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Top-quark pair production with two isolated photons at NLO QCD

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In collaboration with: Malgorzata Worek

Based on [JHEP 08 \(2023\) 179](#)



Collaborative Research Center TRR 257

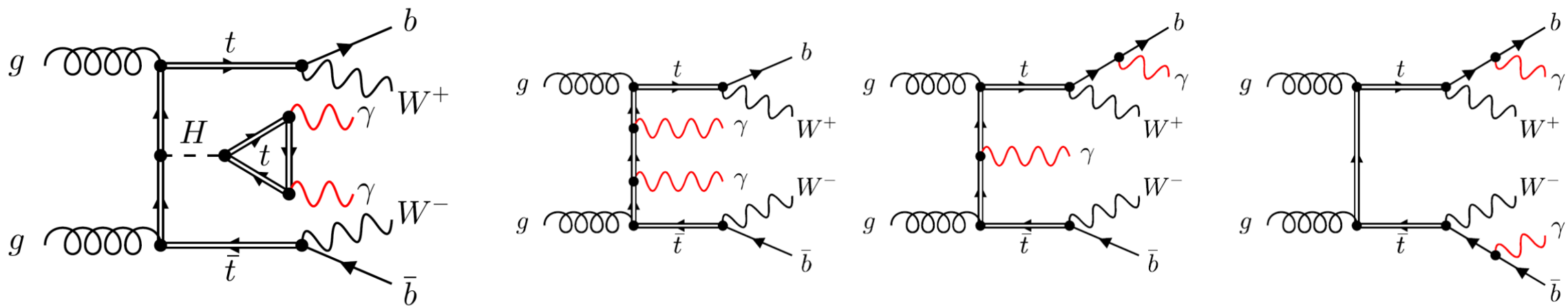
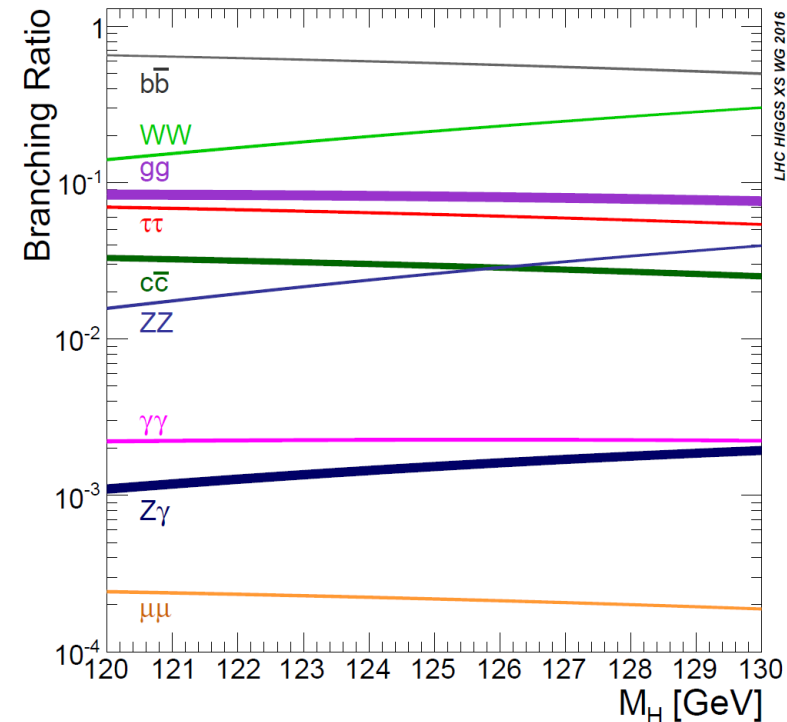


Particle Physics Phenomenology after the Higgs Discovery

Young Scientists Meeting of the CRC TRR 257, Siegen, 17 October 2023

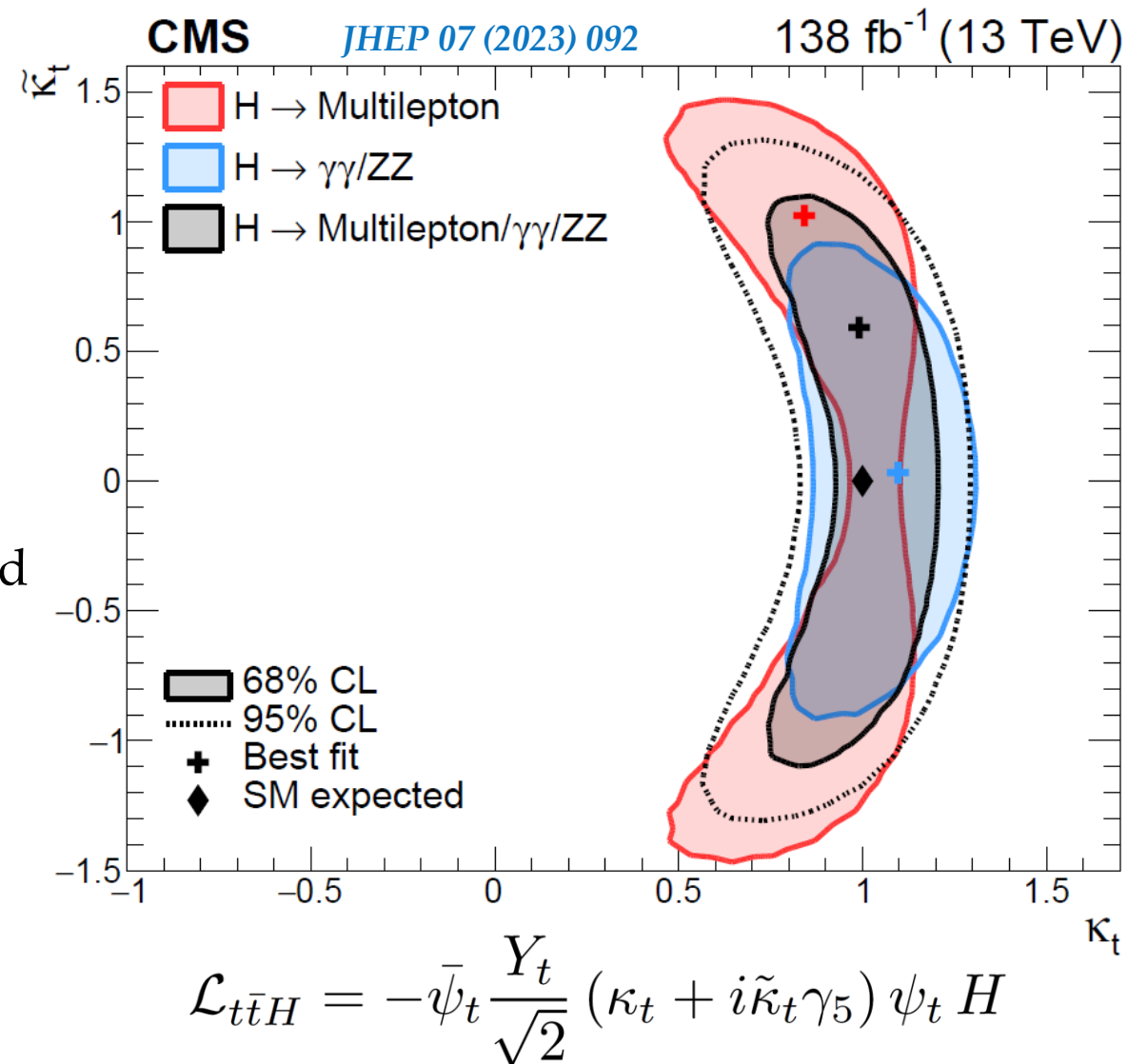
Motivation

- Observation of $pp \rightarrow t\bar{t}H$ in 2018 by ATLAS and CMS
Phys.Lett.B 784 (2018) 173-191
Phys.Rev.Lett. 120 (2018) 23, 231801
- Direct probe of Y_t at tree level
- $H \rightarrow \gamma\gamma$ small branching ratio with $\sim 0.2\%$
- $pp \rightarrow t\bar{t}H(H \rightarrow \gamma\gamma)$ first single-channel observation of $pp \rightarrow t\bar{t}H$
Phys.Rev.Lett. 125 (2020) 6, 061801
Phys.Rev.Lett. 125 (2020) 6, 061802
- Large irreducible background from direct photon production $pp \rightarrow t\bar{t}\gamma\gamma$



Motivation

- In SM: Higgs is CP-even ($\kappa_t = 1, \tilde{\kappa}_t = 0$)
- Pure CP-odd Higgs excluded with 3.9σ (ATLAS, *Phys.Rev.Lett.* 125 (2020) 6, 061802) and 3.7σ (CMS, *JHEP* 07 (2023) 092)
- Possible admixture between CP-even and CP-odd coupling
- Deviations from SM prediction can be interpreted in context of BSM:
 - Extended Higgs sector
 - 2HDM
 - ...



Theory status ($t\bar{t}\gamma\gamma$)

State of the art: **NLO QCD+EW**

- Stable top quarks at NLO QCD

- $pp \rightarrow t\bar{t}\gamma\gamma$

*Alwall, Frederix, Frixione, Hirschi,
Maltoni, Mattelaer, Shao, Stelzer,
Torrielli, Zaro '14
Maltoni, Pagani, Tsinikos '16*

- $pp \rightarrow t\bar{t}\gamma\gamma$ (NLO QCD+EW)

Pagani, Shao, Tsinikos, Zaro '21

- Matched to Parton Showers at NLO QCD

- POWHEL/POWHEG

Kardos, Trócsányi '15

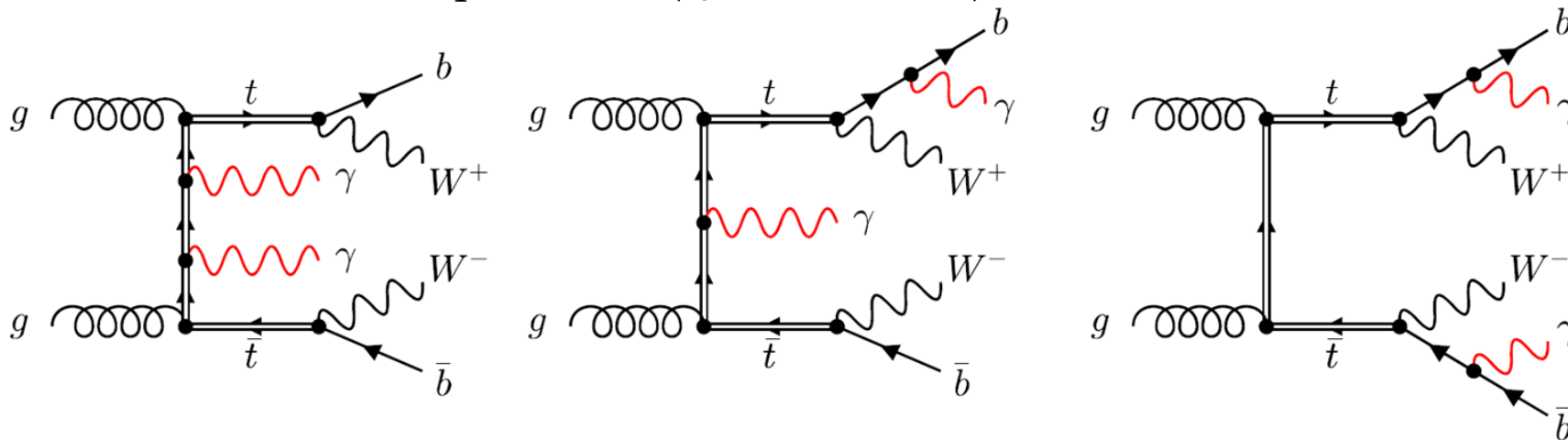
- MC@NLO

van Deurzen, Frederix, Hirschi, Luisoni, Mastrolia '16

Setup

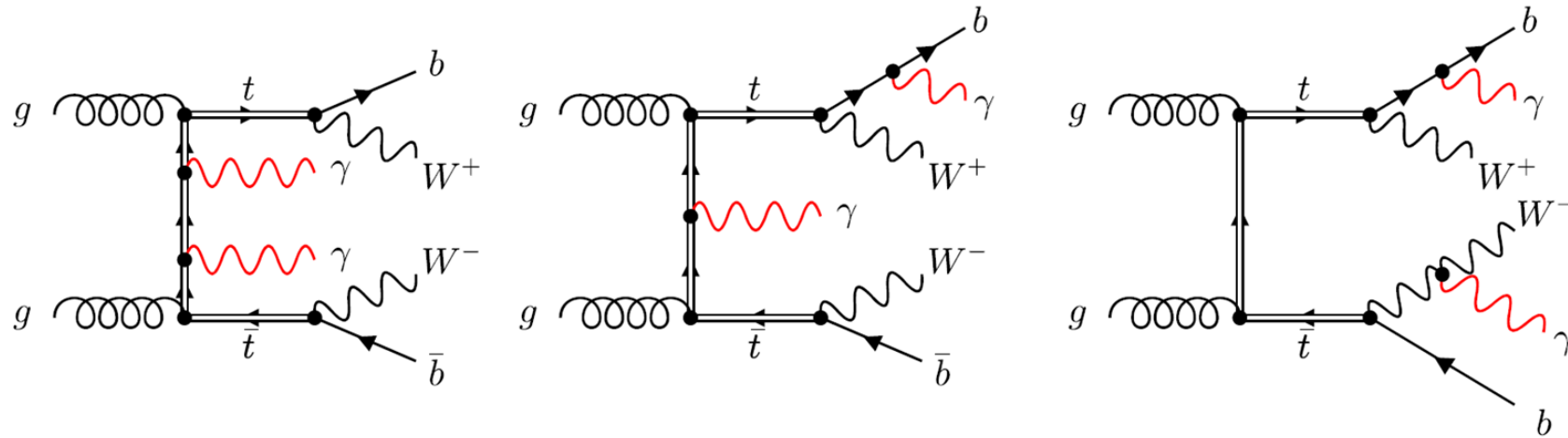
$$pp \rightarrow t\bar{t}(\gamma\gamma) \rightarrow W^+W^-b\bar{b}(\gamma\gamma) \rightarrow \begin{cases} l^+l^- \nu_e\bar{\nu}_e b\bar{b} \gamma\gamma \\ l^-\bar{\nu}_e jj b\bar{b} \gamma\gamma \end{cases} \quad l^\pm = e^\pm, \mu^\pm$$

- LHC with $\sqrt{s} = 13$ TeV
- Calculation performed in [Narrow Width Approximation](#) preserving spin correlations
- [Photon bremsstrahlung](#) and [NLO QCD](#) corrections included in $t\bar{t}$ production and decay
- Diagonal CKM matrix
- 5 flavour scheme ($m_b = 0$)
- Top-quark width treated as fixed parameter ($\Gamma_t^{NLO}(\mu_R = m_t)$)



Process definition

$$d\sigma_{t\bar{t}\gamma\gamma}^{\text{LO}} = \Gamma_t^{-2} \left(\underbrace{d\sigma_{t\bar{t}\gamma\gamma}^{\text{LO}} d\Gamma_{t\bar{t}}^{\text{LO}}}_{\text{Prod.}} + \underbrace{d\sigma_{t\bar{t}\gamma}^{\text{LO}} d\Gamma_{t\bar{t}\gamma}^{\text{LO}}}_{\text{Mixed}} + \underbrace{d\sigma_{t\bar{t}}^{\text{LO}} d\Gamma_{t\bar{t}\gamma\gamma}^{\text{LO}}}_{\text{Decay}} \right)$$



- Full calculation divided into three resonant contributions: **Prod.**, **Mixed** and **Decay**
- NLO QCD corrections calculated for each resonant structure separately

Computational framework

Virtual Corrections

- *Recola* (Actis, Denner, Hofer, Lang, Scharf, Uccirati '17) + *Collier* (Denner, Hofer, Dittmaier, Hofer '17)
- Cross-checked with *HELAC-1LOOP* (van Hameren, Papadopoulos, Pittau '09) with *CutTools* (Ossola, Papadopoulos, Pittau '09) and *OneLOop* (van Hameren '11)

Real Corrections in Helac-Dipoles

- Nagy-Soper subtraction *Bevilacqua, Czakon, Kubocz, Worek '13*
 - Extended to radiative decays
- Cross-checked with Catani-Seymour subtraction *Catani, Seymour '97* *Catani, Dittmaier, Seymour, Trocsanyi '02*
- Theoretical prediction are stored in modified *Les Houches Event Files (LHEFs)* *Bern, Dixon, Febres Cordero, Hoeche, Ita, Kosower, Maitre '14*
- Reweighting to different renormalisation/factorisation scales and PDF sets

Setup of the calculation

- G_μ scheme: $\alpha = \frac{\sqrt{2}}{\pi} G_\mu M_W^2 \left(1 - \frac{M_W^2}{M_Z^2}\right)$
- External photon radiation with $\alpha^{-1} = \alpha^{-1}(0) = 137.035999084$
- Renormalisation/Factorisation scale: $\mu_R = \mu_F = \mu_0 = \frac{E_T}{4}$ $E_T = \sqrt{m_t^2 + p_{T,t}^2} + \sqrt{m_t^2 + p_{T,\bar{t}}^2} + p_{T,\gamma_1} + p_{T,\gamma_2}$
- NNPDF3.1 NLO PDF set with $\alpha_s(M_Z) = 0.118$ *Ball et. al. '17*

- Smooth photon isolation prescription *Frixione '98*

$$\sum_i E_{T_i} \Theta(R - R_{\gamma i}) \leq \epsilon_\gamma E_{T_\gamma} \left(\frac{1 - \cos(R)}{1 - \cos(R_{\gamma j})} \right)^n \quad \text{for all } R \leq R_{\gamma j}$$

- with $R_{\gamma j} = 0.4$ and $\epsilon_\gamma = n = 1$
- Anti- k_T jet algorithm ($R = 0.4$) *Cacciari, Salam, Soyez '08*

Integrated Fiducial cross section in di-lepton channel

$$pp \rightarrow t\bar{t}(\gamma\gamma) \rightarrow W^+W^-b\bar{b}(\gamma\gamma) \rightarrow \ell^+\ell^-\nu_e\bar{\nu}_e b\bar{b}\gamma\gamma$$

μ_0		LO	NLO	$\mathcal{K} = \sigma_{\text{NLO}}/\sigma_{\text{LO}}$
	σ_{Full} [fb]	0.13868(3) ^{+31.2%} _{-22.1%}	0.1773(1) ^{+1.8%} _{-6.2%}	1.28
$E_T/4$	$\sigma_{\text{Prod.}}$ [fb]	0.05399(2) ^{+30.6%} _{-21.7%}	0.07130(6) ^{+2.5%} _{-7.2%}	1.32
	σ_{Mixed} [fb]	0.06022(2) ^{+31.9%} _{-22.5%}	0.07733(8) ^{+1.5%} _{-6.2%}	1.28
	σ_{Decay} [fb]	0.024473(7) ^{+30.9%} _{-22.1%}	0.02863(4) ^{+0.9%} _{-4.9%}	1.17

Stremmer, Worek '23

- NLO QCD corrections $\sim 30\%$
- Scale uncertainties reduced from 31% to 6%
- Relative size to Full: Prod. (40%), Mixed (44%) and Decay (16%)
- Internal PDF uncertainties: NNPDF3.1 1.0%, MSHT20 1.4%, CT18 2.0%

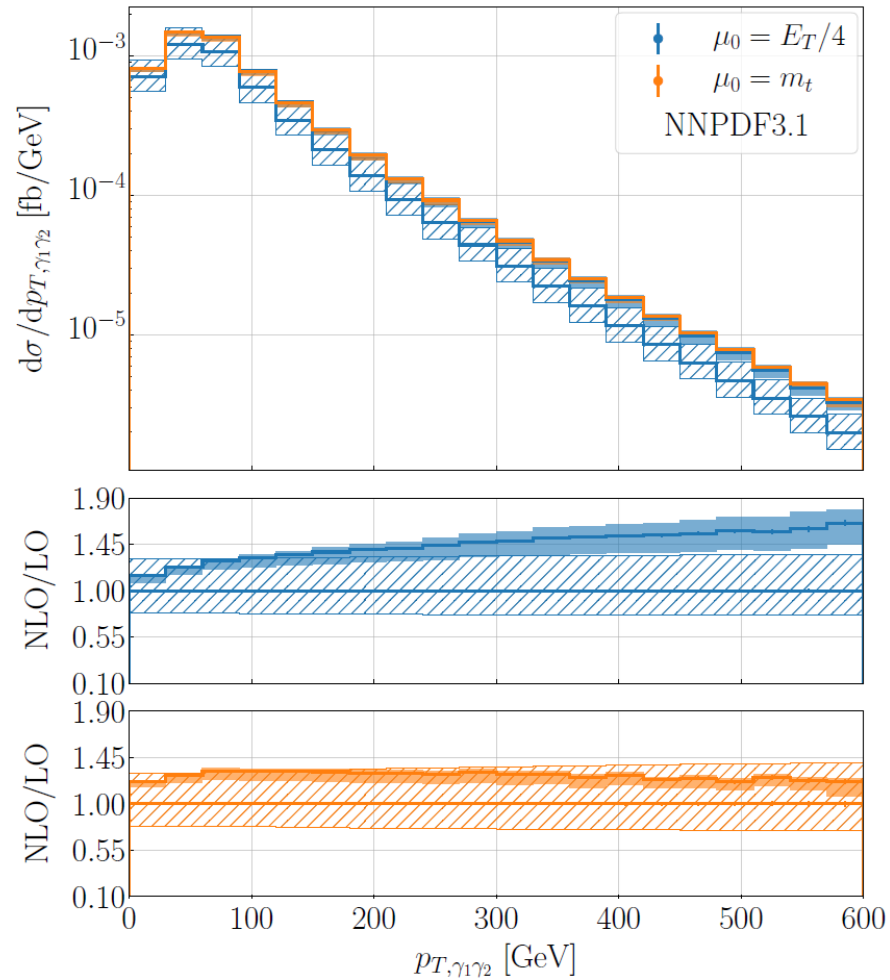
Resonant contributions

		gg	gg/pp	$q\bar{q}$	$q\bar{q}/pp$	$qg + \bar{q}g$	$(qg + \bar{q}g)/pp$
$\sigma_{\text{Full}}^{\text{NLO}}$	[fb]	0.0999(1)	56.4%	0.04307(4)	24.3%	0.03428(4)	19.3%
$\sigma_{\text{Prod.}}^{\text{NLO}}$	[fb]	0.02587(4)	36.3%	0.02672(4)	37.5%	0.01871(3)	26.2%
$\sigma_{\text{Mixed}}^{\text{NLO}}$	[fb]	0.04928(8)	63.7%	0.01408(2)	18.2%	0.01398(2)	18.1%
$\sigma_{\text{Decay}}^{\text{NLO}}$	[fb]	0.02476(4)	86.5%	0.002268(3)	7.9%	0.00160(2)	5.6%

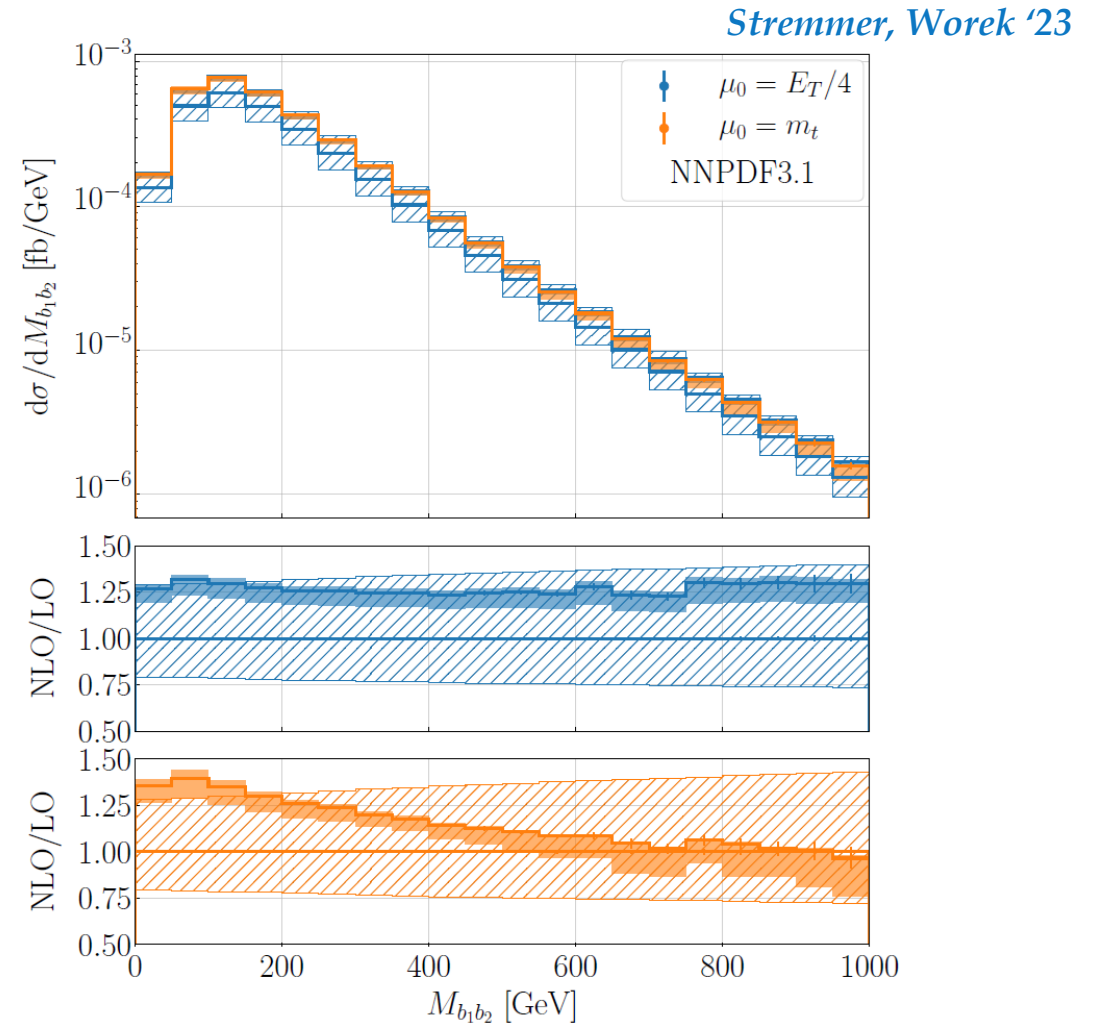
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- Full dominated by gg with 56.4%
- $q\bar{q}$ channel decreases, gg channel increases in absolute size from Prod. to Mixed
- gg channel suppressed for increasing number of photons in $t\bar{t}$ production
- Conclusions also hold in lepton + jet top-quark decay channel

Differential Fiducial cross section



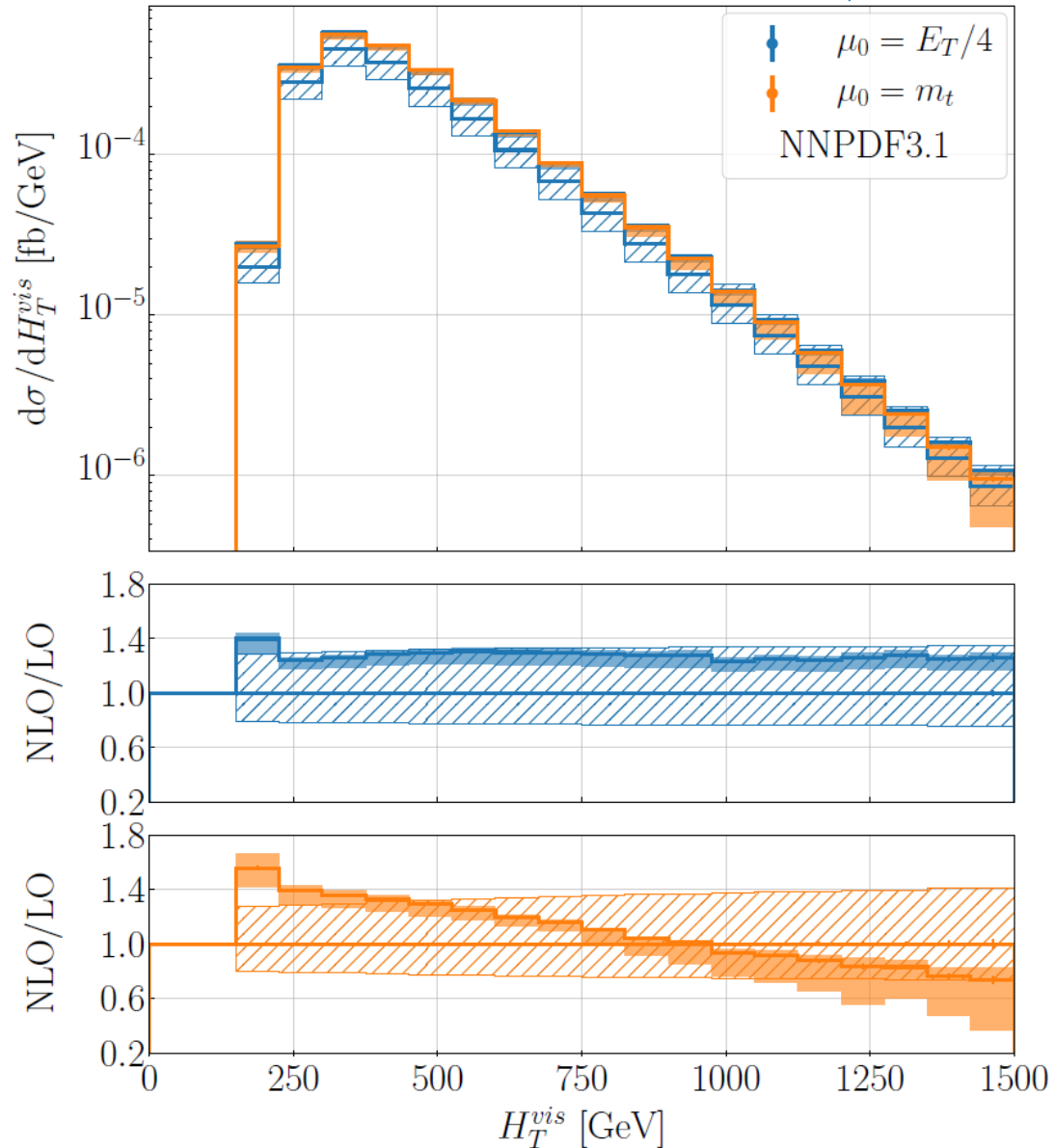
- NLO QCD corrections up to 65%
- Smaller corrections for $\mu_0 = m_t$
- Scale uncertainties 5% – 13%



- NLO QCD corrections ~25% – 30%
- Scale uncertainties reduced from ~35% to 5% – 8%
- Increasing scale uncertainties in tails for $\mu_0 = m_t$

Differential Fiducial cross section

Stremmer, Worek '23



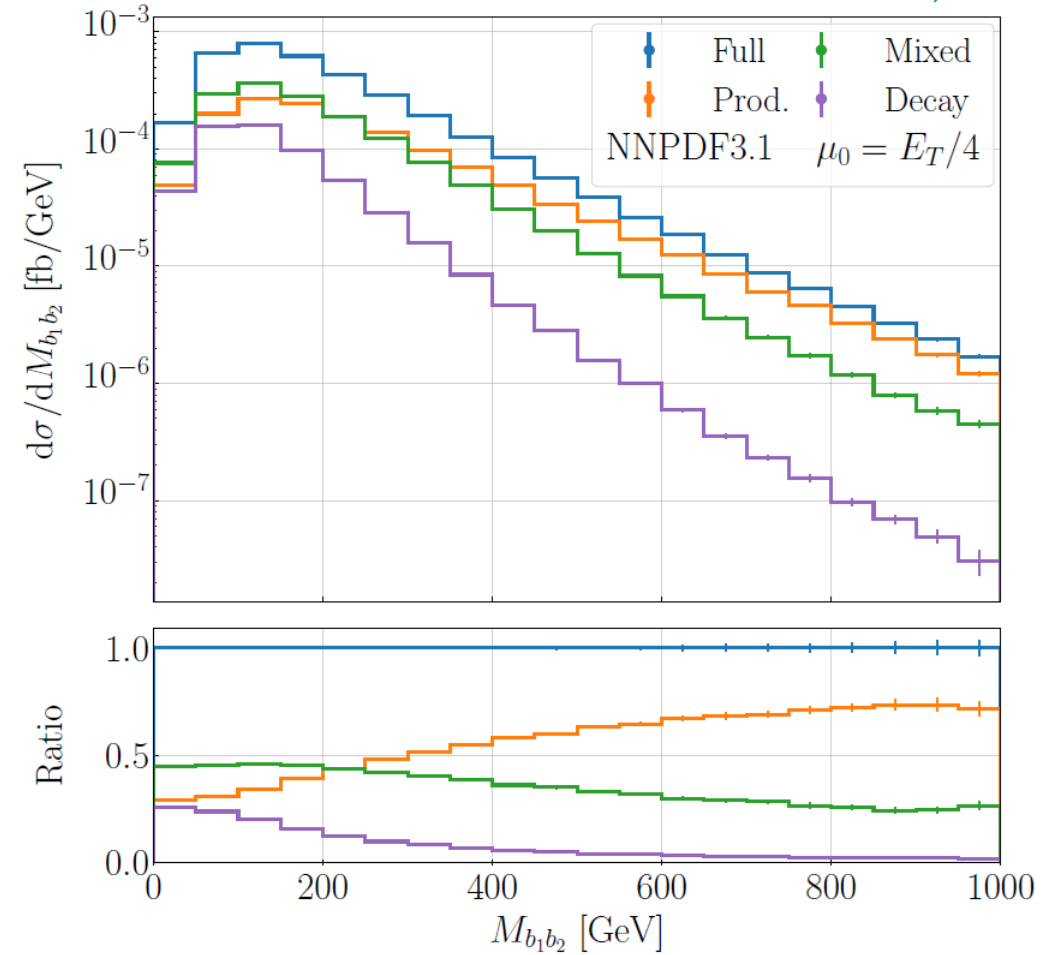
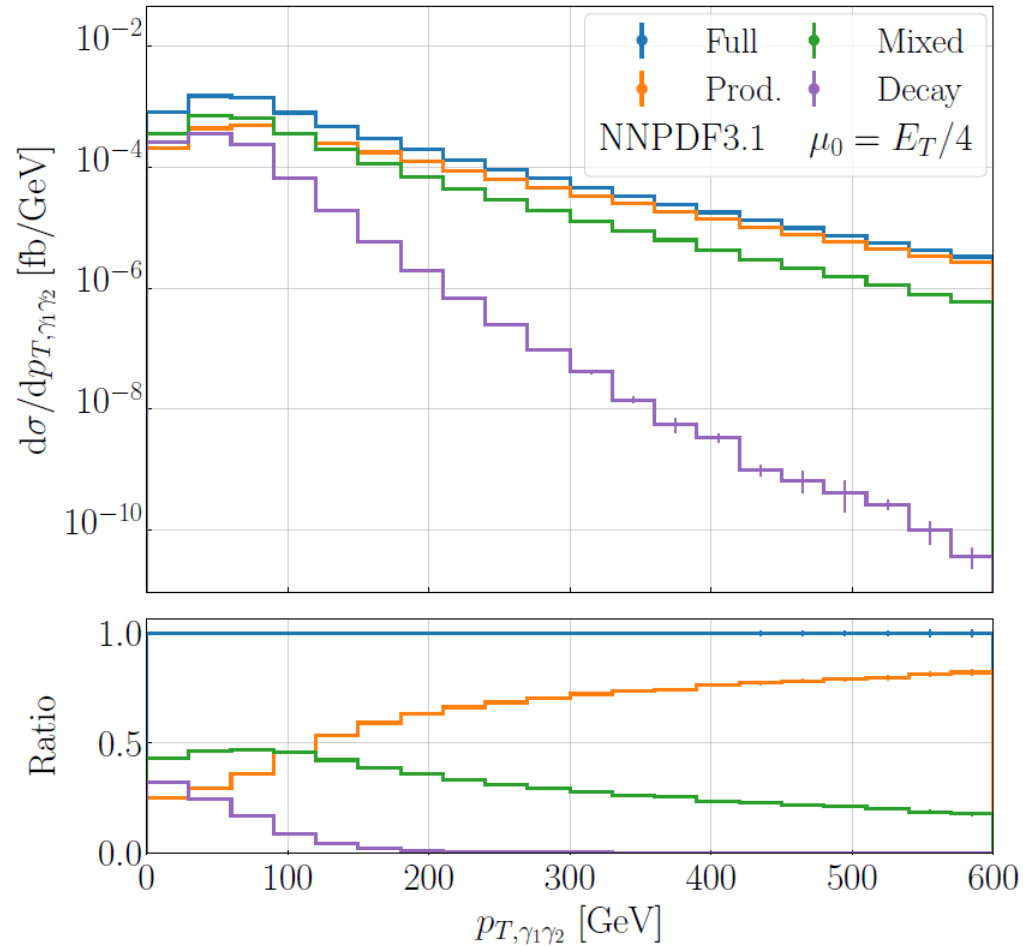
$$H_T^{vis} = p_{T,\ell^+} + p_{T,\ell^-} + p_{T,b_1} + p_{T,b_2} + p_{T,\gamma_1} + p_{T,\gamma_2}$$

- Fixed scale unstable for general dimensionful observables:
 - Large shape distortions
 - NLO scale uncertainties, up to 50%, exceeding LO ones

→ Dynamical scale in general required

Resonant contribution

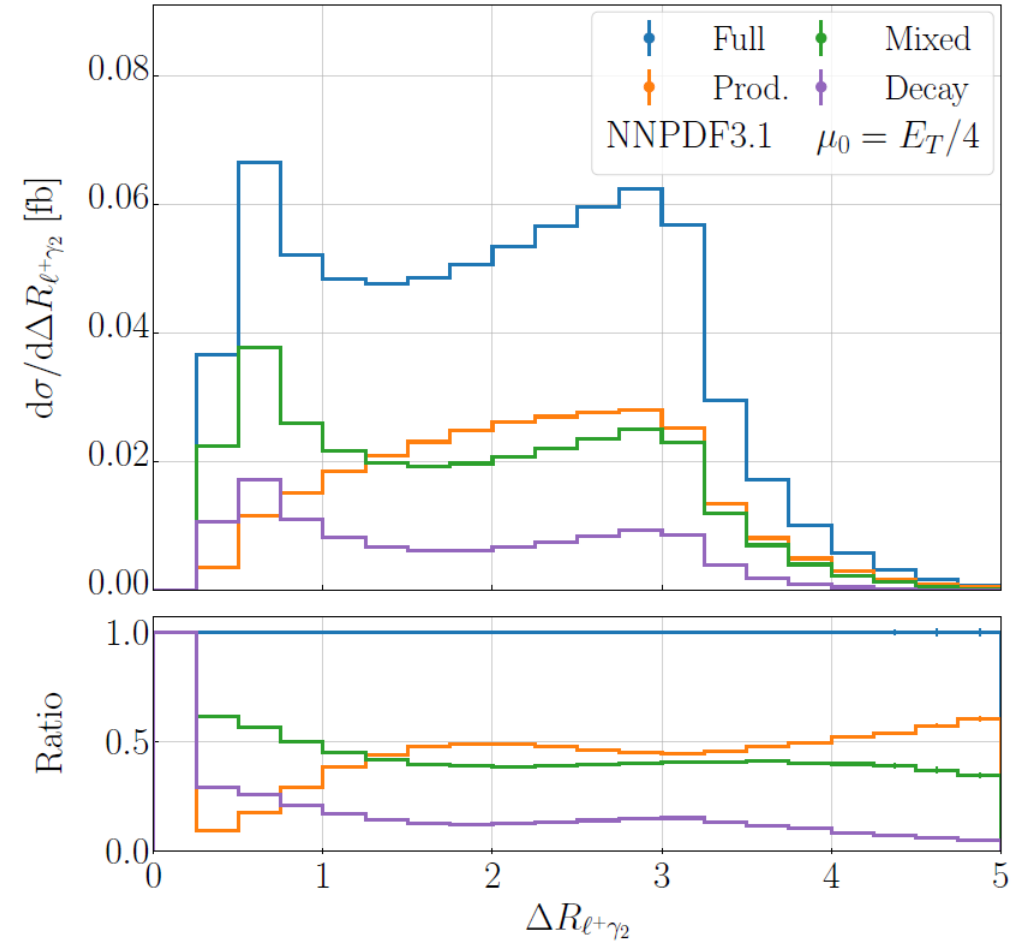
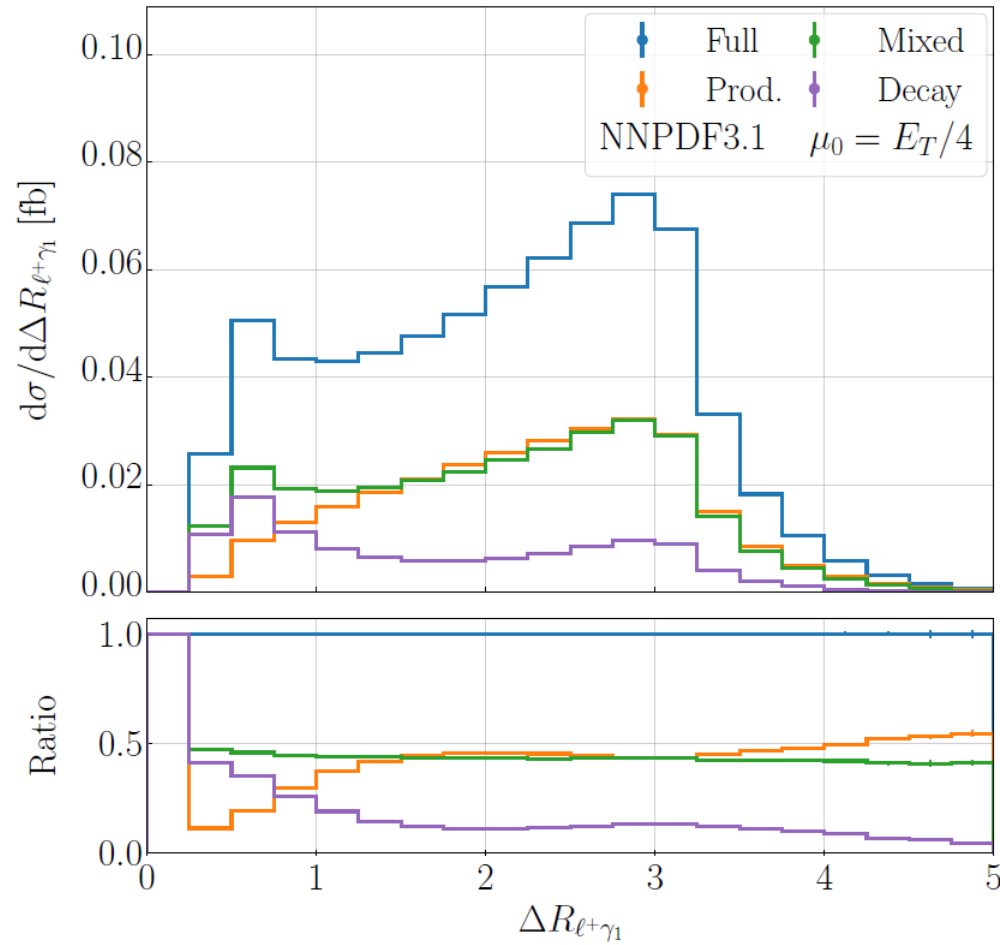
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- Large contributions from photon emission in decays in bulk of distribution
- Tails dominated by **Prod.** (79 – 82% of **Full**)
- **Decay** less suppressed in tails of non-photonic observables

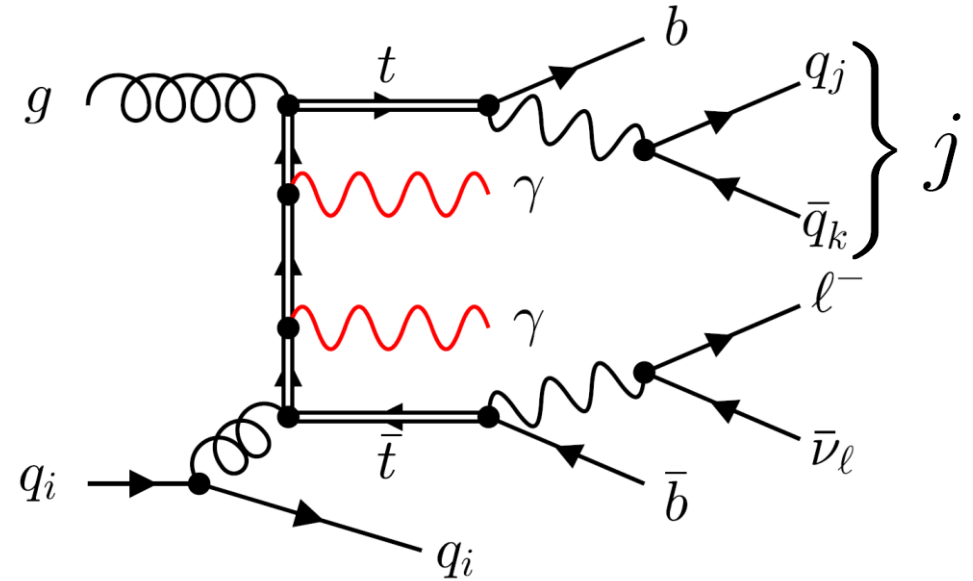
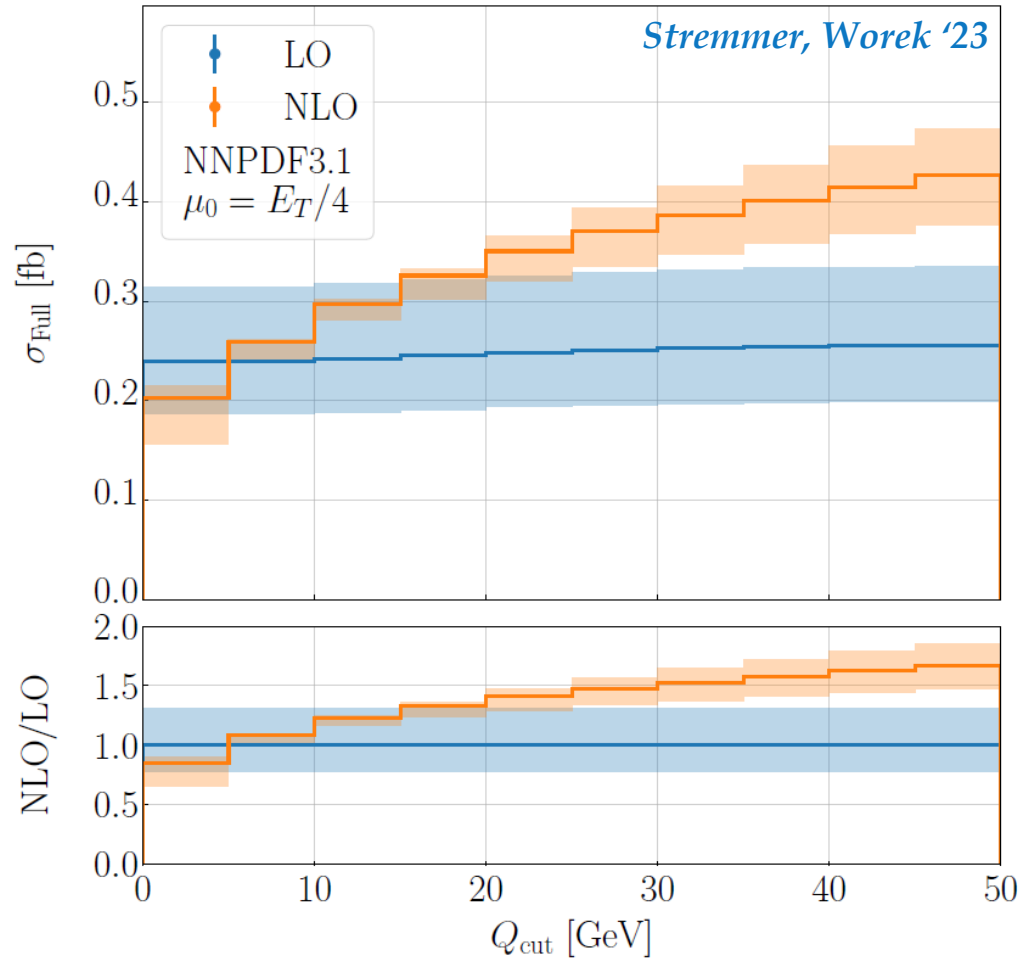
Resonant contribution

Stremmer, Worek '23



- Different peak structures for **Prod.**, **Mixed** and **Decay**
- Only sum leads to reliable predictions

Integrated Fiducial cross section in lepton + jet channel



- Large NLO QCD corrections of $\sim 140\%$ for $Q_{\text{cut}} \rightarrow \infty$ caused by hard radiation in production stage
- NLO QCD corrections drastically reduced by additional $|m_W - M_{jj}| < Q_{\text{cut}}$

Integrated Fiducial cross section in lepton + jet channel

$$|m_W - M_{jj}| < 15 \text{ GeV}$$

μ_0		LO	NLO	$\mathcal{K} = \sigma_{\text{NLO}}/\sigma_{\text{LO}}$
$E_T/4$	σ_{Full} [fb]	$0.24214(4)^{+31.1\%}_{-22.0\%}$	$0.2973(3)^{+1.9\%}_{-5.4\%}$	1.23
	$\sigma_{\text{Prod.}}$ [fb]	$0.11960(3)^{+30.5\%}_{-21.6\%}$	$0.1405(2)^{+2.1\%}_{-4.6\%}$	1.17
	σ_{Mixed} [fb]	$0.09632(3)^{+31.9\%}_{-22.5\%}$	$0.1205(2)^{+1.5\%}_{-5.7\%}$	1.25
	σ_{Decay} [fb]	$0.026230(9)^{+30.9\%}_{-22.1\%}$	$0.03629(7)^{+3.3\%}_{-7.7\%}$	1.38

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- NLO corrections $\sim 23\%$, scale uncertainties reduced from $\sim 31\%$ to $\sim 5\%$
- **Prod.** increased from 40% (**di-lepton**) to 48% (**lepton + jet**) because of by additional cut

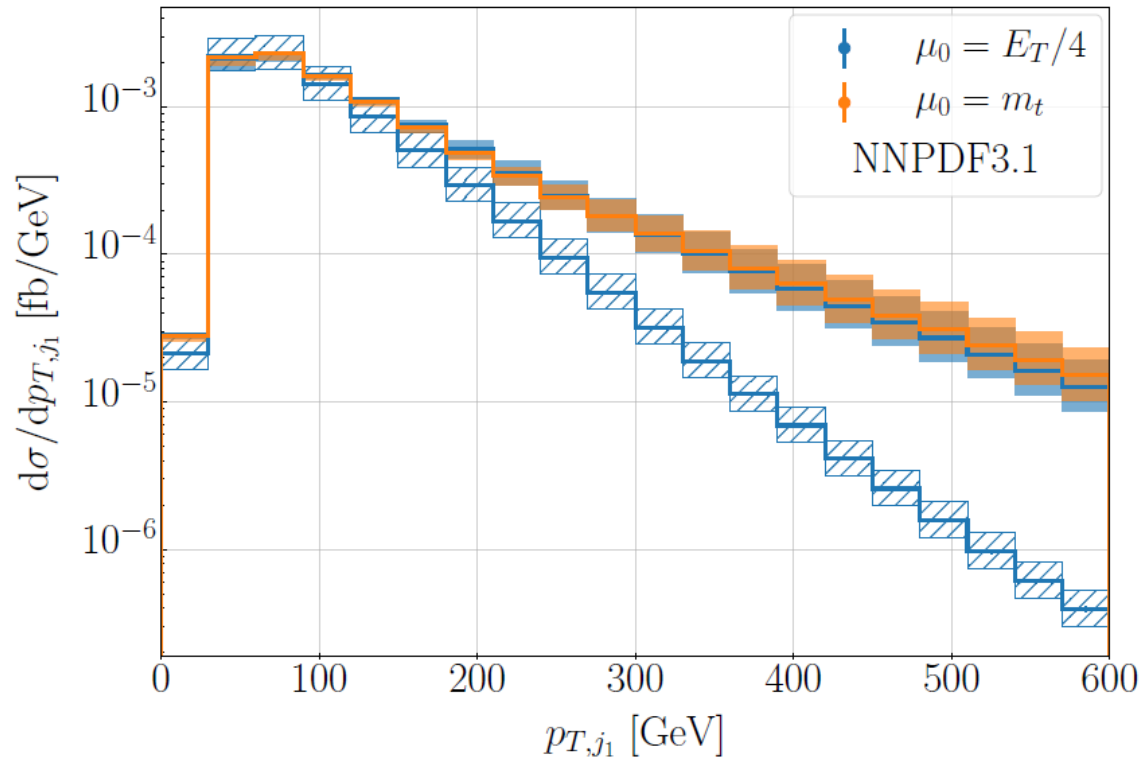
$$\sigma_{\text{Full}}^{\text{NLO}}(\epsilon_\gamma = 0.5) = 0.2832(7) \text{ fb}$$

$$\sigma_{\text{Full}}^{\text{NLO}}(E_{T\gamma} \epsilon_\gamma = 10 \text{ GeV}) = 0.2666(8) \text{ fb}$$

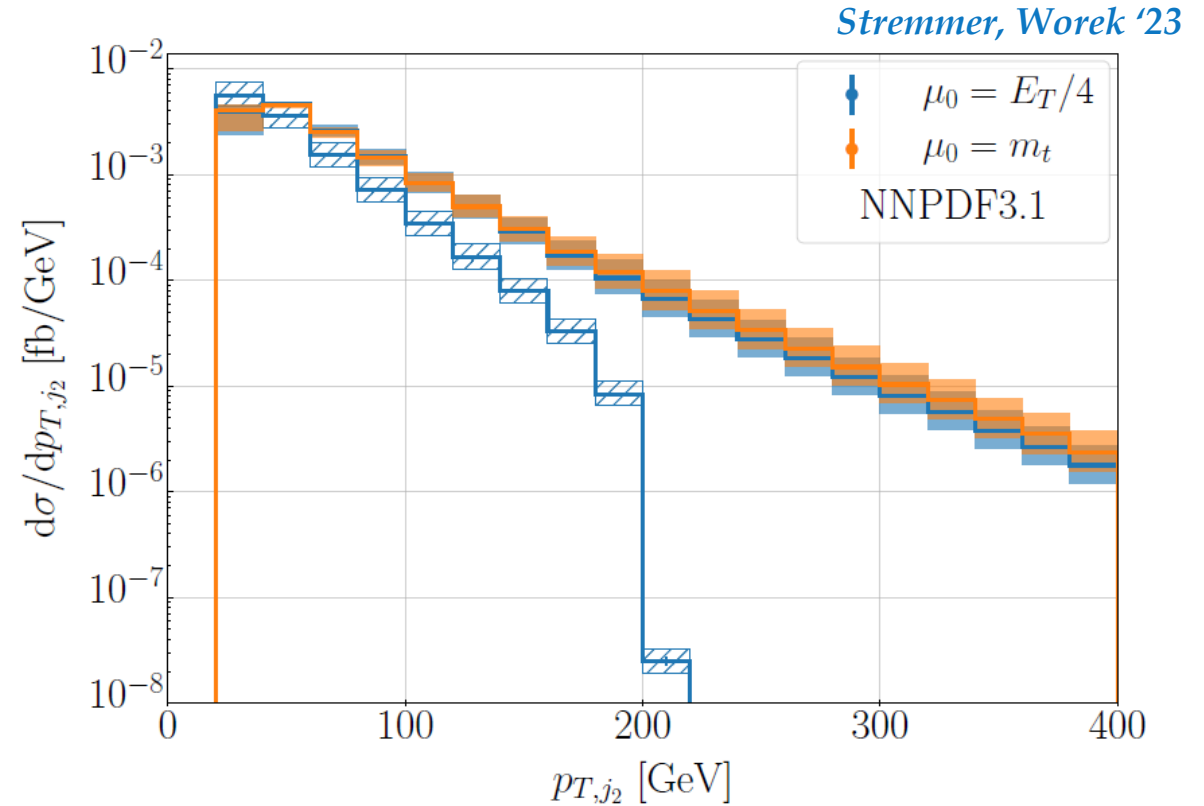
$$\sum_i E_{T_i} \Theta(R - R_{\gamma i}) \leq \epsilon_\gamma E_{T\gamma} \left(\frac{1 - \cos(R)}{1 - \cos(R_{\gamma j})} \right)^n$$

- Significant deviations ($5\% - 10\%$) between different input parameters in Smooth photon isolation prescription

Differential Fiducial cross section in lepton + jet channel



- Huge NLO QCD corrections caused by hard jets in the production stage
- Scale uncertainties in tails $\sim 50\%$



- LO spectrum limited by finite W boson mass
 $p_{T,j_2,max} \sim m_W / \Delta R_{jj} \sim 203$ GeV
- Scale uncertainties in tails $\sim 50\%$

Conclusion

- NLO QCD corrections to $pp \rightarrow t\bar{t}(\gamma\gamma) \rightarrow W^+W^-b\bar{b}(\gamma\gamma) \rightarrow \begin{cases} \ell^+\ell^-\nu_\ell\bar{\nu}_\ell b\bar{b}\gamma\gamma \\ \ell^-\bar{\nu}_\ell jj b\bar{b}\gamma\gamma \end{cases}$
- Photon bremsstrahlung consistently included in production and decay of top-quark pair
- Only 40% – 48% of integrated fiducial cross section from Prod.
- Large NLO QCD corrections in lepton + jet channel reduced by additional cut ($|m_W - M_{jj}| < 15 \text{ GeV}$)
- Still huge NLO QCD corrections in hadronic observables
- Large dependence on input parameters in Smooth photon isolation prescription

Outlook

- Realistic photon isolation based on Fixed Cone Isolation or Democratic Clustering
→ Requires QED subtraction, quark-to-photon and gluon-to-photon fragmentation functions

Backup

Setup of the calculation (2)

- Exclusive in $n_b = 2$

- Event selection:

$$\begin{aligned} p_{T,\ell} > 25 \text{ GeV}, & & |y_\ell| < 2.5, & & \Delta R_{\ell\ell} > 0.4, \\ p_{T,b} > 25 \text{ GeV}, & & |y_b| < 2.5, & & \Delta R_{bb} > 0.4, \\ p_{T,\gamma} > 25 \text{ GeV}, & & |y_\gamma| < 2.5, & & \Delta R_{\gamma\gamma} > 0.4, \\ \Delta R_{bl} > 0.4, & & \Delta R_{\gamma l} > 0.4, & & \Delta R_{\gamma b} > 0.4 \end{aligned}$$

- Additional cuts in lepton+jet channel:

$$\begin{aligned} p_{T,j} > 25 \text{ GeV}, & & |y_j| < 2.5, & & \Delta R_{jj} > 0.4, \\ \Delta R_{\ell j} > 0.4, & & \Delta R_{bj} > 0.4, & & \Delta R_{\gamma j} > 0.4 \end{aligned}$$

$$|m_W - M_{jj}| < 15 \text{ GeV}$$