \\ v_2 + \frac{1}{\sqrt{2}}(\phi_2^0 + i\chi_2^0) \end{pmatrix}$$

Electroweak Symmetry Breaking  $\rightarrow$  5 physical states

$\mathcal{CP}$ -even  $h, H$ ,  $\mathcal{CP}$ -odd  $A$ , Charged  $H^\pm$

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## Higgs Potential

$$V_H = (|\mu|^2 + m_{\mathcal{H}_1}^2)\mathcal{H}_1^\dagger\mathcal{H}_1 + (|\mu|^2 + m_{\mathcal{H}_2}^2)\mathcal{H}_2^\dagger\mathcal{H}_2 \\ + \frac{g_1^2 + g_2^2}{8}(\mathcal{H}_1^\dagger\mathcal{H}_1 - \mathcal{H}_2^\dagger\mathcal{H}_2)^2 - |m_{12}^2|e^{i\zeta}(\mathcal{H}_1\mathcal{H}_2 + h.c.)$$

- ▶  $\mathcal{CP}$ -violating ( $\mathcal{CP}$ ) phase  $\xi$  vanishes at  $V_H^{\min}$ ,  $\zeta$  rotated away

MSSM Higgs sector is  $\mathcal{CP}$ -conserving at lowest order

## 105 new MSSM parameters + 19 from the SM

- ▶ Result from our ignorance of a SUSY-breaking mechanism
- ▶ Appear as masses, mixing angles and  $\mathcal{CP}$ -violating phases
- ▶ Minimal flavour violation  $\Rightarrow$  41 independent parameters

## 12 $\mathcal{CP}$ phases in the MSSM

- ▶ Trilinear couplings  $A_f \rightarrow A_f = |A_f|e^{i\phi_{A_f}}$
- ▶ Higgsino mass parameter  $\mu \rightarrow \mu = |\mu|e^{i\phi_\mu}$
- ▶ Gaugino mass parameters  $\{M_1, M_3\} \rightarrow M_i = |M_i|e^{i\phi_{M_i}}$

## Experimental constraints from EDMs

- ▶ Electron, muon and neutron EDMs most restrictive for  $\mathcal{CP}$  phases

[Barger, Falk, Han, Jiang, Li, Plehn '01], [Ellis, Lee, Pilaftsis '09], [Li, Profumo, Ramsey-Musolf '10], [Arbey, Ellis, Godbole, Mahmoudi '14], [King, Mühlleitner, Nevezorov, Walz '15]



- ▶  $\mathcal{CP}$  in Higgs sector induced via loop corrections



- ▶ Dominant phases in the Higgs sector:  $\phi_{A_{t,b}}, \phi_{M_3}, \phi_\mu$
- ▶ Complex parameters induce  $\mathcal{CP}$   $3 \times 3$  mixing beyond tree level

Tree-level mass eigenstates  $\{h, H, A\}$  mix into loop-corrected mass eigenstates  $\{h_1, h_2, h_3\}$  with  $M_{h_1} \leq M_{h_2} \leq M_{h_3}$

- ▶ Input parameters:  $t_\beta = \frac{v_2}{v_1}$  &  $M_{H^\pm}$

## How do we characterize mixing of external Higgs bosons?

- ▶ Admixed  $h_a, a \in \{1, 2, 3\}$  need correct on-shell properties: mixing matrix  $\hat{\mathbf{Z}}_{aj}$

[Chankowski, Pokorski, Rosiek '93], [Frank, Hahn, Heinemeyer, Hollik, Rzehak, Weiglein, Williams '07, '11]...

- ▶  $\hat{\mathbf{Z}}$  matrix elements  $\hat{\mathbf{Z}}_{aj} = \sqrt{\hat{\mathbf{Z}}_a} \hat{\mathbf{Z}}_{aj} \quad ; j \in \{h, H, A\}$

external wave function  
normalisation factor

on-shell  
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- Amplitude for external Higgs  $h_a$  in terms of  $\hat{Z}$  factors:

$$\mathcal{A}_{h_a} \left( \begin{array}{c} h_a \\ p^2 = M_a^2 \end{array} \right) = \sqrt{\hat{Z}_a} \left( \mathcal{A}_h \left( \begin{array}{c} h \\ \hat{Z}_{ah} \end{array} \right) \begin{array}{c} h_a \\ p^2 = M_a^2 \end{array} + \mathcal{A}_H \left( \begin{array}{c} H \\ \hat{Z}_{aH} \end{array} \right) \begin{array}{c} h_a \\ p^2 = M_a^2 \end{array} + \mathcal{A}_A \left( \begin{array}{c} A \\ \hat{Z}_{aA} \end{array} \right) \begin{array}{c} h_a \\ p^2 = M_a^2 \end{array} \right) + \dots$$

[E. Fuchs, PhD thesis; Fuchs, Weiglein '16, '17]

# Higgs mixing in the MSSM

How do we characterize mixing of internal Higgs bosons?

- ▶ Consider internal Higgs bosons  $h_a, a \in \{1, 2, 3\}$  exchanged b/w two vertices
- ▶ Full mixing propagator  $\Delta_{ij}(p^2)$ ,  $i, j \in \{h, H, A\}$  for the process approximated by  $\hat{\mathbf{Z}}$  factors [E. Fuchs, PhD thesis; Fuchs, Weiglein '16, '17]

$$\Delta_{ij}(p^2) \simeq \hat{\mathbf{Z}}_{1i} h_1 \hat{\mathbf{Z}}_{1j} + \hat{\mathbf{Z}}_{2i} h_2 \hat{\mathbf{Z}}_{2j} + \hat{\mathbf{Z}}_{3i} h_3 \hat{\mathbf{Z}}_{3j}$$

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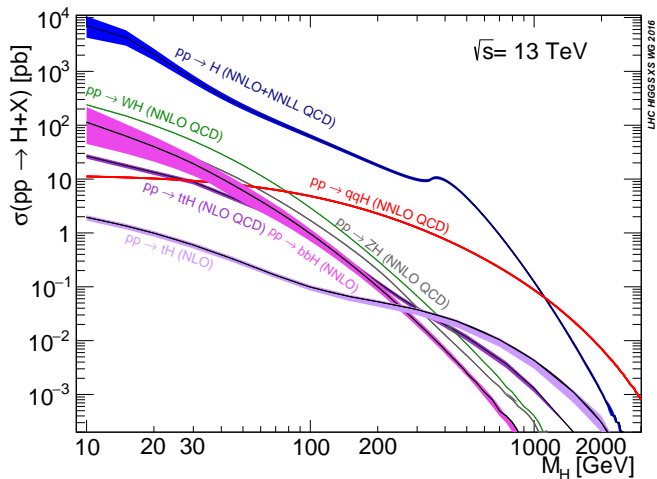
$$\hookrightarrow \boxed{\Delta_{ij}(p^2) \simeq \sum_{a \in \{1, 2, 3\}} \hat{\mathbf{Z}}_{ai} \Delta_a^{\text{BW}}(p^2) \hat{\mathbf{Z}}_{aj}} \quad \text{[Fuchs, Weiglein '17]}$$

with the Breit-Wigner (BW) propagator with complex pole  $\mathcal{M}_{h_a}^2$

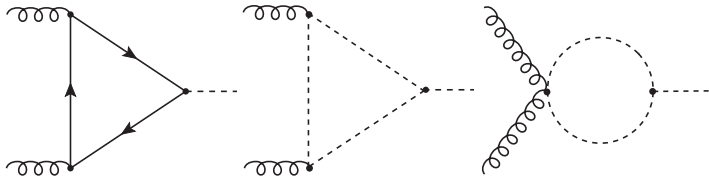
$$\Delta_a^{\text{BW}}(p^2) = \frac{i}{p^2 - \mathcal{M}_{h_a}^2}$$

*CP* phases in Higgs production

# Gluon Fusion in the SM



# Gluon Fusion in the MSSM



- ▶ Gluon-Gluon-Higgs coupling mediated by loops of coloured (s)fermions
- ▶ Primary contribution from (s)top and (s)bottom (s)quarks.
- ▶ In the  $\mathcal{CP}$ -conserving MSSM, XS for gluon fusion Higgs production known at the  $N^3\text{LO}$  for top-quark contribution, and analytically/various expansions at NLO for other contributions
- ▶ The amplitudes for  $\mathcal{CP}$ -even ( $h$  and  $H$ ) and  $\mathcal{CP}$ -odd ( $A$ ) Higgs bosons are non-interfering



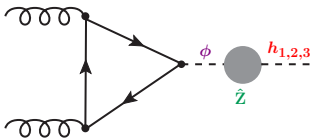
## $\mathcal{CP}$ phases in gluon fusion in the MSSM

$\mathcal{CP}$  phases from **squark loops**,  $\Delta_b$  **corrections** to bottom Yukawa coupling or  $\hat{Z}$  **factors**

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## The $\hat{\mathbf{Z}}$ mixing matrix

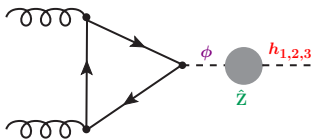


$$\begin{pmatrix} \mathcal{A}_{h_1} \\ \mathcal{A}_{h_2} \\ \mathcal{A}_{h_3} \end{pmatrix} = \hat{\mathbf{Z}} \cdot \begin{pmatrix} \mathcal{A}_h \\ \mathcal{A}_H \\ \mathcal{A}_A \end{pmatrix}$$

# $\mathcal{CP}$ phases in gluon fusion in the MSSM

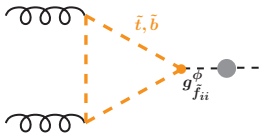
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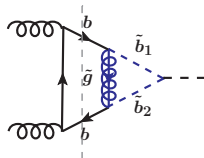
## Higgs-squark vertex



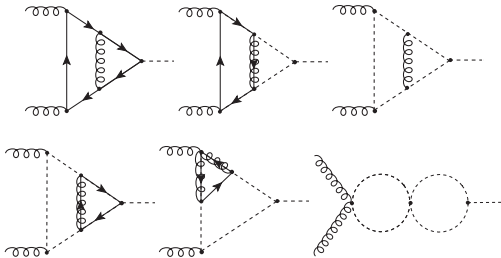
- ▶ Higgs-squark couplings contain  $\mathcal{CP}$  phases
- ▶ Non-zero  $g_{\tilde{f}ii}^A$  coupling

## Complex Yukawa couplings

- ▶ Complex  $\Delta_b$  corrections incorporated in effective bottom Yukawa coupling
- ▶ Non-zero terms  $\propto (g_{b_L}^\phi - g_{b_R}^\phi)$



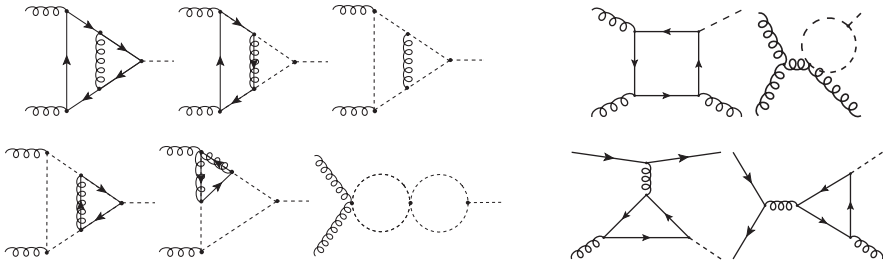
Higher order contributions can arise from **virtual loops**



$$\sigma_{\text{NLO}}^{e/o}(pp \rightarrow h_a + X) = \sigma_0^{h_a, e/o} \tau_{h_a} \mathcal{L}^{gg}(\tau_{h_a}) \left[ 1 + C^{e/o} \frac{\alpha_s}{\pi} \right]$$

- ▶ Known for the MSSM with real parameters analytically/in various expansions
- ▶ Need to be adapted and modified for the case of complex parameters

Higher order contributions can arise from **virtual loops** and **real radiation**



$$\sigma_{\text{NLO}}^{e/o}(pp \rightarrow h_a + X) = \sigma_0^{h_a, e/o} \tau_{h_a} \mathcal{L}^{gg}(\tau_{h_a}) \left[ 1 + C^{e/o} \frac{\alpha_s}{\pi} \right] \\ + \Delta\sigma_{gg}^{e/o} + \Delta\sigma_{gq}^{e/o} + \Delta\sigma_{q\bar{q}}^{e/o}$$

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- ▶ Need to be adapted and modified for the case of complex parameters

# Implementation to tools: SusHiMi and FeynHiggs

**SusHi**: neutral Higgs boson production XS through gluon fusion,  $b\bar{b}$  (5FS) in SM, 2HDM, (N)MSSM. [Harlander Liebler Mantler '12, '16],[Liebler '15],[Liebler, SP, Weiglein '16]: [sushi.hepforge.org](http://sushi.hepforge.org)

**FeynHiggs**: masses, couplings,  $\hat{Z}$  factors of the Higgs sector in MSSM.

[Hahn, Heinemeyer, Hollik, Rzehak, Weiglein]: [feynhiggs.de](http://feynhiggs.de)

## ► Implementation of gluon fusion and bottom quark annihilation XS in SusHiMi

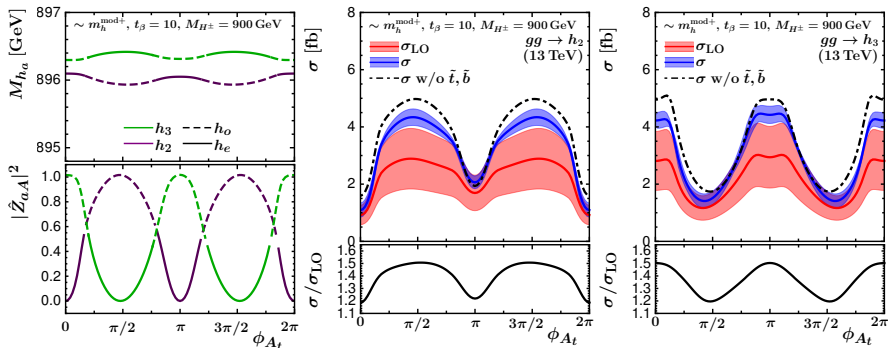
[Full details of the calculation in 1611.09308]

```
#-----#
# SusHi: (Supersymmetric) Higgs production through #
# gluon fusion and bottom-quark #
# annihilation #
# [Diagrams] #
# Version 1.7.0 May 2017 #
# R. Harlander, S. Liebler, and H. Mantler #
# (harlander@physik.rwth-aachen.de) #
# (stefan.liebler@desy.de) #
# (hendrik.mantler@kit.edu) #
# BU Wuppertal, RWTH Aachen, DESY, KIT #
#-----#
# Extension for CP violation in the Higgs sector: #
# SusHiMi by S. Liebler, and S. Patel #
# (shruti.patel@desy.de) #
#-----#
# SusHi is based on a number of calculations #
# due to various groups. Please acknowledge these #
# efforts by citing the list of references which #
# are included in the output file of every run. #
#-----#
SusHi (info): SUSHI(21) defaults to 0: All bbh@nnl0 subprocesses included.
SusHi (info): SusHi was called with the SLHA-block 'FEYNHIGGS'.
SusHi (info): Thus FeynHiggs is used for the calculation of SUSY
SusHi (info): Higgs masses, mu and stop, sbottom masses/angles.
No Block ALPHA found.
No Block FEYNHIGGSFLAGS found.
SusHi (info): VEGAS will be called only once.
#-----#
FeynHiggs 2.13.0
built on Jun 26, 2017
H. Bahl, T. Hahn, S. Heinemeyer, W. Hollik, S. Passehr, H. Rzehak, G. Weiglein
http://feynhiggs.de
```

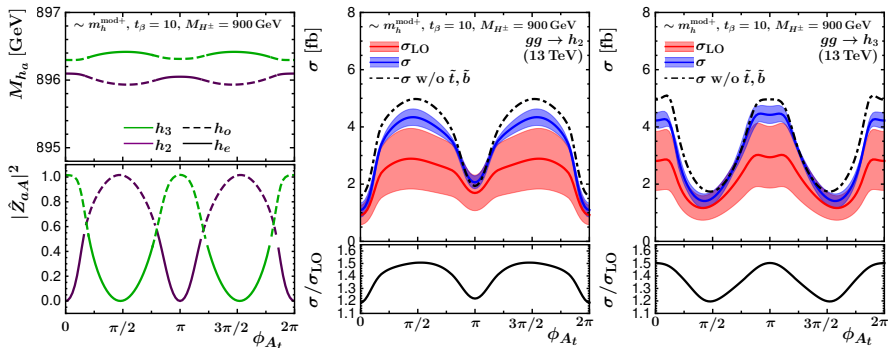
# Gluon Fusion: Admixture of Higgs bosons

[Liebler, SP, Weiglein '16]

Variation of  $\sigma(gg \rightarrow h_2, h_3)$  with  $\phi_{A_t}$  in the  $\sim m_h^{\text{mod}+}$  scenario with  $t_\beta = 10$



Variation of  $\sigma(gg \rightarrow h_2, h_3)$  with  $\phi_{A_t}$  in the  $\sim m_h^{\text{mod}+}$  scenario with  $t_\beta = 10$



- ▶ Nearly mass degenerate and  $\mathcal{CP}$ -admixed  $h_2$  and  $h_3$
- ▶ Might not be possible to resolve  $h_2$  and  $h_3$  as separate signals
- ▶ Expt. measured quantity: total  $\sigma \times \text{BR}$  with interference contributions



# Interference effects in MSSM Higgs searches

[E. Fuchs, talk at Higgs Days '17]

In general:  $\Delta M \leq \Gamma_1 + \Gamma_2 \implies$  Overlapping resonances

## Interfering Higgses in the MSSM

Real MSSM	$h, H$	$M_h \simeq M_H$ at high $\tan\beta$ , low $M_A$
Complex MSSM	$h_2, h_3$	$M_{h_2} \simeq M_{h_3}$ in the decoupling limit

If  $\mathbb{C}$ : incoherent sum  $\sigma(H) + \sigma(A)$  insufficient in heavy Higgs searches

$\rightarrow$  interference effects important

Standard NWA: Interference terms **neglected**

- Amplitude of Higgs  $h_a$  exchanged in production and decay  $I \rightarrow h_a \rightarrow F$

$$\hat{\Gamma}_{h_a}^I \text{---} h_a \text{---} \hat{\Gamma}_{h_a}^F = \sum_{i,j \in \{h,H,A\}} \hat{\Gamma}_i^I \text{---} h_a \text{---} \hat{\Gamma}_j^F$$

$\hat{Z}_{ai}$        $\hat{Z}_{aj}$

$$\mathcal{A}_{h_a} \equiv \hat{\Gamma}_{h_a}^I \Delta_a^{\text{BW}}(p^2) \hat{\Gamma}_{h_a}^F = \sum_{i,j \in \{h,H,A\}} \hat{\Gamma}_i^I \hat{Z}_{ai} \Delta_a^{\text{BW}}(p^2) \hat{Z}_{aj} \hat{\Gamma}_j^F$$

- Amplitude of Higgs  $h_a$  exchanged in production and decay  $I \rightarrow h_a \rightarrow F$

$$\hat{\Gamma}_{h_a}^I \text{---} h_a \text{---} \hat{\Gamma}_{h_a}^F = \sum_{i,j \in \{h,H,A\}} \hat{\Gamma}_i^I \text{---} \hat{Z}_{ai} \text{---} h_a \text{---} \hat{Z}_{aj} \text{---} \hat{\Gamma}_j^F$$

$$\mathcal{A}_{h_a} \equiv \hat{\Gamma}_{h_a}^I \Delta_a^{\text{BW}}(p^2) \hat{\Gamma}_{h_a}^F = \sum_{i,j \in \{h,H,A\}} \hat{\Gamma}_i^I \hat{Z}_{ai} \Delta_a^{\text{BW}}(p^2) \hat{Z}_{aj} \hat{\Gamma}_j^F$$

- Total amplitude  $\mathcal{A}$  for  $I \rightarrow h_1, h_2, h_3 \rightarrow F$ :

$$\hat{\Gamma}_{h_1}^I \text{---} h_1 \text{---} \hat{\Gamma}_{h_1}^F + \hat{\Gamma}_{h_2}^I \text{---} h_2 \text{---} \hat{\Gamma}_{h_2}^F + \hat{\Gamma}_{h_3}^I \text{---} h_3 \text{---} \hat{\Gamma}_{h_3}^F$$

- Total  $\sigma(I \rightarrow F) \propto |\mathcal{A}|^2$

# Coherent and incoherent squared amplitudes

[Fuchs, Weiglein '17]

▶  $\mathcal{CP}$  phases  $\Rightarrow \sigma(I \rightarrow h_1, h_2, h_3 \rightarrow F)$  contains interference terms  $\mathcal{A}_{h_a} \mathcal{A}_{h_b}^* \neq 0$

▶ **Coherent sum** contains interference terms

$$|\mathcal{A}|_{\text{coh}}^2 = \left| \begin{array}{c} \text{---} h_1 \text{---} \\ \text{---} h_2 \text{---} \\ \text{---} h_3 \text{---} \end{array} \right|^2$$

▶ **Incoherent sum** does not

$$|\mathcal{A}|_{\text{incoh}}^2 = \left| \begin{array}{c} \text{---} h_1 \text{---} \\ \text{---} h_2 \text{---} \\ \text{---} h_3 \text{---} \end{array} \right|^2 + \left| \begin{array}{c} \text{---} h_2 \text{---} \\ \text{---} h_3 \text{---} \end{array} \right|^2 + \left| \begin{array}{c} \text{---} h_3 \text{---} \end{array} \right|^2$$

▶ **Interference contribution** to  $\sigma(I \rightarrow h_1, h_2, h_3 \rightarrow F)$

$$|\mathcal{A}|_{\text{int}}^2 = |\mathcal{A}|_{\text{coh}}^2 - |\mathcal{A}|_{\text{incoh}}^2 = \sum_{a < b} 2 \operatorname{Re}[\mathcal{A}_{h_a} \mathcal{A}_{h_b}^*]$$

## Theoretical predictions with interference factor

- ▶ Relative **interference term** for  $I \rightarrow h_1, h_2, h_3 \rightarrow F$

$$\eta^{IF} = \frac{\sigma_{\text{int}}^{IF}}{\sigma_{\text{incoh}}^{IF}}$$

- ▶ Split into individual  $h_a$  interference contributions

$$\eta_a^{IF} = \frac{\sigma_{\text{int}_{ab}}^{IF}}{\sigma_{h_a}^{IF} + \sigma_{h_b}^{IF}} + \frac{\sigma_{\text{int}_{ac}}^{IF}}{\sigma_{h_a}^{IF} + \sigma_{h_c}^{IF}}$$

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## Framework: modified $\sigma \times \text{BR} \rightarrow$ Generalised Narrow Width Approximation

- ▶ Factorisation of production and decay of  $h_a$  rescaled by  $\eta_a^{IF}$

$$\sigma(pp \rightarrow I \rightarrow h_{1,2,3} \rightarrow F) \simeq \sum_{a=1}^3 \sigma(pp \rightarrow I \rightarrow h_a) \cdot (1 + \eta_a^{IF}) \cdot \text{BR}(h_a \rightarrow F)$$

[Fuchs, Weiglein '17]

- ▶  $\eta_a^{IF}$  calculation in SusHiMi for  $I \in \{gg, b\bar{b}\}$  and  $F \in \{\tau^+\tau^-, b\bar{b}, t\bar{t}\}$

[SP, Fuchs, Liebler, Weiglein '18, PhD thesis-SP '17]

- ▶  $\sigma(gg, b\bar{b})$  and  $\eta$  factors from SusHiMi, BRs from FeynHiggs-2.14.3

$b\bar{b}$  XS reweighted from: [Bonvini, Papanastasiou, Tackmann '15, '16], [Forte, Napoletano, Ubiali '15, '16]

# Benchmark Scenario: $M_{h_1}^{125}$ (CPV)

[Bahl, Fuchs, Hahn, Heinemeyer, Liebler, SP, Slavich, Stefaniak, Wagner, Weiglein: 1808.07542]

## Motivation

$\mathcal{CP}$  scenarios not analysed by CMS and ATLAS so far

## Defining the scenario $\rightarrow$ decoupling limit

- ▶ SM-like  $h_1$  with  $M_{h_1} \sim 125 \pm 3$  GeV in  $\{M_{H^\pm}, \tan \beta\}$  plane
- ▶  $M_{h_2} \simeq M_{h_3}$  with strong  $H - A$  admixture  $\Rightarrow$  interference b/w  $h_2, h_3$
- ▶ EDMs from  $\mathcal{CP}$  phases within expt. limits
- ▶ **Large interference universal feature of such scenarios**

## $M_{h_1}^{125}$ (CPV) parameter points

$$M_{\text{SUSY}} = 2 \text{ TeV}, \quad \mu = 1.65 \text{ TeV},$$

$$M_1 = M_2 = 1 \text{ TeV}, \quad M_3 = 2.5 \text{ TeV},$$

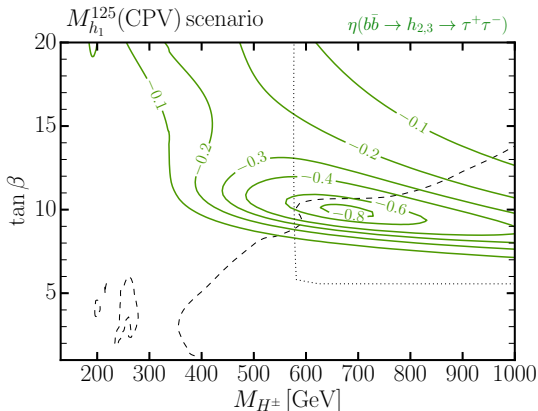
$$|A_t| = \mu \cot \beta + 2.8 \text{ TeV}, \quad \phi_{A_t} = \frac{2\pi}{15}, \quad A_b = A_\tau = |A_t|,$$

$$M_{(Q,U,D,L,E)_3} = M_{(Q,U,D)_{1,2}} = M_{\text{SUSY}}$$



# Interference factor in $M_{h_1}^{125}$ (CPV) scenario

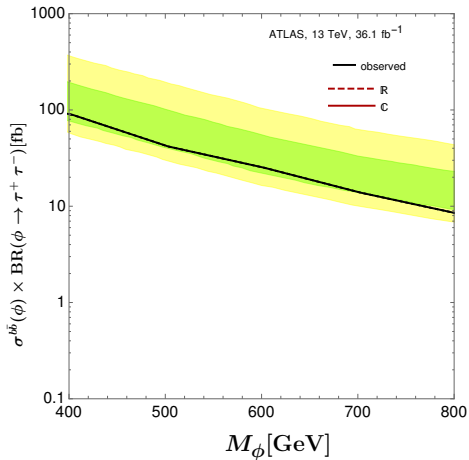
Plot of relative interference factor  $\eta^{b\bar{b},\tau\tau}$  for  $b\bar{b} \rightarrow h_2, h_3 \rightarrow \tau^+\tau^-$   
( $\eta^{gg,\tau\tau}$  contour similar in size and pattern)



Large, destructive interference:  $\eta_{\min}^{b\bar{b},\tau\tau} \simeq -96\%$

[Bahl, Fuchs, Hahn, Heinemeyer, Liebler, SP, Slavich, Stefaniak, Wagner, Weiglein: 1808.07542]

## Comparison of $\sigma \times \text{BR}$ containing $\eta^{b\bar{b},\tau\tau}$ with experimental limits

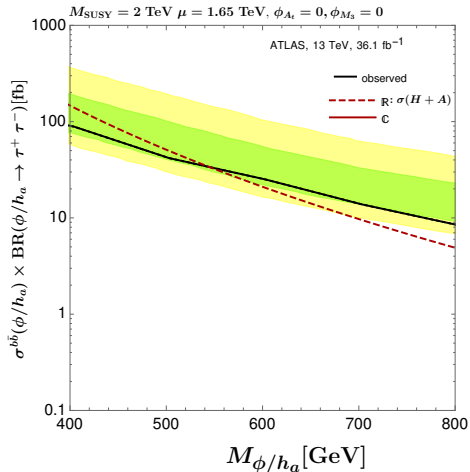


95 % CL upper limits on  $\sigma \times \text{BR}$  for  $b\bar{b} \rightarrow H/A \rightarrow \tau^+ \tau^-$  by ATLAS at 13 TeV

[ATLAS-CONF-2016-085]

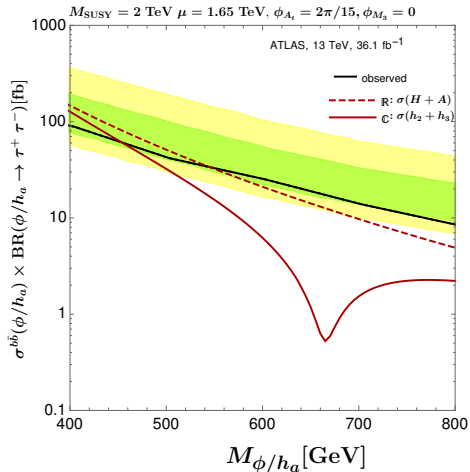
**CP-violation not taken into account in experimental analyses so far**

## Comparison of $\sigma \times \text{BR}$ containing $\eta^{b\bar{b}, \tau\tau}$ with experimental limits



**Real MSSM:**  
 $\sigma \times \text{BR}(H+A)$  (no interference)  
 at  $\tan\beta = 10$

## Comparison of $\sigma \times \text{BR}$ containing $\eta^{b\bar{b}, \tau\tau}$ with experimental limits

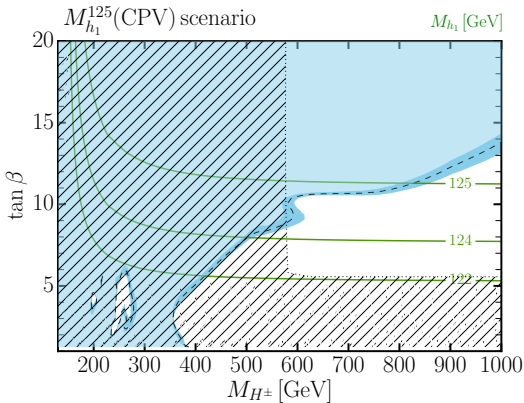


**Complex MSSM:**  
 Modified  $\sigma \times \text{BR}$  for  $h_2, h_3$   
 interference at  $\tan \beta = 10$

# Impact on LHC exclusion bounds

HiggsBounds-5.2.0beta:  $\sigma \times \text{BR}$  modified by  $\eta^{b\bar{b},\tau\tau}, \eta^{gg,\tau\tau}$

- ▶ **Unexcluded "bay"** due to destructive interference around  $\eta^{b\bar{b},\tau\tau} \lesssim -70\%$
- ▶ Minimal rate for  $h_2, h_3 \sim 4\%$  of value without interference
- ▶ Even with full Run 2 luminosity, the bay might remain unexcluded
- ▶ Important to consider the possibility of a  $CP$ -violating MSSM Higgs sector



[Bahl, Fuchs, Hahn, Heinemeyer, Liebler, SP, Slavich, Stefaniak, Wagner, Weiglein: 1808.07542]

## Higgs sector of the MSSM

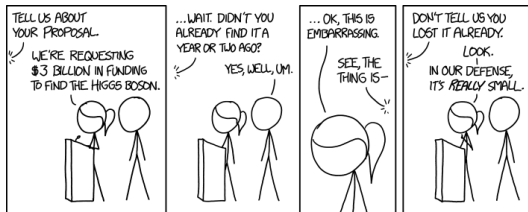
- ▶  $\mathcal{CP}$  gives rise to loop-corrected mass eigenstates  $h_1, h_2$  and  $h_3$

## $\mathcal{CP}$ phases in Higgs production

- ▶ Strongly admixed  $h_2$  and  $h_3$  in  $m_h^{\text{mod}+}$ -inspired scenario  $\rightarrow$  interference effects important

## Impact of interference effects on MSSM Higgs searches

- ▶ Accounting for destructive interference contributions in  $\sigma \times \text{BR}$  of  $gg, b\bar{b} \rightarrow \tau^+\tau^-$  weakens LHC exclusion bounds



[Comic: XKCD]

**1** Higgs mixing and interference

**2** Gluon fusion and higher orders

**3** Phenomenology of  $\mathcal{CP}$  MSSM

# Propagators and self-energies

- ▶ The propagator matrix given by

$$\Delta_{hHA}(p^2) = - \left[ \hat{\Gamma}_{hHA}(p^2) \right]^{-1},$$

- ▶ Irreducible 2-point vertex functions

$$\hat{\Gamma}_{ij}(p^2) = i \left[ (p^2 - m_i^2) \delta_{ij} + \hat{\Sigma}_{ij}(p^2) \right]$$

form the elements of  $\hat{\Gamma}_{hHA}(p^2) = i \left[ p^2 \mathbf{1} - \mathbf{M}(p^2) \right]$

3×3 propagator matrix

$$\Delta_{hHA}(p^2) = \begin{pmatrix} \Delta_{hh}(p^2) & \Delta_{hH}(p^2) & \Delta_{hA}(p^2) \\ \Delta_{Hh}(p^2) & \Delta_{HH}(p^2) & \Delta_{HA}(p^2) \\ \Delta_{Ah}(p^2) & \Delta_{AH}(p^2) & \Delta_{AA}(p^2) \end{pmatrix} \\ = i \begin{pmatrix} p^2 - m_h^2 + \hat{\Sigma}_{hh}(p^2) & \hat{\Sigma}_{hH}(p^2) & \hat{\Sigma}_{hA}(p^2) \\ \hat{\Sigma}_{Hh}(p^2) & p^2 - m_H^2 + \hat{\Sigma}_{HH}(p^2) & \hat{\Sigma}_{HA}(p^2) \\ \hat{\Sigma}_{Ah}(p^2) & \hat{\Sigma}_{AH}(p^2) & p^2 - m_A^2 + \hat{\Sigma}_{AA}(p^2) \end{pmatrix}^{-1}.$$

The neutral Higgs masses are determined as the complex poles of the propagators,

$$\mathcal{M}^2 = M^2 - iM\Gamma,$$

These complex poles are the roots of the determinant of the matrix  $\hat{\Gamma}_{hHA}(p^2)$ ,

$$\det \left[ \hat{\Gamma}_{hHA}(p^2) \right] = - \left( \det[\Delta_{hHA}(p^2)] \right)^{-1} = 0.$$



## Definition of $\hat{\mathbf{Z}}$ factors

- ▶  $\hat{\mathbf{Z}}$  factors provide the correct normalisation of a matrix element with an external on-shell Higgs boson  $h_a$ ,  $a \in \{1, 2, 3\}$ , at  $p^2 = \mathcal{M}_a^2$

$$\lim_{p^2 \rightarrow \mathcal{M}_a^2} -\frac{i}{p^2 - \mathcal{M}_a^2} \left( \hat{\mathbf{Z}} \cdot \hat{\Gamma}_{hHA} \cdot \hat{\mathbf{Z}}^T \right)_{hh} = 1,$$

$$\lim_{p^2 \rightarrow \mathcal{M}_b^2} -\frac{i}{p^2 - \mathcal{M}_b^2} \left( \hat{\mathbf{Z}} \cdot \hat{\Gamma}_{hHA} \cdot \hat{\mathbf{Z}}^T \right)_{HH} = 1,$$

$$\lim_{p^2 \rightarrow \mathcal{M}_c^2} -\frac{i}{p^2 - \mathcal{M}_c^2} \left( \hat{\mathbf{Z}} \cdot \hat{\Gamma}_{hHA} \cdot \hat{\mathbf{Z}}^T \right)_{AA} = 1.$$

- ▶ The wave function normalisation factors for an external Higgs boson  $i \in \{h, H, A\}$

$$\hat{Z}_i^a := \text{Res}_{\mathcal{M}_a^2} \{ \Delta_{ii}(p^2) \} = \frac{1}{1 + \hat{\Sigma}_{ii}^{\text{eff}'}(\mathcal{M}_a^2)}.$$

- ▶ On-shell transition ratio

$$\hat{Z}_{ij}^a = \left. \frac{\Delta_{ij}(p^2)}{\Delta_{jj}(p^2)} \right|_{p^2 = \mathcal{M}_a^2}.$$

- ▶ Finally

$$\hat{\mathbf{Z}}_{aj} = \sqrt{\hat{Z}_a} \hat{Z}_{aj}$$

# Calculation of interference terms

## Amplitude of $h_a$

$$\begin{aligned}\mathcal{A}_{h_a} &= \hat{\Gamma}_{h_a}^X \Delta_a^{\text{BW}}(p^2) \hat{\Gamma}_{h_a}^Y = \sum_{i,j \in \{h,H,A\}} \left( \hat{\Gamma}_i^X \hat{\mathbf{Z}}_{ai} \right) \Delta_a^{\text{BW}}(p^2) \left( \hat{\mathbf{Z}}_{aj} \hat{\Gamma}_j^Y \right) \\ &= \sum_{i,j \in \{h,H,A\}} \hat{\Gamma}_i^X \left( \hat{\mathbf{Z}}_{ai} \Delta_a^{\text{BW}}(p^2) \hat{\mathbf{Z}}_{aj} \right) \hat{\Gamma}_j^Y.\end{aligned}$$

## Interference contribution:

$$|\mathcal{A}|_{\text{int}}^2 = 2\text{Re} \left[ \mathcal{A}_{h_1} \mathcal{A}_{h_2}^* + \mathcal{A}_{h_2} \mathcal{A}_{h_3}^* + \mathcal{A}_{h_1} \mathcal{A}_{h_3}^* \right]$$

## Mixing between the two heavy Higgses $h_2$ and $h_3$

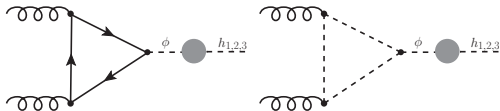
$$|\mathcal{A}|_{\text{int}}^2 = 2\text{Re} \left[ \left( \hat{\Gamma}_{h_2}^I \Delta_2^{\text{BW}}(\hat{s}) \hat{\Gamma}_{h_2}^F \right) \left( \hat{\Gamma}_{h_3}^I \Delta_3^{\text{BW}}(\hat{s}) \hat{\Gamma}_{h_3}^F \right)^* \right]$$

evaluated at  $p^2 = \hat{s} = \left( \frac{M_{h_2} + M_{h_3}}{2} \right)^2$ . [E. Fuchs, PhD thesis; Fuchs, Weiglein '16, '17]

## Integrate over phase space

$$\begin{aligned}\sqrt{s}_{\text{min}} &= p - 5 \left( \frac{\hat{\Gamma}_{h_2} + \hat{\Gamma}_{h_3}}{2} \right), \quad \sqrt{s}_{\text{max}} = p + 5 \left( \frac{\hat{\Gamma}_{h_2} + \hat{\Gamma}_{h_3}}{2} \right), \\ \sigma(|\mathcal{A}|_{\text{int}}^2) &= \int_{s_{\text{min}}}^{s_{\text{max}}} ds \, 2\text{Re} \left[ \left( \hat{\Gamma}_{h_2}^I \Delta_2^{\text{BW}}(s) \hat{\Gamma}_{h_2}^F \right) \left( \hat{\Gamma}_{h_3}^I \Delta_3^{\text{BW}}(s) \hat{\Gamma}_{h_3}^F \right)^* \right].\end{aligned}$$

# Leading order cross section



$$\sigma_{\text{LO}}(pp \rightarrow h_a) = \sigma_0^{h_a} \tau_{h_a} \mathcal{L}^{gg}(\tau_{h_a}) \quad , \quad \mathcal{L}^{gg}(\tau) = \int_{\tau}^1 \frac{dx}{x} g(x) g(\tau/x), \quad \tau_{h_a} = \frac{M_{h_a}^2}{s}$$

$$\sigma_0^{h_a} = \frac{G_F \alpha_s^2(\mu_R)}{288 \sqrt{\pi}} \left[ \left| \mathcal{A}^{h_a, e} \right|^2 + \left| \mathcal{A}^{h_a, o} \right|^2 \right]$$

with  $\mathcal{A}^{h_a, e} = \hat{\mathbf{Z}}_{ah} \mathcal{A}_+^h + \hat{\mathbf{Z}}_{aH} \mathcal{A}_+^H + \hat{\mathbf{Z}}_{aA} \mathcal{A}_-^A$   
and  $\mathcal{A}^{h_a, o} = \hat{\mathbf{Z}}_{ah} \mathcal{A}_-^h + \hat{\mathbf{Z}}_{aH} \mathcal{A}_-^H + \hat{\mathbf{Z}}_{aA} \mathcal{A}_+^A$

$$\phi_e = h, H: \quad \mathcal{A}_+ = \sum_{q \in \{t, b\}} (a_{q,+} + \tilde{a}_q), \quad \mathcal{A}_- = \sum_{q \in \{t, b\}} a_{q,-}$$

$$\phi = A: \quad \mathcal{A}_- = \sum_{q \in \{t, b\}} (a_{q,-} + \tilde{a}_q), \quad \mathcal{A}_+ = \sum_{q \in \{t, b\}} a_{q,+}^A$$

## Full LO cross section

$$\mathcal{A}_+^{\phi^e} = \sum_{q \in \{t, b\}} \left( a_{q,+}^{\phi^e} + \tilde{a}_q^{\phi^e} \right), \quad \mathcal{A}_-^{\phi^e} = \sum_{q \in \{t, b\}} a_{q,-}^{\phi^e}$$

$$a_{q,+}^{\phi^e} = \frac{1}{2} \left( g_{qL}^{\phi^e} + g_{qR}^{\phi^e} \right) \frac{3}{2} \tau_q^{h_a} \left[ 1 + (1 - \tau_q^{h_a}) f(\tau_q^{h_a}) \right], \quad a_{q,-}^{\phi^e} = \frac{i}{2} \left( g_{qR}^{\phi^e} - g_{qL}^{\phi^e} \right) \frac{3}{2} \tau_q^{h_a} f(\tau_q^{h_a}),$$

$$\tilde{a}_q^{\phi^e} = -\frac{3}{8} \tau_q^{h_a} \sum_{i=1}^2 g_{\tilde{q}ii}^{\phi^e} \left[ 1 - \tau_{\tilde{q}i}^{h_a} f(\tau_{\tilde{q}i}^{h_a}) \right].$$

$$\mathcal{A}_-^A = \sum_{q \in \{t, b\}} \left( a_{q,-}^A + \tilde{a}_q^A \right), \quad \mathcal{A}_+^A = \sum_{q \in \{t, b\}} a_{q,+}^A$$

$$a_{q,+}^A = \frac{1}{2} \left( g_{qL}^A + g_{qR}^A \right) \frac{3}{2} \tau_q^{h_a} f(\tau_q^{h_a}), \quad a_{q,-}^A = \frac{i}{2} \left( g_{qL}^A - g_{qR}^A \right) \frac{3}{2} \tau_q^{h_a} \left[ 1 + (1 - \tau_q^{h_a}) f(\tau_q^{h_a}) \right],$$

$$\tilde{a}_q^A = -\frac{3}{8} \tau_q^{h_a} \sum_{i=1}^2 g_{\tilde{q}ii}^A \left[ 1 - \tau_{\tilde{q}i}^{h_a} f(\tau_{\tilde{q}i}^{h_a}) \right].$$

$$f(\tau) = \begin{cases} \arcsin^2 \frac{1}{\sqrt{\tau}}, & \tau \geq 1 \\ -\frac{1}{4} \left( \log \frac{1+\sqrt{1-\tau}}{1-\sqrt{1-\tau}} - i\pi \right)^2, & \tau < 1. \end{cases}$$

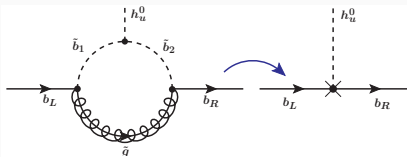
## $\Delta_b$ corrections to bottom Yukawa coupling

- ▶ Leading  $\tan\beta$  enhanced  $\Delta_b$  corrections from gluino-sbottom loops absorbed in effective bottom Yukawa coupling

$$\mathcal{L}_{\text{eff}} = -\lambda_b \bar{b}_R \left[ h_d^0 + \frac{\Delta_b}{t_\beta} h_u^{0*} \right] b_L + h.c.$$

$$\Delta_b = \frac{2}{3\pi} \alpha_s \mu^* M_3^* t_\beta I(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, m_{\tilde{g}}^2)$$

### Eff. bottom Yukawa couplings with full $\Delta_b$ corrections @ LO

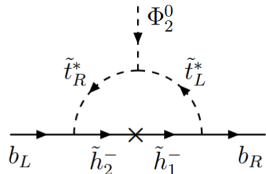
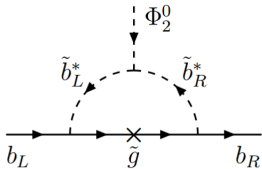


$$\begin{aligned} \text{▶ } g_{b_L}^h &= (g_{b_R}^h)^* = \frac{1}{1+\Delta_b} \left[ \frac{\sin\alpha}{\cos\beta} + \frac{\cos\alpha}{\sin\beta} \Delta_b \right] \\ \text{▶ } g_{b_L}^H &= (g_{b_R}^H)^* = \frac{1}{1+\Delta_b} \left[ \frac{\cos\alpha}{\cos\beta} + \frac{\sin\alpha}{\sin\beta} \Delta_b \right] \\ \text{▶ } g_{b_L}^A &= (g_{b_R}^A)^* = \frac{1}{1+\Delta_b} \left[ \tan\beta \left( 1 - \frac{\Delta_b}{\tan^2\beta} \right) \right] \end{aligned}$$

- ▶ A *simplified*  $\Delta_b$  correction used at NLO:

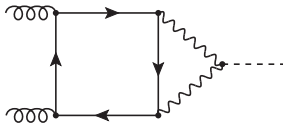
$$g_{b_L}^\phi = g_{b_R}^\phi = \frac{1}{|1 + \Delta_b|} f(\alpha, \beta)$$

# $\Delta_b$ corrections



$$\begin{aligned}
 &= \Delta m_{\tilde{b}}^{\tilde{g}} + \Delta m_{\tilde{b}}^{\tilde{h}} \\
 &= \frac{2}{3} \frac{\alpha_s}{\pi} \mu^* M_3^* t_\beta I \left( m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, m_{\tilde{g}}^2 \right) + \frac{\alpha_t}{4\pi} A_t^* \mu^* t_\beta I \left( m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2, |\mu|^2 \right)
 \end{aligned}$$

[1103.1335]



- ▶ Full NLO EW corrections are known only in SM
- ▶ For MSSM, EW amplitude constructed only for  $h$  and  $H$
- ▶ No coupling of  $A$  to gauge bosons, EW corrections to  $\mathcal{CP}$ -odd Higgs negligible

$$\sigma_{\text{NLO, EW}}^e = \sigma_{\text{NLO}}^e (1 + \delta_{\text{EW}}^{\text{lf}})$$

$$\delta_{\text{EW}}^{\text{lf}} = \frac{\alpha_{\text{EM}}}{\pi} \frac{2\text{Re}(\mathcal{A}^{h_a, e} \mathcal{A}^{h_a, \text{EW}*})}{|\mathcal{A}^{h_a, e}|^2}$$

Electroweak amplitude [Bondani, Degrossi, Vicini '11]

$$\mathcal{A}^{h_a, \text{EW}} = -\frac{3}{8} \frac{1}{x_W s_W^2} \left[ \frac{2}{c_W^4} \left( \frac{5}{4} - \frac{7}{3} s_W^2 + \frac{22}{9} s_W^4 \right) A_1[x_Z] + 4A_1[x_W] \right] \cdot \left( -\hat{\mathbf{Z}}_{ah} \sin \alpha \cos \beta + \hat{\mathbf{Z}}_{aH} \cos \alpha \sin \beta \right),$$

with

$$x_V = \frac{M_{h_a}^2}{\left( m_V - i \frac{\Gamma_V}{2} \right)^2}, \quad V \in \{W, Z\}.$$

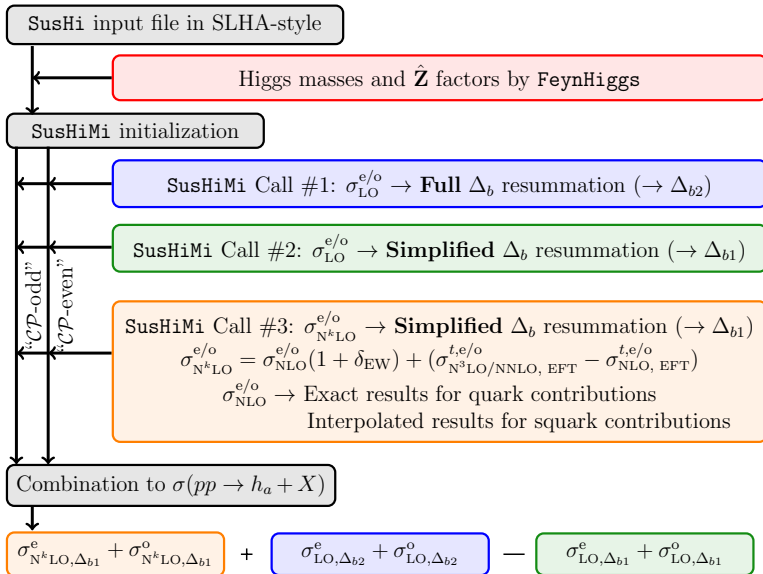
# Gluon fusion beyond LO

- ▶ Complex Yukawa coupling only induced for the b-quark through  $\Delta_b$  contributions.
- ▶ For  $g_t^\phi$ , left- and right-handed components identical  $\Rightarrow$  can take over known higher-order QCD corrections to the top loop contribution
- ▶ For bottom contribution at NLO (SM) QCD, use simplified version of the  $\Delta_b$  corrections to the bottom coupling  $\Rightarrow$  higher-order quark contributions, both real and virtual, of the same structure as in the  $\mathcal{CP}$ -conserving MSSM.
- ▶ **Real corrections:** only new ingredients are Higgs–squark couplings to the  $\mathcal{CP}$ -odd,  $g_{\tilde{q}ii}^A$ . Squark induced contributions of  $\mathcal{CP}$ -odd components  $\propto g_{\tilde{q}ii}^A$  added as a complex component to the  $\mathcal{CP}$ -even couplings. Real corrections split in  $\Delta\sigma^e$  and  $\Delta\sigma^o$
- ▶ **Virtual corrections:** Quark induced contributions taken over from SusHi [Harlander, Kant '05]. Squark induced contributions interpolated from real case (known in various expansions). Finally:

$$C^{e/o} = 2\text{Re} \left[ \frac{\mathcal{A}_{\text{NLO}}^{h_{a,e/o}}}{\mathcal{A}^{h_{a,e/o}}} \right] + \pi^2 + \beta_0 \log \left( \frac{\mu_R^2}{\mu_F^2} \right). \quad (1)$$

with  $\mathcal{A}_{\text{NLO}}^{h_{a,e}} = \hat{\mathbf{Z}}_{ah} \mathcal{A}_{\text{NLO}}^h + \hat{\mathbf{Z}}_{aH} \mathcal{A}_{\text{NLO}}^H$  and  $\mathcal{A}_{\text{NLO}}^{h_{a,o}} = \hat{\mathbf{Z}}_{aA} \mathcal{A}_{\text{NLO}}^A$ ,  $\mu_F$  denotes the factorisation scale, and  $\beta_0 = 11/2 - n_f/3$  with  $n_f = 5$ .





Scenario Parameter	$m_h^{\text{mod+}}$ <b>inspired</b>
$m_t$	173.2
$M_{H^\pm}$ (or $M_A$ )	<i>Varied</i>
$\tan \beta$	<i>Varied</i>
$M_{\text{SUSY}}$	1000
$M_{l_3}$	1000
$X_t/M_{\text{SUSY}}$	1.5
$A_b$	$ A_t $
$A_\tau$	$ A_t $
$\mu$	1000
$M_1$	250
$M_2$	500
$M_3$	$1500e^{i\phi_{M_3}}$
$M_{\tilde{q}_{1,2}}$	$M_{\text{SUSY}}$
$M_{\tilde{l}_{1,2}}$	$M_{\text{SUSY}}$
$A_{f \neq t, b, \tau}$	0

# Theoretical uncertainties

## PDF + $\alpha_s$ uncertainties

- ▶ Uncertainties in cross-section predictions can be induced by PDF fits and associated  $\alpha_s$
- ▶ MMHT2014 PDF sets used for LO, NLO and NNLO for  $gg\Phi$  and  $bb\Phi$
- ▶ PDF +  $\alpha_s$  uncertainties function of  $m_{h_a}$
- ▶ Can be taken over from description for MSSM Higgses in LHCHXSWG report 4 [arXiv:1610.07922]

## Scale uncertainties

- ▶ Central scale choice:  $(\mu_R^0, \mu_F^0) = (m_{h_a}/2, m_{h_a}/2)$  for  $gg\Phi$  and  $(\mu_R^0, \mu_F^0) = (m_{h_a}, m_{h_a}/4)$  for  $bb\Phi$
- ▶ Scale unc. obtained by taking maximal deviation from central scale choice  $\{(2\mu_R^0, 2\mu_F^0), (2\mu_R^0, \mu_F^0), (\mu_R^0, 2\mu_F^0), (\mu_R^0, \mu_F^0/2), (\mu_R^0/2, \mu_F^0), (\mu_R^0/2, \mu_F^0/2)\}$
- ▶ 
$$\Delta\sigma^{\text{scale}} = \sqrt{\left(\Delta\sigma_{\mathbf{N}^k \text{LO}}^{\Delta b1}\right)^2 + \left(\Delta\sigma_{\text{LO}}^{\Delta b2} - \Delta\sigma_{\text{LO}}^{\Delta b1}\right)^2}$$

## Interpolation uncertainties

- ▶ Interpolation of two-loop virtual squark-gluino contributions induces an unc. due to non-exact results
- ▶ 
$$\Delta\sigma^{\text{int}} = \sin^2(\phi_z)|\sigma(0) - \sigma(\pi)|/2$$

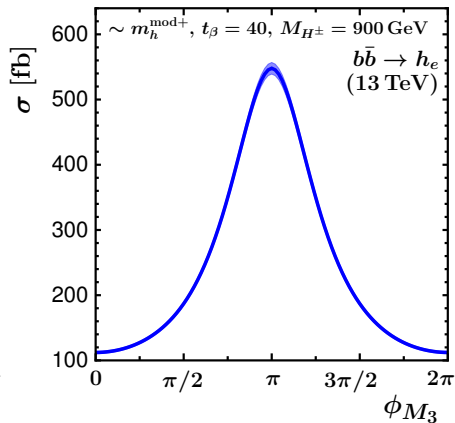
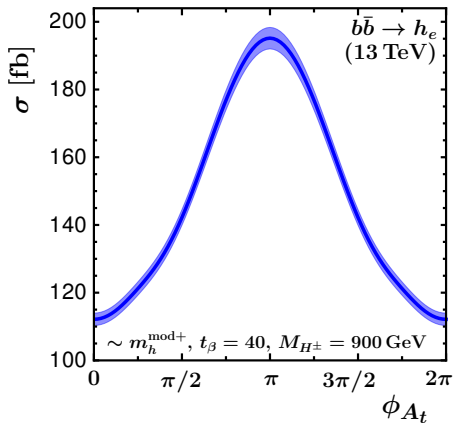
- ▶ SusHi employs the 5FS for the bottom-quark annihilation process for SM Higgs at NNLO QCD<sup>1</sup>
- ▶ For MSSM with real parameters, SusHi links  $\text{bbh@nnlo}$  for the inclusive cross section  $\sigma_{b\bar{b}H^0}$  in the SM at NNLO QCD which uses  $m_b^{\overline{\text{MS}}}(\mu_R)$  for the bottom-Yukawa coupling, subsequently reweighted by the resummed SUSY coupling  $g_b^\phi$
- ▶ For  $h_a$  production in the MSSM with  $\mathcal{CP}$  in SusHiMi, the results for the SM Higgs boson reweighted to the MSSM with  $|\hat{\mathbf{Z}}_{ah}g_b^h + \hat{\mathbf{Z}}_{aH}g_b^H|^2 + |\hat{\mathbf{Z}}_{aA}g_b^A|^2$ , includes  $\tan\beta$ -enhanced squark effects through simplified  $\Delta_b$  resummation
- ▶ In case of non-equal left- and right-handed couplings  $g_{bL}$  and  $g_{bR}$  due to the full resummation the SM cross section multiplied with

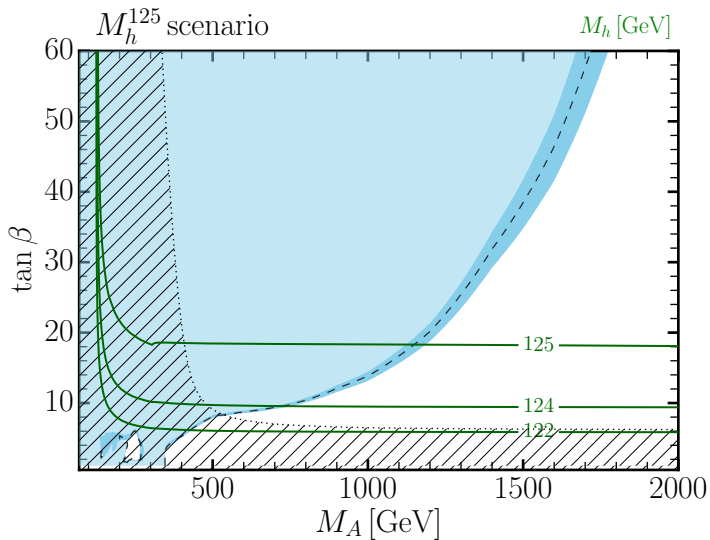
$$\begin{aligned} & |\hat{\mathbf{Z}}_{ah}(g_{bL}^h + g_{bR}^h) + \hat{\mathbf{Z}}_{aH}(g_{bL}^H + g_{bR}^H) + i\hat{\mathbf{Z}}_{aA}(g_{bL}^A - g_{bR}^A)|^2 \\ & + |i\hat{\mathbf{Z}}_{ah}(g_{bR}^h - g_{bL}^h) + i\hat{\mathbf{Z}}_{aH}(g_{bR}^H - g_{bL}^H) + \hat{\mathbf{Z}}_{aA}(g_{bL}^A + g_{bR}^A)|^2. \end{aligned}$$

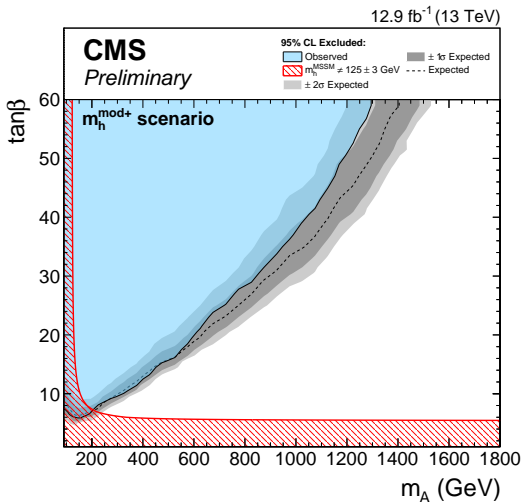
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<sup>1</sup>Latest benchmark scenario uses the updated cross sections with resummed logs combining 4FS and 5FS [Bonvini, Papanastasiou, Tackmann, '15, '16], [Forte, Napoletano, Ubiali, '15, '16]

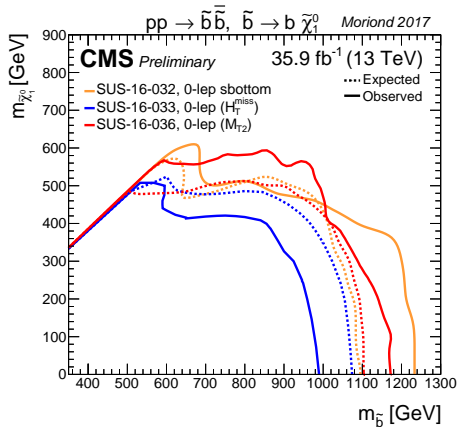
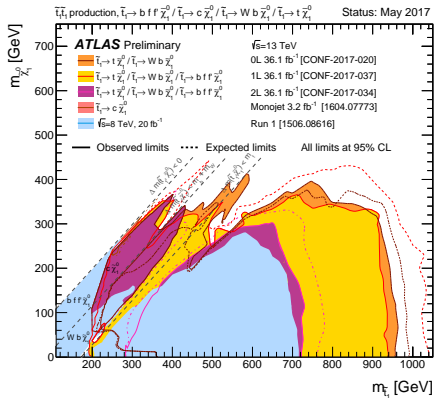
# $b\bar{b}$ cross section





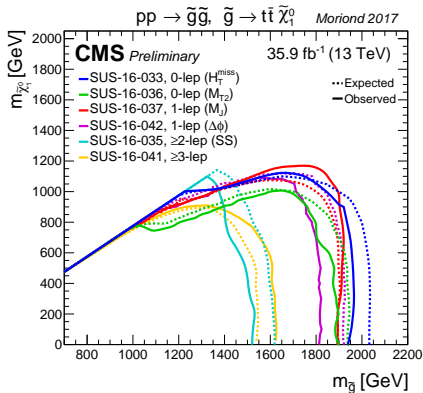
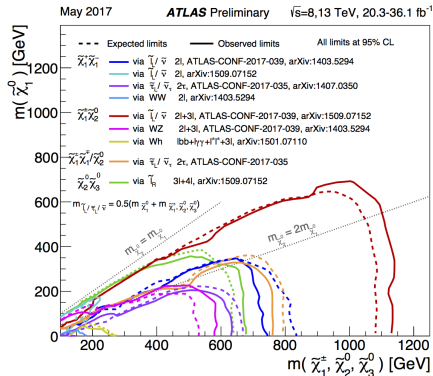


# Stops and bottoms





# Glino and chargino



# Electric Dipole Moments (EDMs)

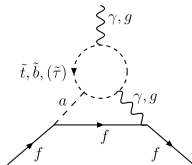
## EDM experiments

eg:

- ▶ **ACME: Advanced Cold Molecule Electron EDM**
- ▶ **Storage Ring EDM collaboration:**  
proton, deuteron nuclei

## SUSY contributions

eg[hep-ph/9902371]:



constraint	value [e cm]	Ref.
EDM electron $d_e$	$8.7 \cdot 10^{-29}$	[ACME '14]
EDM neutron $d_n$	$4.7 \cdot 10^{-26}$	[hep-ex/0602020]
EDM mercury $d_{\text{Hg}}$	$3.5 \cdot 10^{-29}$	[PhysRevLett.102.101601]

95% CL upper limits on the EDMs of the electron, neutron and mercury.

- ▶ MSSM contributions to EDMs contribute at the one-loop level, primarily involve the 1st 2 gen. of squark and sleptons
- ▶ Severe constraints on phases of  $A_q$  for  $q \in \{u, d, s, c\}$  and  $A_l$  for  $l \in \{e, \mu\}$
- ▶ Third-generation trilinear coupling phases weakly constrained [Li, Profumo, Ramsey-Musolf, '10]
- ▶ Maximal  $\phi_{A_t}$  ruled out [1612.08090], however still significant room for variation