

# Phenomenological Aspects of Flavoured Majorana Dark Matter

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In collaboration with H. Acaroglu, M. Blanke,  
J. Heisig and M. Krämer

Young Scientists Meeting

Siegen

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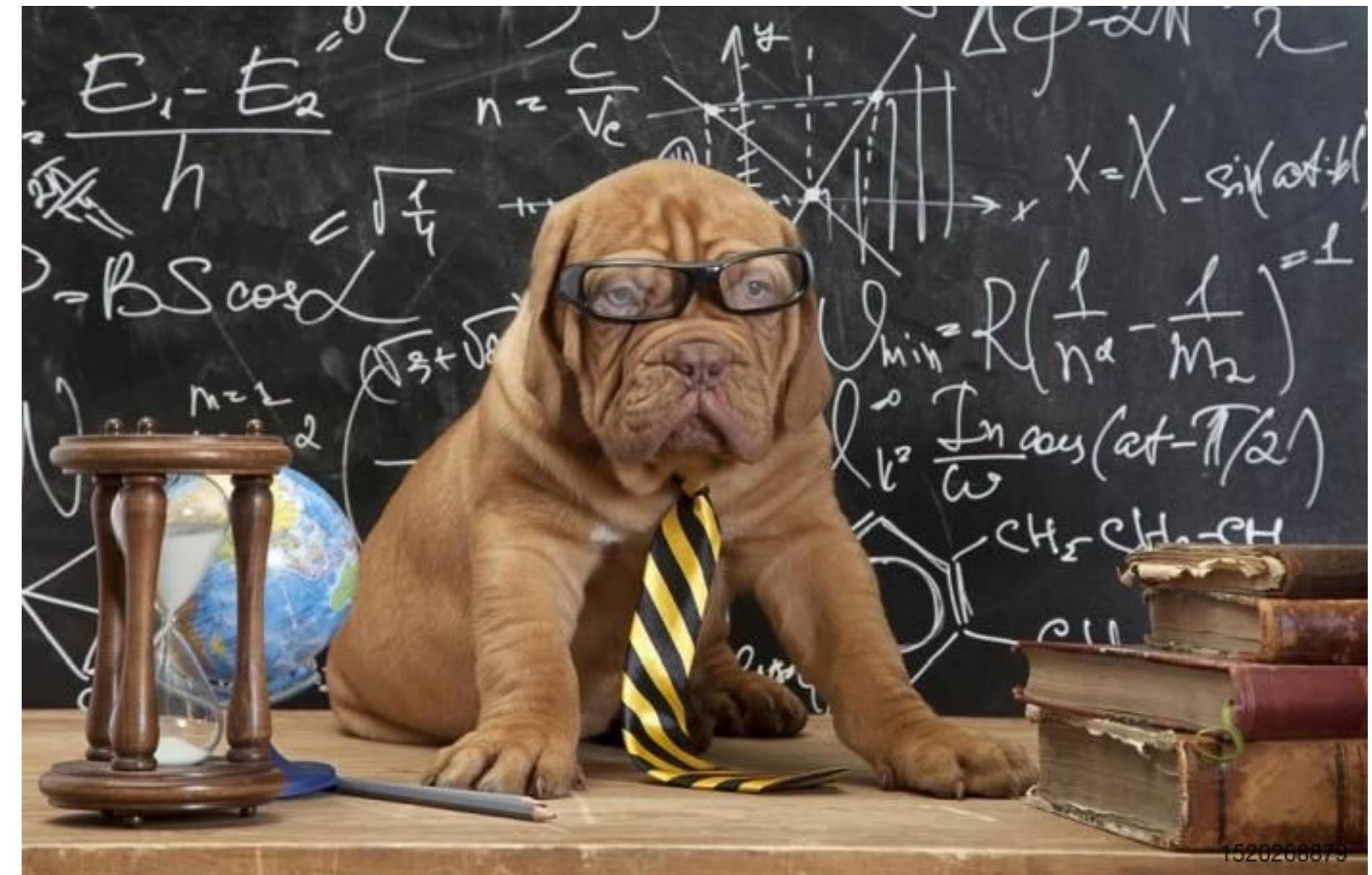
# Outline

## Dark Matter model

- Flavoured Majorana Dark Matter
- Previous analysis and results

## Freeze-out scenarios

- Freeze-out with coannihilations
- Conversion driven freeze-out



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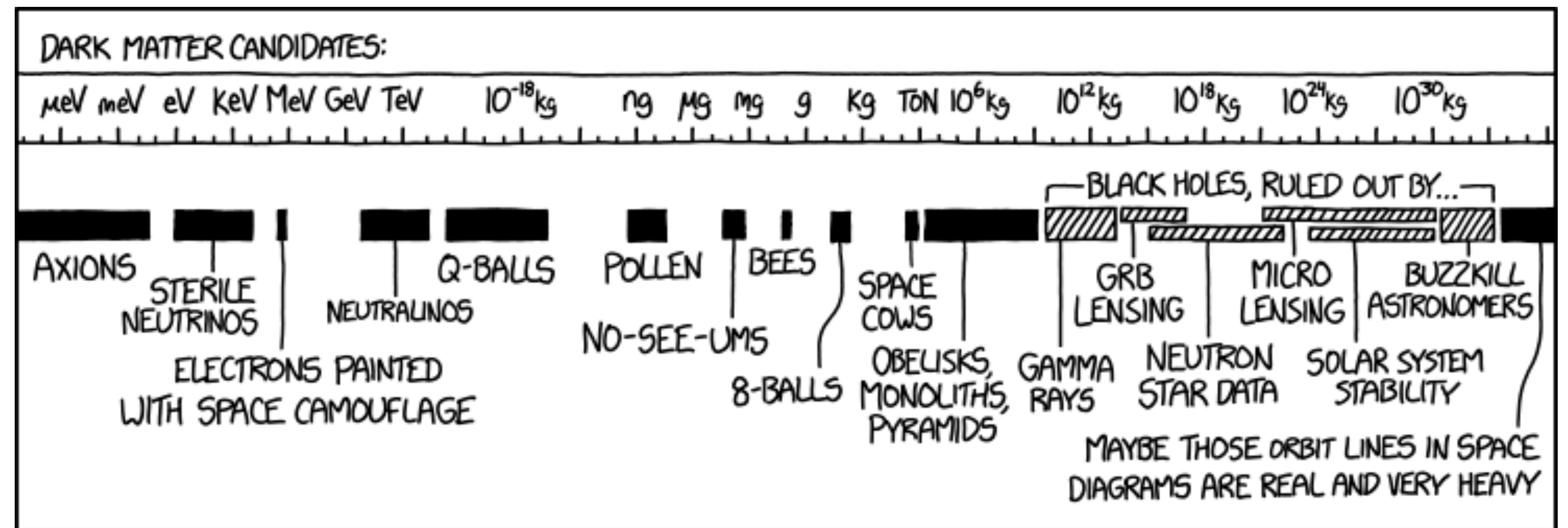
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# Why Flavoured Dark Matter?

- Simple weakly interacting massive particle (WIMP) models under severe pressure
  - Assume Dark Matter (DM) is charged under non-trivial flavour symmetry
- New source of flavour and CP violation → different phenomenology
- More degrees of freedom → opens up parameter space



<https://xkcd.com/2035/>

# Dark Minimal Flavour Violation

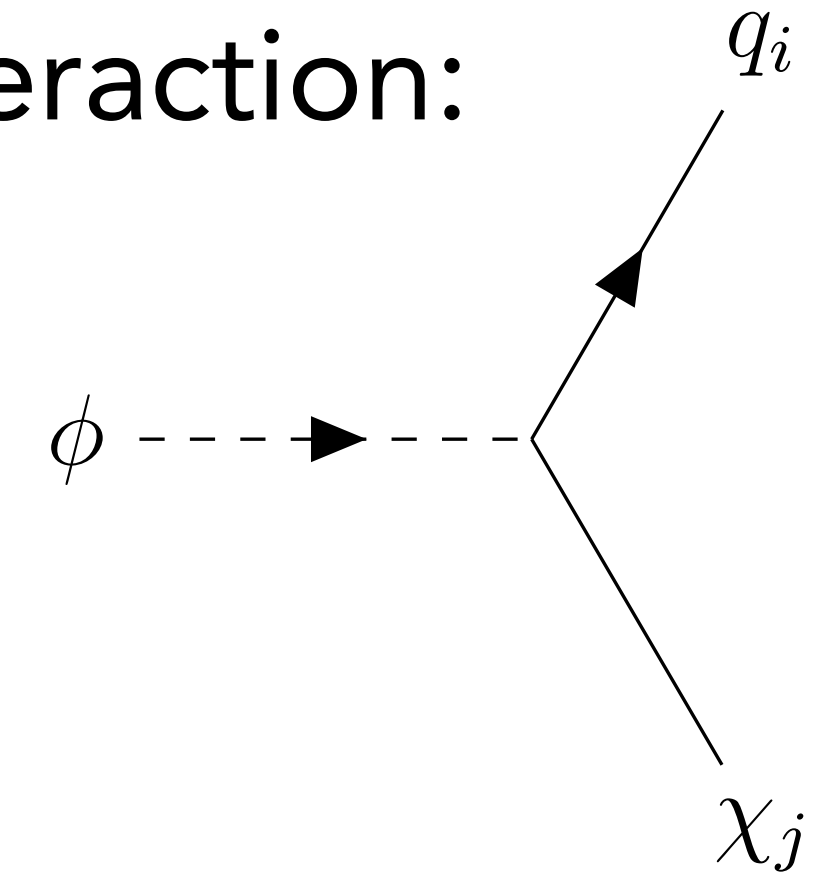
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- Dark Minimal Flavour Violation (DMFV) framework: Extend SM by new flavour symmetry and new fields (DM flavour triplet  $\chi_i$  and mediator  $\phi$ )
- Dirac DMFV models have been studied for DM coupling to
  - ▶ right-handed down-type quarks Agrawal, Blanke, Gemmler [1405.6709]
  - ▶ right-handed up-type quarks Blanke, Kast [1702.08457]
  - ▶ left-handed quarks Blanke, Das, Kast [1711.10493]
- Here: Consider flavoured Majorana DM which couples to right-handed up-type quarks via a scalar mediator Acaroglu, Blanke [2109.10357]

# Flavoured Majorana DM

- New physics contribution with flavour and CP violating interaction:

$$\mathcal{L}_{\text{NP}} \supset \frac{1}{2}(i\bar{\chi}\not{\partial}\chi - M_{\chi}\bar{\chi}\chi) - (\lambda_{ij}\bar{u}_{R_i}\chi_j\phi + \text{h.c.}) + (D_{\mu}\phi)^{\dagger}(D^{\mu}\phi) - m_{\phi}^2\phi^{\dagger}\phi$$



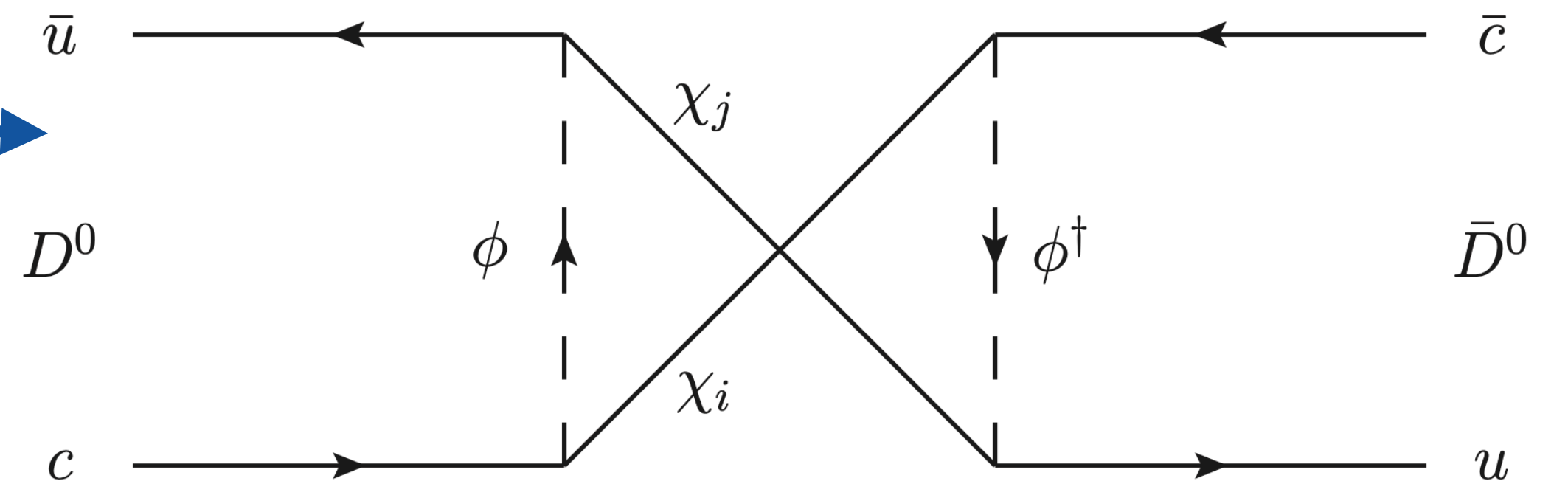
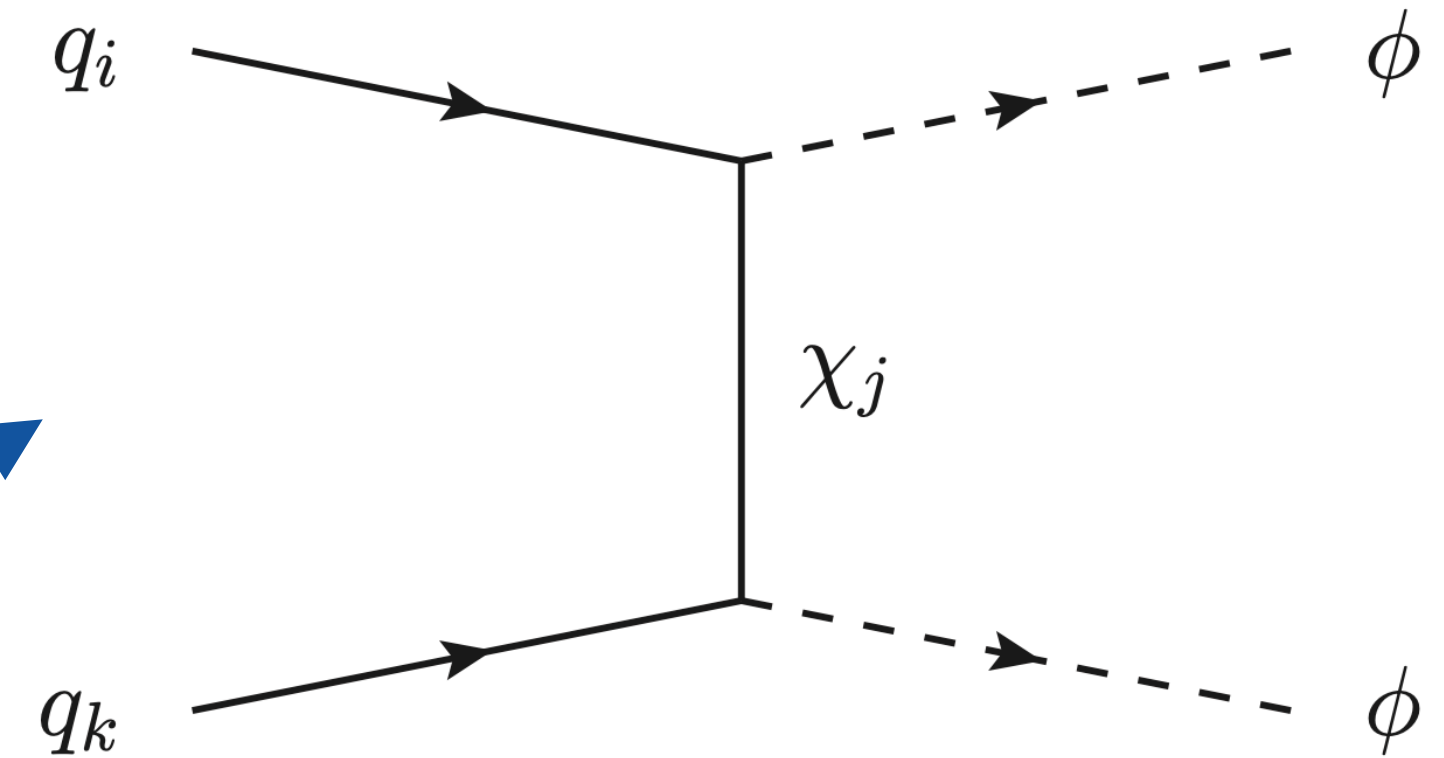
- Mass matrix cannot be generic  $\rightarrow$  expand mass matrix in powers of  $\lambda$ :

$$M_{\chi} = m_{\chi} \left( \mathbf{1} + \frac{\eta}{2}(\lambda^{\dagger}\lambda + \lambda^T\lambda^*) \right) \xrightarrow{\text{Diagonalize}} M_{\chi}^D = \text{diag}(m_{\chi_1}, m_{\chi_2}, m_{\chi_3})$$

with  $m_{\chi_1} > m_{\chi_2} > m_{\chi_3}$  and  $m_{\phi} > m_{\chi_3}$

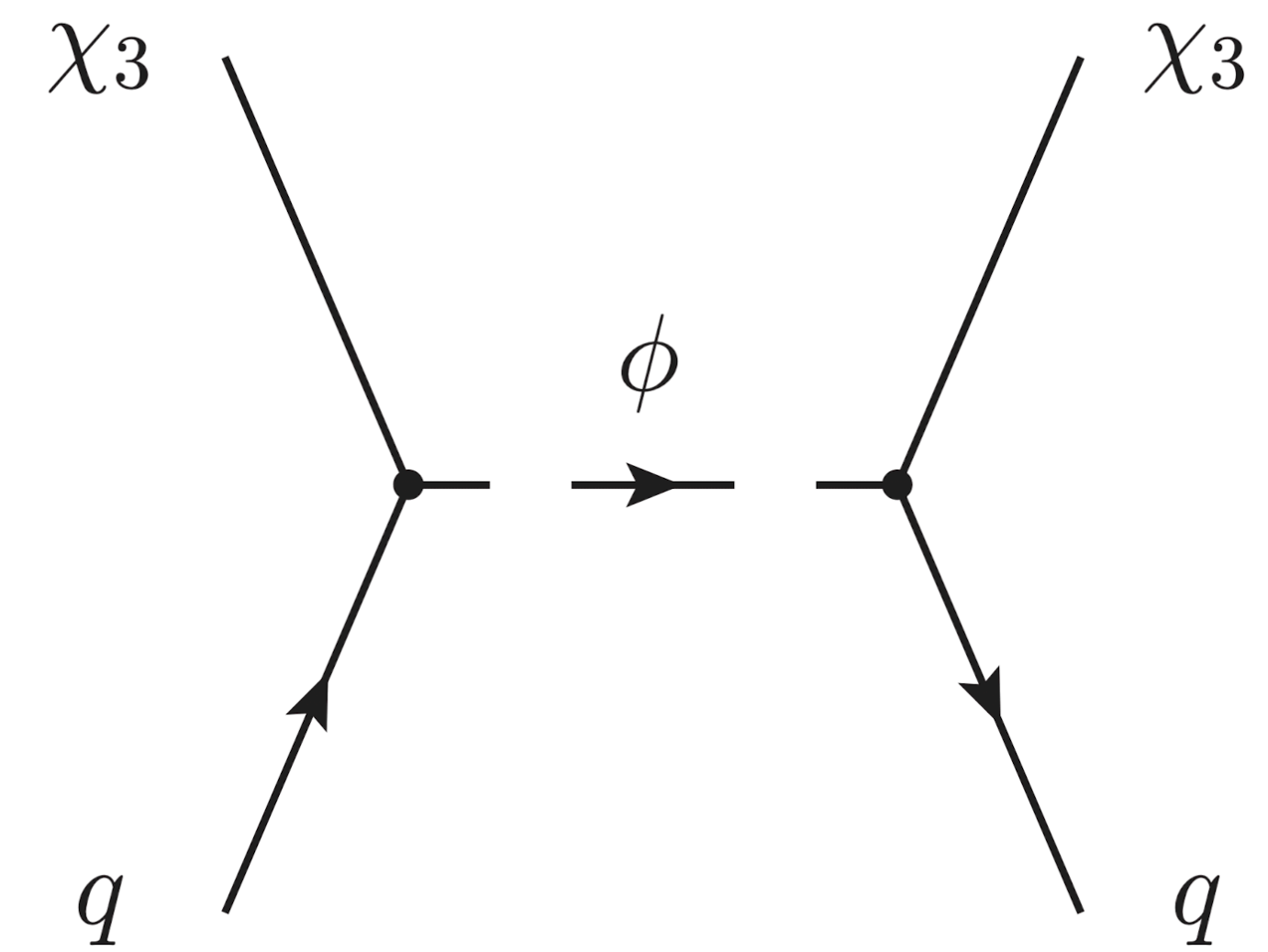
# Previous Analysis

- Phenomenology studied in Acaroglu, Blanke [2109.10357]
- Collider: Relevant signatures tops +  $\cancel{E}$  and jets +  $\cancel{E}$ , Majorana-specific same-sign signature  $tt + \cancel{E}$
- Flavour Physics: Limits from  $D^0 - \bar{D}^0$  mixing, additional crossed diagram extends allowed parameter space



# Previous Analysis

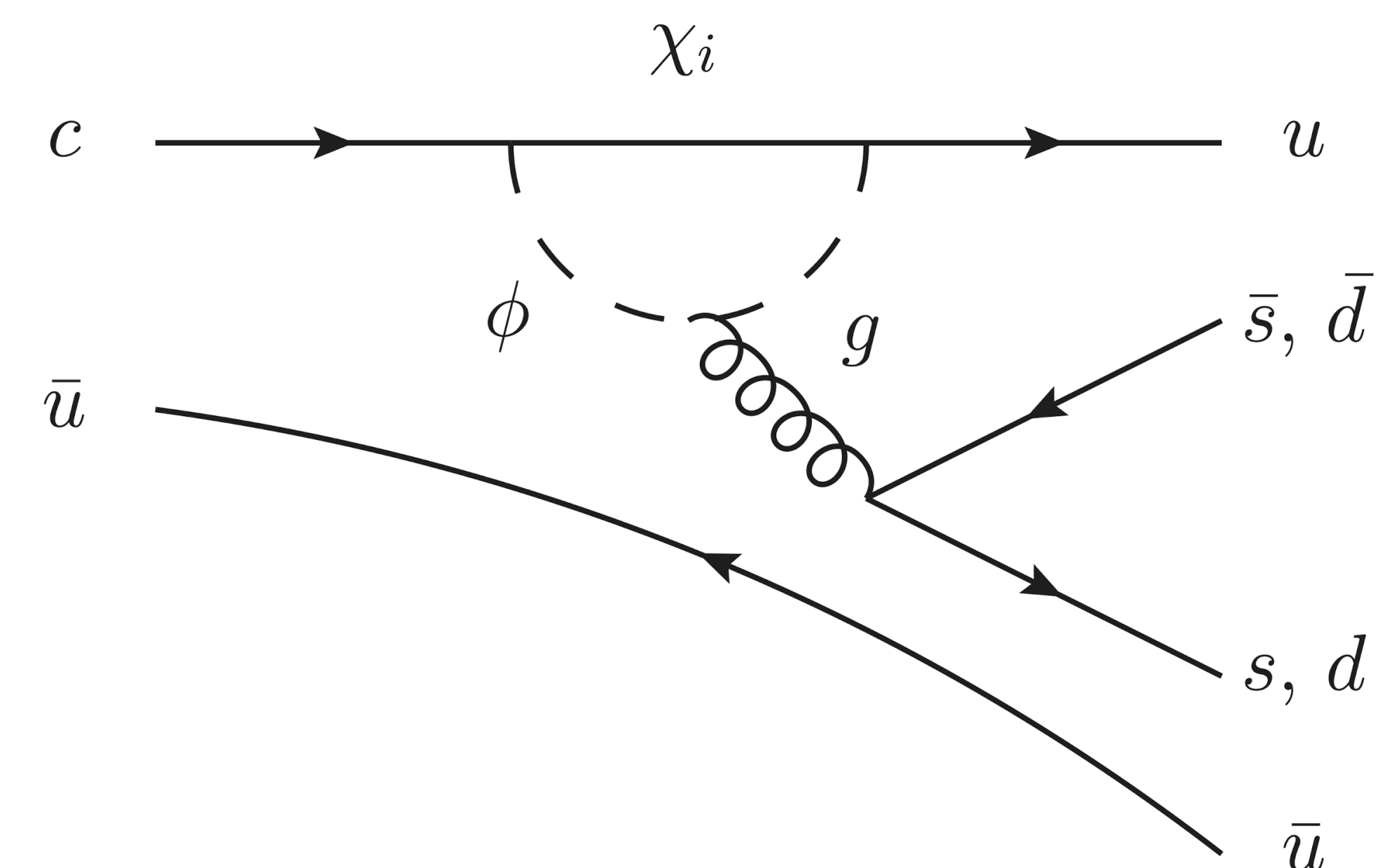
- Direct detection: Limits from spin-dependent and spin-independent WIMP-nucleon scattering



- CP violation in charm decays: Model is able to explain large measured value of CP asymmetry



$$\Delta A_{\text{CP}}^{\text{dir}} = A_{\text{CP}}(D \rightarrow K^+ K^-) - A_{\text{CP}}(D \rightarrow \pi^+ \pi^-)$$





# Cosmological Constraints

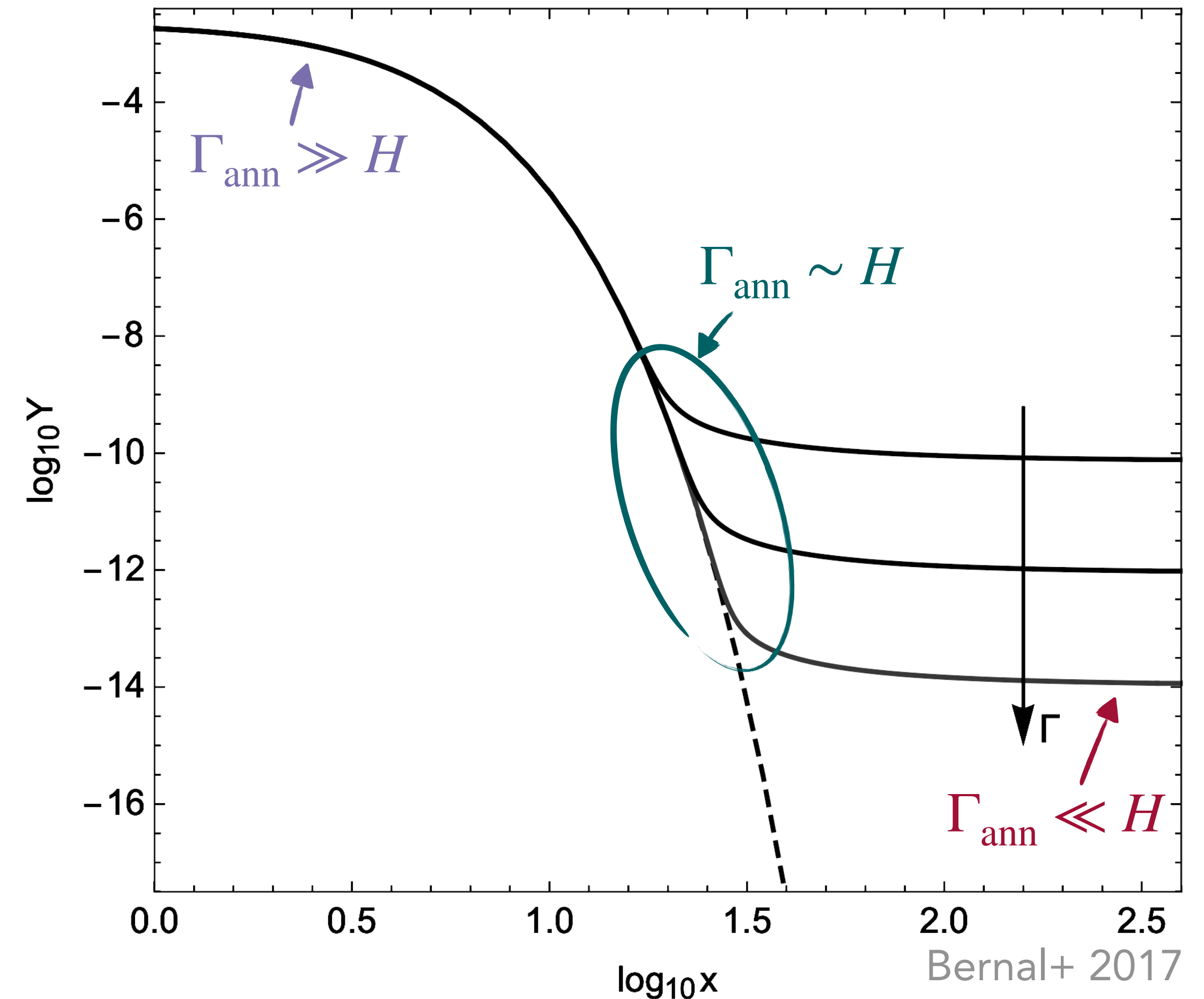
- Freeze-out mechanism: solve Boltzmann equation for  $Y = n/s$  and  $x = m_\chi/T$

$$\frac{dY}{dx} = - \frac{1}{3H} \frac{ds}{dx} \langle \sigma_{\chi\chi} v \rangle (Y^2 - Y_{\text{eq}}^2)$$

Expansion of  
Universe

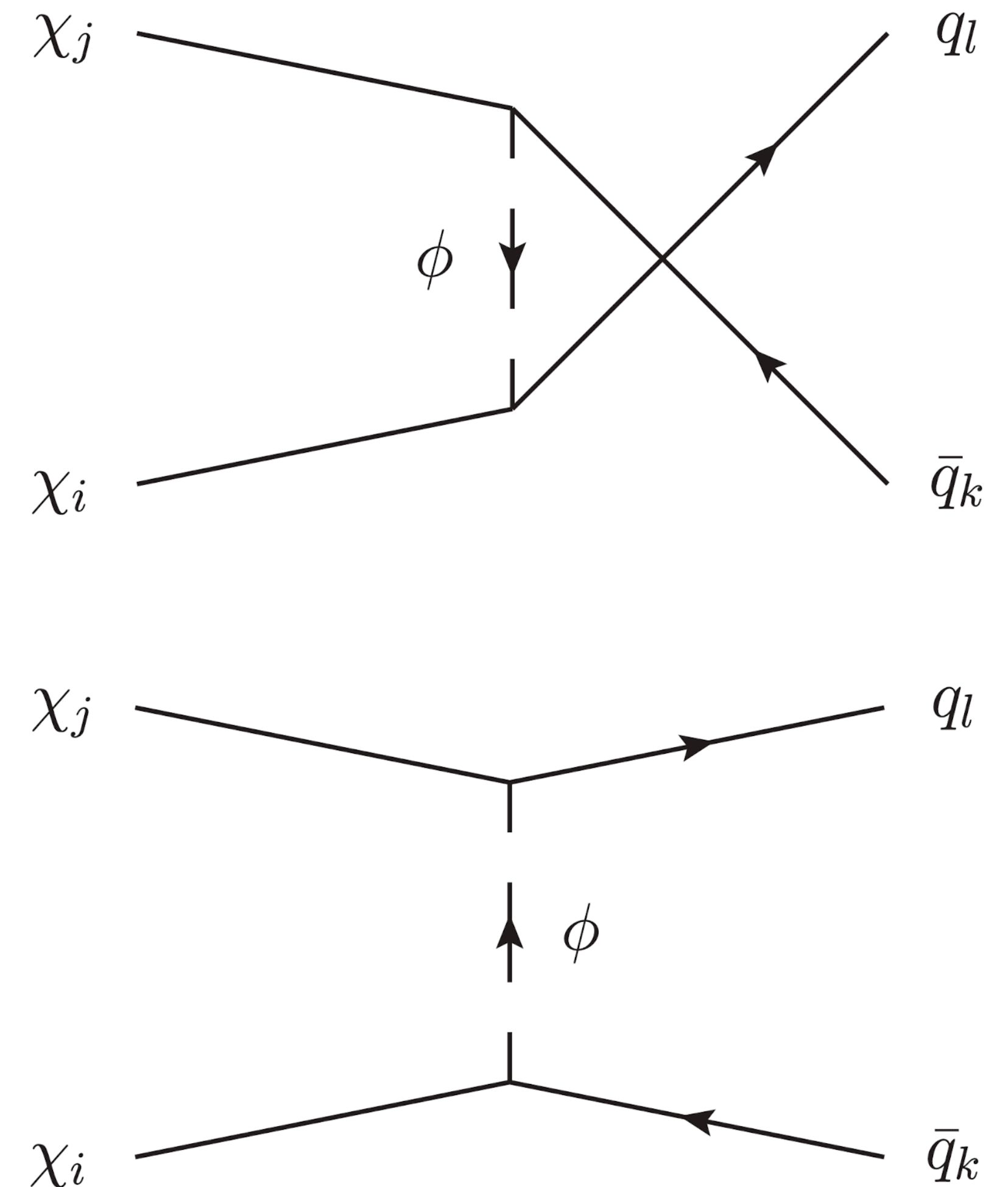
Number-changing  
interactions

- Three regions for  $\Gamma_{\text{ann}} = n_\chi \langle \sigma_{\chi\chi} v \rangle$ :
  - $\Gamma_{\text{ann}} \gg H$ : DM in thermal equilibrium
  - $\Gamma_{\text{ann}} \sim H$ : Freeze-out
  - $\Gamma_{\text{ann}} \ll H$ : Constant abundance  $Y$



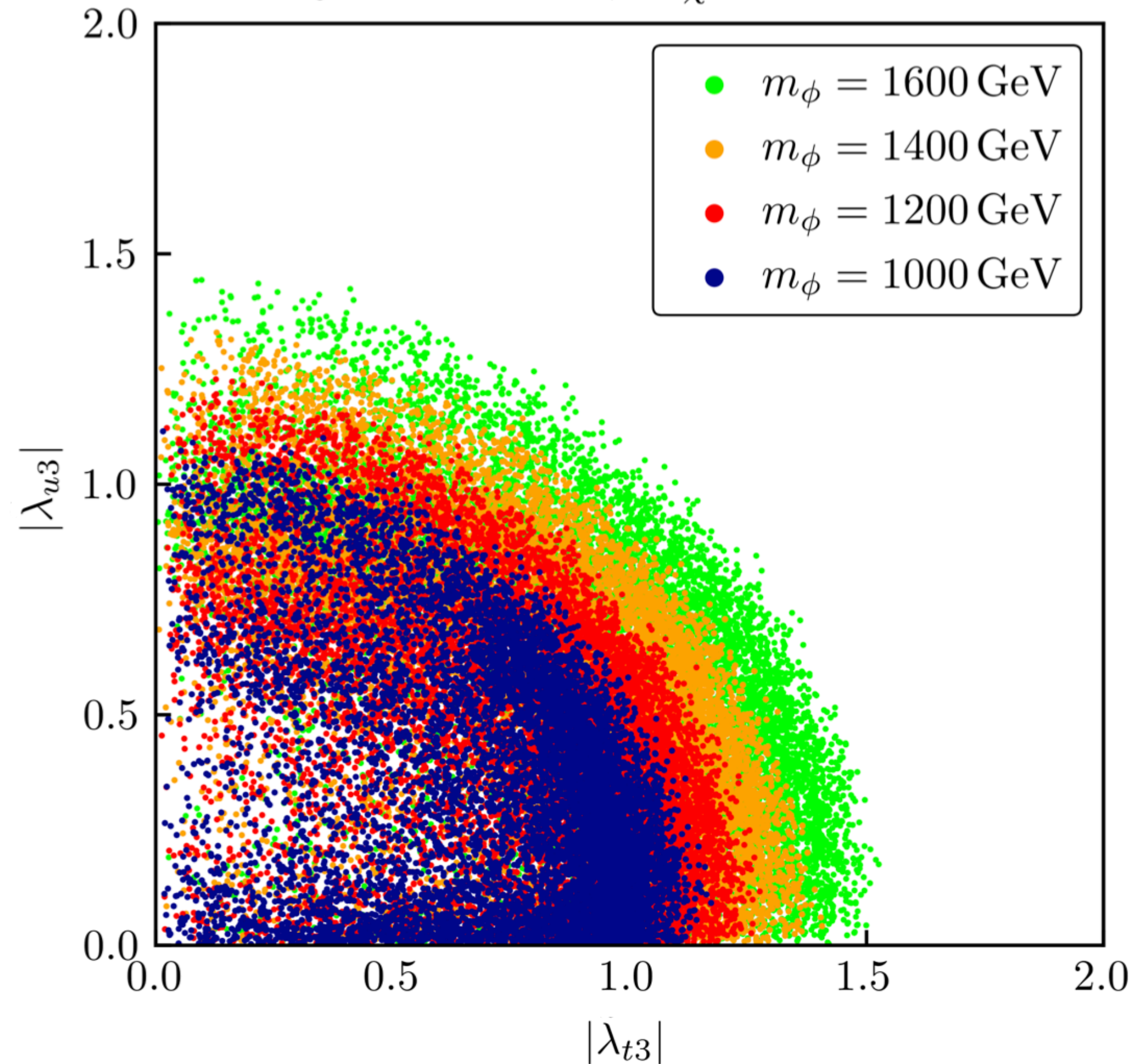
# Cosmological Constraints

- Two benchmark freeze-out scenarios:
  - Quasi-Degenerate Freeze-Out (QDF): mass splitting below 1%
  - Single-Flavour Freeze-Out (SFF): mass splitting above 10%
- $\phi$  does not contribute to freeze-out
- Low-velocity expansion  $\langle\sigma v\rangle = a + b\langle v^2\rangle$   
with  $\langle v^2\rangle = 6T_f/m_\chi \approx 0.3$
- Compare to  $\langle\sigma v\rangle \approx 2.2 \cdot 10^{-26} \text{cm}^3/\text{s}$

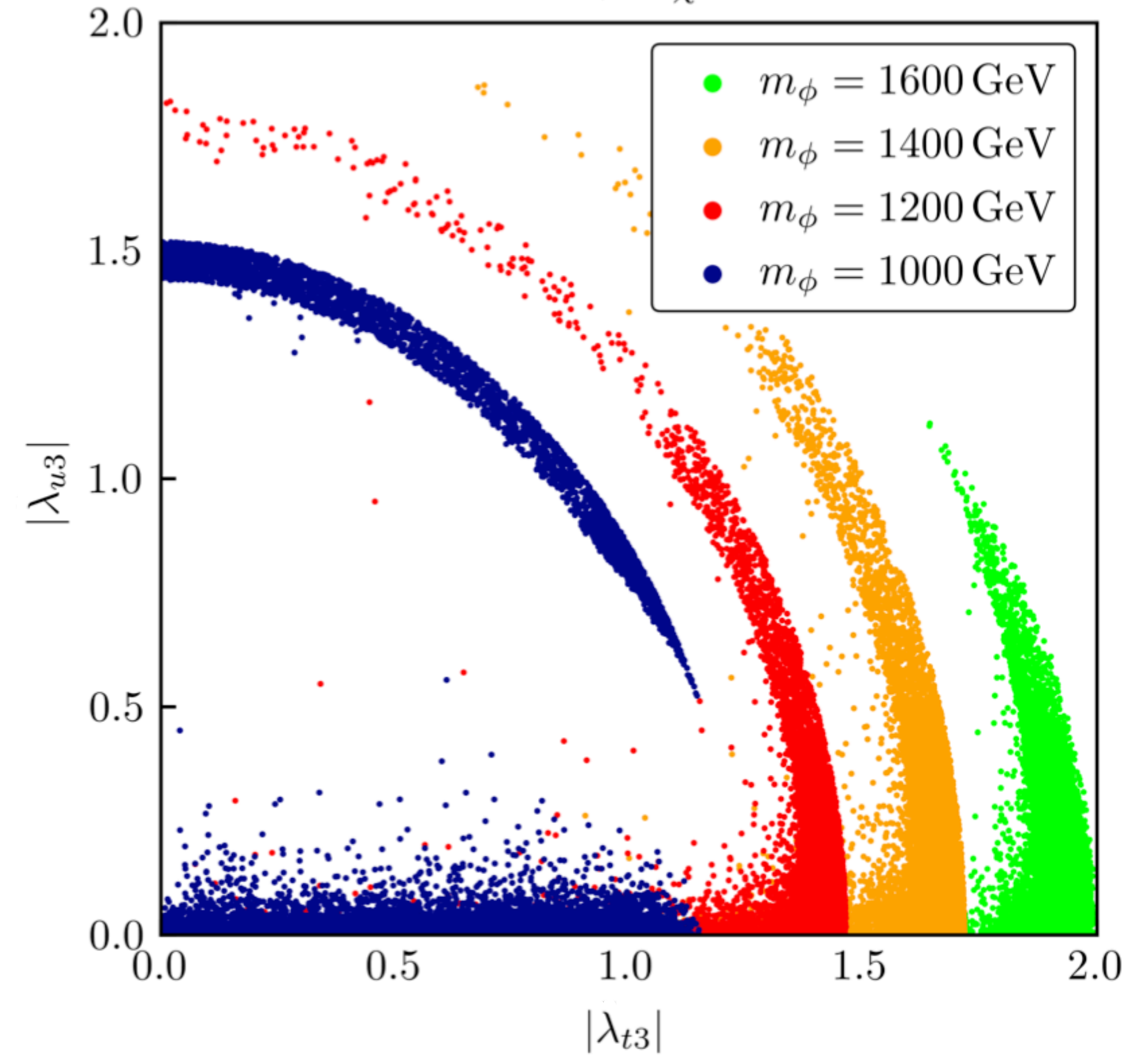


# Combined Analysis

QDF Scenario,  $m_\chi = 350$  GeV



SFF Scenario,  $m_\chi = 350$  GeV



→ DM mostly top-flavoured with larger coupling, flavour and relic abundance constraints dominant

# Outline

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# Freeze-Out with Coannihilations

- Include coannihilations of all  $\chi_i$  and  $\phi$  Edsjö, Gondolo [hep-ph/9704361]
- All particles decay into lightest  $\rightarrow$  abundance can be described with  $n = \sum_i n_i$
- Assuming efficient conversion rates  $\rightarrow$  dark sector in thermal equilibrium  
 $\frac{n_i}{n} \approx \frac{n_i^{\text{eq}}}{n^{\text{eq}}} \rightarrow$  approximation
- One Boltzmann equation (BME) for  $Y = n/s$  and  $x = m_{\chi_3}/T$ :

$$\frac{dY}{dx} = -\frac{1}{3H} \frac{ds}{dx} \langle \sigma_{\text{eff}} v \rangle (Y^2 - Y_{\text{eq}}^2)$$

where

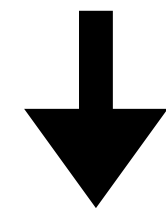
$$\langle \sigma_{\text{eff}} v \rangle = \sum_{ij} \langle \sigma_{ij} v_{ij} \rangle \frac{n_i^{\text{eq}}}{n^{\text{eq}}} \frac{n_j^{\text{eq}}}{n^{\text{eq}}}$$

# Freeze-Out with Coannihilations

- Example:

$$m_{\chi} = 800 \text{ GeV}, m_{\phi} = 816 \text{ GeV},$$

$$\lambda = \begin{pmatrix} 0 & 0 & 1.9 \cdot 10^{-7} \\ 0 & 0.5 & 0 \\ 0.55 & 0 & 0 \end{pmatrix}$$



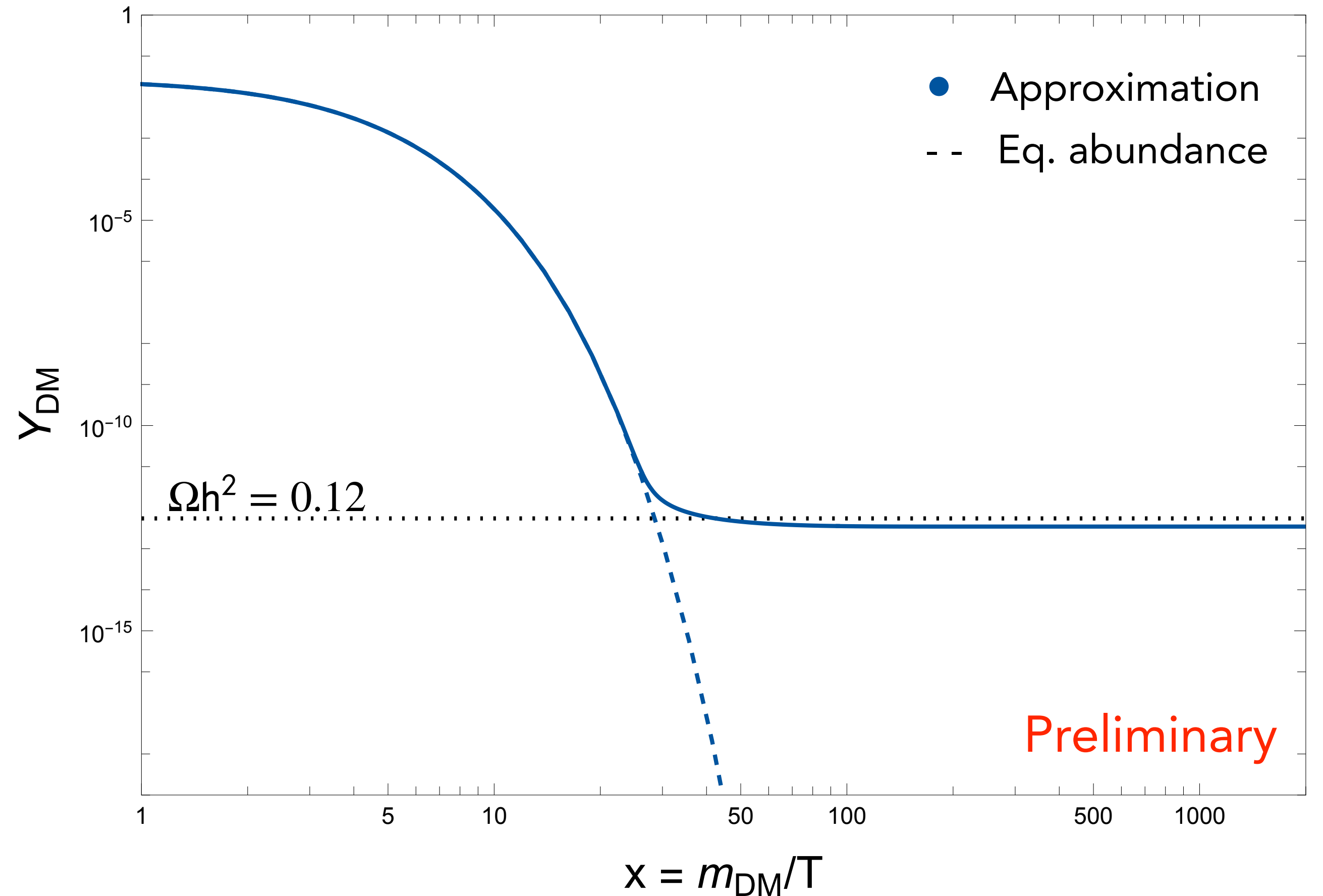
$$m_{\chi_1} = 969 \text{ GeV}, m_{\chi_2} = 940 \text{ GeV},$$

$$m_{\chi_3} = 800 \text{ GeV}$$

- Can be solved by micrOMEGAs (code for calculation of DM properties)

[Bélanger, Boudjema, Pukhov, Semenov]

DM abundance



# Conversion Driven Freeze-Out

- Conversions  $\chi_i \leftrightarrow \chi_j$  or  $\chi_i \leftrightarrow \phi$  can become inefficient during freeze-out when conversion rate  $\Gamma \sim H$
- Chemical equilibrium breaks down  $\rightarrow$  coupled BME of all particles need to be solved

$$\frac{dY_{\chi_i}}{dx} = \frac{1}{3H} \frac{ds}{dx} \left( \langle \sigma_{\chi_i \chi_j} v \rangle (Y_{\chi_i} Y_{\chi_j} - Y_{\chi_i}^{\text{eq}} Y_{\chi_j}^{\text{eq}}) + \frac{\Gamma_{\chi_i \rightarrow \chi_j}}{s} \left( Y_{\chi_i} - Y_{\chi_j} \frac{Y_{\chi_i}^{\text{eq}}}{Y_{\chi_j}^{\text{eq}}} \right) + \langle \sigma_{\phi \chi_i} v \rangle (Y_{\chi_i} Y_{\phi} - Y_{\chi_i}^{\text{eq}} Y_{\phi}^{\text{eq}}) - \frac{\Gamma_{\phi \rightarrow \chi_i}}{s} \left( Y_{\phi} - Y_{\chi_i} \frac{Y_{\phi}^{\text{eq}}}{Y_{\chi_i}^{\text{eq}}} \right) \right)$$

$$\frac{dY_{\phi}}{dx} = \frac{1}{3H} \frac{ds}{dx} \left( \frac{1}{2} \langle \sigma_{\phi \phi} v \rangle (Y_{\phi}^2 - (Y_{\phi}^{\text{eq}})^2) + \langle \sigma_{\phi \chi_i} v \rangle (Y_{\chi_i} Y_{\phi} - Y_{\chi_i}^{\text{eq}} Y_{\phi}^{\text{eq}}) + \frac{\Gamma_{\phi \rightarrow \chi_i}}{s} \left( Y_{\phi} - Y_{\chi_i} \frac{Y_{\phi}^{\text{eq}}}{Y_{\chi_i}^{\text{eq}}} \right) \right)$$

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All coannihilations



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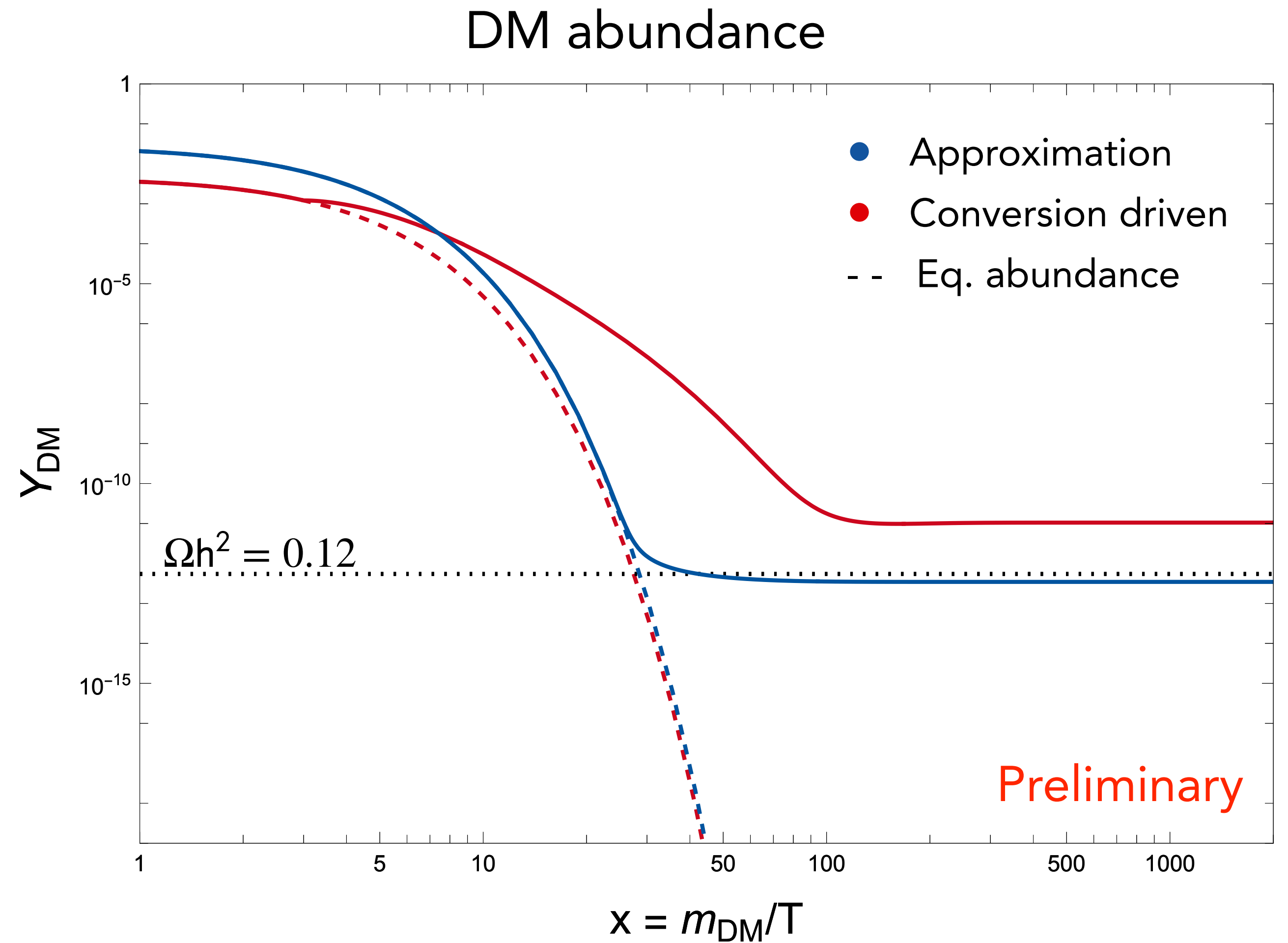
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All conversions including decays

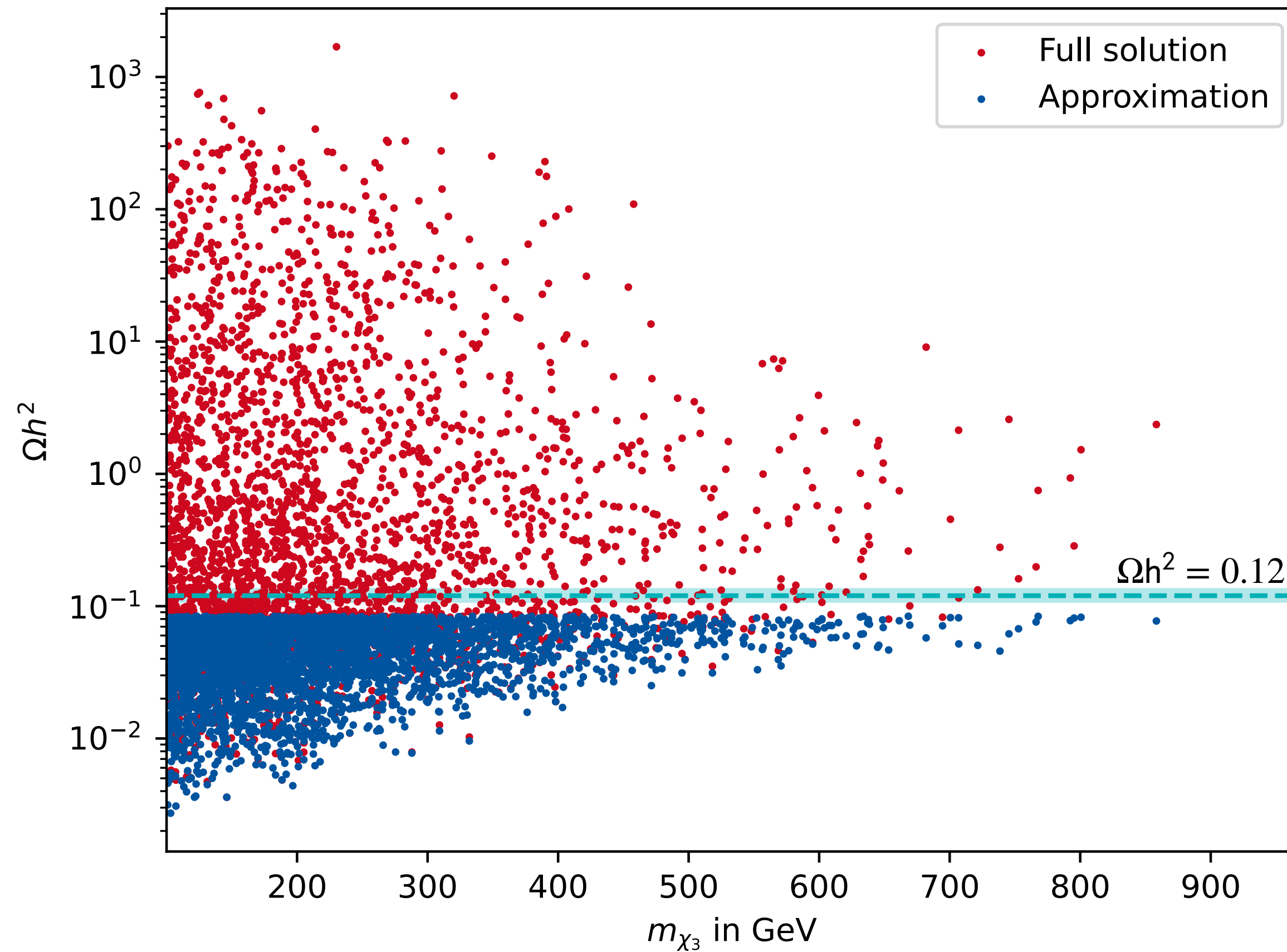
# Conversion Driven Freeze-Out

- Using same parameter values, relic abundance is enhanced significantly as  $\chi_3 \leftrightarrow \phi$  conversions become inefficient
- Requires very small couplings  $\lambda_{t3} = 1.9 \cdot 10^{-7}$
- Cannot be solved by micrOMEGAs out of the box
- Studied in Garny et al. [1705.09292] for one generation  $\chi$  with conversions  $\chi \leftrightarrow \phi$

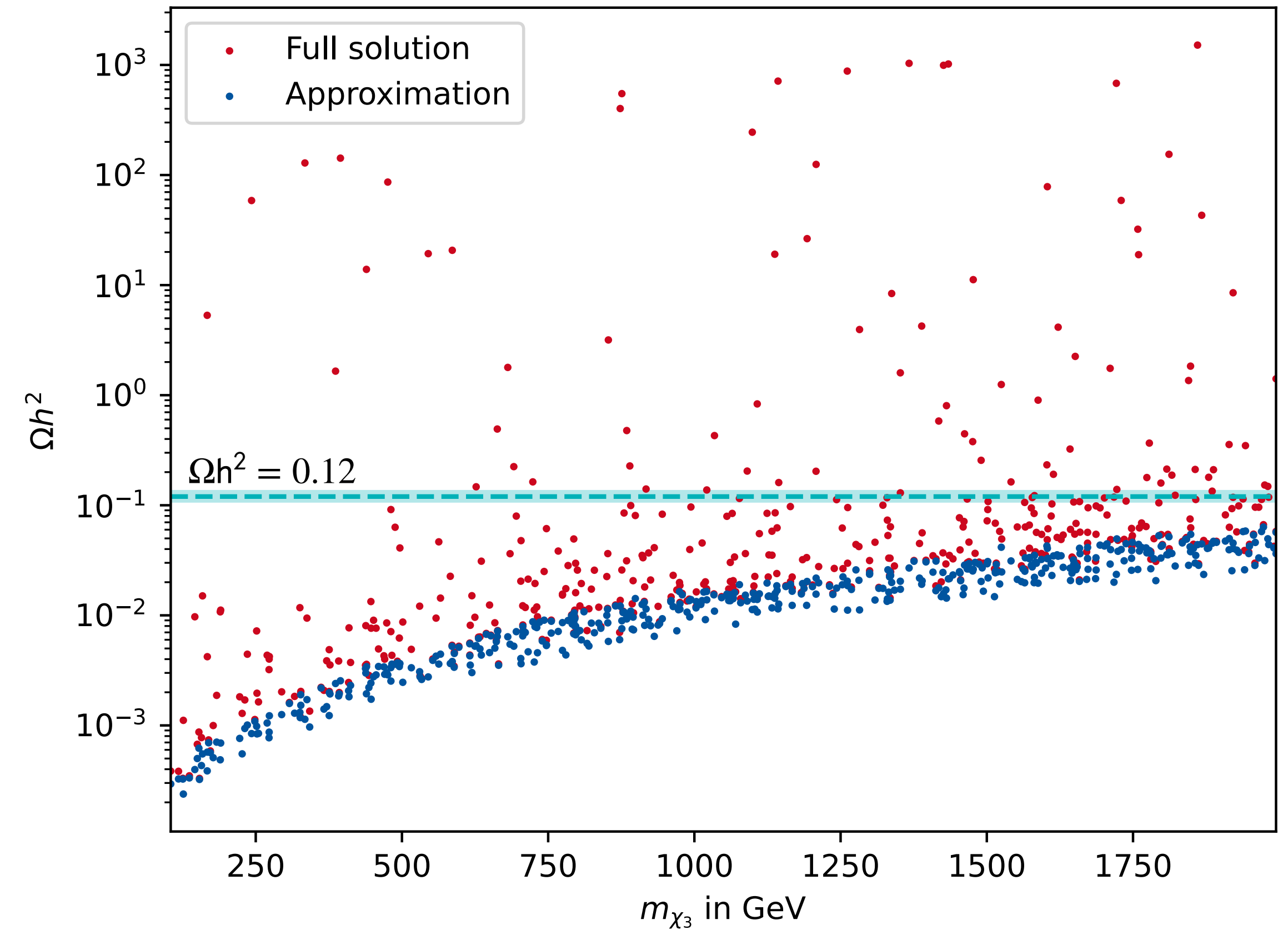


# Parameter Scans

$\chi_2 \leftrightarrow \chi_3$  conversions inefficient,  
 $\chi_3$  couples to up

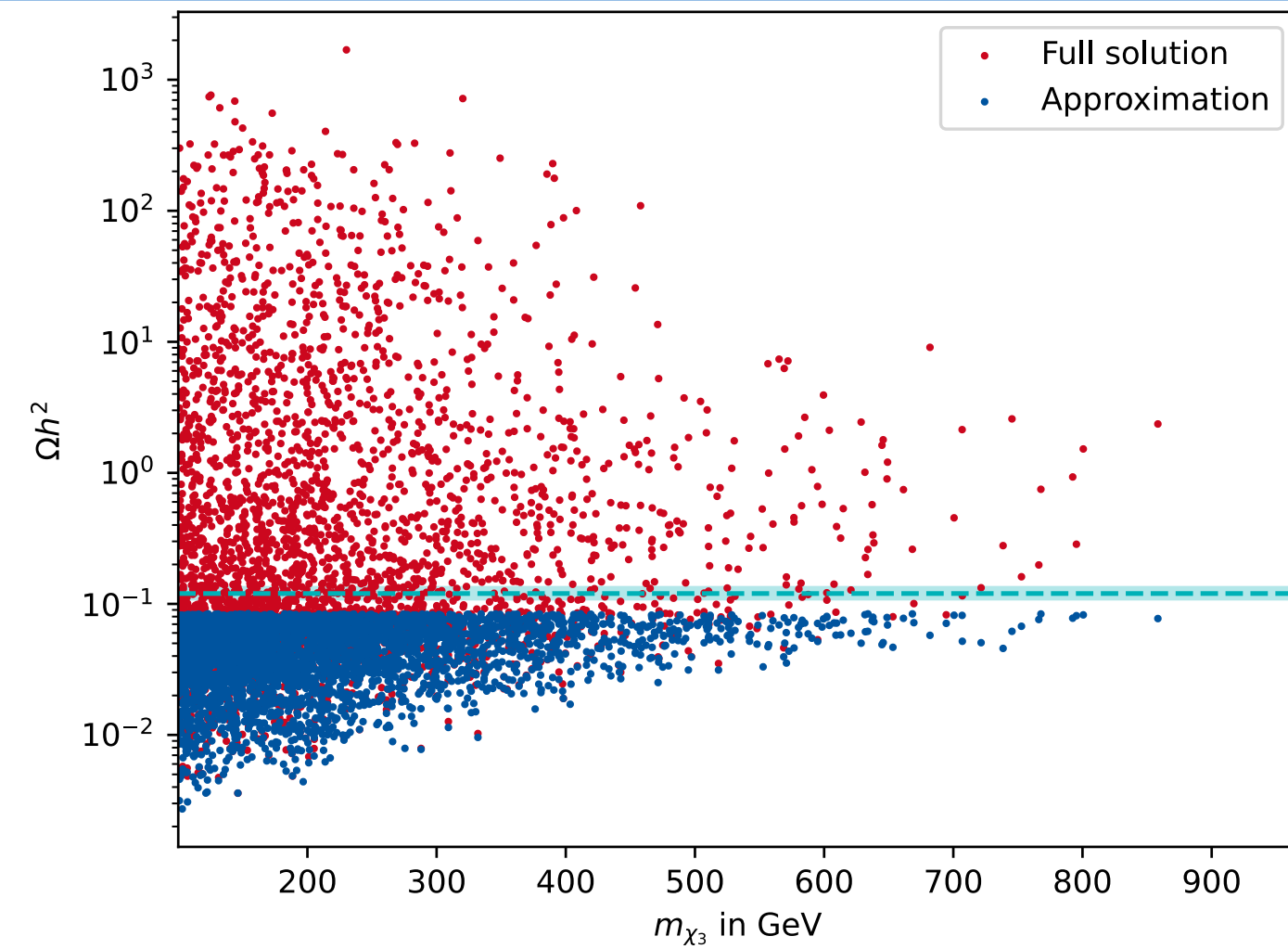


$\phi \leftrightarrow \chi_3$  conversions inefficient,  
 $\chi_3$  couples to up



# Obtaining the Correct Relic Abundance

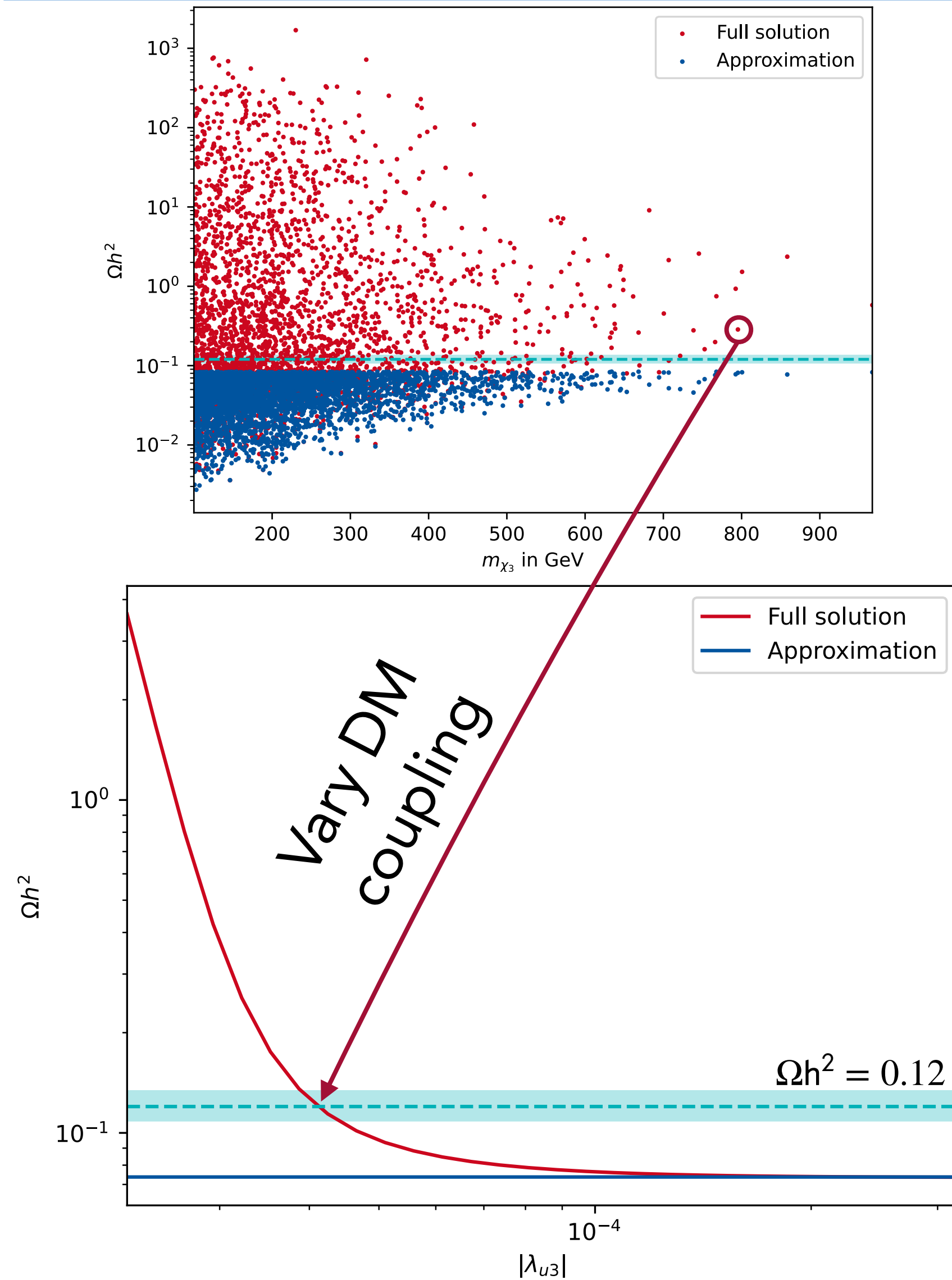
Preliminary



$$\Omega h^2 = 0.12$$

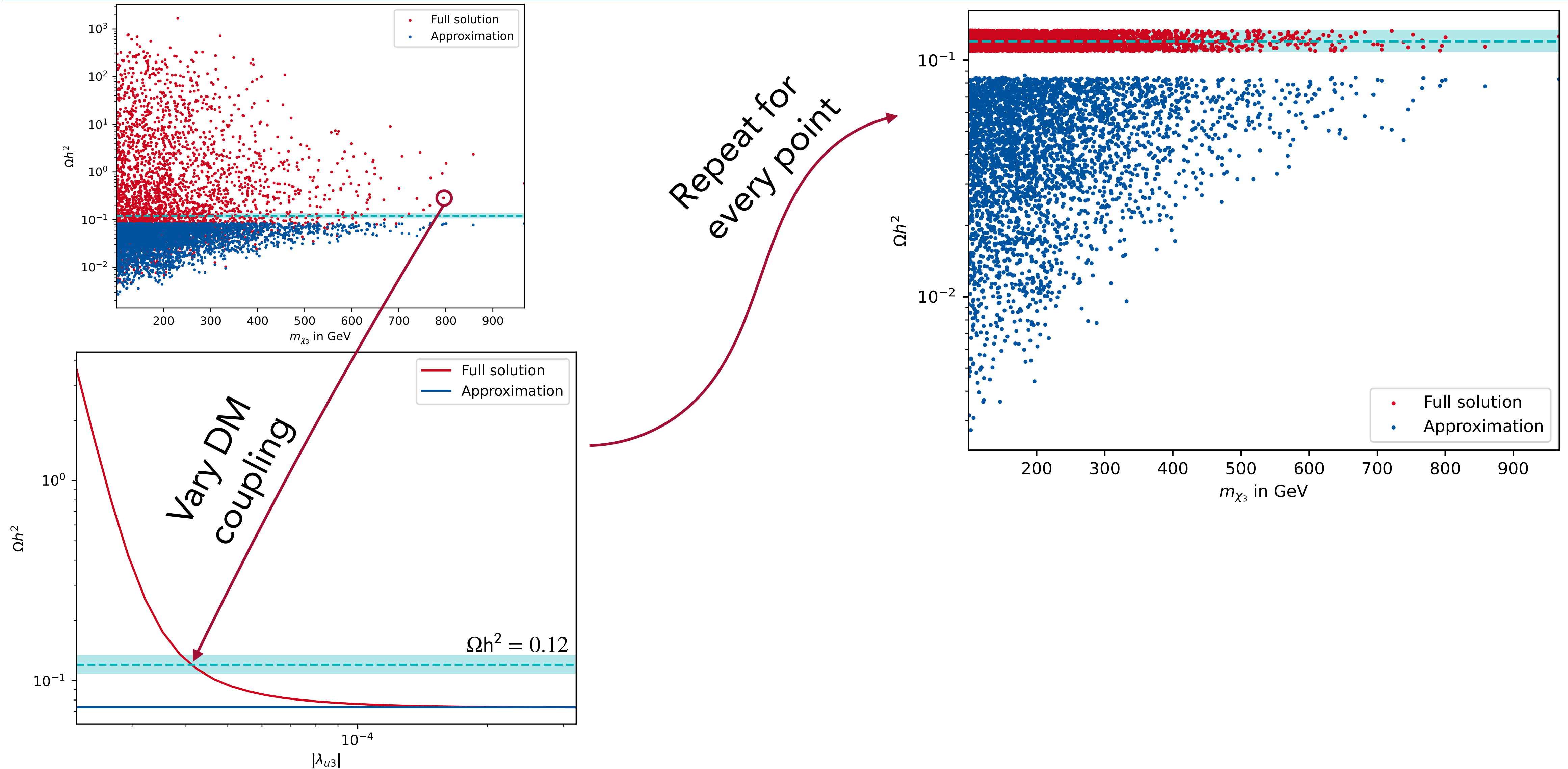
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Preliminary



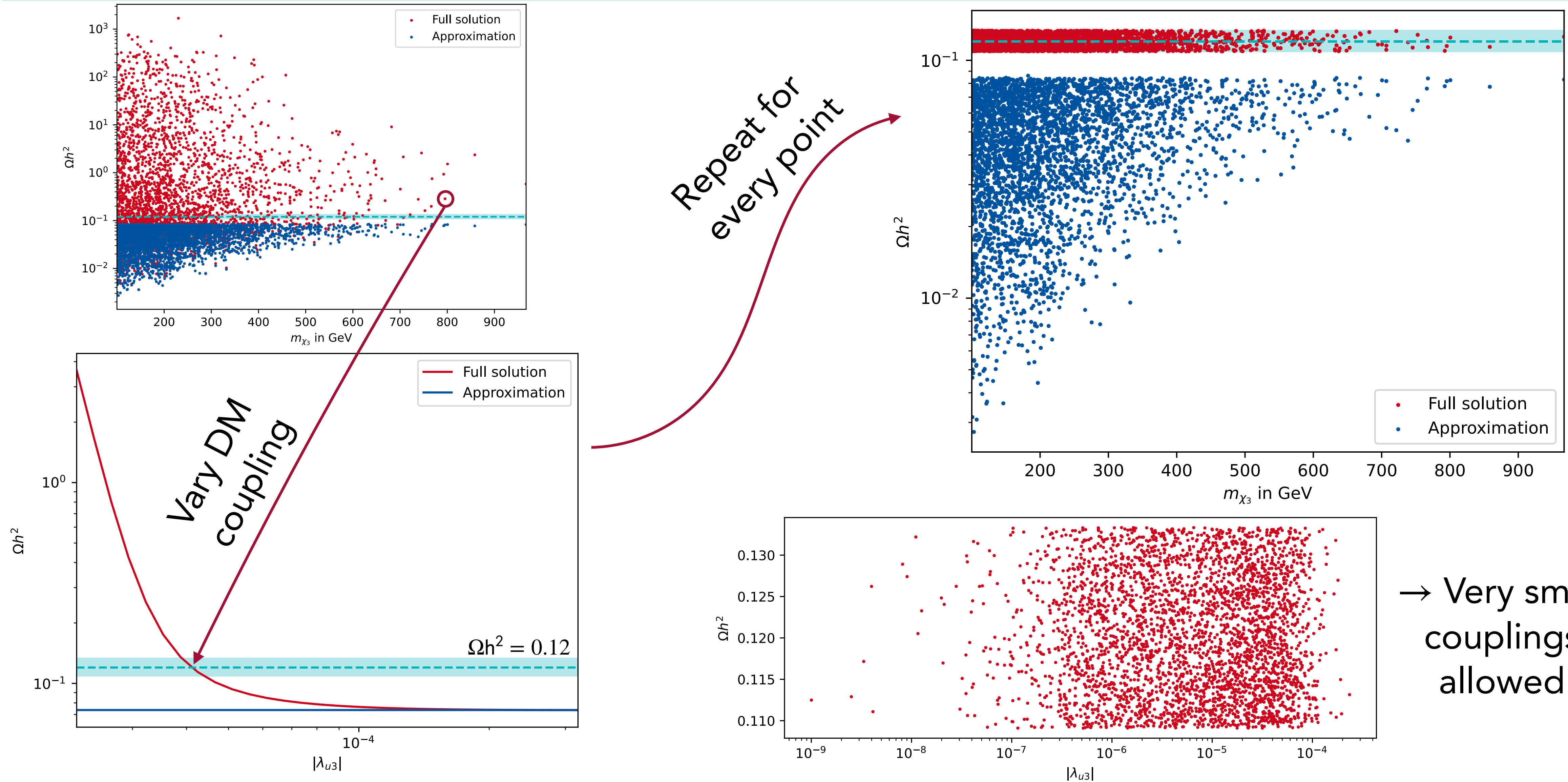
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# Summary and Outlook

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- Flavoured DM models have rich phenomenology
- Combined analysis of QDF and SFF scenario generally compatible with larger DM coupling to tops
- Considering coannihilations and conversion driven freeze-out opens up parameter space
  - very small couplings and up-flavoured DM also allowed
- Outlook: New signatures at LHC



# Summary and Outlook

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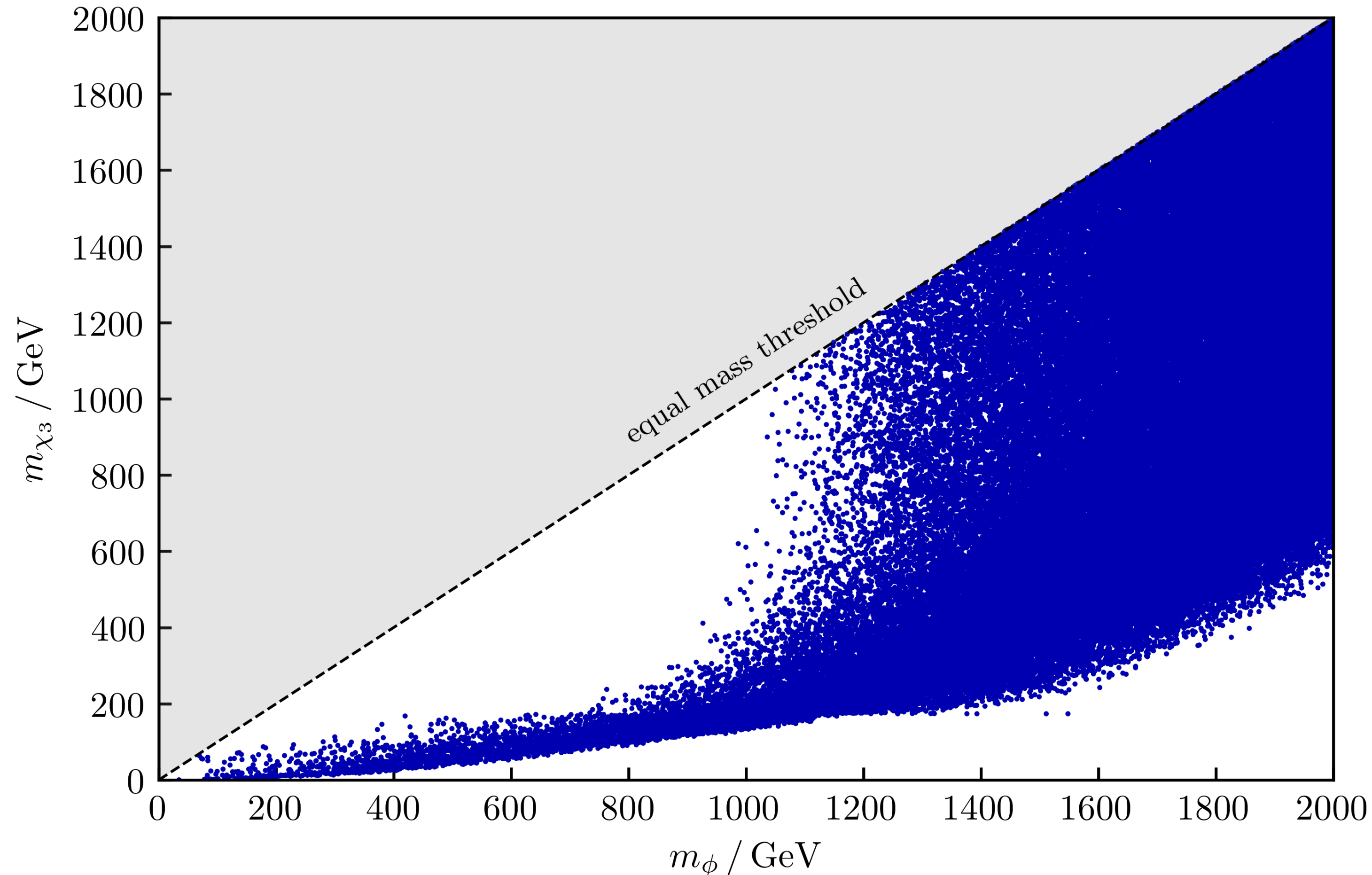
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**Thank you!**

# Backup

# Combined Analysis

Allowed Masses in the SFF Scenario



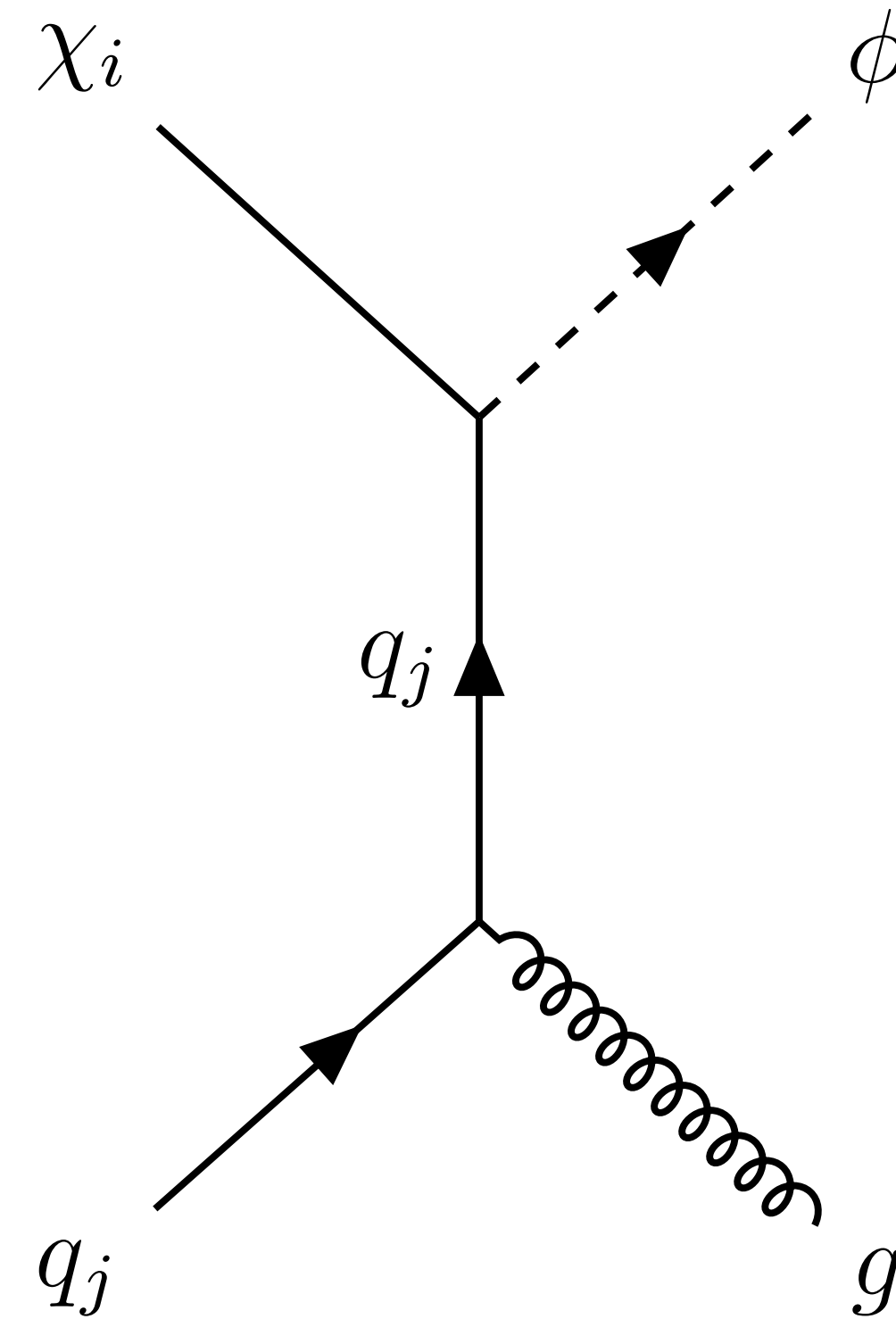
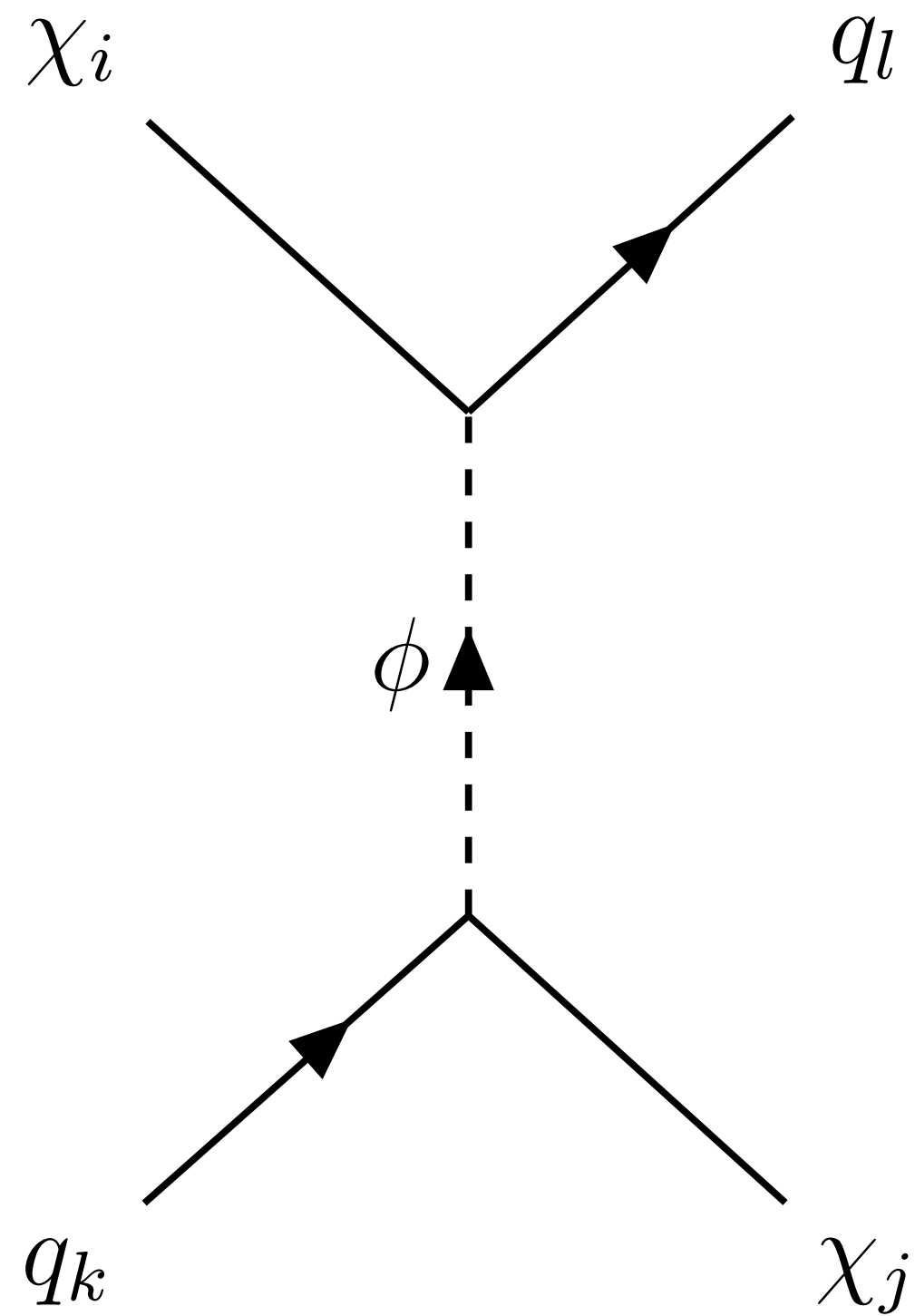
- Upper bound on  $m_{\chi_3}$  in SFF scenario because of large mass splitting vs. small couplings

$$M_{\chi} = m_{\chi} \left( \mathbf{1} + \frac{\eta}{2} (\lambda^{\dagger} \lambda + \lambda^T \lambda^*) \right)$$

- Lower bound on  $m_{\chi_3}$  in SFF and QDF scenario due to upper limit on couplings

# Conversions

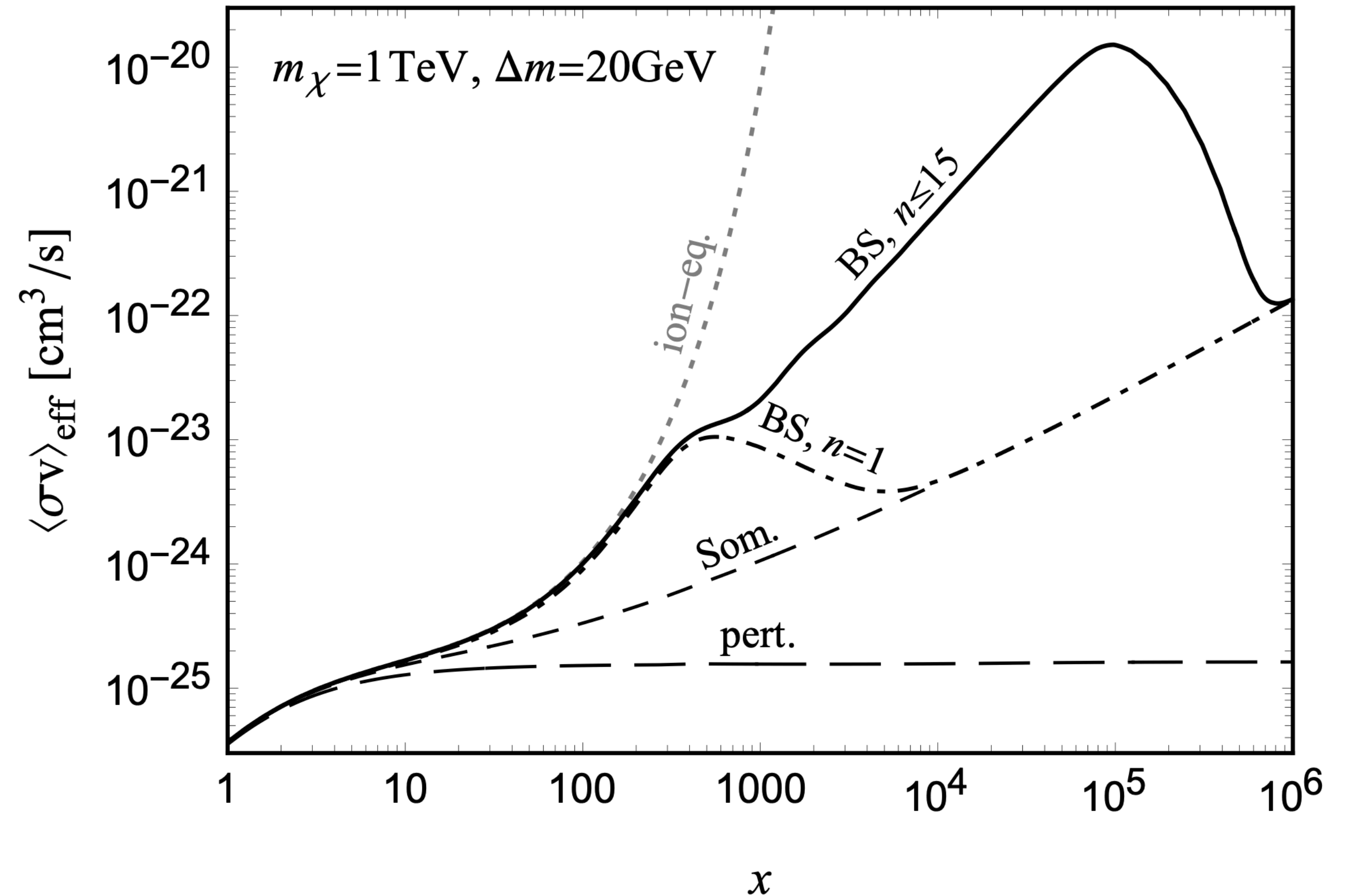
- Examples for conversions  $\chi_i \leftrightarrow \chi_j$  and  $\chi_i \leftrightarrow \phi$



# Sommerfeld Enhancement & Bound State Effects

- Sommerfeld enhancement and bound state effects for Majorana singlet  $\chi$  and scalar mediator

Garny, Heisig [2112.01499]



# Experiments used for analysis

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- LHC: ATLAS and CMS
- Flavour Physics: LHCb
- Direct detection: Limits from spin-dependent scattering from PICO-60 and spin-independent scattering from XENON1T
- CP violation in charm decays: LHCb