Neutrino masses and mixings –

Direct mass measurements

Christoph Wiesinger (Technical University of Munich), ISAPP school, 17.09.2024

What we know about neutrinos

- three active **flavor eigenstates** v_l with $l \in \{e, \mu, \tau\}$
- flavor eigenstates are linear combinations of mass eigenstates v_i

$$\nu_l = \sum_i U_{li} \nu_i$$

• mass squared differences

$$\Delta m_{ij}^2~=~m_i^2~-~m_j^2$$

> neutrino **oscillations**

 $P(\nu_l \rightarrow \nu_m) > 0$

[Kajita, McDonald, Nobel Prize in Physics 2015]



mass eigenstates

 v_1

 ν_2



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- flavor eigenstates are linear combinations of mass eigenstates v_i

$$\nu_l = \sum_i U_{li} \nu_i$$

mass squared differences

$$\Delta m_{ii}^2 = m_i^2 - m$$

- > neutrino oscillations $P(\nu_l \rightarrow \nu_m) > 0$ [Kajita, McDonald, Nobel Prize in Physics 2015]
- > at least two neutrinos have mass
- matter effects in sun $m_1 < m_2$ [Mikheyev, Smirnov, Sov.J.Nucl.Phys. 42 (1985) 913-917; Wolfenstein, PRD 17 (1978) 2369-2374]
- > there are two ordering scenarios

Joachim Kopp's lecture





 v_3



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- How can we measure the absolute neutrino mass?
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Neutrino mass probes

• Supernovae, time-of-flight



Cosmology



• Beta decay kinematics, direct neutrino mass measurements

• Neutrinoless double beta decay





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Time-of-flight



Velocity of relativistic neutrino



t:

Travel time

Time difference

$$= \frac{d}{v} = \frac{d}{c\sqrt{1 - \frac{m^2 c^4}{E^2}}} \approx \frac{d}{c} \left(1 + \frac{1}{2} \frac{m^2 c^4}{E^2}\right)$$

$$\Delta t = \frac{d}{v_1} - \frac{d}{v_2} = \frac{d}{2c} m^2 c^4 \left(\frac{1}{E_1^2} - \frac{1}{E_2^2} \right)$$

$$\rightarrow mc^2 = \sqrt{\frac{2c\Delta t}{d} \left(\frac{1}{E_1^2} - \frac{1}{E_2^2}\right)^{-1}}$$

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Time-of-flight



distance d

Velocity of relativistic neutrino

 $v \approx c \sqrt{1 - \frac{m^2 c^4}{E^2}}$

Travel time

 $t = \frac{d}{v} = \frac{d}{c\sqrt{1 - \frac{m^2c^4}{E^2}}} \approx \frac{d}{c} \left(1 + \frac{1}{2}\frac{m^2c^4}{E^2}\right)$

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SN1987A: $d = 170\ 000\ ly = 1.7 \cdot 10^{21}\ m$, $E_1 = 6\ MeV$, $E_2 = 36\ MeV$, $\Delta t = 12\ s \rightarrow mc^2 = 12\ eV$

Supernova limits

• SN1987A data from Kamiokande, IMB and Baksan, 25 events in total, recent supernova electron antineutrino emission model [Pagliaroli, Rossi-Torres, Vissani, Astropart.Phys. 33 (2010) 287-291]

m_v < 5.8 eV (95% CL)

> independent, but not competitive bound

- **1-3 supernovae per century** in our galaxy, more powerful detectors online (e.g. SuperKamiokande) or under construction (e.g. DUNE)
- sub-eV sensitivity expected, but depends on circumstances (e.g. supernova distance, available detectors)
 [Pompa et al., PRL 129 (2022) 12, 121802]

Neutrino mass probes

• Supernovae, time-of-flight



- Cosmology
- Beta decay kinematics, direct neutrino mass measurements



• Neutrinoless double beta decay



Neutrinos in the cosmos

Miguel Escudero's lecture

- present in primordial plasma, freeze-out as temperature drops below weak interaction scale, cosmic neutrino background (CvB)
- > most abundant known massive particle in the universe
- neutrino mass defines transition from radiation to matter behaviour
- modifies background evolution, redshift to matter-to-radiation equality
- heavy non-relativistic matter clumps on small scales, neutrinos disperse energy across overdensities, effectiveness depends on neutrino mass
- > neutrino mass impacts structure growth, matter power spectrum



Sum of neutrino mass eigenstates, $\Sigma = \sum_{i} m_{i}$



• minimum at **0.06 eV** (normal ordering), **0.10 eV** (inverted ordering)

Sum of neutrino mass eigenstates, $\Sigma = \sum_i m_i$



- minimum at 0.06 eV (normal ordering), 0.10 eV (inverted ordering)
- most stringent bounds driven by Planck and DESI data [Aghanim et al., A&A 641 (2020) A6; Adame et al., arXiv:2404.03002]

Σ < 0.07 eV (95% CI)

- model dependence can weaken bounds
 - extended cosmology (e.g. dark energy dynamics, ..), x2
 [Choudhury, Hannestad, JCAP 07 (2020) 037, ..]
 - non-standard neutrino physics (e.g. invisible neutrino decay, time-dependent neutrino mass, ..), x10
 [Escudero et al., JHEP 12 (2020) 119; Dvali, Funke, PRD 93 (2016) 11, 113002, ..]
- future observatories and missions (e.g. EUCLID) [Brinckmann et al., JCAP 01 (2019) 059, ..]



..), x2

Neutrino mass probes



Cosmology



• Beta decay kinematics, direct neutrino mass measurements



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Enrico Fermi: β decay kinematics "Let's express this with the kinetic energy of the electron and the mass of Fermi function phase space factor the neutrino." $\frac{d\Gamma}{dE} \propto F(E,Z) \cdot E_e \cdot E_\nu \cdot p_e \cdot p_\nu$ differential decay rate $= F(E,Z) \cdot (E + m_e) \cdot (E_0 - E) \cdot \sqrt{(E + m_e)^2 - m_e^2} \cdot \sqrt{(E_0 - E)^2 - m_v^2}$ h grande electron energy neutrino energy electron momentum neutrino momentum (endpoint E_0) $(E^2 = p^2 + m^2)$ piccolo

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β decay kinematics

Fermi function

 $\frac{d\Gamma}{dE} \propto F(E,Z) \cdot E_e \cdot E_\nu \cdot p_e \cdot p_\nu$

Enrico Fermi: "Let's express this with the kinetic energy of the electron and the mass of the neutrino."



$$= F(E,Z) \cdot (E + m_e) \cdot (E_0 - E) \cdot \sqrt{(E + m_e)^2 - m_e^2} \cdot \sqrt{(E_0 - E)^2 - m_v^2}$$

$$= \sum_{i} |U_{ei}|^2 \cdot F(E,Z) \cdot (E + m_e) \cdot (E_0 - E) \cdot \sqrt{(E + m_e)^2 - m_e^2} \cdot \sqrt{(E_0 - E)^2 - m_i^2}$$

$$\approx F(E,Z) \cdot (E + m_e) \cdot (E_0 - E) \cdot \sqrt{(E + m_e)^2 - m_e^2} \cdot \sqrt{(E_0 - E)^2 - m_{\beta}^2}$$

[Fermi, Nuovo Cim. 11 (1934) 1-19] E_0

piccolo

differential decay rate

h grande

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phase space factor

effective electron (anti-)neutrino mass, $m_{\beta} =$ incoherent sum of mass eigenstates

Shoichi Sakata: "But there are three neutrino mass eigenstates."

 $\sqrt{\sum_{i} |U_{ei}|^2 m_i^2}$ Effective electron neutrino mass, $m_{\beta} =$



- minimum at 0.01 eV (normal ordering), 0.05 eV (inverted ordering)
- current experiments (KATRIN) probe degenerate regime, $m_1 \approx m_2 \approx m_3$
- technology development for future experiments that aim to enter hierarchical regime, m₁ < m₂ ≪ m₃ or m₃ ≪ m₁ ≈ m₂

- How can we measure the absolute neutrino mass?
- What is a direct neutrino mass measurement?
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Experimental challenge

measure sub-eV scale **spectral distortion** close to keV-scale **kinematic endpoint**

- high-activity source, low Q-value
 - tritium ³H (T_{1/2} = 12.3 yr, E₀ = 18.6 keV)
 - holmium ¹⁶³Ho (T_{1/2} = 4570 yr, E₀ = 2.8 keV)
- high acceptance, excellent energy resolution (O(1) eV, < 0.01 %), low background (mcps)
- **high precision** understanding of theoretical spectrum and experimental response



Experimental approaches



Experimental approaches



Karlsruhe Tritium Neutrino (KATRIN) experiment

Offenfalle

000

Glastralle

Working principle



Working principle



Working principle







windowless gaseous tritium source

- molecular tritium, closed
 loop operation
- high activity, up to 100 GBq



windowless gaseous tritium source

- molecular tritium, closed
 loop operation
- high activity, up to 100 GBq

transport section

- tritium gas/ion removal
- > reduction by > 10¹⁴







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surplus energy (eV)



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second result, **m**_β < **0.8 eV** (90% CL)

[Aker et al., Nature Phys. 18 (2022) 2, 160-166]

Analysis procedure

• maximum likelihood fit of model $\Gamma(qU) \propto A \cdot \int_{qU}^{E_0} D(E, m_\beta^2, E_0) \cdot R(qU, E) dE + B$

with free squared neutrino mass m_{β}^2 , effective endpoint E_0 , amplitude A and background B

• theoretical (Fermi theory, molecular excitations) and experimental inputs (calibration measurements)

(Selected) experimental improvements

- reconfiguration of main spectrometer, shifted analyzing plane [Lokhov et al., EPJ C 82 (2022) 3, 258]
 - 2-fold reduction of background, Rydberg-induced background +
 - increased spectrometer field variance, use detector segmentation -
- ^{83m}Kr co-circulation mode, conversion electrons, calibrate source potential and spectrometer fields, neutrino mass scans under same conditions [A. Marsteller et al., INST 17 (2022) 12, P12010]
- improved **electron gun**, mono-energetic angular-selective photoelectron source, probe **scattering effects** [Aker et al., EPJ C 81 (2021) 7, 579]

Analysis challenge

• 7 different configurations, 59 spectra, **1609 data points**, **parameter correlations** across datasets

2-stage blinding, simulated data, blinded molecular final states,
 2 analysis frameworks, neural network surrogate [Karletal., EPJC 82 (2022) 5, 439]

Fit result

• 7 different configurations, 59 spectra, **1609 data points**, **parameter correlations** across datasets

2-stage blinding, simulated data, blinded molecular final states,
 2 analysis frameworks, neural network surrogate [Karletal., EPJC 82 (2022) 5, 439]

> p-value = 0.84, best-fit $m_{\beta}^2 = -0.14^{+0.13} - 0.15 eV^2$ [Aker et al., arXiv:2406.13516]

Uncertainty breakdown

 6-fold increase in statistics, 2-fold reduction of background

• **3-fold reduction of systematic uncertainties**, source effects leading

 statistical uncertainty dominates, improved calibration precision in recent campaigns

Neutrino mass limit

 new world-best direct neutrino mass constraint [Aker et al., arXiv:2406.13516]

m_β < 0.45 eV (90% CL)

using **Lokhov-Tkachov** confidence interval construction, recovers **sensitivity** for negative best-fit value

[Lokhov, Tkachov, Phys.Part.Nucl. 46 (2015) 3, 347-365]

• Feldman-Cousins construction, benefits from negative best-fit value, $m_{\beta} < 0.31 \text{ eV}$ (90% CL)

best-fit value, i.e. $m_{\beta}^2 = -0.14 \text{ eV}^2$

Outlook

 new world-best direct neutrino mass constraint [Aker et al., arXiv:2406.13516]

m_β < **0.45 eV** (90% CL)

 data taking ongoing until end-2025, projected final sensitivity below

m_β < **0.3 eV** (90% CL)

Outlook

 new world-best direct neutrino mass constraint [Aker et al., arXiv:2406.13516]

m_β < **0.45 eV** (90% CL)

 data taking ongoing until end-2025, projected final sensitivity below

m_β < **0.3 eV** (90% CL)

- sensitivity beyond KATRIN requires new technology
- m_{β} has **minimum value**, guaranteed measurement

Beyond KATRIN

- sub-eV scale differential measurement
 - + better use of statistics
 - + lower background

- + avoid broadening effect
- + avoid limiting T₂ systematics
- KATRIN++ efforts, development of micro calorimeters, time-offlight concepts, atomic tritium technology, ..

Experimental approaches

Cyclotron radiation emission spectroscopy (CRES)

• electromagnetic radiation emitted by charged particles undergoing cyclotron motion

$$\omega(\gamma) = \frac{\omega_0}{\gamma} = \frac{e B}{E + m_e}$$

> measure cyclotron frequency of trapped electron to determine energy [Monreal, Formaggio, PRD 80 (2009) 051301]

Cyclotron radiation emission spectroscopy (CRES)

- **source transparent** to microwave radiation
- > no electron extraction needed
- differential frequency measurement
- > eV-scale resolution, low background

challenges

- sensitivity to low power signal (< 10⁻¹⁵ W)
- homogeneous magnetic field (10⁻⁷)
- large volume trap (m³)

Project8

• cold atomic tritium trap, resonant cavity

CJ

ഹ

Ξ

10 m

atomic source

- **proof-of-concept**, single electron spectroscopy
- molecular tritium endpoint measurement, first neutrino mass result [Ashtari Esfahani et al., PRL 131 (2023) 10, 102502]

m_β < 155 eV (90% CL)

- m³-scale traps (antenna array or cavity resonator), atomic tritium source
- > sensitivity down to 0.04 eV [Ashtari Esfahani et al., arXiv:2203.07349]

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Experimental approaches

Holmium-163

- electron capture decay, energy shared between excitation and neutrino
- super-low Q-value (2.8 keV),
 sub-eV sensitivity with MBq-scale activity
 [Eliseev et al., PRL 115 (2015) 6, 062501]
- > calorimetric measurement of decay energy [De Rujula, Lusignoli, PLB 118 (1982) 429]

Cryogenic calorimetry

- holmium implanted in absorber with small heat capacity C_{tot}
- > small volume, low tempertures (mK)

$$C_{tot} = \left(\frac{T}{T_D}\right)^3$$
 (Debye Law)

> detection of **temperature increase** from decay energy

$$\frac{\Delta T}{E} \approx \frac{1}{C_{tot}} = O(1) \ mK/keV$$

thermal bath

Cryogenic calorimetry

- **source = detector** concept, all decay energy is measured
- eV-scale differential measurement

challenges

- **pile-up** limits activity per pixel, multiplexed read-out
- difficult theoretical **spectrum calculation**

thermal bath

- array of **metallic magnetic calorimeters** (MMC) with ¹⁶³Ho-implanted absorber
- first neutrino mass result, 4 pixels with 0.2 Bq each m_{β} < 150 eV (95% CL) [Velte et al., EPJ C 79 (2019) 12, 1026]
- second result, 34 pixels with 0.7 Bq each [Neutrino 2024]

m_β < **19 eV** (90% CL)

- array of transition edge sensors (TES) coupled to ¹⁶³Ho-implanted absorber
- **first result**, 48 pixels with 0.3 Bq each [Neutrino 2024]

m_β < **28 eV** (90% CI)

sensitivity for **coming phases** of ECHO/HOLMES:

[Gastaldo, TAUP 2023]

 $\sqrt{\sum_i |U_{ei}|^2 m_i^2}$ Effective electron neutrino mass, $m_{\beta} =$

- minimum at 0.01 eV (normal ordering), 0.05 eV (inverted ordering)
- most stringent bound by KATRIN, first five campaigns [Aker et al., arXiv:2406.13516]

 promising technologies for future experiments, differential detectors (e.g. CRES, cryogenic calorimeters), atomic tritium, holmium, ..

[Ashtari Esfahani et al., arXiv:2203.07349]

Project8 goal: $m_{\beta} < 0.04 \text{ eV}$ (90% CL)

Side note: sterile neutrinos

additional sterile neutrino state, mixing with electron neutrino

$$\begin{pmatrix} \nu_{e} \\ \nu_{\mu} \\ \nu_{\tau} \\ \nu_{s} \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} \\ U_{s 1} & U_{s 2} & U_{s 3} & U_{s 4} \end{pmatrix} \begin{pmatrix} \nu_{1} \\ \nu_{2} \\ \nu_{3} \\ \nu_{4} \end{pmatrix}$$

- motivated by anomalies (eV-scale), viable dark matter candidate (keV-scale)
- > additional spectral component, kink-like signature
- unique test of eV-scale parameter space with KATRIN [Aker et al., PRD 105 (2022) 7, 072004]
- deep spectral exploration to search for keV-sterile neutrinos with TRISTAN upgrade of KATRIN, silicon drift detector array

[Mertens et al., J.Phys.G 46 (2019)]

Side note: relic neutrinos

• cosmic neutrino background (CvB)

 $\rho_{C\nu B} = 300 \ cm^{-3} \text{ and } T_{C\nu B} = 1.95 \text{ K}$

• capture on tritium, no energy threshold, above endpoint

 $T \rightarrow {}^{3}He + e^{-} + \bar{\nu_e}$

- $\nu_e + T \rightarrow {}^{3}He + e^{-}$
- capture rate doubles for Majorana neutrinos (see tomorrow)
- ~10 μg KATRIN target, constraint on local overdensity [Aker et.al, PRL 129 (2022) 1, 011806]

 $\eta < 1.1 \cdot 10^{11} (95\% CL)$

> **100x improvement** over previous laboratory bound

PTOLEMY

• monoatomic tritium in graphene matrix, cyclotron emission tagging, dynamic electromagnetic filter, micro calorimeters [Betti et al., Prog.Part.Nucl.Phys. 106 (2019) 120-131]

Interplay with cosmology

- β-decay kinematics offers **model-independent laboratory test** of absolute neutrino mass
- **complementary** to cosmological probes
- interplay will allow model discrimination

energy conservation

Neutrino mass probes

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