

# Neutrino oscillation experiments

ISAPP School  
„Neutrinos and Dark Matter“  
KIT/Bad Liebenzell, 20 Sep 2024

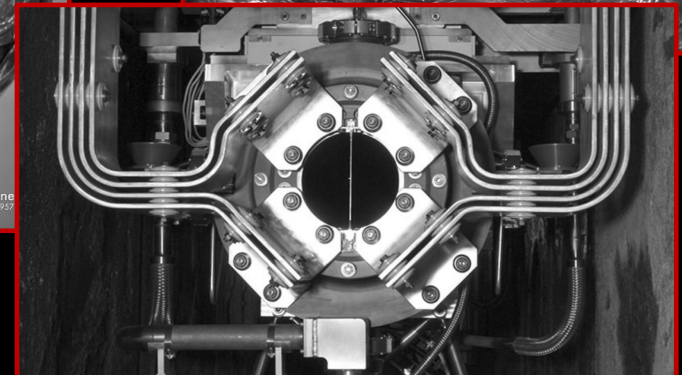
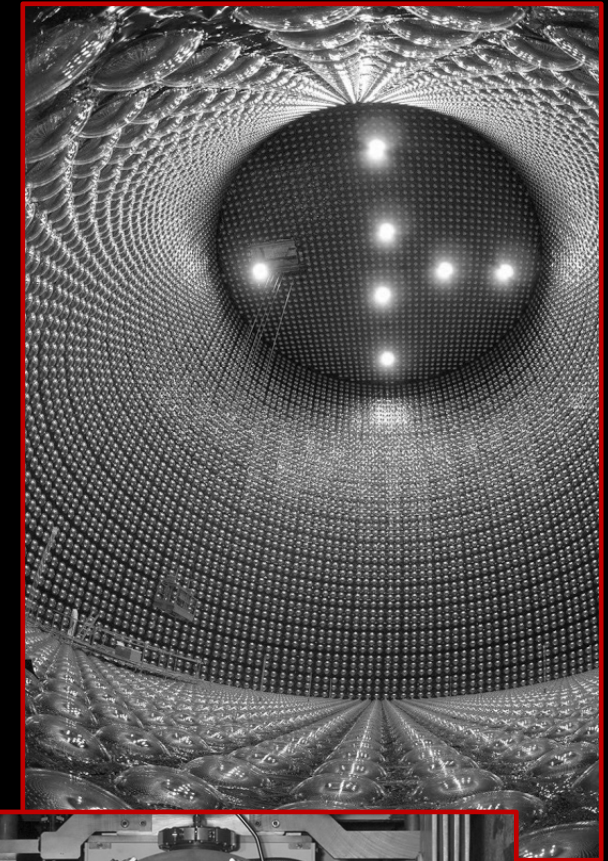
Michael Wurm  
JGU Mainz/PRISMA<sup>+</sup>





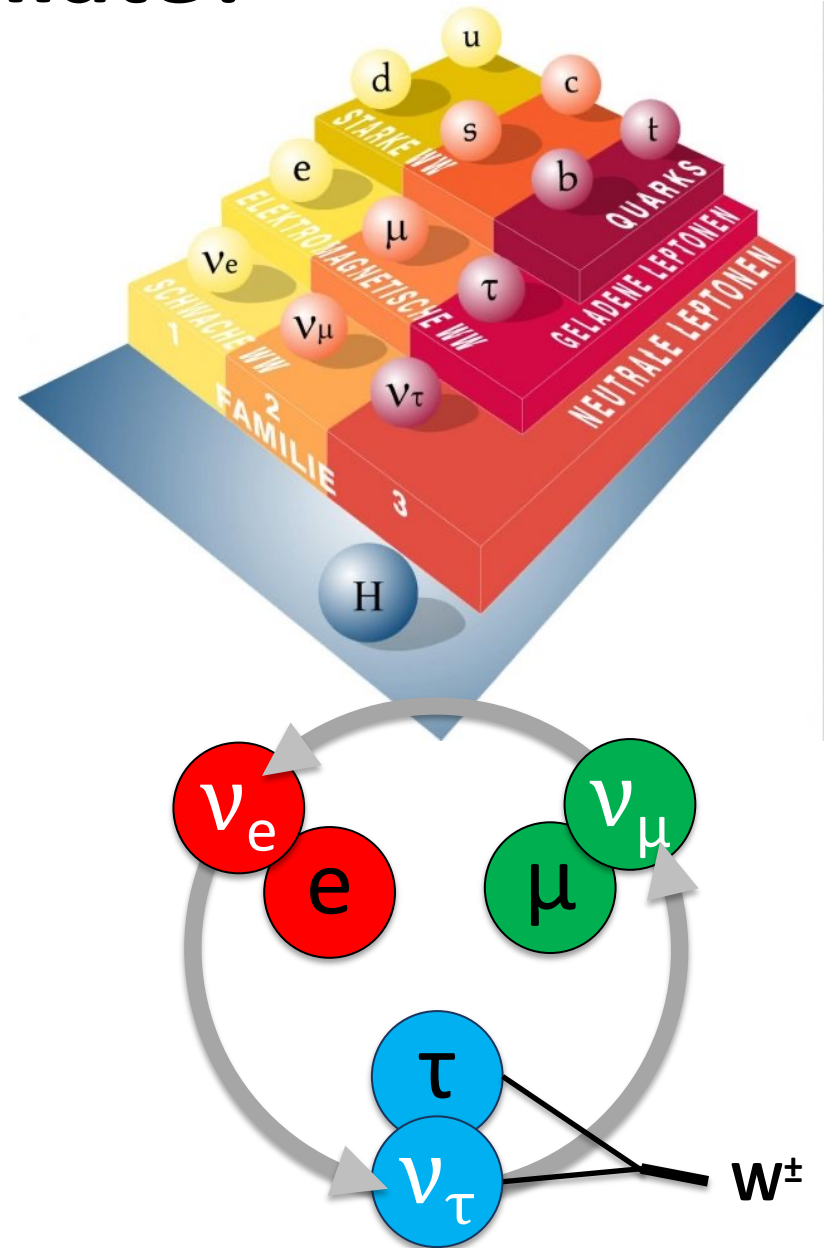
# Contents of this talk

- Neutrino oscillations in a nut-shell
- Discovery of neutrino oscillations
- Current knowledge on oscillation parameters
- Two ways to order neutrino masses
- Accelerator neutrinos and CP violation



# Why can neutrinos oscillate?

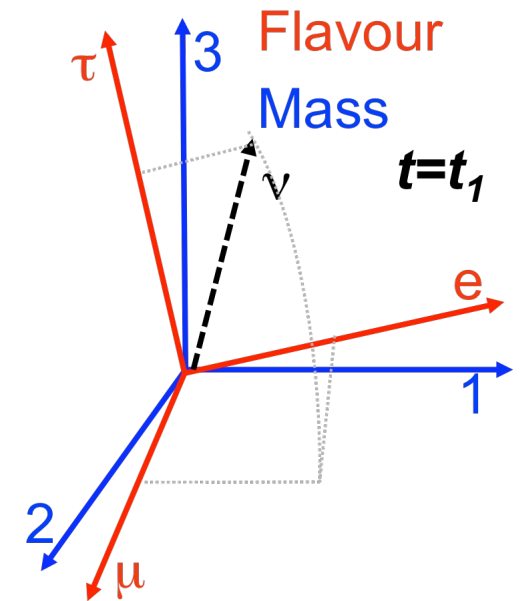
- Neutrinos appear in three families
- Neutrinos appear to be massless  
→ upper limit:  $m_\beta < 0.5 \text{ eV}$
- Participate only in weak interactions  
→ only left-handed neutrinos or right-handed antineutrinos  
→ assumed mass-less in the Standard Model (mostly for convenience)
- but IF they have tiny masses mass and flavor eigenstates can be different (rotated)
- IF so, eigenstates will interfere while propagating → neutrino oscillations



# Neutrino masses and mixing

QM: For **massive** neutrinos with **different masses**,

- the three neutrino **flavor-eigenstates** (taking part in weak interactions) can be a **superposition** of
- the three **mass-eigenstates** (propagating through space)
- The relative fractions of mass in flavor states are described by a **3x3-mixing matrix**



**PMNS-mixing matrix** corresponds to a 3D-rotation between flavor and mass eigenspaces

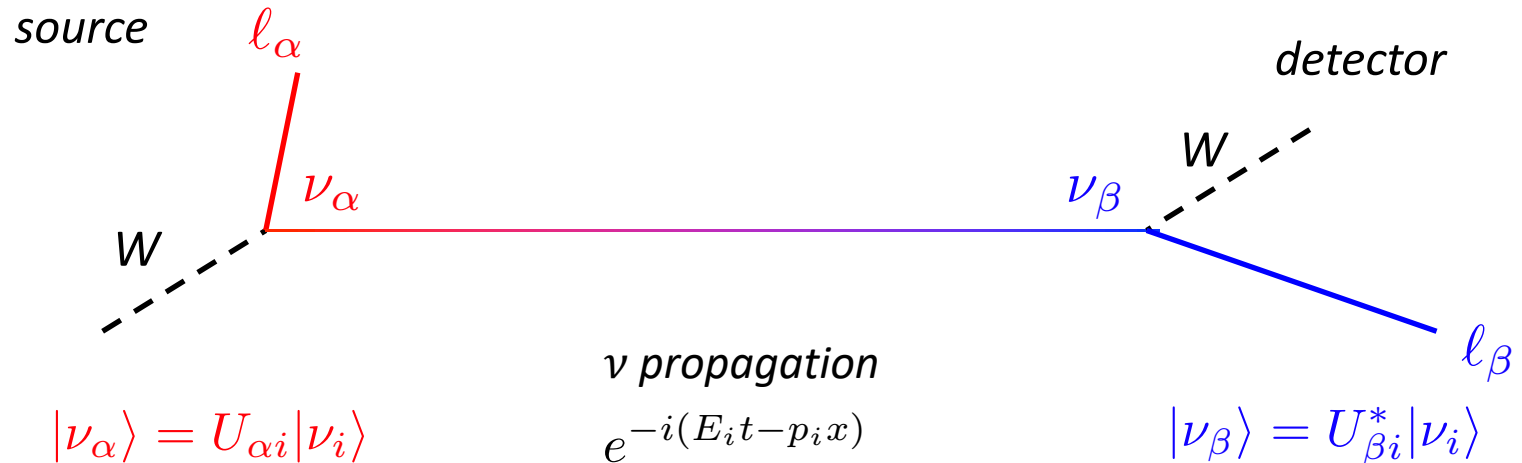
→ cf. CKM-matrix in quark-sector

$$\begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{bmatrix} \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix}$$

**flavor-states**
**mass-states**



# Neutrino oscillation formalism



- propagation for  $p_i = p, m_i \ll E$ 

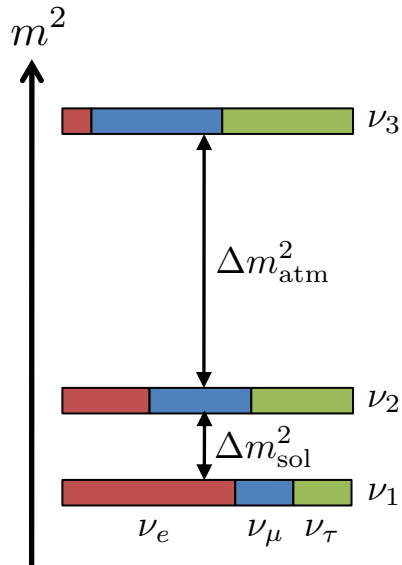
$$E_i = \sqrt{m_i^2 + p^2} = p + \frac{m_i^2}{2p} = E + \frac{m_i^2}{2E}$$
- amplitude:  $\mathcal{A}_{\nu_\alpha \rightarrow \nu_\beta} = \langle \nu_\beta | \text{propagation} | \nu_\alpha \rangle = \sum_i U_{\beta i} U_{\alpha i}^* e^{-i(\frac{m_i^2}{2E})L}$
- probability:  $P_{\nu_\alpha \rightarrow \nu_\beta} = |\mathcal{A}_{\nu_\alpha \rightarrow \nu_\beta}|^2 = \sum_{i,j} U_{\beta i} U_{\alpha i}^* U_{\beta j}^* U_{\alpha j} e^{-i(\frac{m_i^2 - m_j^2}{2E})L}$

# Parametrization of three-flavor mixing

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}}_{\text{atmospheric mixing}} \underbrace{\begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix}}_{\text{reactor mixing \& CP violation}} \underbrace{\begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\text{solar mixing}} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

$U_{3 \times 3} = U_{\text{PMNS}}$

*flavor states*
*atmospheric mixing*
*reactor mixing & CP violation*
*solar mixing*
*mass states*



mixing angles :  $c_{ij} = \cos \theta_{ij}$ ,  $s_{ij} = \sin \theta_{ij}$   
 CP violating phase :  $\delta$

mass squared differences :

- $\Delta m_{\text{sol}}^2 = \Delta m_{21}^2$
- $\Delta m_{\text{atm}}^2 = \Delta m_{32}^2 \approx \Delta m_{31}^2$



# Pontecorvo – The ‘inventor’ of $\nu$ oscillations



Бруно Понтекорво

*1957*

*“... the neutrino may be a particle mixture and ... there is a possibility of real transitions neutrino to antineutrino in vacuum, provided that the lepton (neutrino) charge is not conserved.”*

*1968*

*“If the lepton charge is not an exactly conserved quantum number, and the neutrino mass is different from zero, oscillations similar to those in  $K^0$  beams become possible in neutrino beams.”*

***“From an observational point of view  
the ideal object is the sun.”***

# Neutrinos from the Sun

from Learn Something New Every Day:

<http://www.lsned.com/neutrino/>



**FACT:** about 65 million neutrinos pass through your thumbnail every second.



# Neutrinos from the Sun

from Learn Something New Every Day:

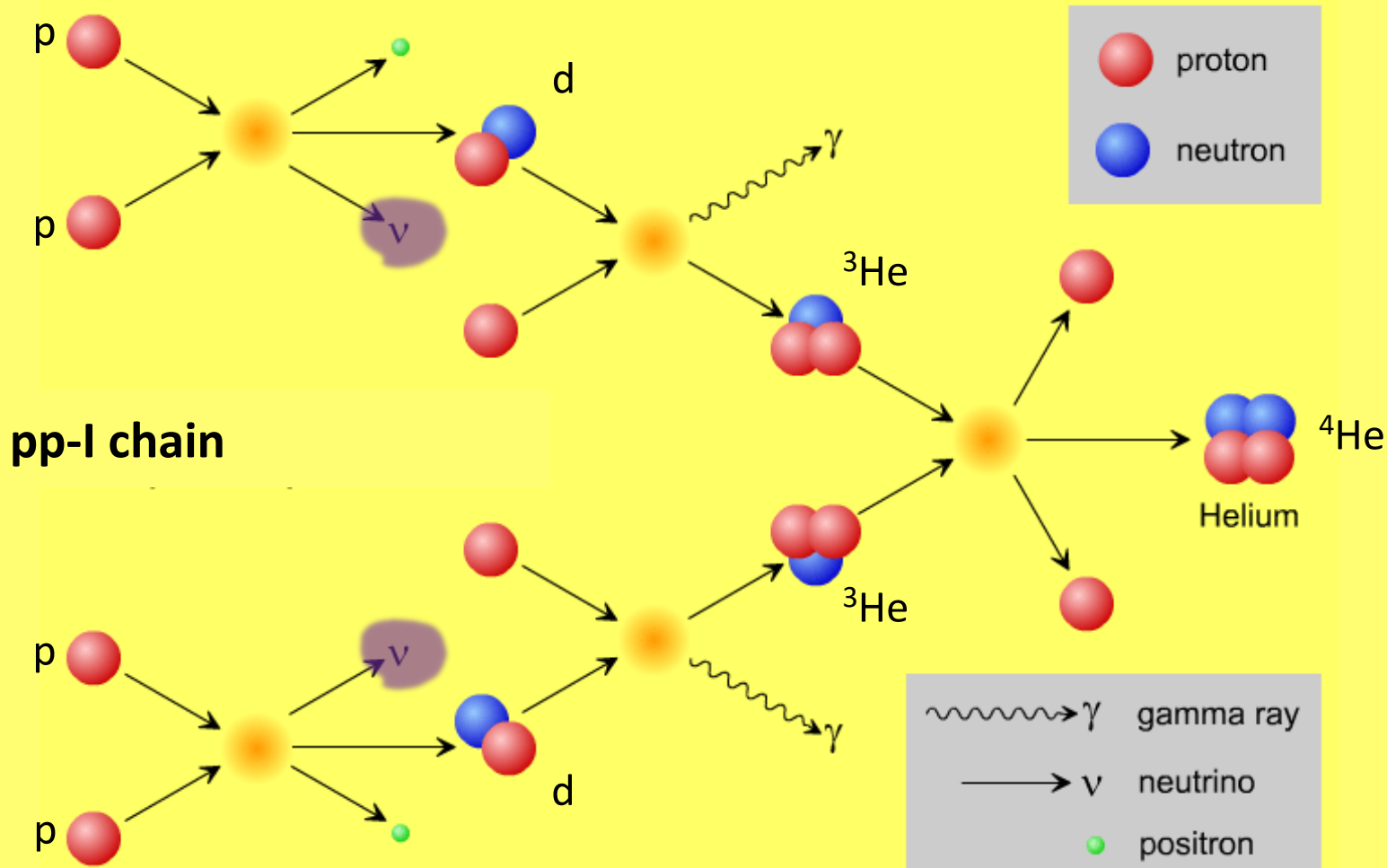
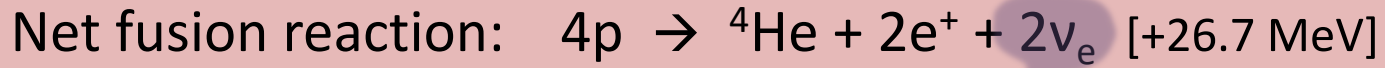
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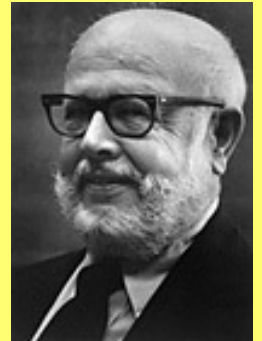
*65 billion!*

**FACT:** about ~~65 billion~~ neutrinos pass through your thumbnail every second.

# Hydrogen burning in the Sun



*H. Bethe*



*W. Fowler*



# Expected solar neutrino flux

electromagnetic luminosity

$$L_{\odot} = 3.85 \times 10^{26} \text{ W}$$



flux at Earth

$$\Phi_{\gamma} \approx 4 \times 10^{21} / \text{m}^2 \text{ s}$$
$$\rightarrow S_{\gamma} = 1367 \text{ W/m}^2$$

neutrino luminosity

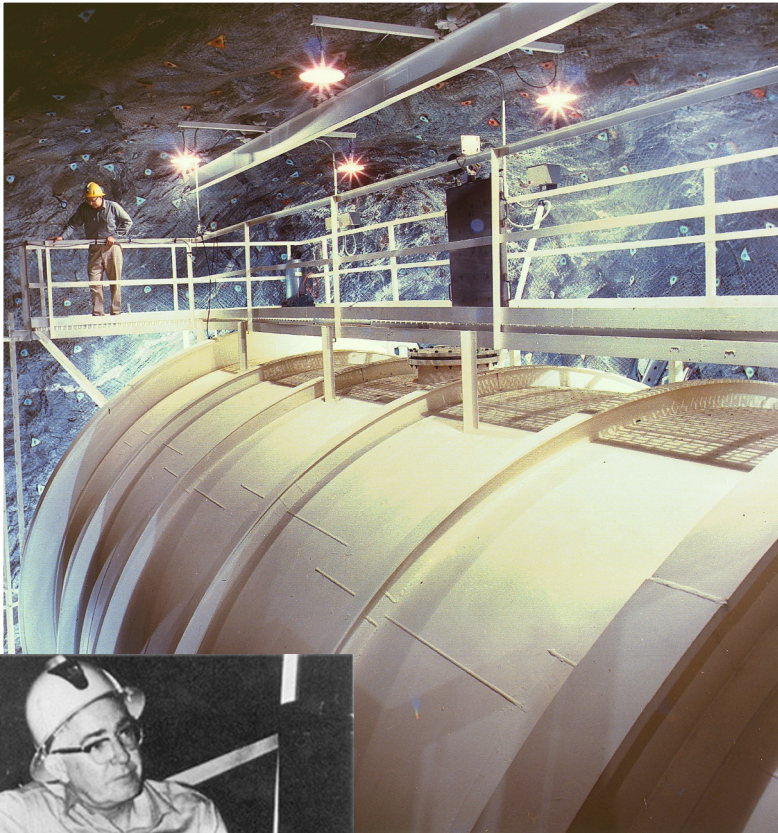
$$L_{\nu} \approx 2\% L_{\odot}$$



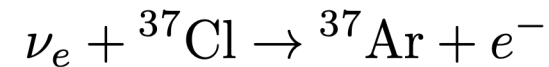
$$\Phi_{\nu} = \frac{S_{\gamma}}{Q_{4p \rightarrow \text{He}}} \times 2$$
$$\approx 6.6 \times 10^{14} / \text{m}^2 \text{ s}$$



# First detection of solar neutrinos: Davis



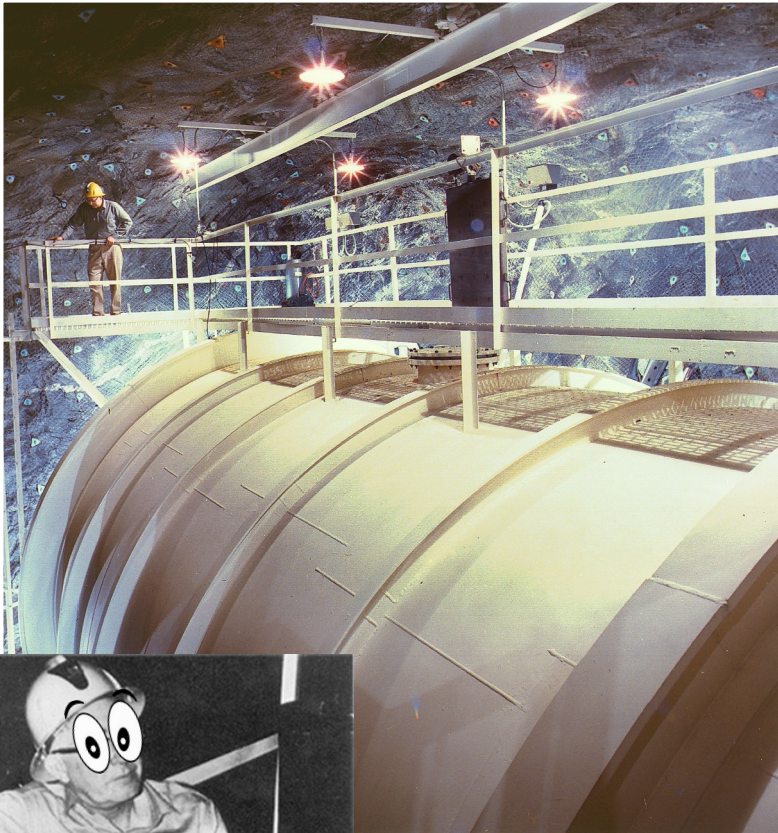
- Location: Homestake mine (US)
- Depth: 1478 m
- Target material: 615 tons of  $C_2Cl_4$   
→ ca.  $6 \times 10^{30}$  atoms of  $^{37}Cl$
- Detection reaction:



*Ray Davis Jr.*

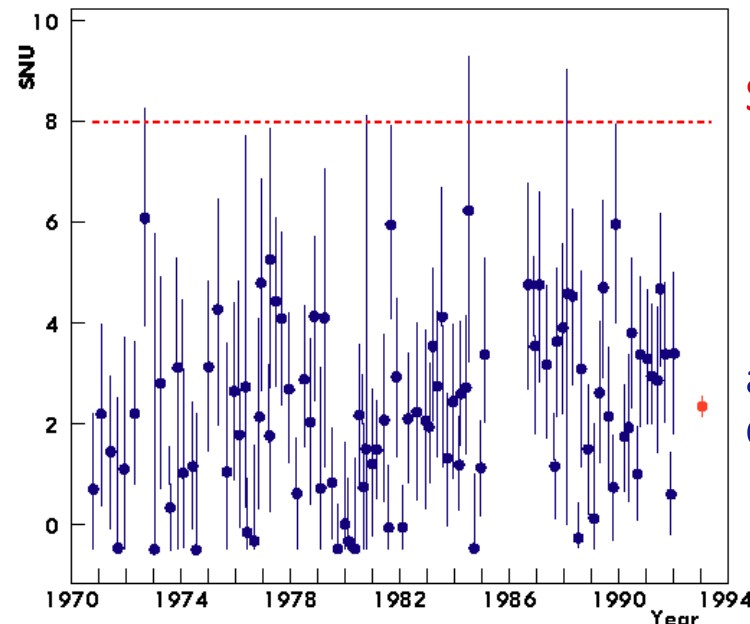
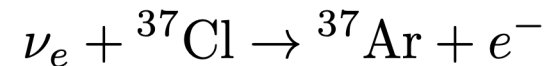


# First detection of solar neutrinos: Davis



Ray Davis Jr.

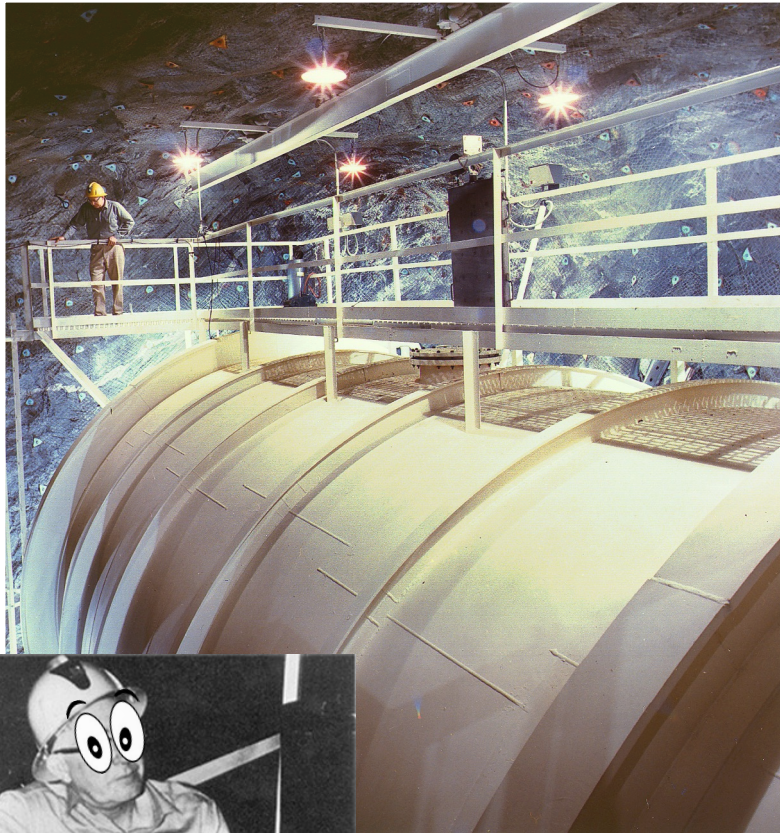
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SSM expectation:  
1.5 per day

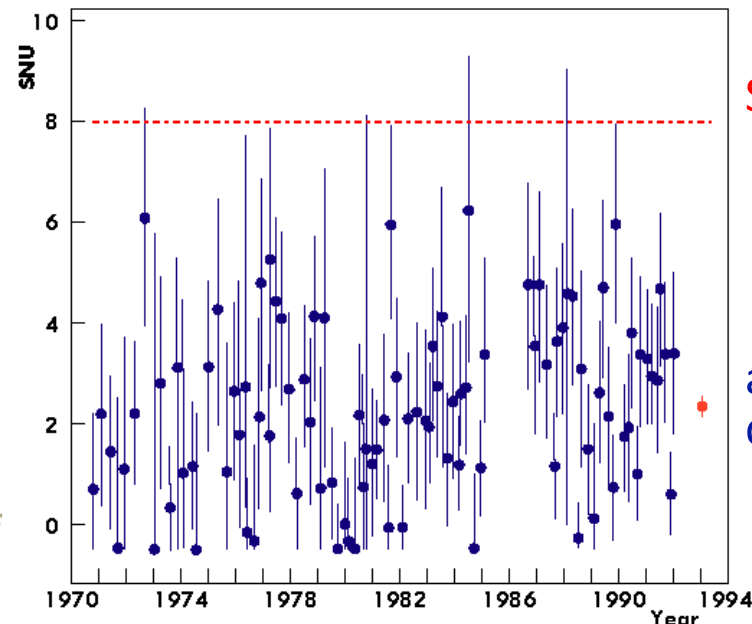
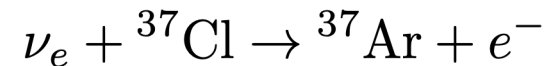
average of  
detected rate:  
0.5 per day

# First detection of solar neutrinos: Davis



„for pioneering contributions to astrophysics, in particular for the detection of cosmic neutrinos“

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→ ca.  $6 \times 10^{30}$  atoms of  $^{37}Cl$
- Detection reaction:



SSM expectation:  
1.5 per day

average of  
detected rate:  
0.5 per day



# Solar neutrinos: Two-flavor approximation

2x2 mixing:

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

*flavor states*  *mass states*

Oscillation probability:

$$P(\nu_e \rightarrow \nu_e) = 1 - \sin^2(2\theta_{12}) \sin^2\left(\frac{\Delta m_{21}^2 L}{4E}\right)$$

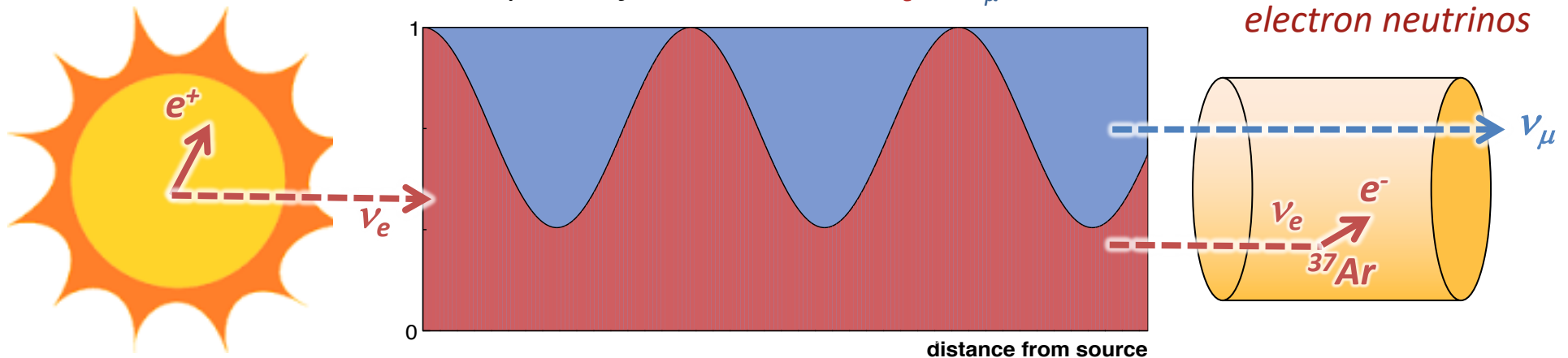
*oscillation amplitude*  *oscillation frequency/length*

*baseline-over-energy*

*electron neutrinos created in solar fusion processes*

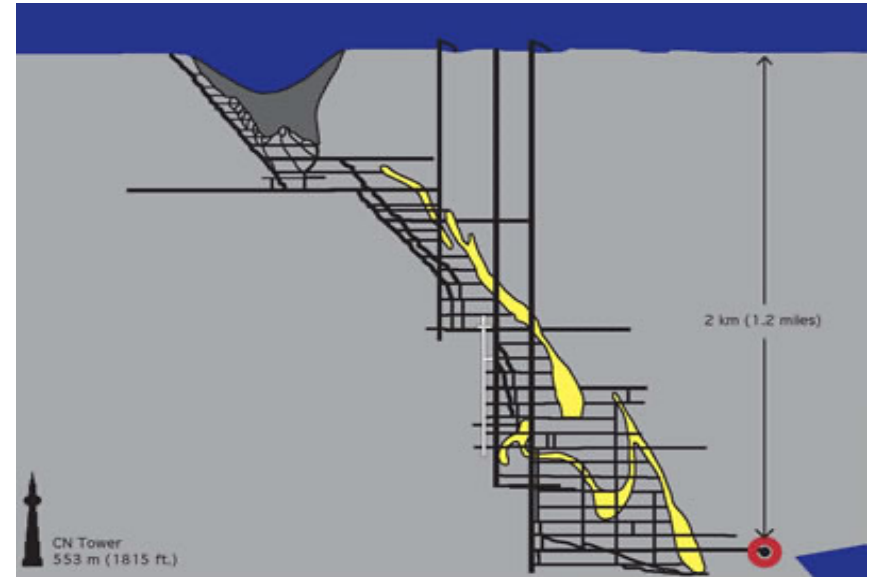
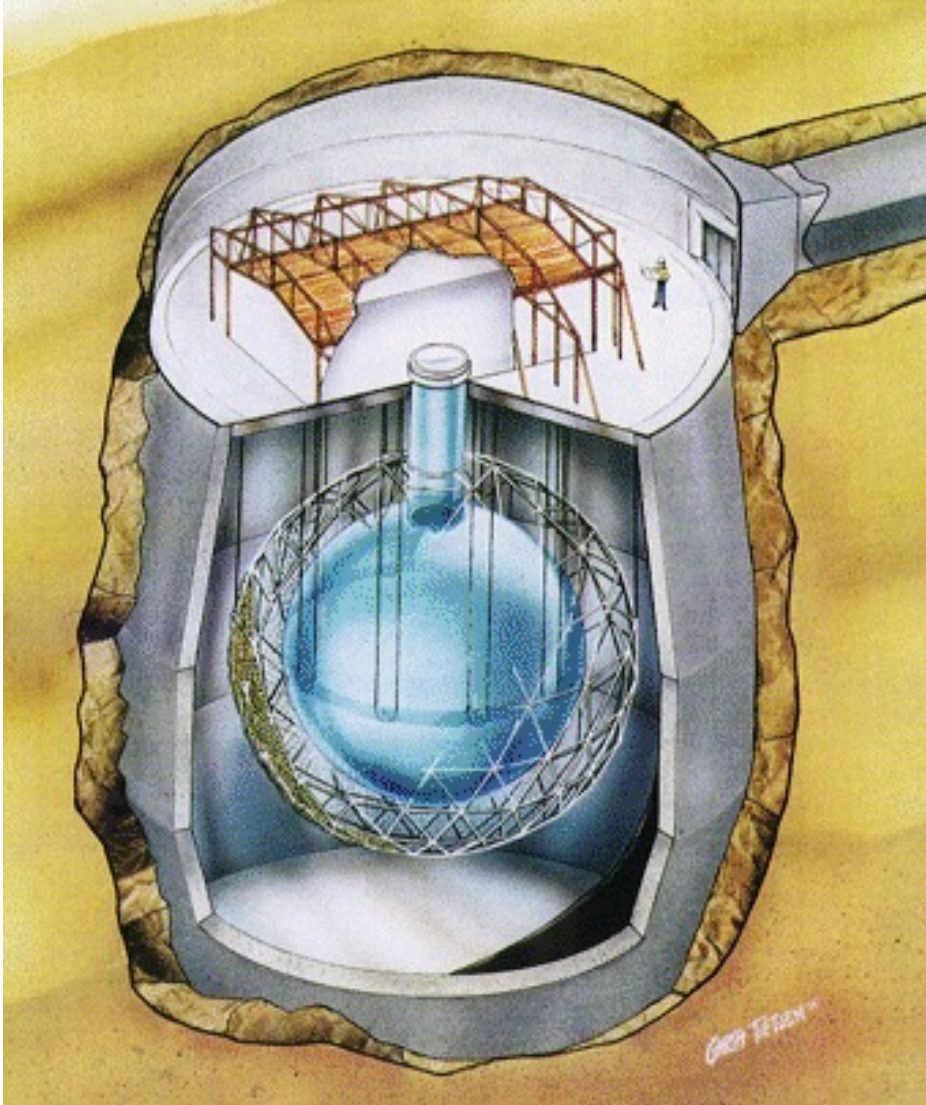
*neutrinos propagate → oscillate partial flavor transition  $\nu_e \rightarrow \nu_\mu$*

*detectors only sensitive to electron neutrinos*



→ observation of rate deficit!! but how to prove it is flavor oscillations?

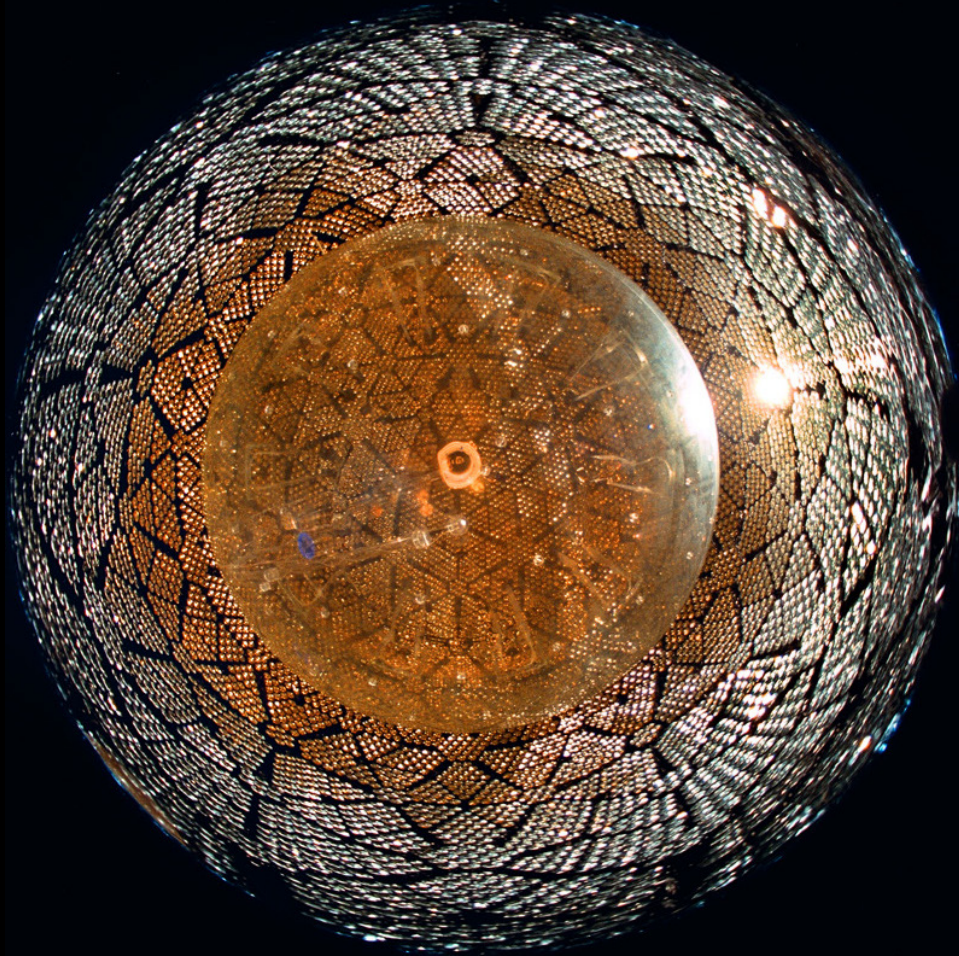
# Sudbury Neutrino Observatory (SNO)



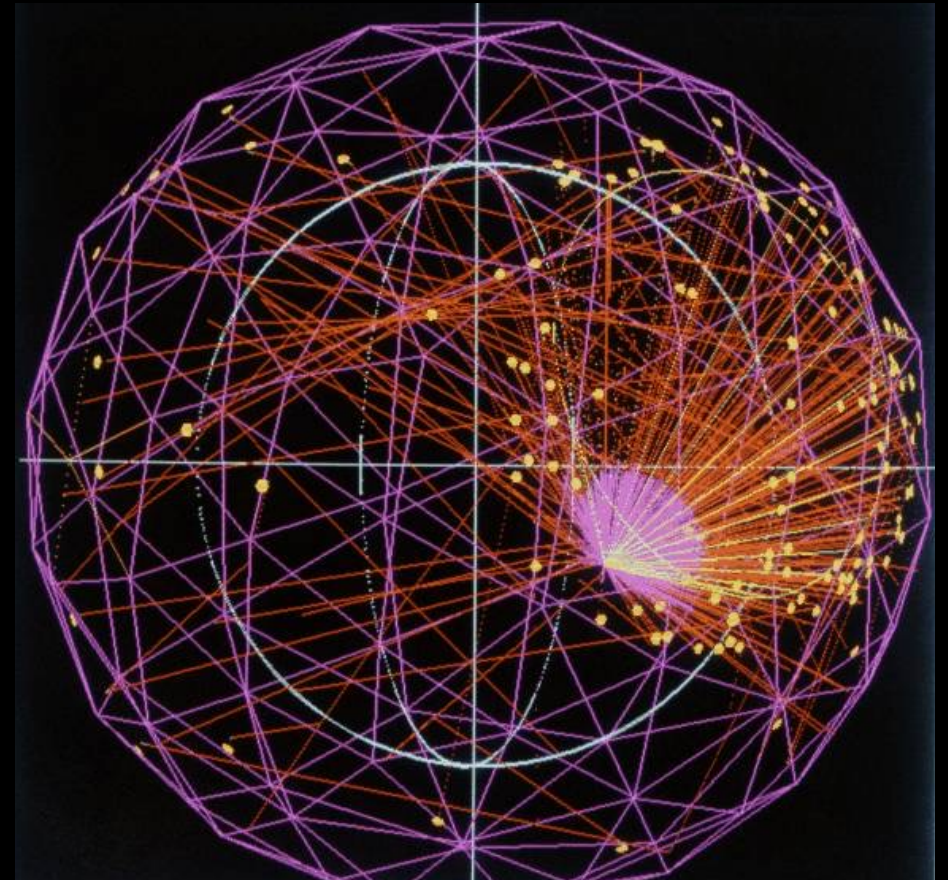
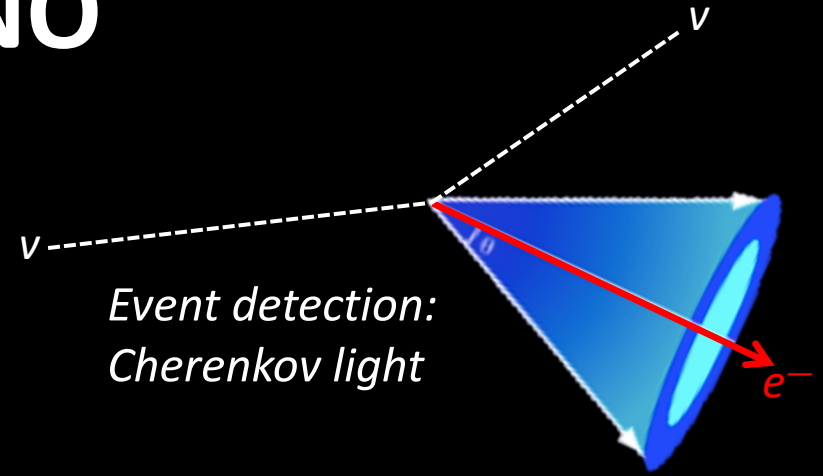
- **Water Cherenkov detector**  
Underground water tank to measure neutrino interactions by final-state charged particles
- **Location:** Sudbury mine  
depth: 2000 m → 6000 mwe
- **Target mass:** 1 kt of D<sub>2</sub>O



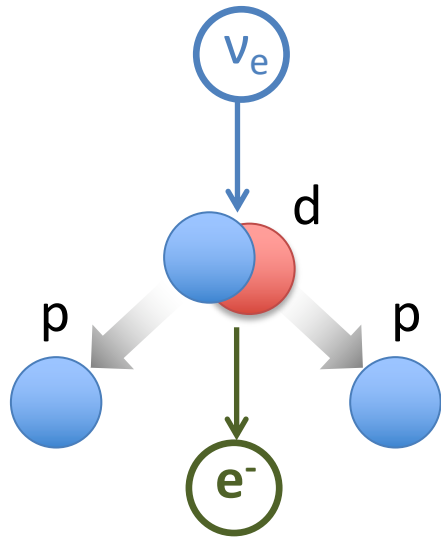
# Neutrino detection in SNO



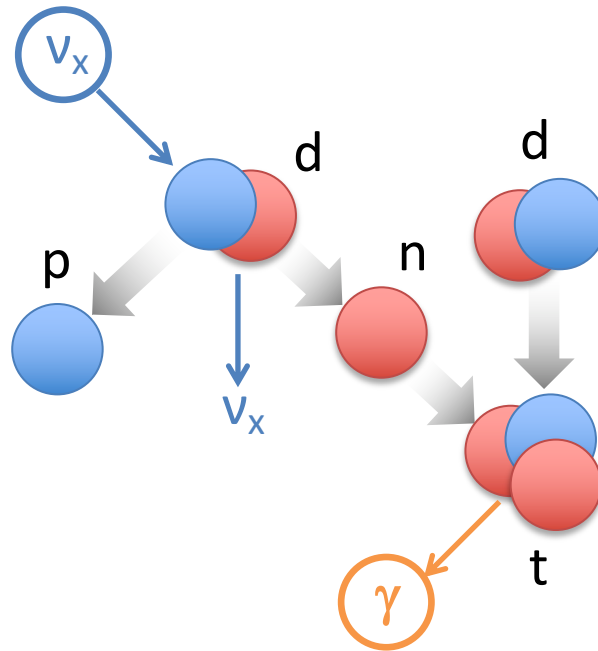
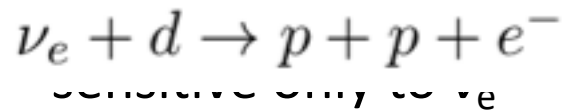
*10,000 photomultiplier tubes*



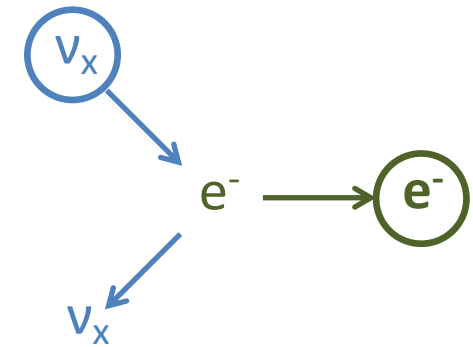
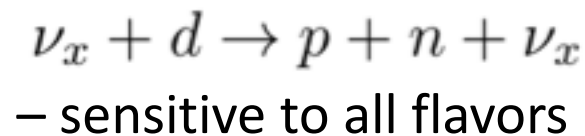
# Detection reactions in heavy water



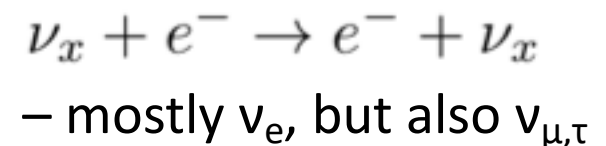
**(CC) on deuterons**



**(NC) on deuterons**



**elastic scattering  
on electrons (ES)**



→ determine **total neutrino flux (all flavors)** and  **$\nu_e$ -flux** separately



# 2002: SNO result on flavor conversion

The fluxes measured via the three channels were:

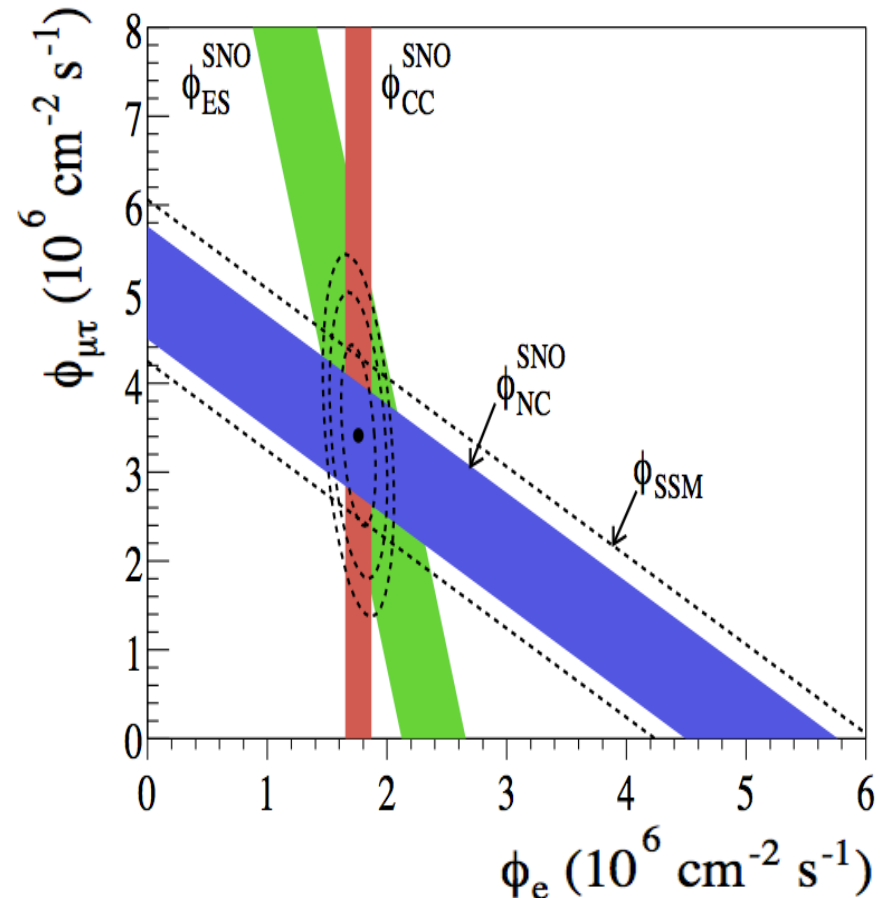
$$\left. \begin{array}{l} \Phi_{\text{CC}} = 1.76 \pm 0.11 \\ \Phi_{\text{ES}} = 2.39 \pm 0.27 \\ \Phi_{\text{NC}} = 5.09 \pm 0.62 \end{array} \right\} \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

The Standard Solar Model prediction for  ${}^8\text{B}$ - $\nu$ 's is:

$$\Phi_{\text{SSM}} = (5.05^{+1.01}_{-0.81}) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

- The survival probability for  $\nu_e$  measured in (CC) channel is  $P_{ee} \approx 35\%$ .
- The overall neutrino flux of (NC) corresponds to the SSM prediction as  $\nu_e$  converted to  $\nu_{\mu,\tau}$  still contribute to the (NC) rate.

- total flux (all flavors) as predicted by SSM
- $\nu_e$  flux suppressed by oscillations
- cross-check: elastic scattering (mostly  $\nu_e$ )



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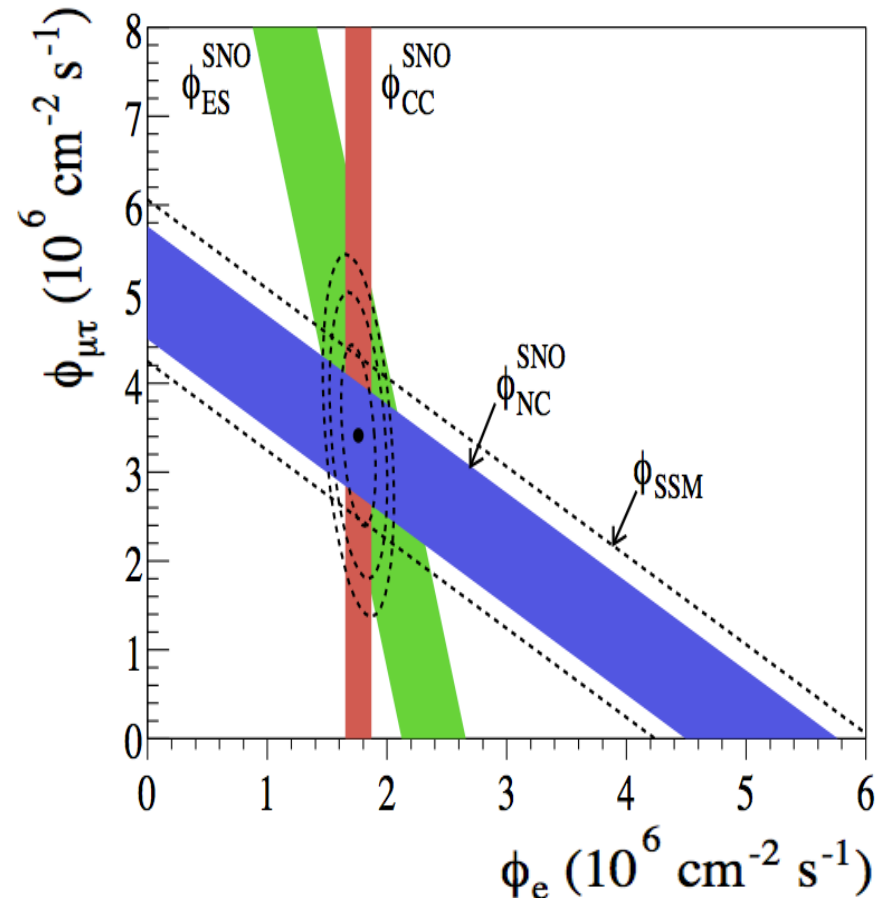
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- total flux (all flavors) as predicted by SSM
- $\nu_e$  flux suppressed by oscillations
- cross-check: elastic scattering (mostly  $\nu_e$ )



**but:**  
SNO proves only flavor conversion  
what about the oscillation pattern?

# LECTURE QUIZ

## Question 1

How many solar neutrinos are passing through your thumbnail every second?

B : 60 thousand

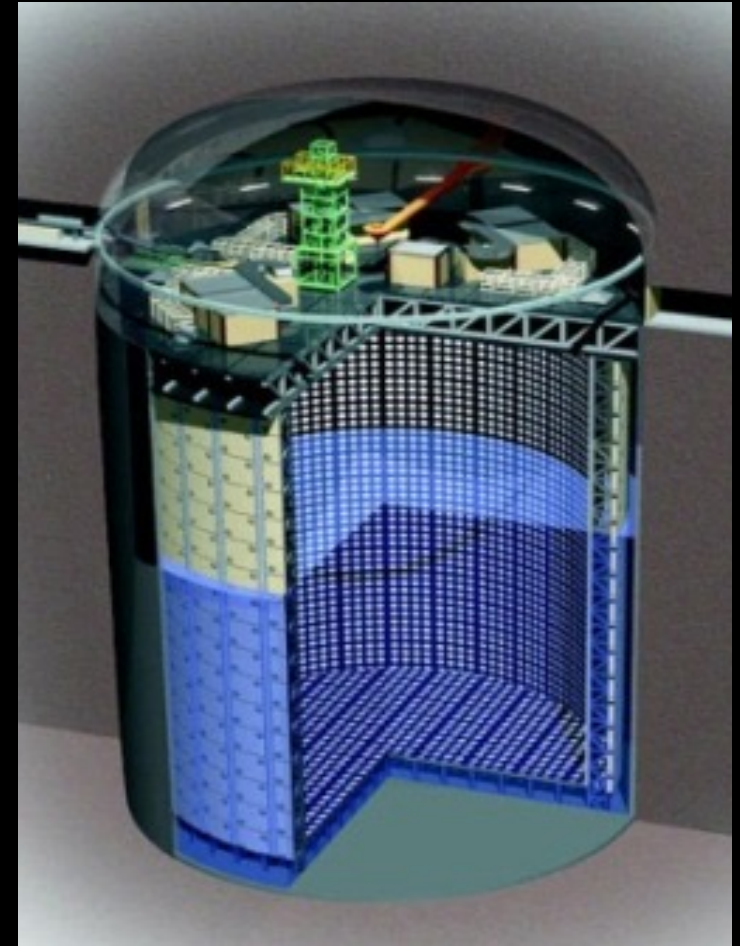
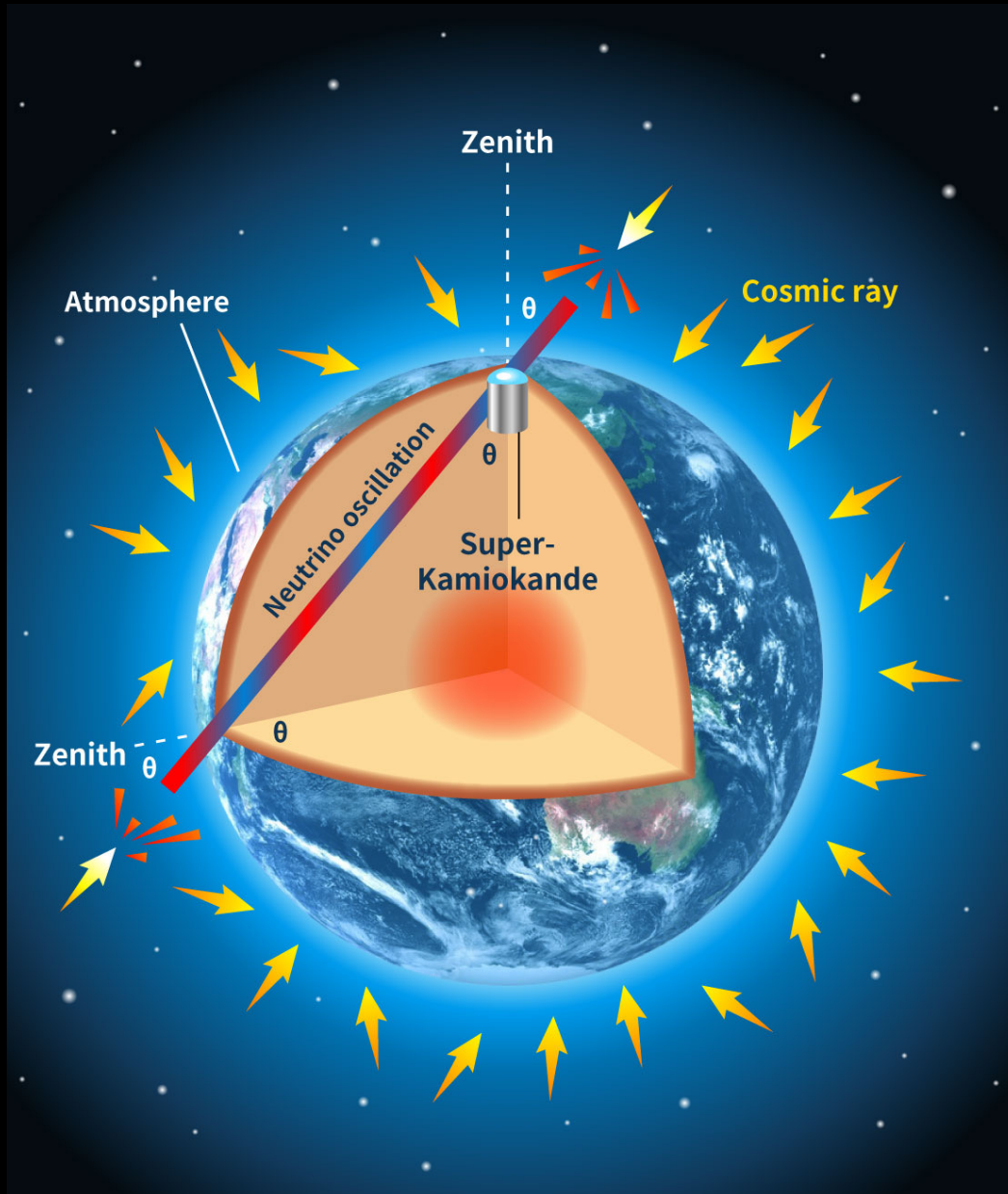
C : 60 million

D : 60 billion



Note down the **letter** in front of the solution.

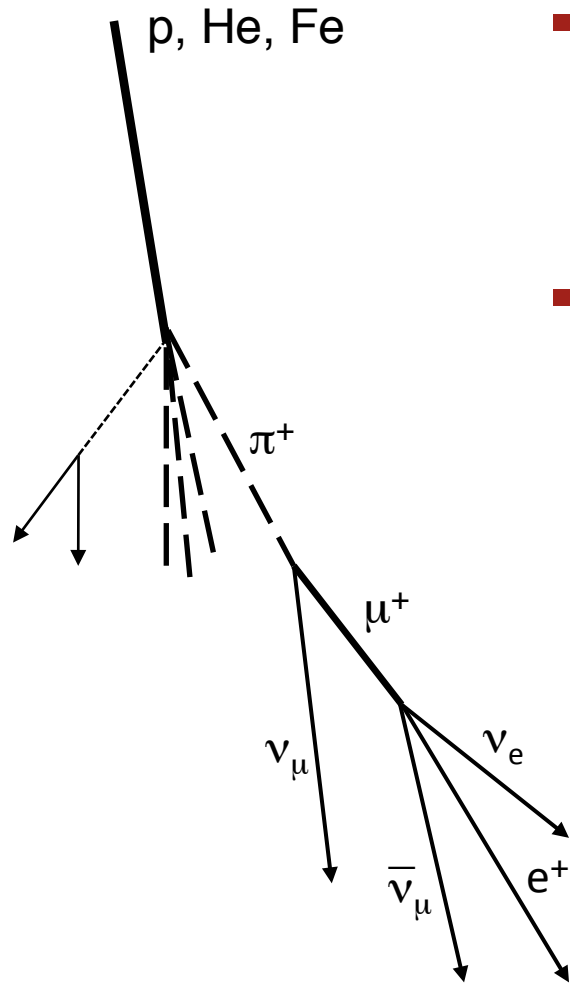
# Atmospheric $\nu$ 's in Super-Kamiokande



Super-Kamiokande  
dimensions: 45m x 45m  
target mass: 50 kton  
light readout: 11,200 20"-PMTs



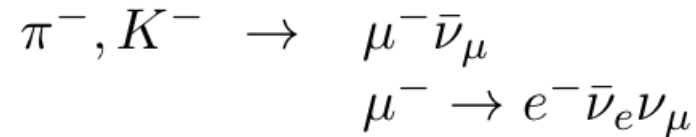
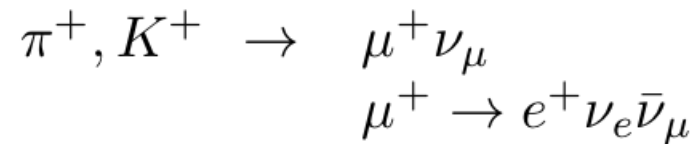
# Atmospheric neutrino production



- High-energy cosmic rays collide with nitrogen in the Earth's atmosphere



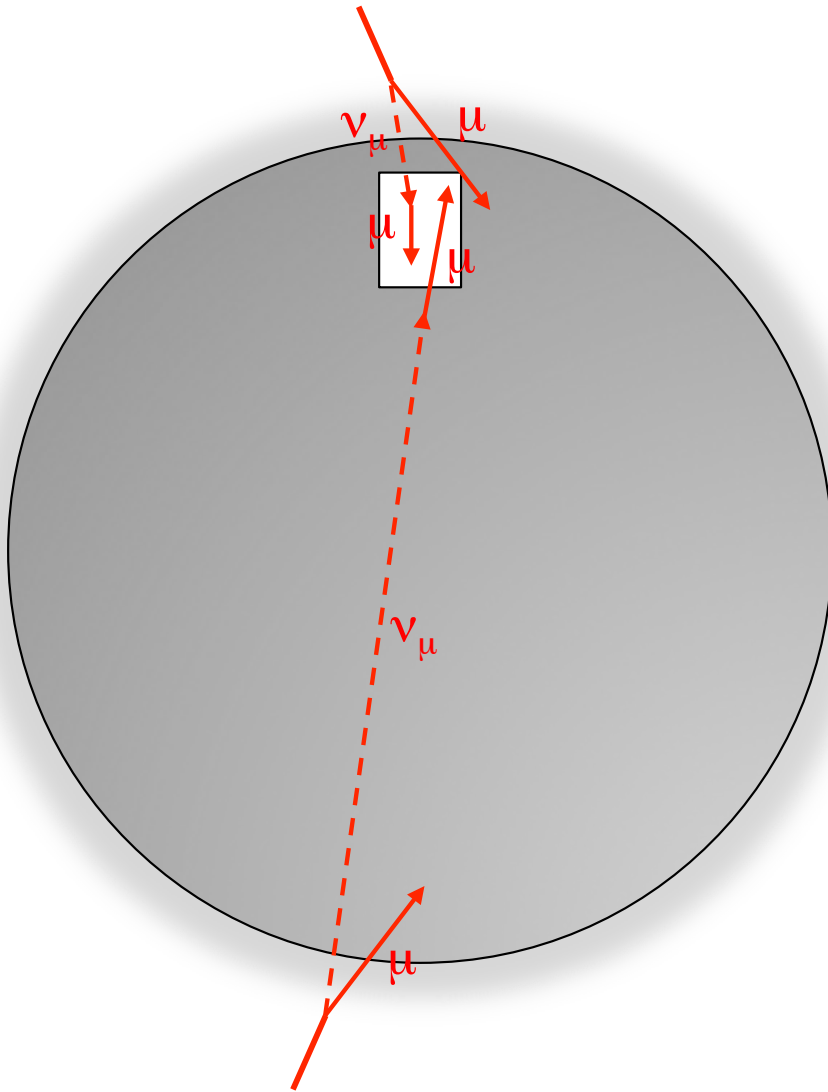
- Charged mesons decay into neutrinos:



→ **Flavor ratio:**

At GeV energies, the expected ratio of  $\nu_\mu$  to  $\nu_e$  is  $R_{\text{th}} = 2$ .

# Angular distribution of atmospheric $\nu$ 's

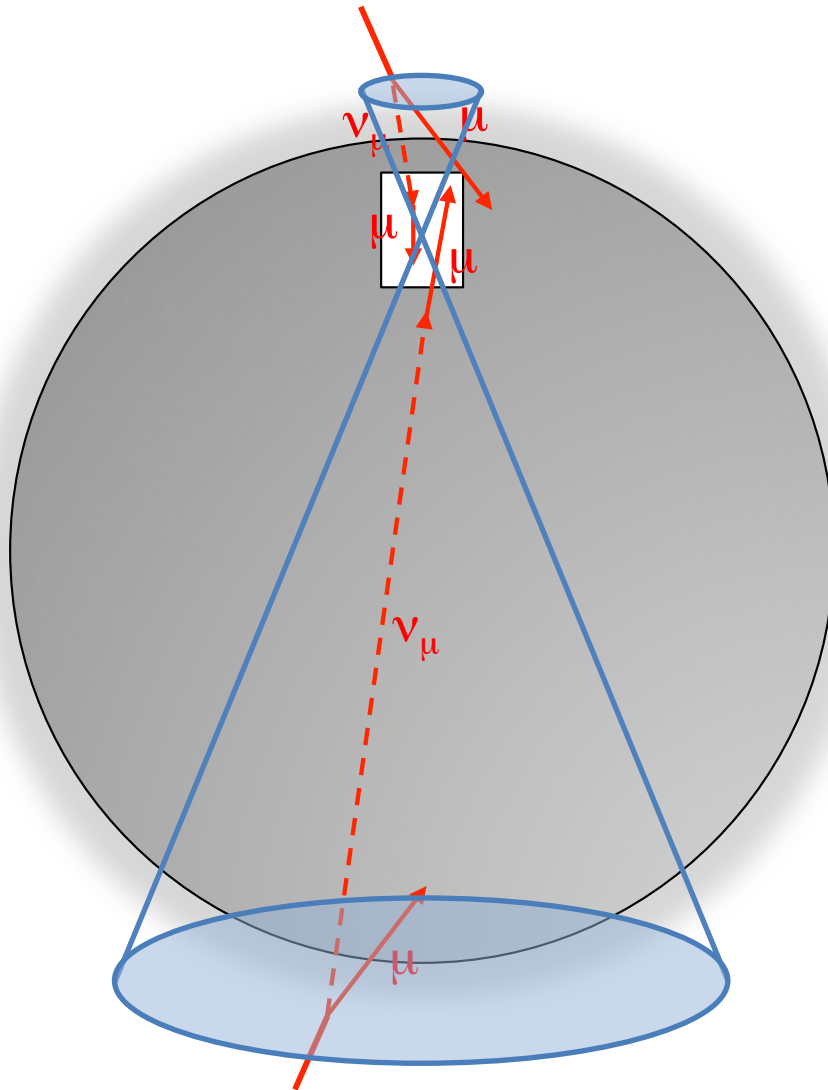


- Neutrinos are the only particles to cross the Earth from the antipodes.
- Arrival direction described by zenith angle:

$\cos\theta = +1$  for zenith

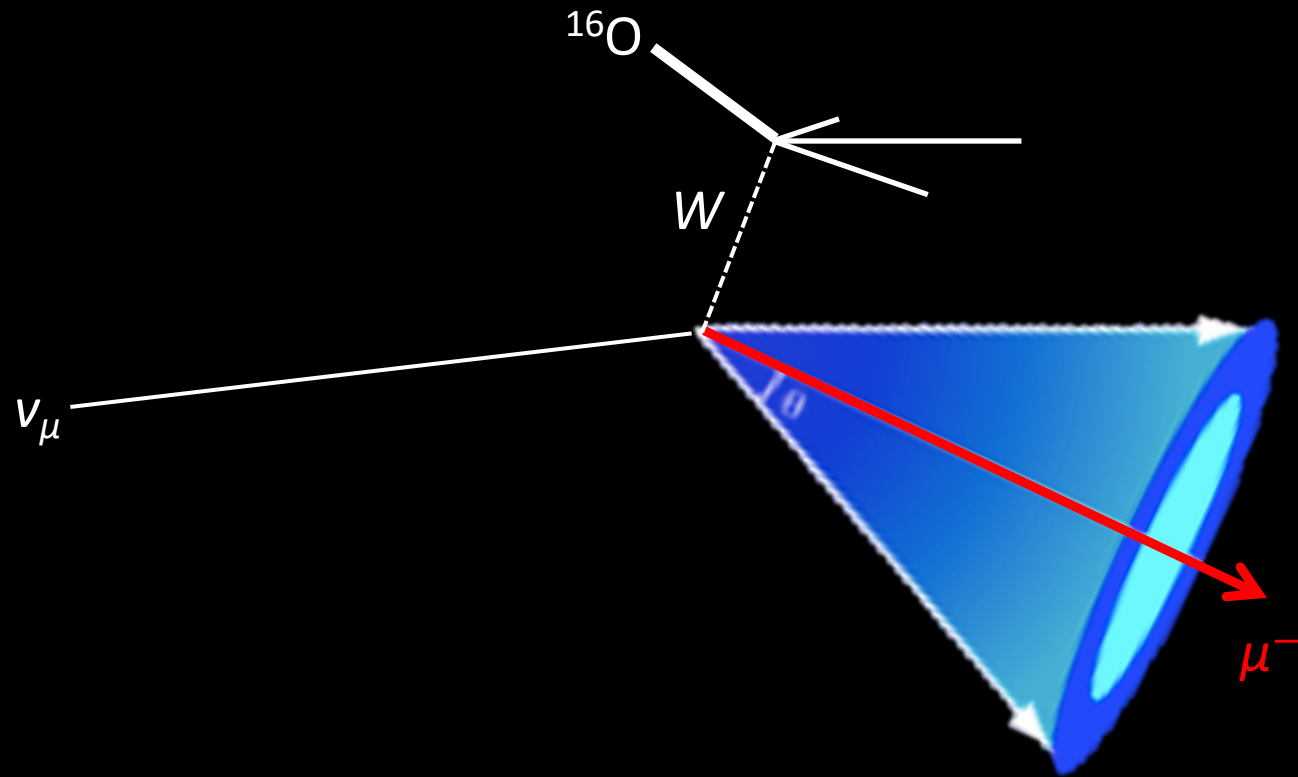
$\cos\theta = -1$  for nadir

# Angular distribution of atmospheric $\nu$ 's



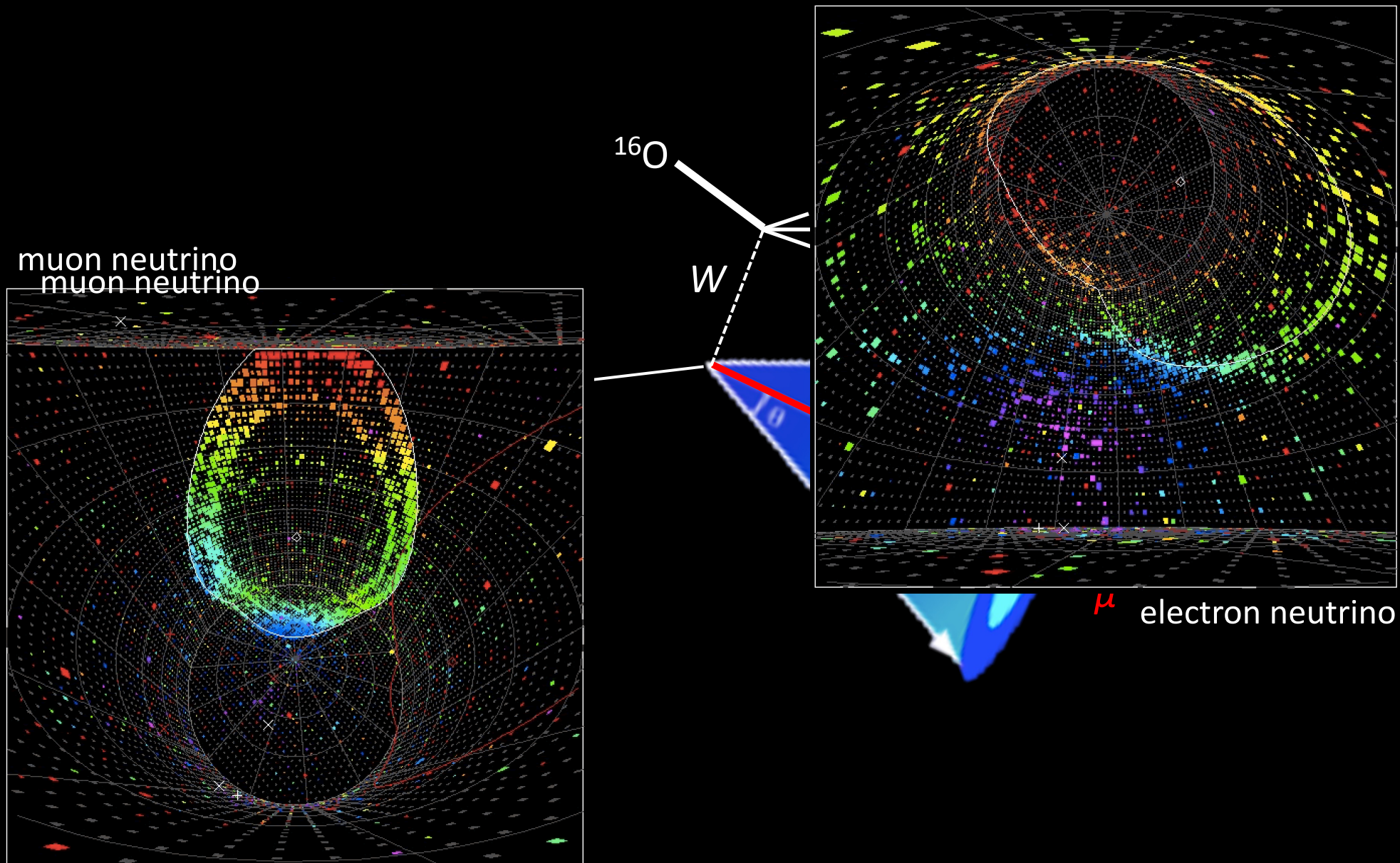
- Neutrinos are the only particles to cross the Earth from the antipodes.
  - Arrival direction described by zenith angle:  
 $\cos\theta = +1$  for zenith  
 $\cos\theta = -1$  for nadir
- In first approximation, the atmospheric  $\nu$  flux should be independent of the zenith angle  $\theta$ .

# Neutrino detection by Cherenkov effect





# Flavor identification by ring *fuzziness*

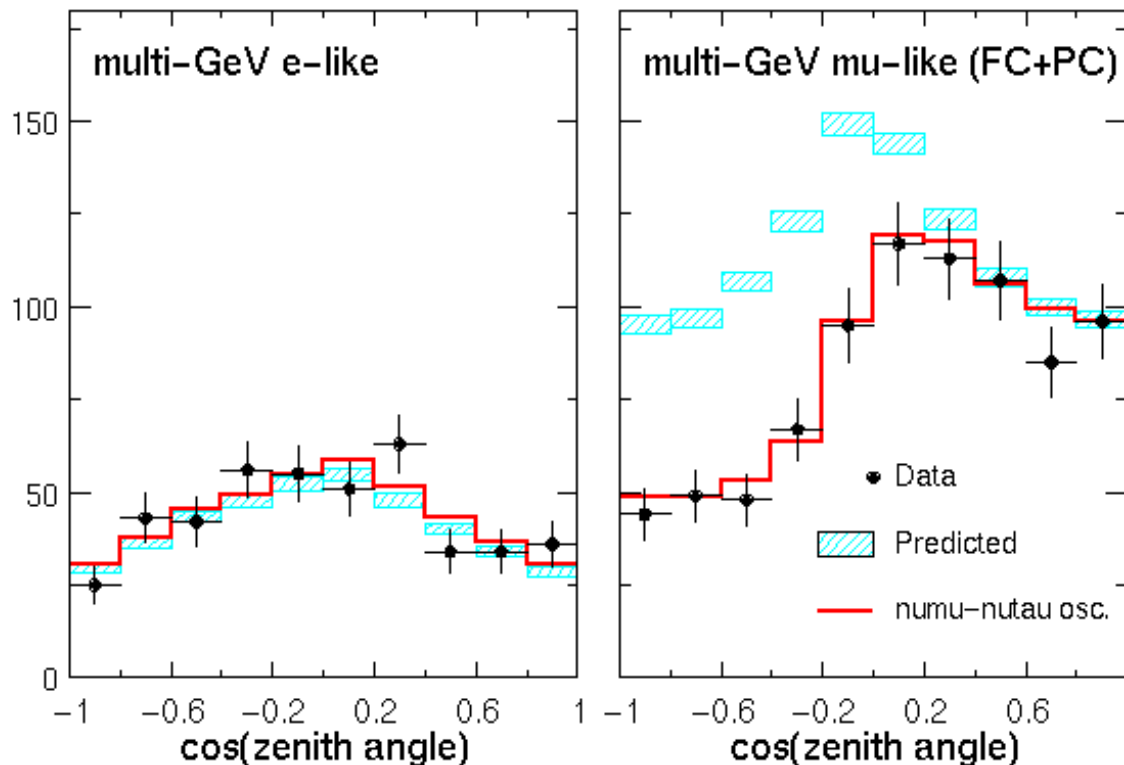


# 1998: Super-Kamiokande result

- At low neutrino energies, the measured ratio  $R_{\text{exp}}$  of  $\nu_{\mu} : \nu_e$  was lower than the expectation:

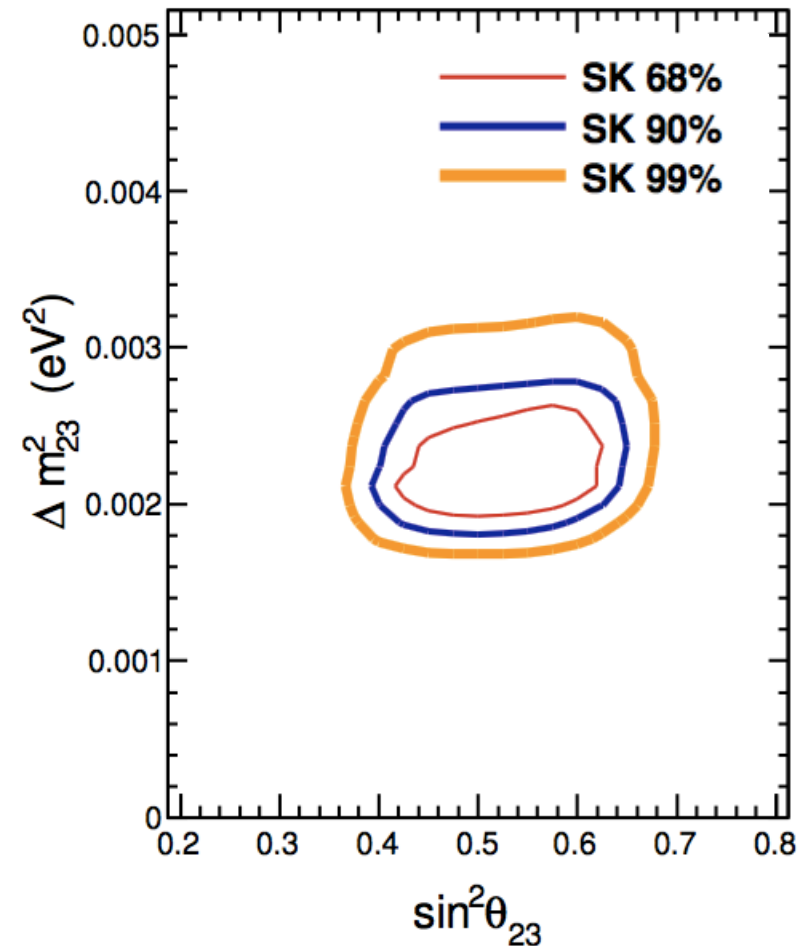
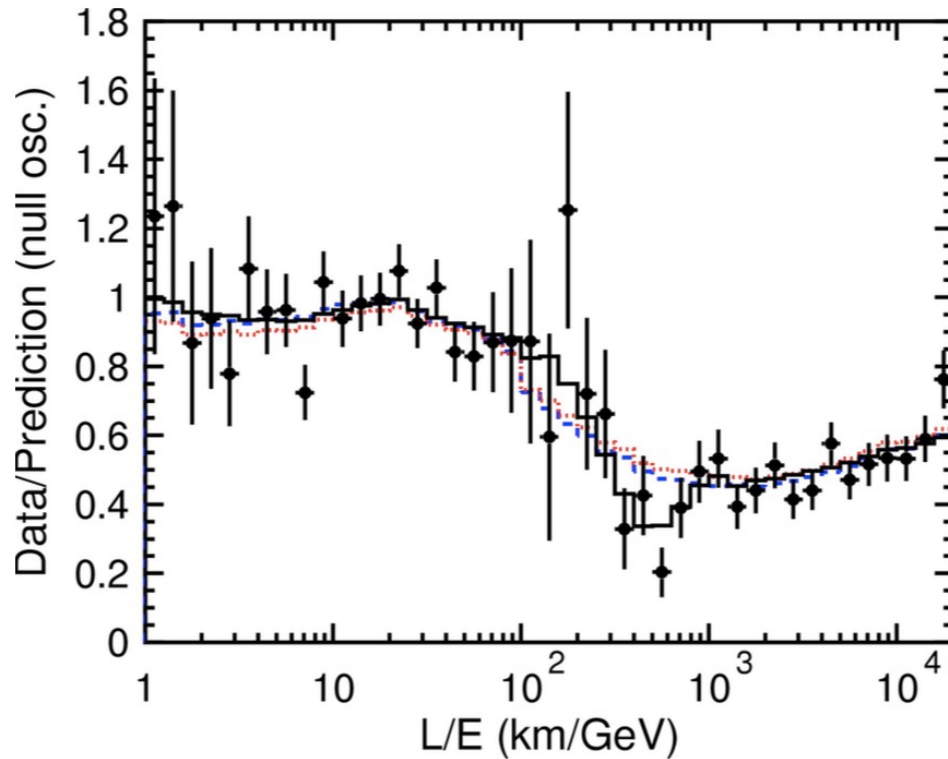
$$R_{\text{exp}}/R_{\text{th}} = 0.63 \pm 0.03_{\text{stat}} \pm 0.05_{\text{syst}}$$

- At high neutrino energies, asymmetry in angular distribution



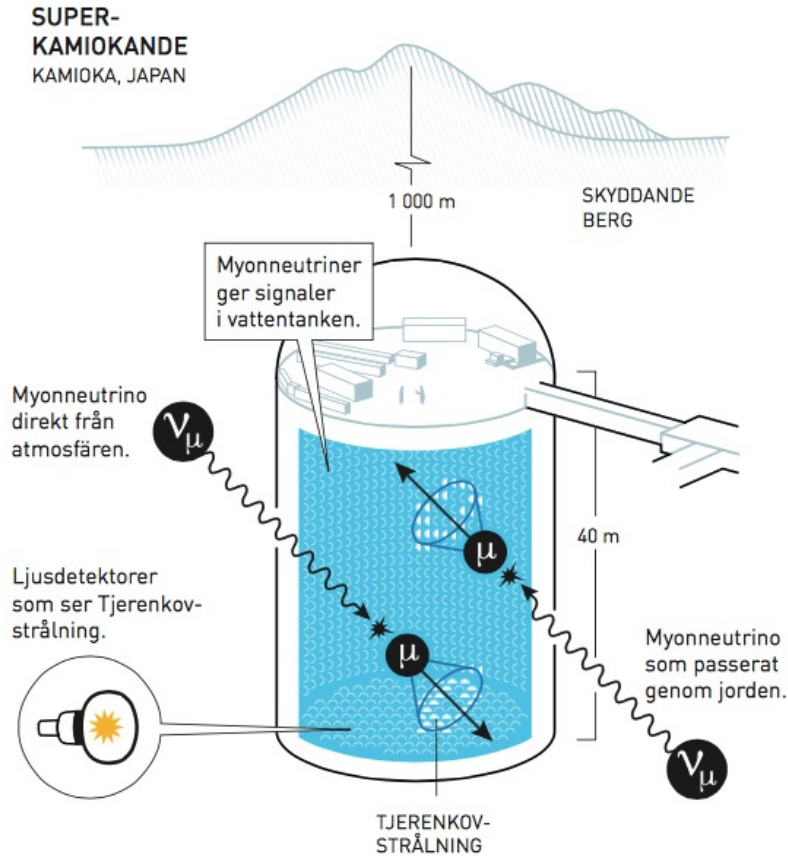
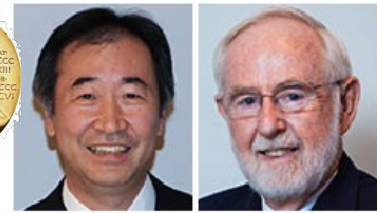
- down-going ( $\cos\theta=1$ ):  
baseline:  $\sim 20$  km  
 $\rightarrow$  no oscillations
- up-going ( $\cos\theta=-1$ ):  
baseline  $\leq 13,000$  km  
 $\rightarrow \nu_{\mu}$  disappearance
- no  $\nu_e$  excess observed:  
 $\rightarrow$  oscillations are  $\nu_{\mu} \rightarrow \nu_{\tau}$
- surprise: large amplitude!  
 $\rightarrow$  today:  $\theta_{23} \approx 45^\circ$

# Later SK data on atmospheric $\nu$ 's

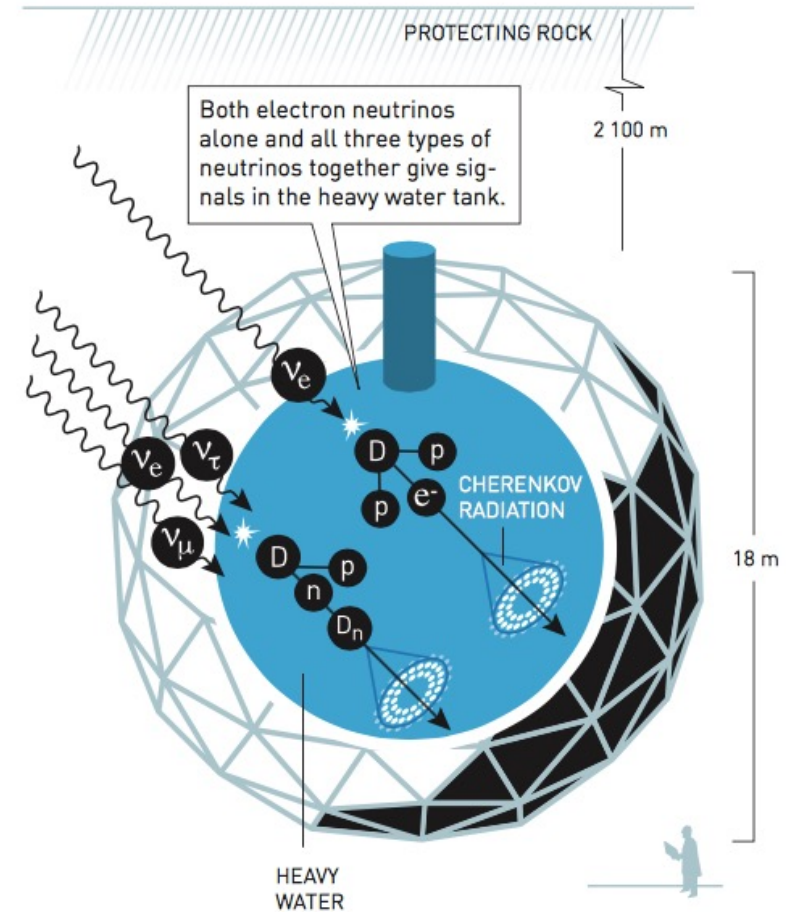


- oscillation-like L/E structure found
- evidence ( $4.6\sigma$ ) for  $\nu_\tau$ -appearance in the detector
- still unclear whether  $\sin^2 2\theta_{23} < 1$  ( $\theta_{23} \neq 45^\circ$ )

# Nobel Prize in Physics 2015



→  $\nu_\mu$  disappear with the correct L/E dependence of oscillations



→  $\nu_e$  disappear and re-appear as  $\nu_{\mu,\tau}$

→ neutrinos undergo **flavor oscillations** and at least 2 neutrino states have mass!



# LECTURE QUIZ

## Question 2

What is the expected ratio of electron to muon neutrinos created by pion decay in the Earth's atmosphere (i.e. without oscillations)?

G) 2:1

H) 1:1

I) 1:2



# Current Status of Neutrino Oscillations

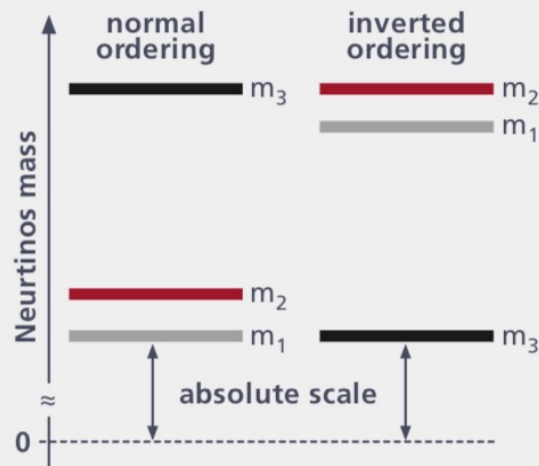
## Mixing angles

PMNS mixing matrix  $U_{3 \times 3} \rightarrow 3$  mixing angles + CP phase

$$\text{flavor states} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \text{mass states}$$

## Mass splittings

- Squared mass differences  $\rightarrow$  oscillation frequencies
- Absolute mass scale not constrained by oscillations



## Mixing angles

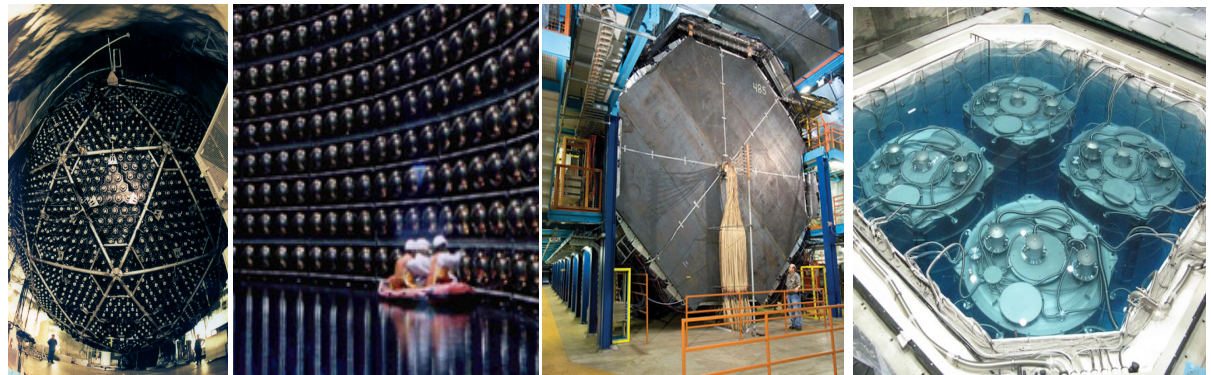
(NMO,  $1\sigma$  unc.)

- $\theta_{12} = 33.7^\circ \pm 0.7^\circ$
- $\theta_{23} = 49.1^\circ \begin{smallmatrix} +1.3^\circ \\ -1.0^\circ \end{smallmatrix}$
- $\theta_{13} = 8.5^\circ \pm 0.1^\circ$

## Mass splittings (NMO, $1\sigma$ unc.)

- $\Delta m_{21}^2 = 7.4 \pm 0.2 \times 10^{-5} \text{eV}^2$
- $\Delta m_{31}^2 = 2.51 \pm 0.03 \times 10^{-3} \text{eV}^2$

based on combination of results from solar, reactor, atmospheric, accelerator ... experiments



# Open Issues in 3-Flavor Oscillations

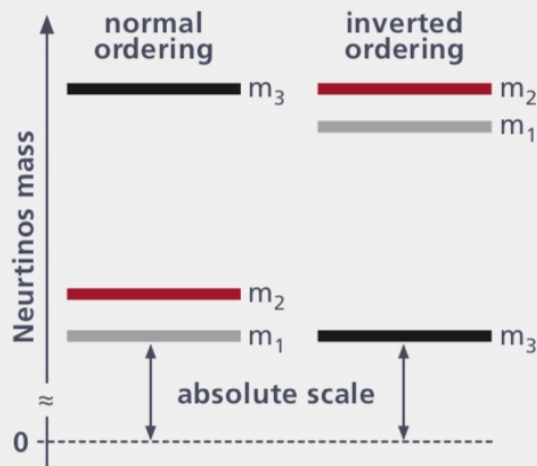
## Mixing Angles

PMNS mixing matrix  $U_{3 \times 3} \rightarrow 3$  mixing angles + CP phase

$$\text{flavor states} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \text{mass states}$$

## Mass Splittings

- Squared mass differences  $\rightarrow$  oscillation frequencies
- Absolute mass scale not constrained by oscillations



What is the octant of  $\theta_{23}$ ?

What is the phase  $\delta_{CP}$  of leptonic CP violation?

Is the PMNS matrix unitary?

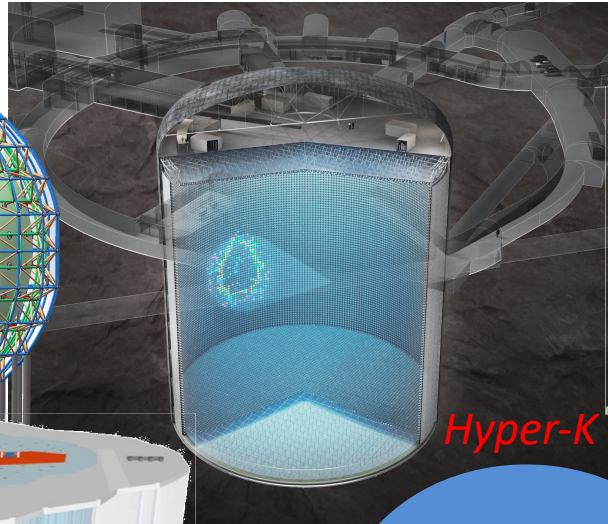
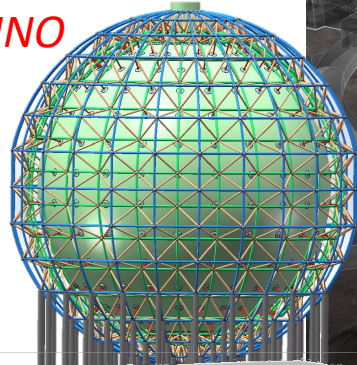
Is it the cause of baryon asymmetry?

What is the neutrino mass ordering?

Are there additional sterile neutrinos?

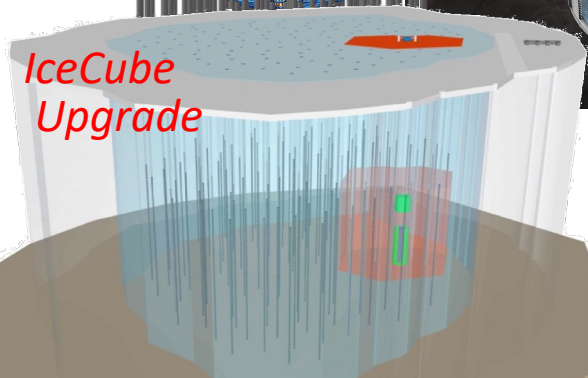
# Upcoming Oscillation Experiments

JUNO

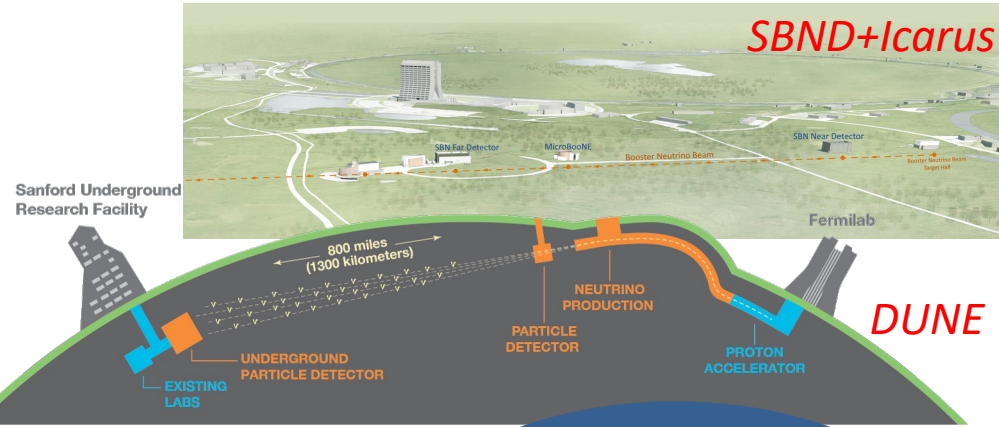
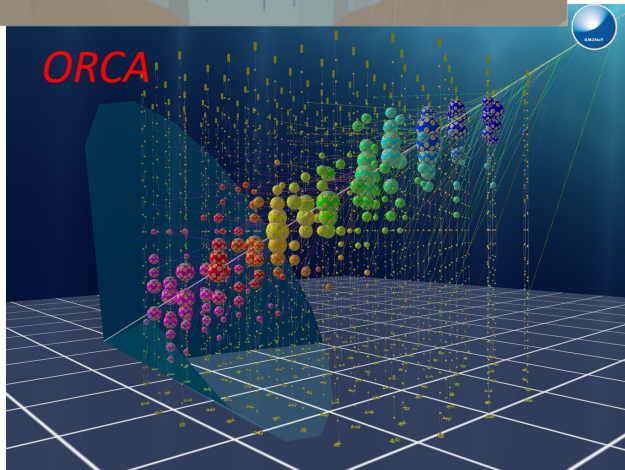


Hyper-K

IceCube Upgrade



ORCA



SBND+Icarus

DUNE

What is the octant of  $\theta_{23}$ ?

Is the PMNS matrix unitary?

What is the phase  $\delta_{CP}$  of leptonic CP violation?

Is it the cause of baryon asymmetry?

What is the neutrino mass ordering?

Are there additional sterile neutrinos?



# LECTURE QUIZ

## Question 3

At what precision do we know the neutrino mixing angles?

M :  $0.1^\circ$

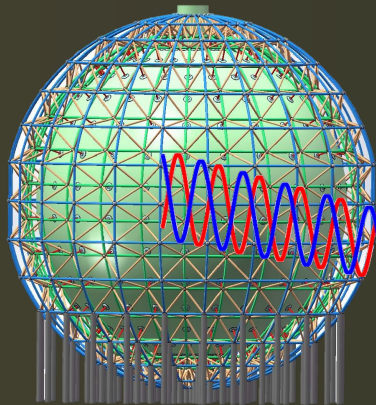
N :  $1^\circ$

O :  $10^\circ$

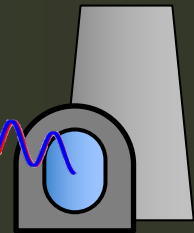


# Experiments for Neutrino Mass Ordering

DUNE.



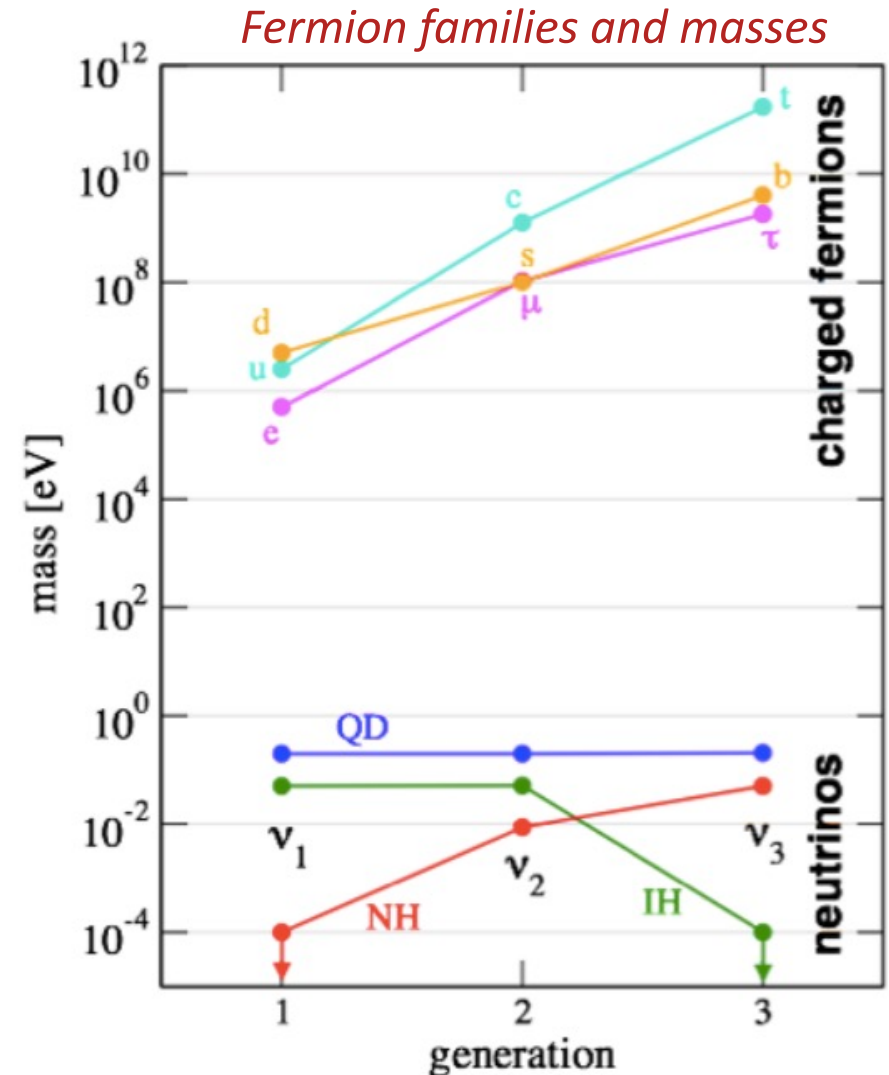
JUNO.



ORCA/PINGU  
Hyper-K

# Neutrino Mass Ordering (Hierarchy)

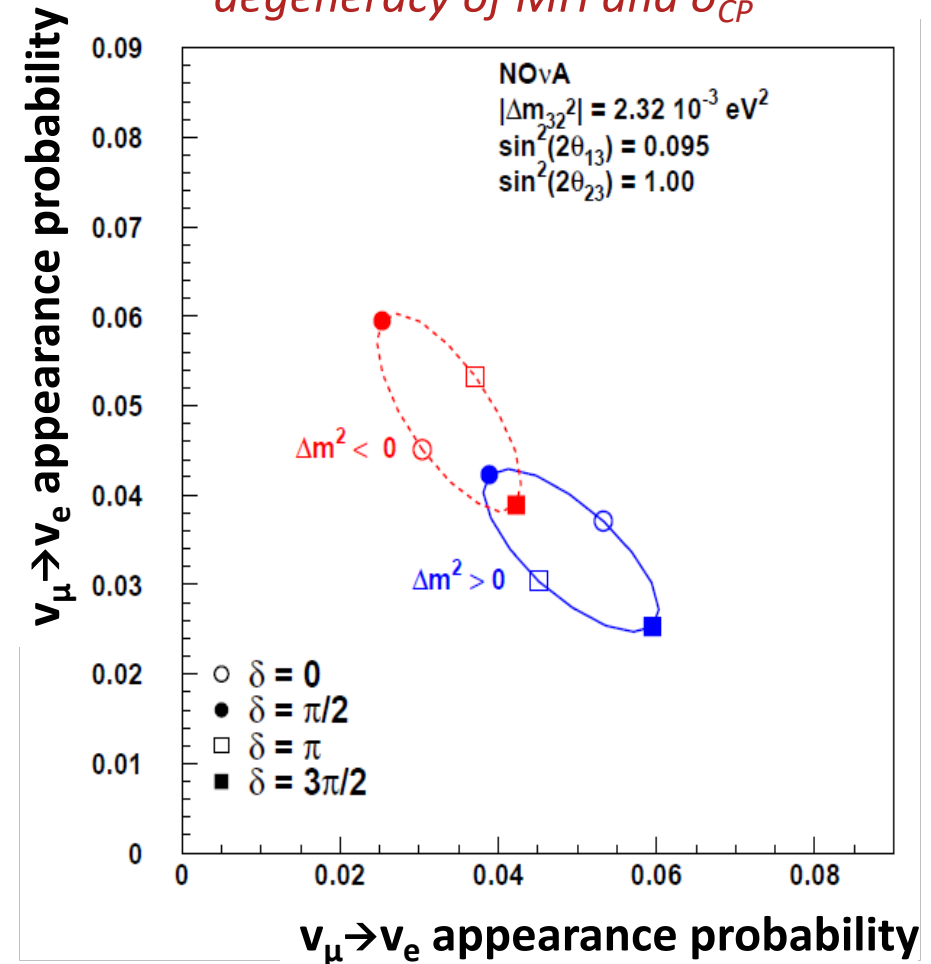
- **Arrangement** of the neutrino masses
  - as in quark sector  
→ normal mass ordering (NMO)
  - opposed to it  
→ inverted mass ordering (IMO)
  - w/o clear ordering  
→ quasi-degenerate (QD)



# Neutrino Mass Ordering (Hierarchy)

- **Arrangement** of the neutrino masses
  - as in quark sector
    - normal mass ordering (NMO)
  - opposed to it
    - inverted mass ordering (IMO)
  - w/o clear ordering
    - quasi-degenerate (QD)
  
- resolving the **degeneracy** in the interpretation of  $\delta_{CP}$  measurements

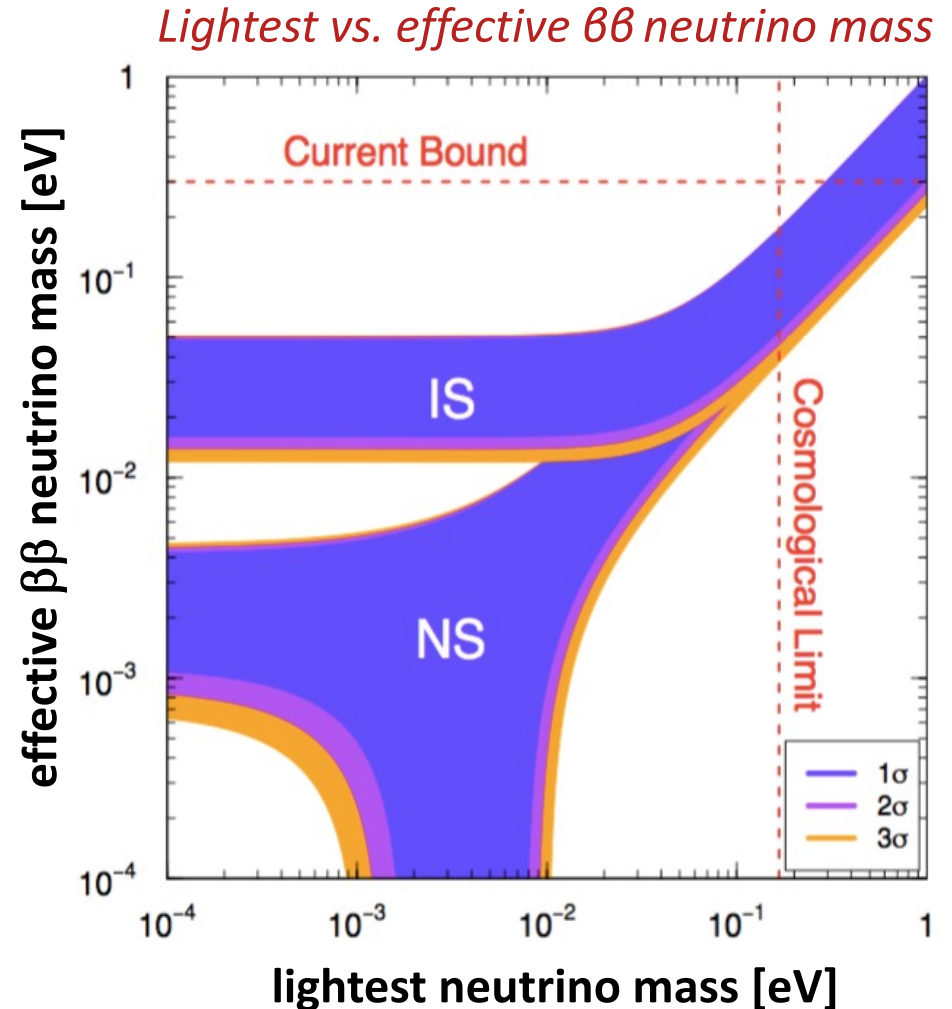
*long baseline experiments:  
degeneracy of MH and  $\delta_{CP}$*





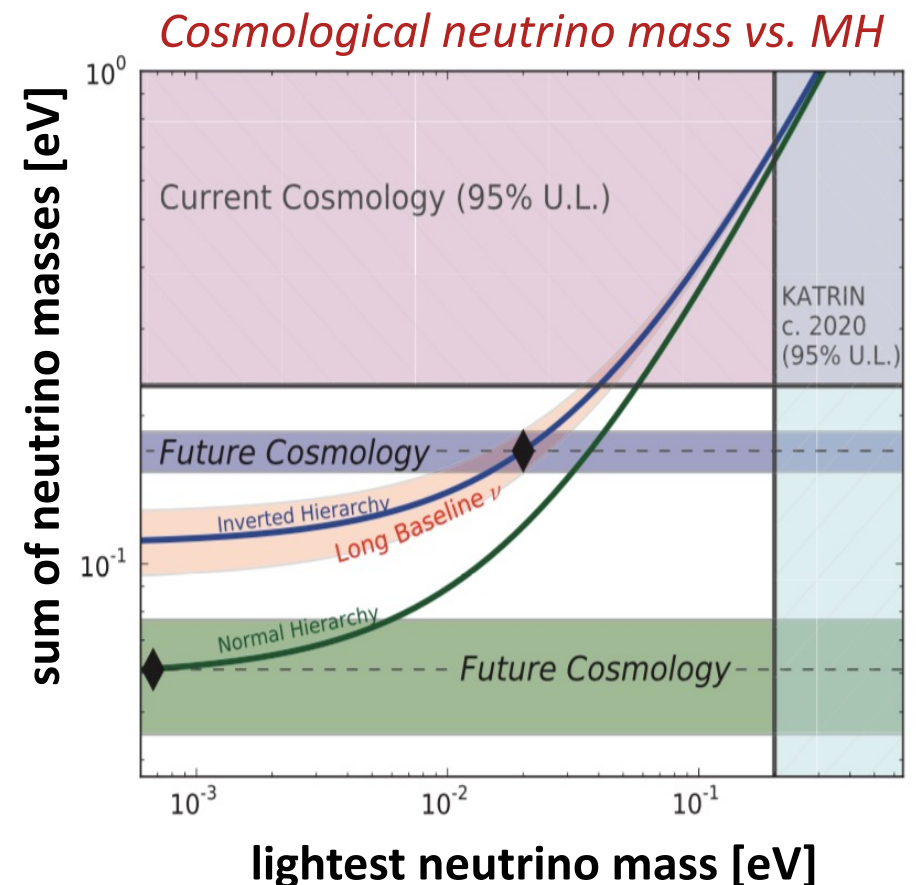
# Neutrino Mass Ordering (Hierarchy)

- **Arrangement** of the neutrino masses
  - as in quark sector
    - normal mass ordering (NMO)
  - opposed to it
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    - quasi-degenerate (QD)
- resolving the **degeneracy** in the interpretation of  $\delta_{CP}$  measurements
- target range for **sensitivity** of  $0\nu\beta\beta$  decay experiments



# Neutrino Mass Ordering (Hierarchy)

- **Arrangement of the neutrino masses**
  - as in quark sector  
→ normal mass ordering (NMO)
  - opposed to it  
→ inverted mass ordering (IMO)
  - w/o clear ordering  
→ quasi-degenerate (QD)
- resolving the **degeneracy** in the interpretation of  $\delta_{CP}$  measurements
- target range for **sensitivity** of  $0\nu\beta\beta$  decay experiments
- combination with **cosmology** to find **lightest neutrino mass**



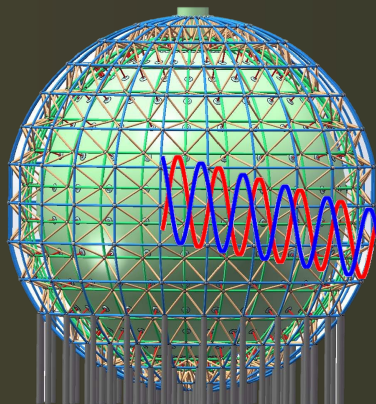
# Measuring the Neutrino Mass Ordering

1 Mid-baseline reactor neutrino oscillations

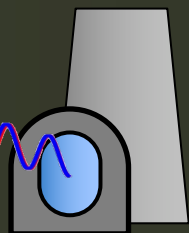
2 Low-energy atmospheric neutrino oscillations

3 Very-Long Baseline Neutrino Beams

DUNE.



JUNO.

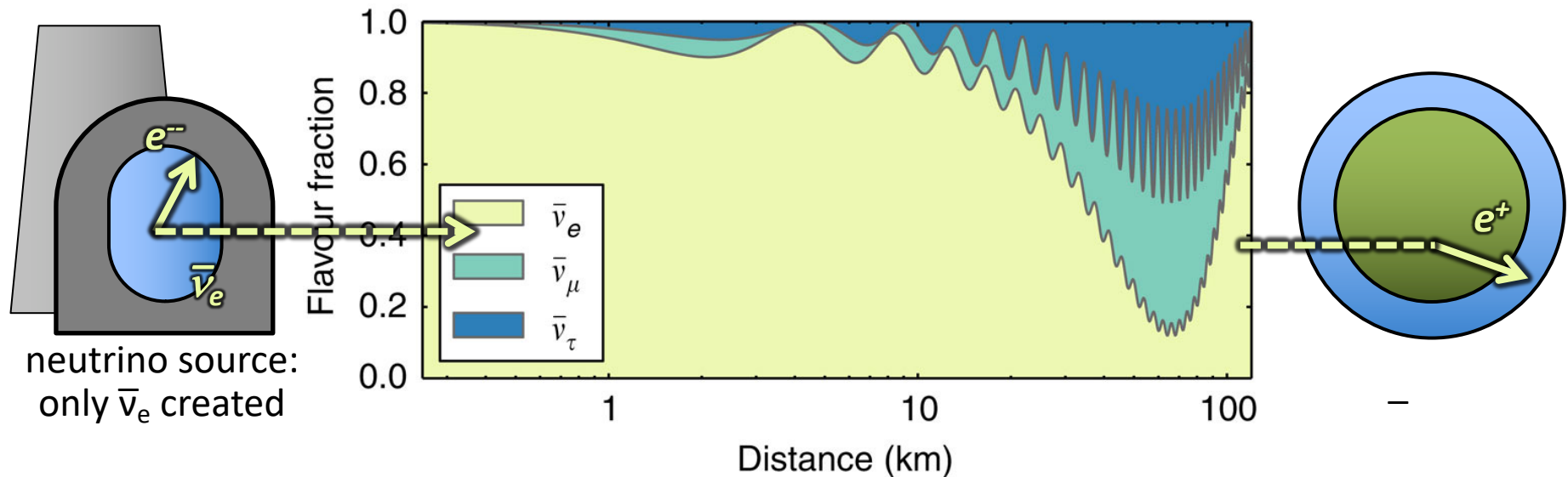


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# Standard oscillations and $\Delta m^2_{ij}$ values

Common three-flavor reactor electron-antineutrino survival probability:

$$P_{ee} = 1 - \sin^2(2\theta_{13}) \sin^2\left(\frac{\Delta m^2_{31}}{4E}\right) - \sin^2(2\theta_{12}) \sin^2\left(\frac{\Delta m^2_{21}}{4E}\right)$$



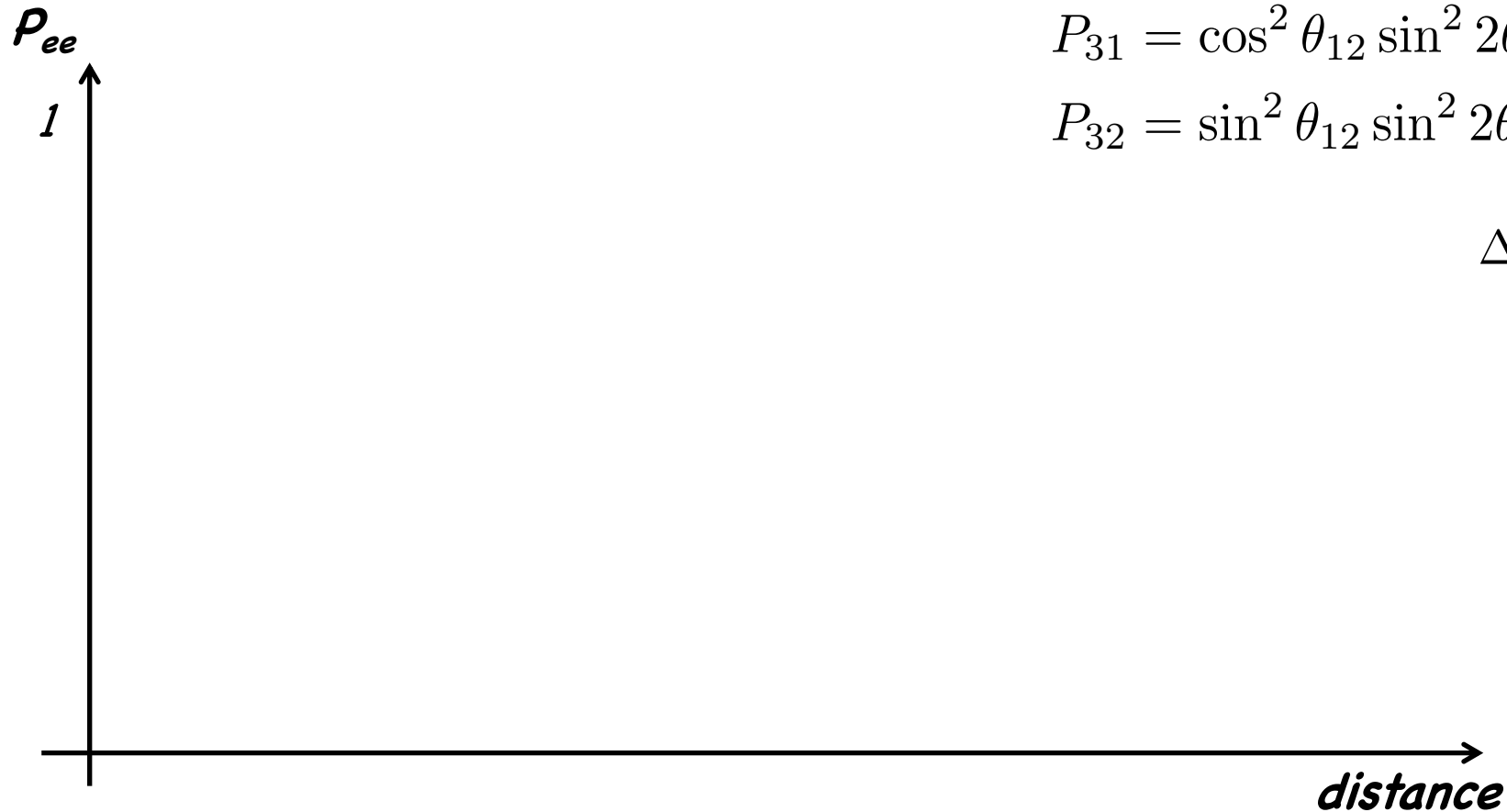
→ oscillation parameters are extracted from  $\bar{\nu}_e$  **disappearance pattern**

→ due to the  $\sin^2$  terms,  $P_{ee}$  terms do not depend on sign of  $\Delta m^2_{ij}$

→ however, the formula above implicitly assumes  $\Delta m^2_{31} = \Delta m^2_{32}$



# NMO from reactor $\bar{\nu}_e$ disappearance



*Survival probability*

$$P_{\bar{e}\bar{e}} = 1 - P_{21} - P_{31} - P_{32}$$

$$P_{21} = \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21}$$

$$P_{31} = \cos^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 \Delta_{31}$$

$$P_{32} = \sin^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 \Delta_{32}$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2 L}{4E}$$

# NMO from reactor $\bar{\nu}_e$ disappearance

*Survival probability*

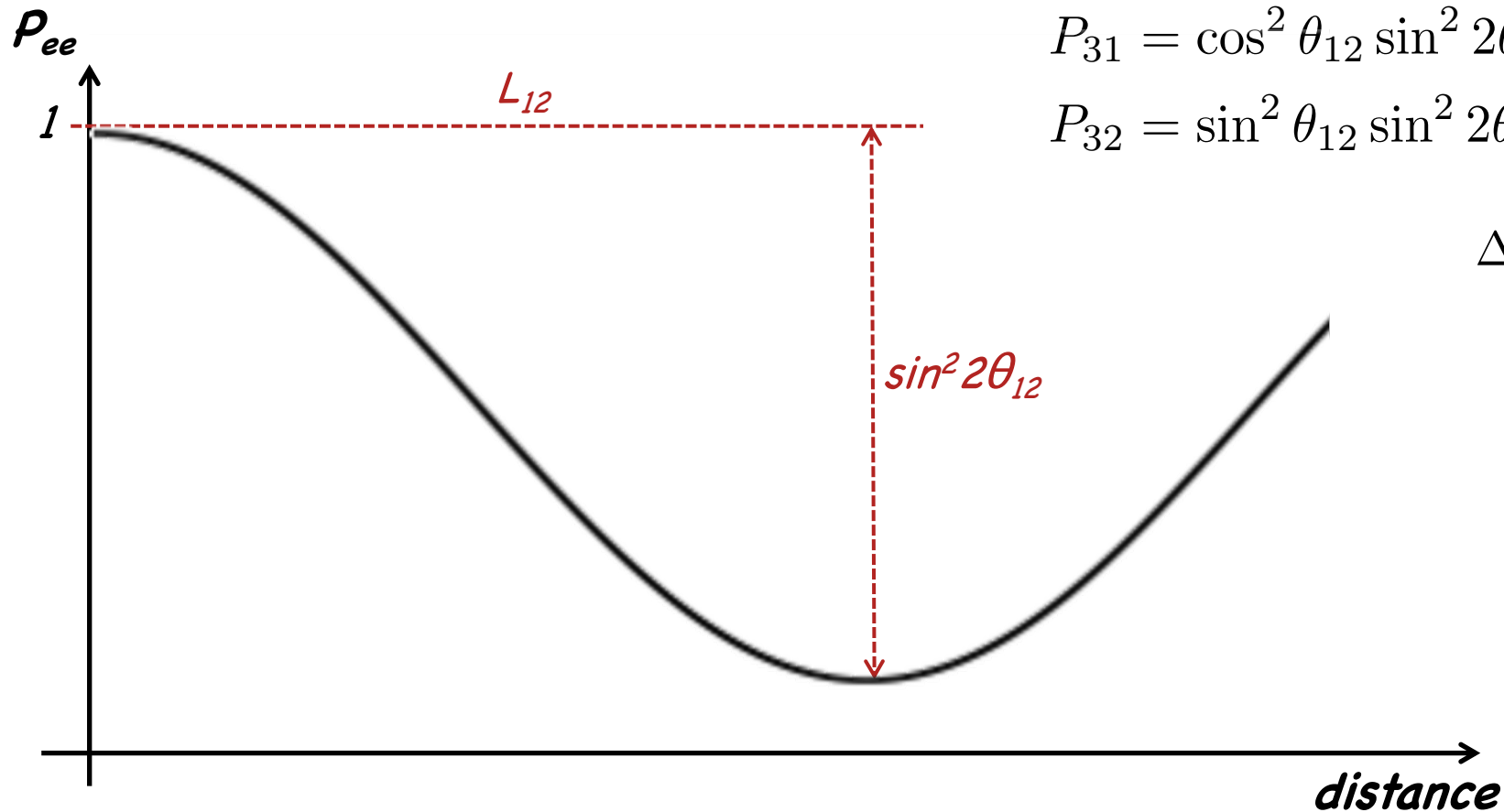
$$P_{\bar{e}\bar{e}} = 1 - P_{21} - P_{31} - P_{32}$$

$$P_{21} = \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21}$$

$$P_{31} = \cos^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 \Delta_{31}$$

$$P_{32} = \sin^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 \Delta_{32}$$

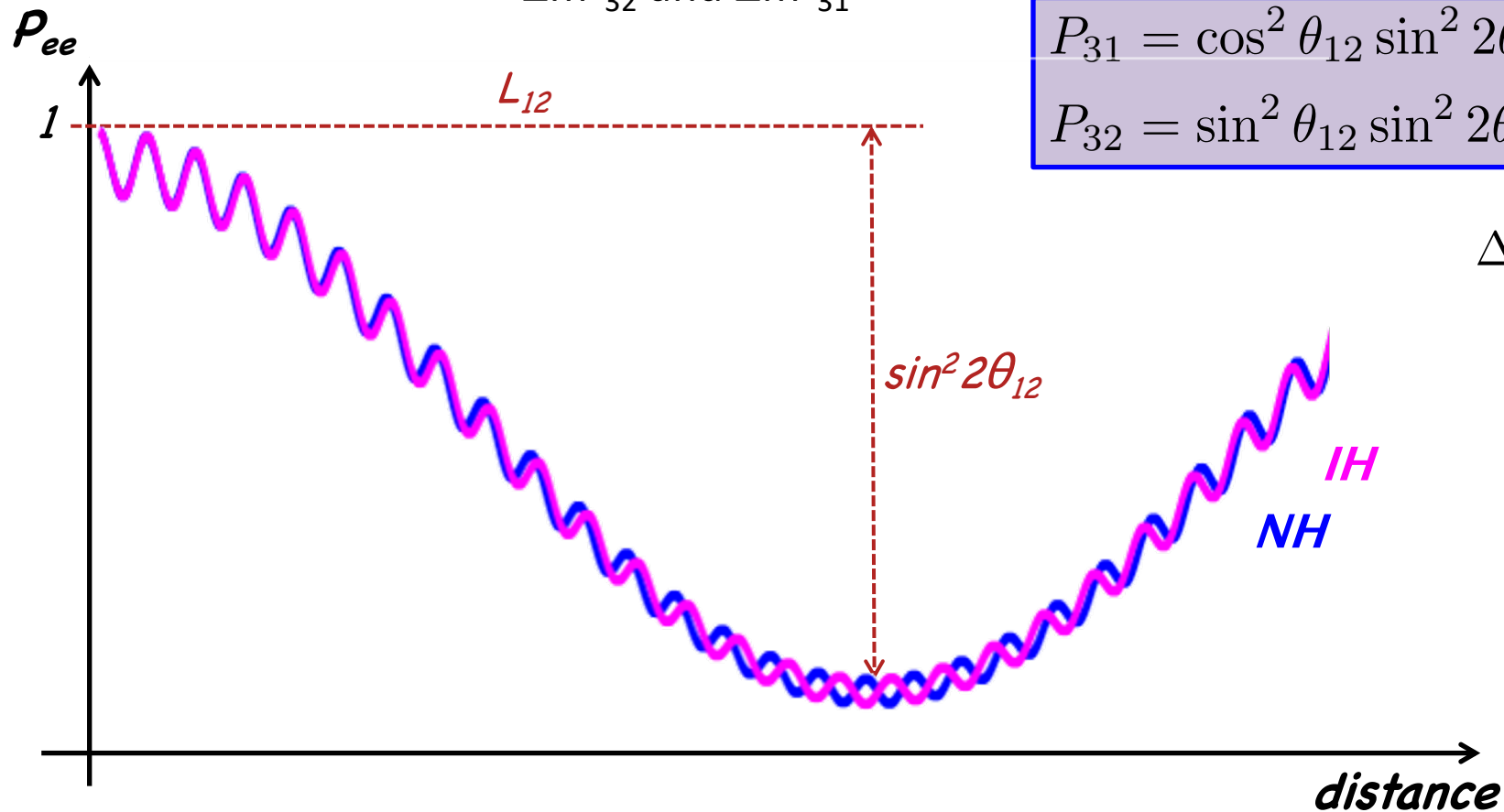
$$\Delta_{ij} = \frac{\Delta m_{ij}^2 L}{4E}$$



# NMO from reactor $\bar{\nu}_e$ disappearance

→ subdominant oscillation pattern depends on phase terms of  $P_{31}/P_{32}$

→ depends on **relative sizes** of  $\Delta m^2_{32}$  and  $\Delta m^2_{31}$



**Survival probability**

$$P_{\bar{e}\bar{e}} = 1 - P_{21} - P_{31} - P_{32}$$

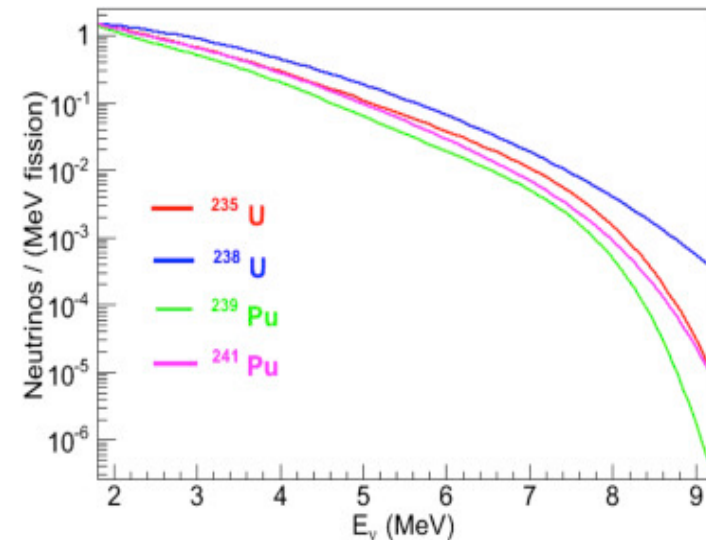
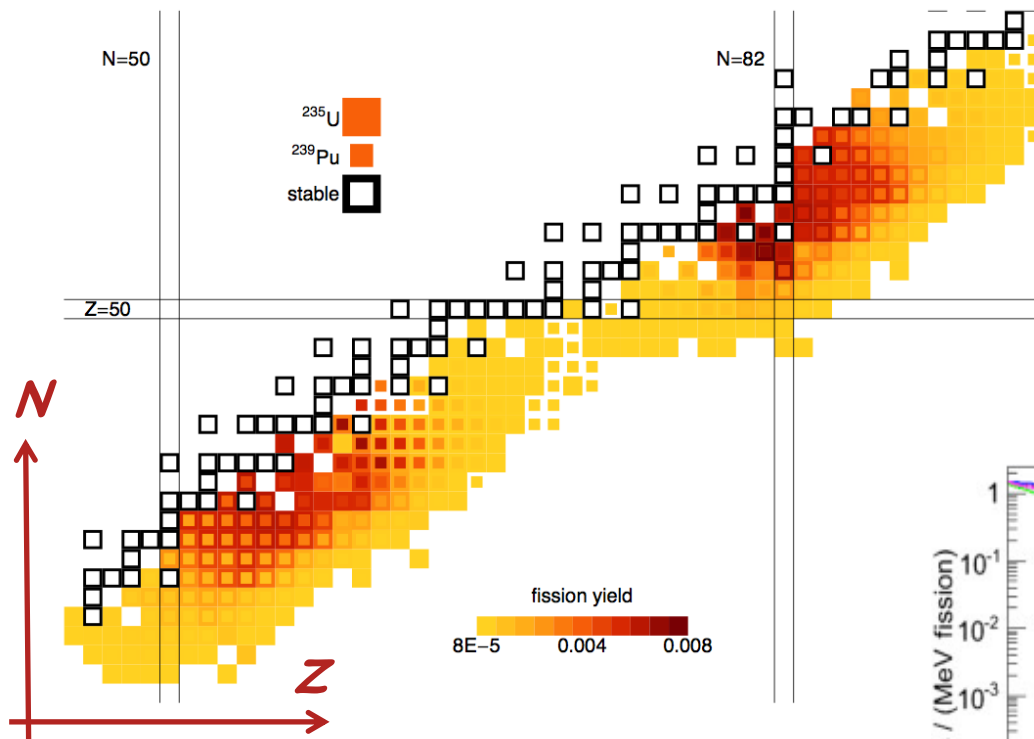
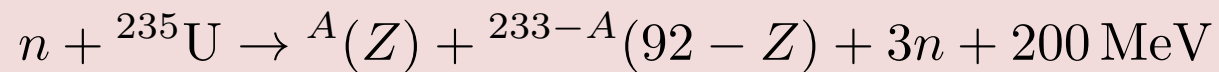
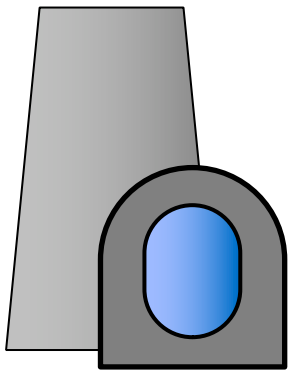
$$P_{21} = \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21}$$

$$P_{31} = \cos^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 \Delta_{31}$$

$$P_{32} = \sin^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 \Delta_{32}$$

$$\Delta_{ij} = \frac{\Delta m^2_{ij} L}{4E}$$

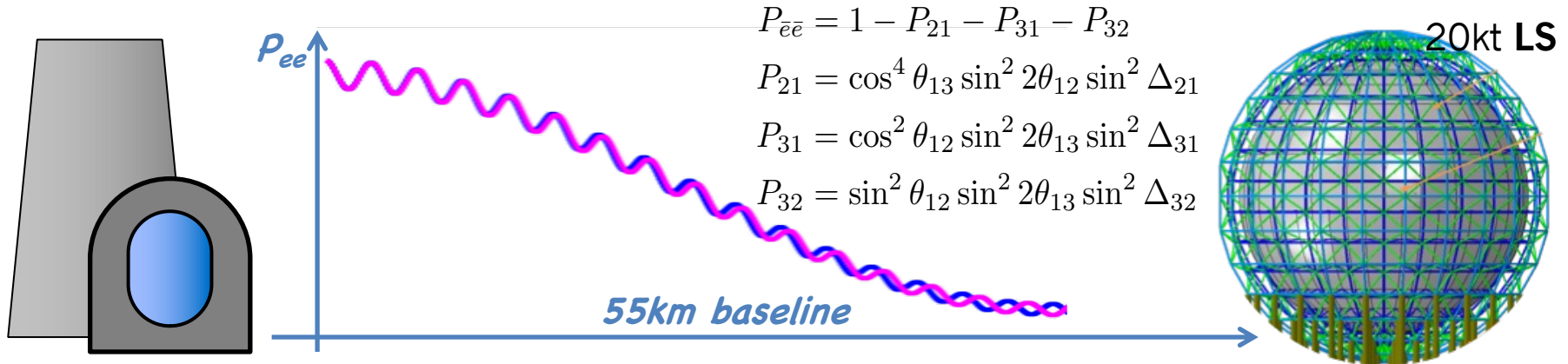
# Nuclear reactors as intense $\bar{\nu}_e$ source



- $\bar{\nu}$ 's from  $\beta^-$ -decays of neutron-rich fission products
- $\sim 6 \bar{\nu}_e$ 's per fission (200MeV)  $\rightarrow$  **intense!**  $\sim 10^{20} \bar{\nu}/\text{GW}_{th}$
- **energy spectra:** up to  $\sim 8$  MeV

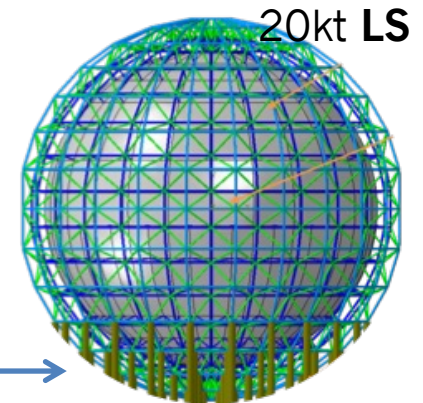
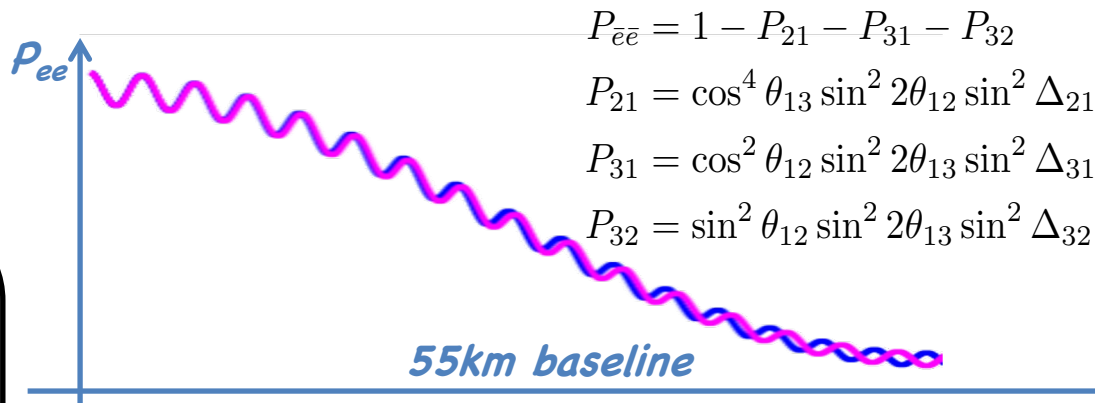
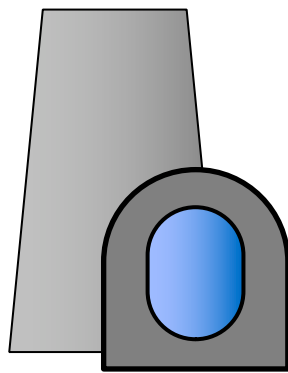


# Mid-distance $\bar{\nu}_e \rightarrow \bar{\nu}_e$ oscillations



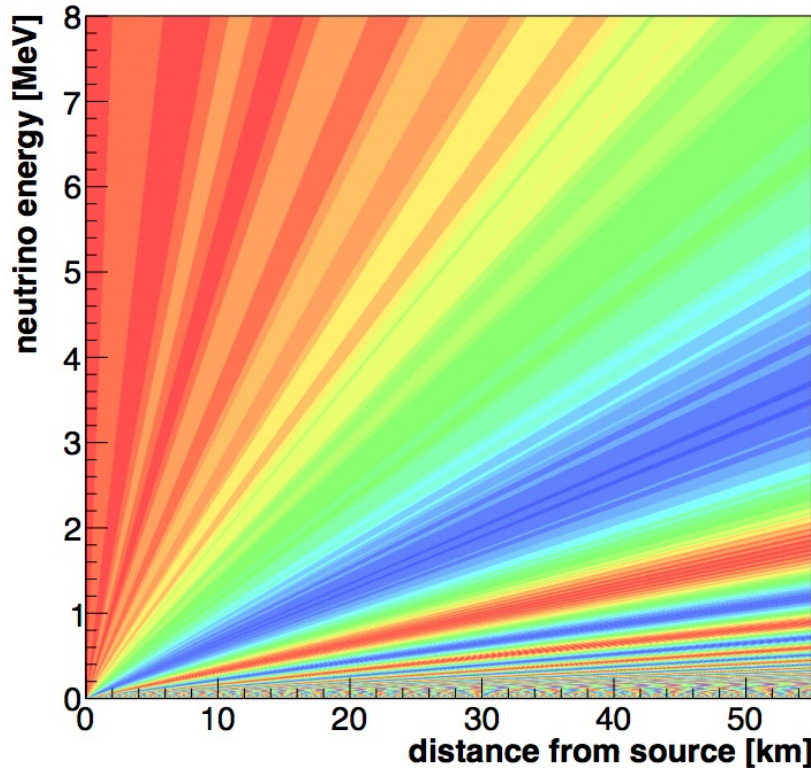
Nuclear  
reactor(s)  
 $\Sigma P \sim 30\text{GW}$

# Mid-distance $\bar{\nu}_e \rightarrow \bar{\nu}_e$ oscillations

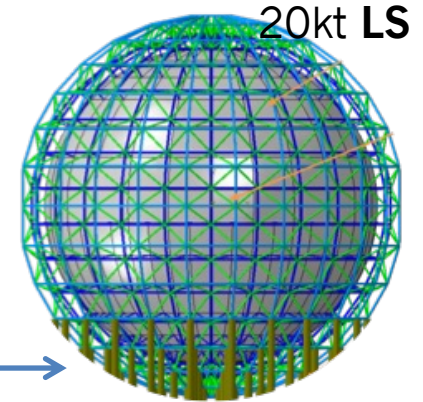
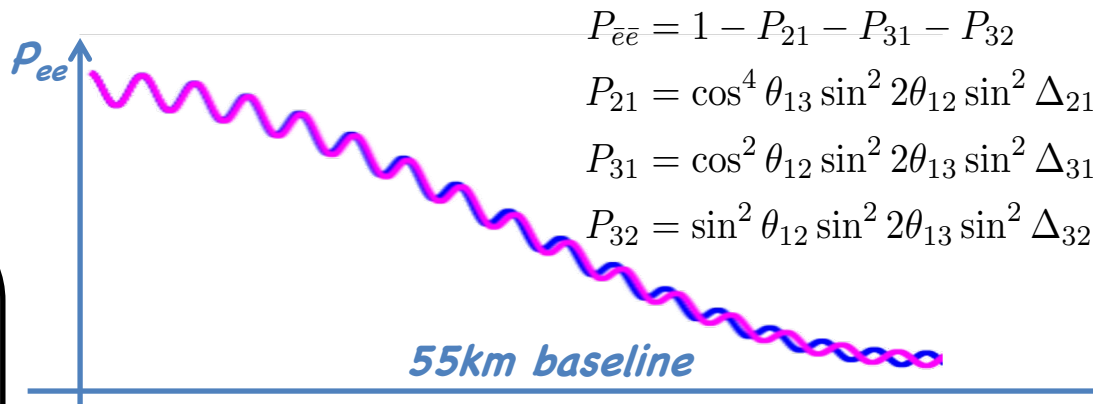
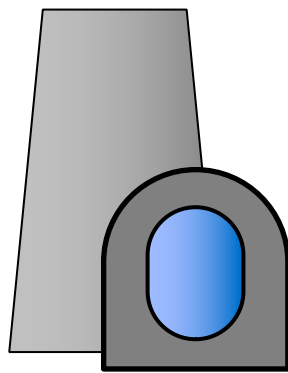


Nuclear reactor(s)  
 $\Sigma P \sim 30\text{GW}$

energy range of reactor spectrum

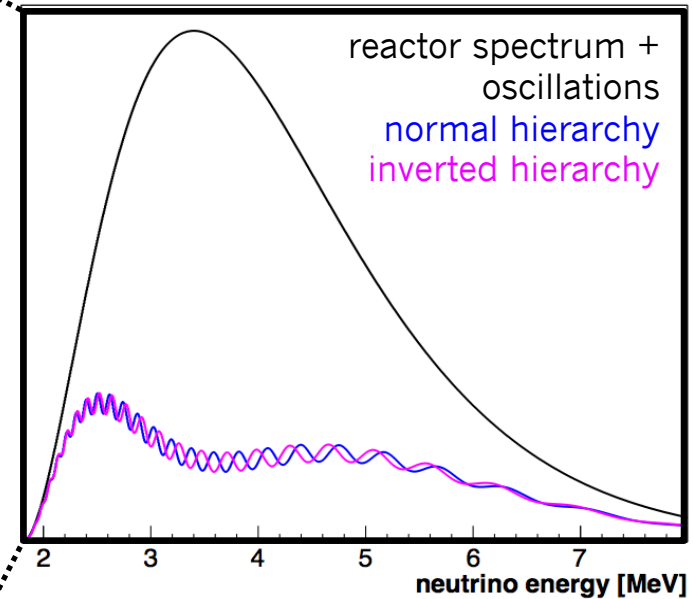
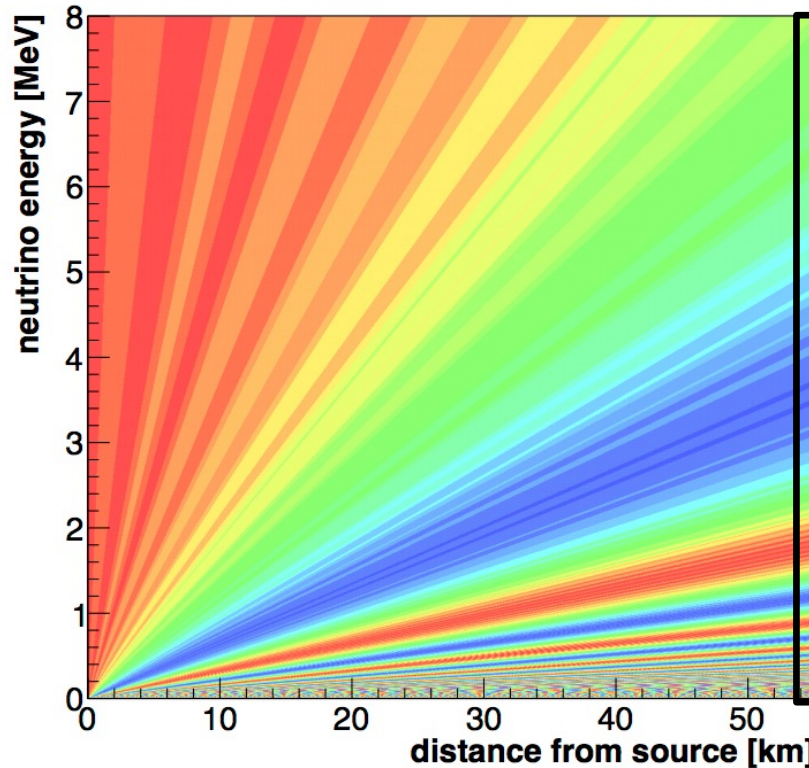


# Mid-distance $\bar{\nu}_e \rightarrow \bar{\nu}_e$ oscillations



Nuclear reactor(s)  
 $\Sigma P \sim 30\text{GW}$

energy range of reactor spectrum

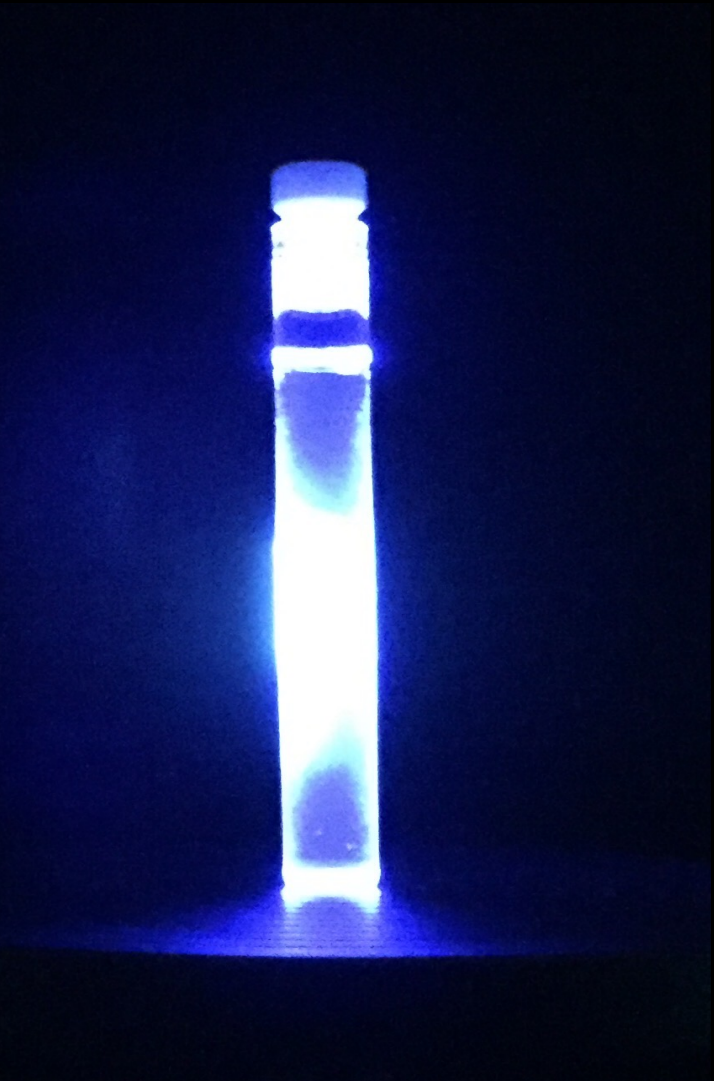


→ **MH from position of spectral wiggles!**



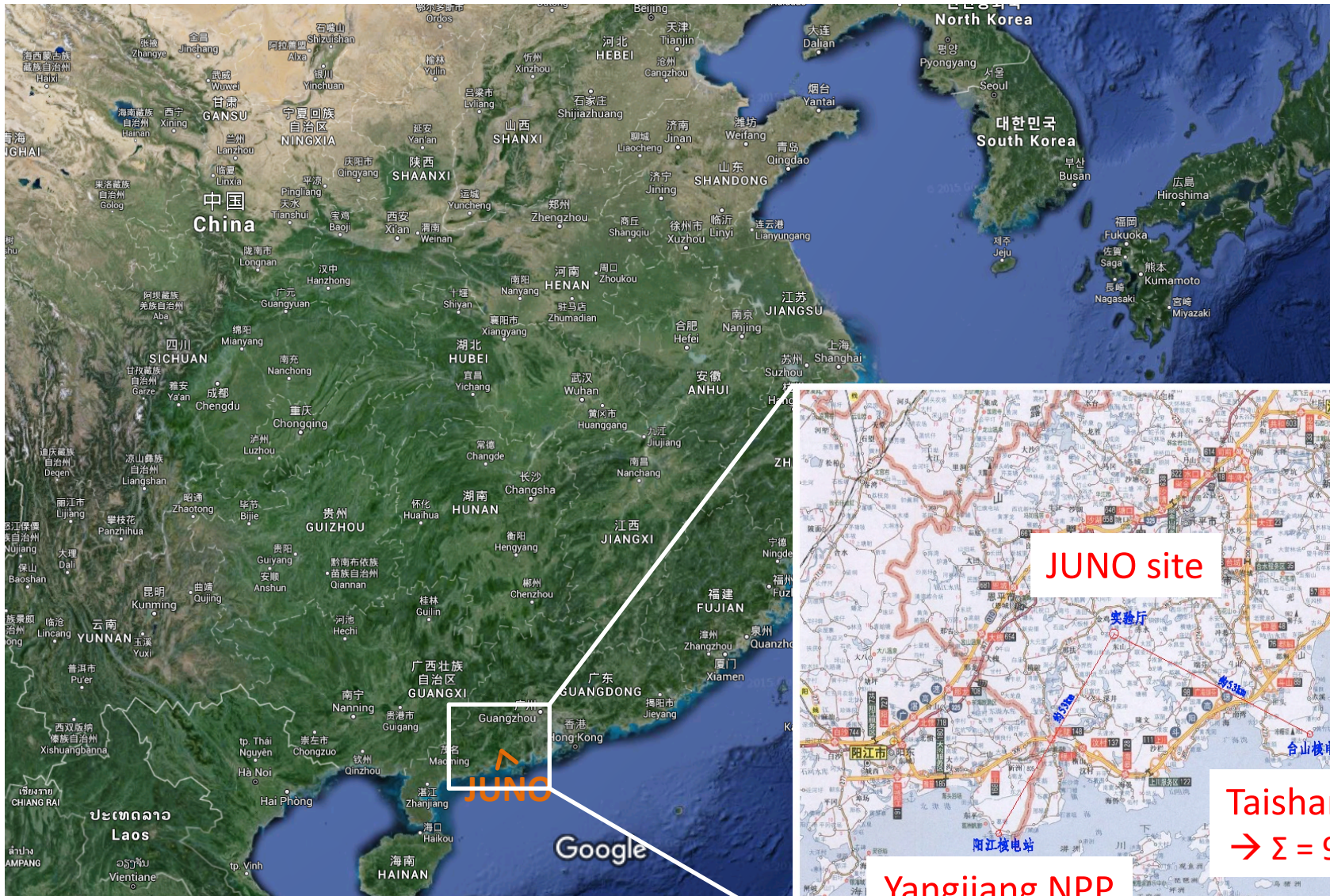
# Basic Detector Requirements for JUNO

- reactor antineutrinos at MeV energies
  - **Liquid-scintillator detector**
  - Detection by inverse beta decay
- signature in position of spectral wiggles
  - **~3% energy resolution** at 1 MeV
  - photoelectron yield: **~1,100 pe/MeV**
- large distance to source and high-statistics measurement
  - large target mass: **20 kilotons of LAB**
- cosmogenic background
  - rock overburden of **~600 m**





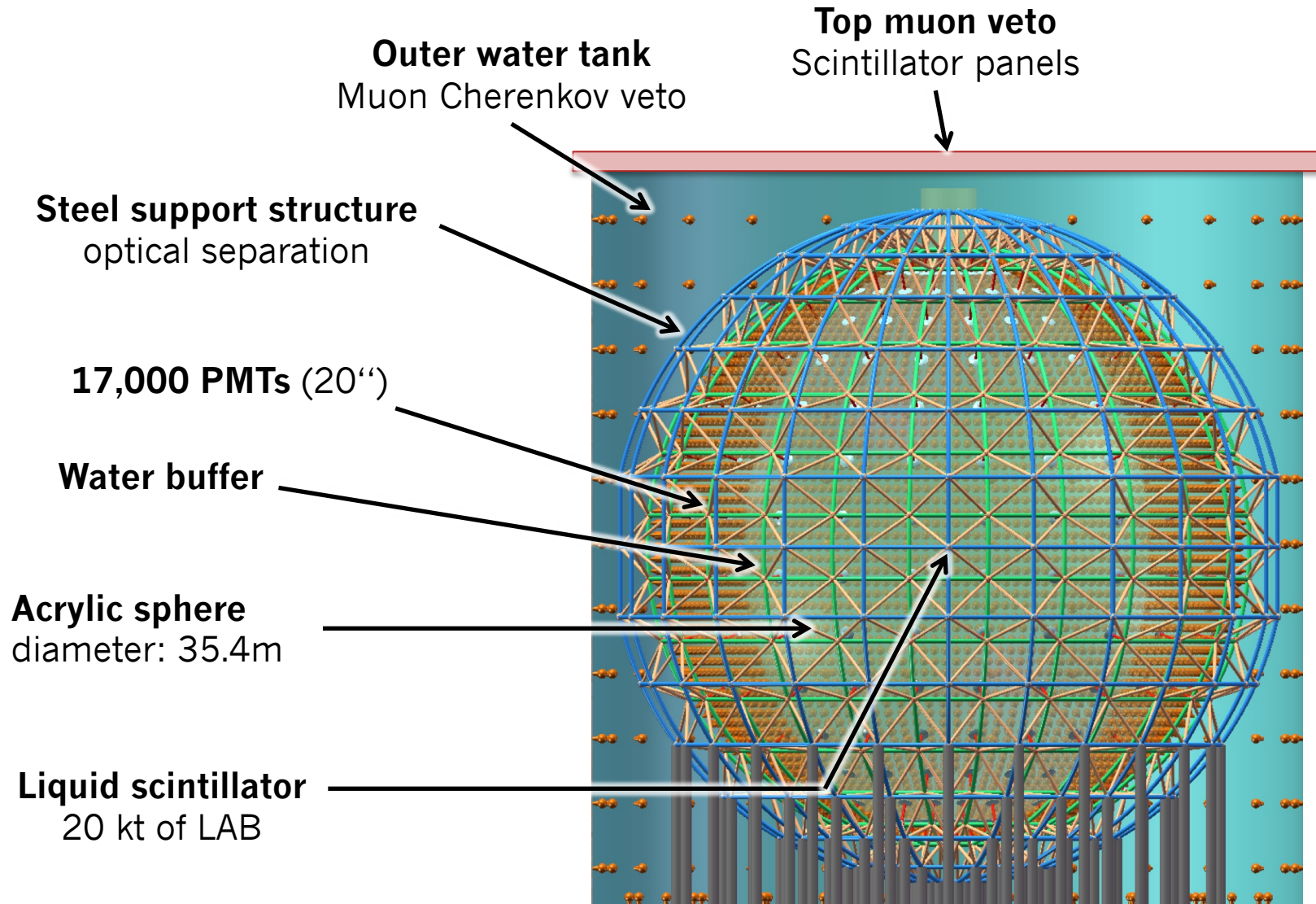
# Experimental Setup of JUNO



Bilder © 2015 Landsat, Data SIO, NOAA, U.S. Navy, NGA, GEBCO, Ka



# JUNO Detector Layout



600m below ground

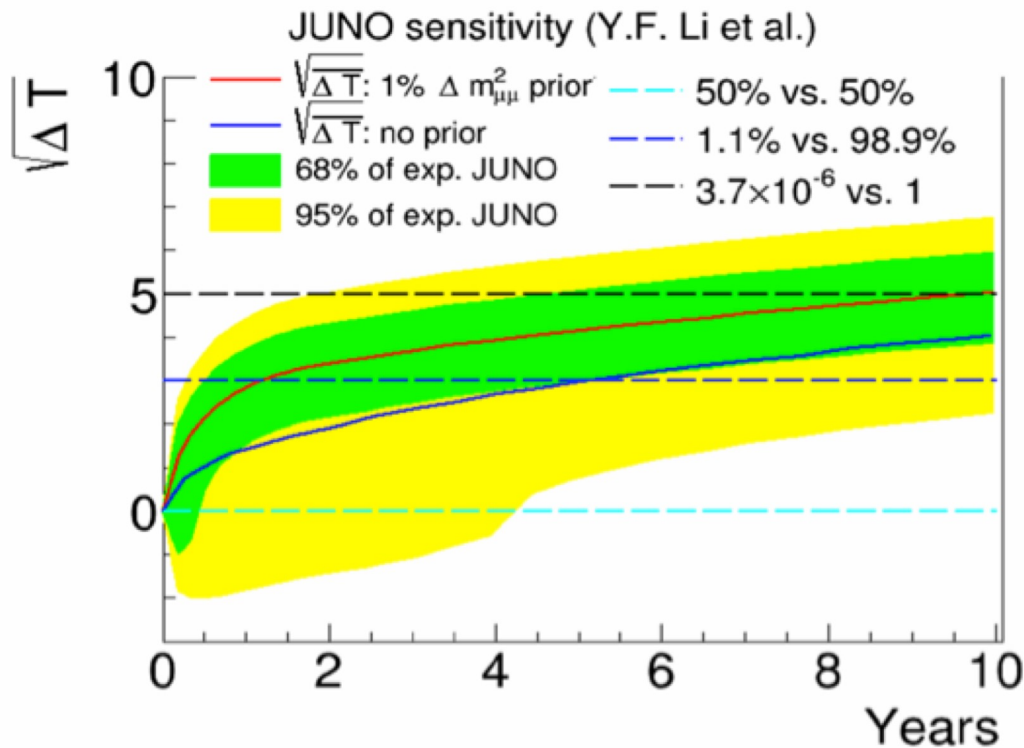


# JUNO: Current Status

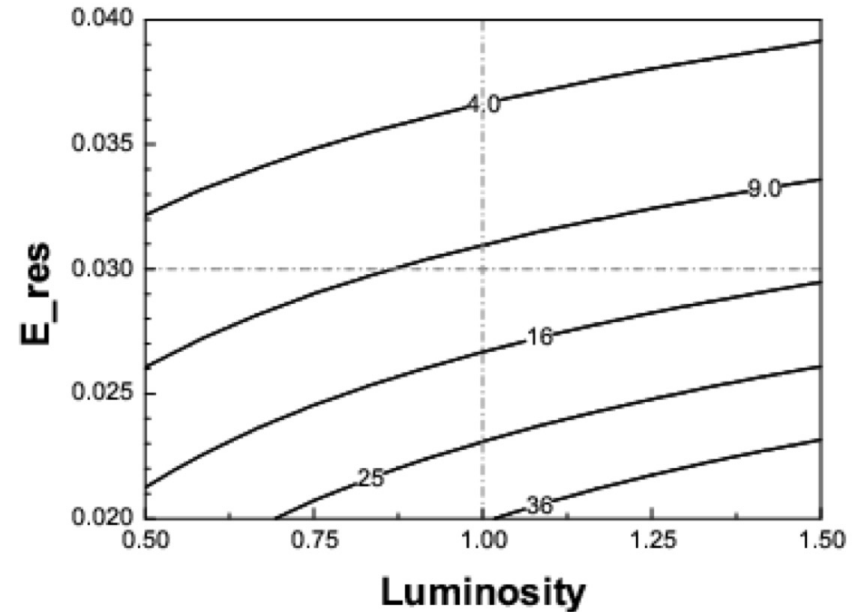


# JUNO Sensitivity

- sensitivity to NMO: about 6 years ( $10^5$  events) to reach  $3\sigma$
- depends strongly on energy resolution and energy scale linearity
- combination with existing experiments increases sensitivity to  $4\sigma$  after 6 years



NMO sensitivity over time



sensitivity as function of energy resolution/exposure



# LECTURE QUIZ

## Question 4

How large is the scintillator target mass to be deployed in JUNO?

L : 200 tons

M : 2 kt

N : 20 kt



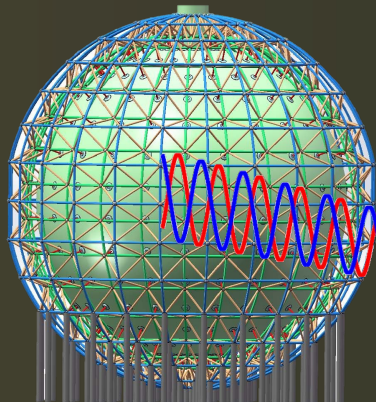
# Measuring the Neutrino Mass Ordering

1 Mid-baseline reactor neutrino oscillations

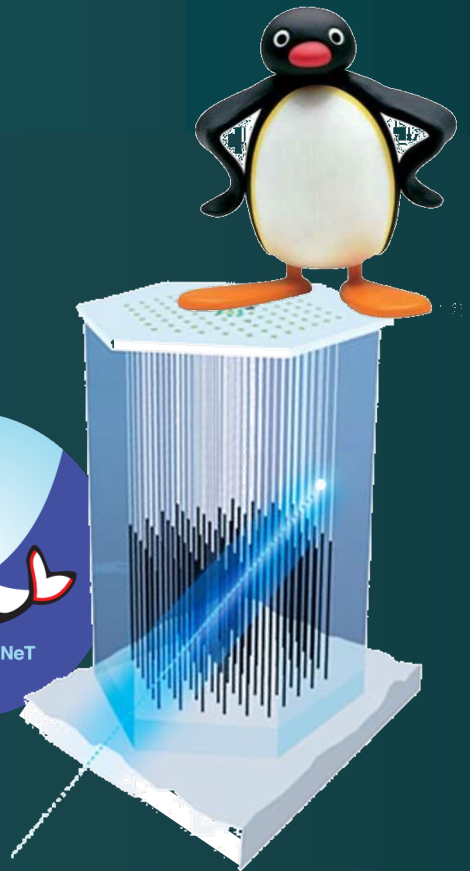
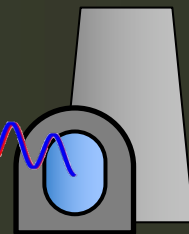
2 Low-energy atmospheric neutrino oscillations

3 Very-Long Baseline Neutrino Beams

DUNE.



JUNO.



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# $\nu_\mu \rightarrow \nu_e$ oscillation probability

Oscillation probability for  $\nu_e$  appearance  
in a  $\nu_\mu$  neutrino beam:

$$\begin{aligned} P_{\mu e(\bar{\mu}\bar{e})} = & \sin^2 \theta_{23} \sin^2 2\theta_{13} \left( \frac{\Delta_{13}}{B_\pm} \right)^2 \sin^2 \left( \frac{B_\pm L}{2} \right) \\ & + \cos^2 \theta_{23} \sin^2 2\theta_{12} \left( \frac{\Delta_{12}}{A} \right)^2 \sin^2 \left( \frac{AL}{2} \right) \\ & + J \frac{\Delta_{12}}{A} \frac{\Delta_{13}}{B_\pm} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{B_\pm L}{2} \right) \cos \left( \mp \delta - \frac{\Delta_{13}L}{2} \right) \end{aligned}$$

good approximation  
for 1st atmospheric  
oscillation maximum

---

$$J = \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23}$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2}{2E_\nu} \quad B_\pm = |A \pm \Delta_{13}| \quad A = \sqrt{2}G_F N_e$$

# $\nu_\mu \rightarrow \nu_e$ oscillation probability

Oscillation probability for  $\nu_e$  appearance

in a  $\nu_\mu$  neutrino beam:

$$P_{\mu e(\bar{\mu}\bar{e})} = \underbrace{\sin^2 \theta_{23} \sin^2 2\theta_{13} \left(\frac{\Delta_{13}}{B_\pm}\right)^2 \sin^2 \left(\frac{B_\pm L}{2}\right)}_{\text{atmospheric oscillations}} + \underbrace{\cos^2 \theta_{23} \sin^2 2\theta_{12} \left(\frac{\Delta_{12}}{A}\right)^2 \sin^2 \left(\frac{AL}{2}\right)}_{\text{solar oscillations}} \approx 0 + \underbrace{J \frac{\Delta_{12}}{A} \frac{\Delta_{13}}{B_\pm} \sin \left(\frac{AL}{2}\right) \sin \left(\frac{B_\pm L}{2}\right) \cos \left(\mp \delta - \frac{\Delta_{13}L}{2}\right)}_{\text{neutrino-antineutrino asymmetry term}}$$

---

$$J = \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23}$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2}{2E_\nu} \quad B_\pm = |A \pm \Delta_{13}| \quad A = \sqrt{2}G_F N_e$$



# $\nu_\mu \rightarrow \nu_e$ oscillation probability: CP violation

Oscillation probability for  $\nu_e$  appearance  
in a  $\nu_\mu$  neutrino beam:

$$\begin{aligned}
 P_{\mu e(\bar{\mu}\bar{e})} = & \textit{atmospheric oscillations} \\
 & \sin^2 \theta_{23} \sin^2 2\theta_{13} \left( \frac{\Delta_{13}}{B_\pm} \right)^2 \sin^2 \left( \frac{B_\pm L}{2} \right) \\
 & \textit{solar oscillations} \\
 & + \cos^2 \theta_{23} \sin^2 2\theta_{12} \left( \frac{\Delta_{12}}{A} \right)^2 \sin^2 \left( \frac{AL}{2} \right) \approx 0 \\
 & + J \frac{\Delta_{12}}{A} \frac{\Delta_{13}}{B_\pm} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{B_\pm L}{2} \right) \cos \left( \mp \delta - \frac{\Delta_{13}L}{2} \right) \\
 & \textit{neutrino-antineutrino asymmetry term}
 \end{aligned}$$

*leptonic CP violation*

$$J = \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23}$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2}{2E_\nu} \quad B_\pm = |A \pm \Delta_{13}| \quad A = \sqrt{2}G_F N_e$$

# $\nu_\mu \rightarrow \nu_e$ oscillation probability: NMO

Oscillation probability for  $\nu_e$  appearance  
in a  $\nu_\mu$  neutrino beam:

$$\begin{aligned}
 P_{\mu e(\bar{\mu} \bar{e})} = & \text{atmospheric oscillations} \rightarrow T2K \quad \sin^2 \theta_{23} \sin^2 2\theta_{13} \left( \frac{\Delta_{13}}{B_\pm} \right)^2 \sin^2 \left( \frac{B_\pm L}{2} \right) \\
 & \text{solar oscillations} \quad + \cos^2 \theta_{23} \sin^2 2\theta_{12} \left( \frac{\Delta_{12}}{A} \right)^2 \sin^2 \left( \frac{AL}{2} \right) \approx 0 \\
 & \text{neutrino-antineutrino asymmetry term} \quad + J \frac{\Delta_{12}}{A} \frac{\Delta_{13}}{B_\pm} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{B_\pm L}{2} \right) \cos \left( \mp \delta - \frac{\Delta_{13} L}{2} \right)
 \end{aligned}$$

*effects of weak matter potential* (arrow pointing to  $B_\pm$ )

*leptonic CP violation* (arrow pointing to  $\mp \delta$ )

$$J = \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23}$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2}{2E_\nu}$$

$$B_\pm = |A \pm \Delta_{13}|$$

*weak matter potential A*

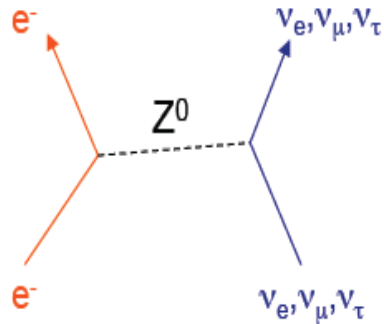
$$A = \sqrt{2} G_F N_e$$

$\nu \leftrightarrow \bar{\nu}$  asymmetry if  $A \sim \Delta_{13}$ !

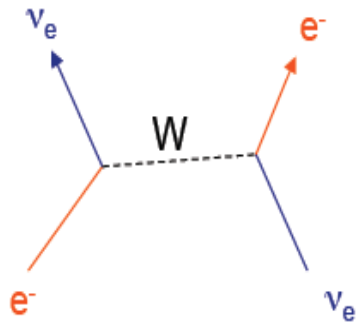
# Matter effect on neutrino oscillations

Forward-scattering of  $\nu$ 's in matter:

- NC the same for all flavors



- CC on electrons only for  $\nu_e$



- $\nu_e$  pick up an effective mass term
- impact on  $\Delta m^2$  values AND osc. amplitudes

*a.k.a. the MSW-effect (1985)*

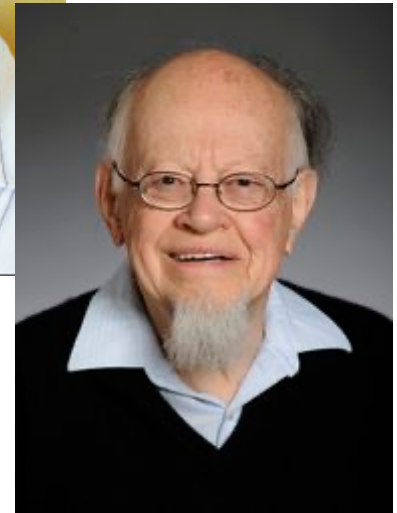
Mikheyev



Smirnov

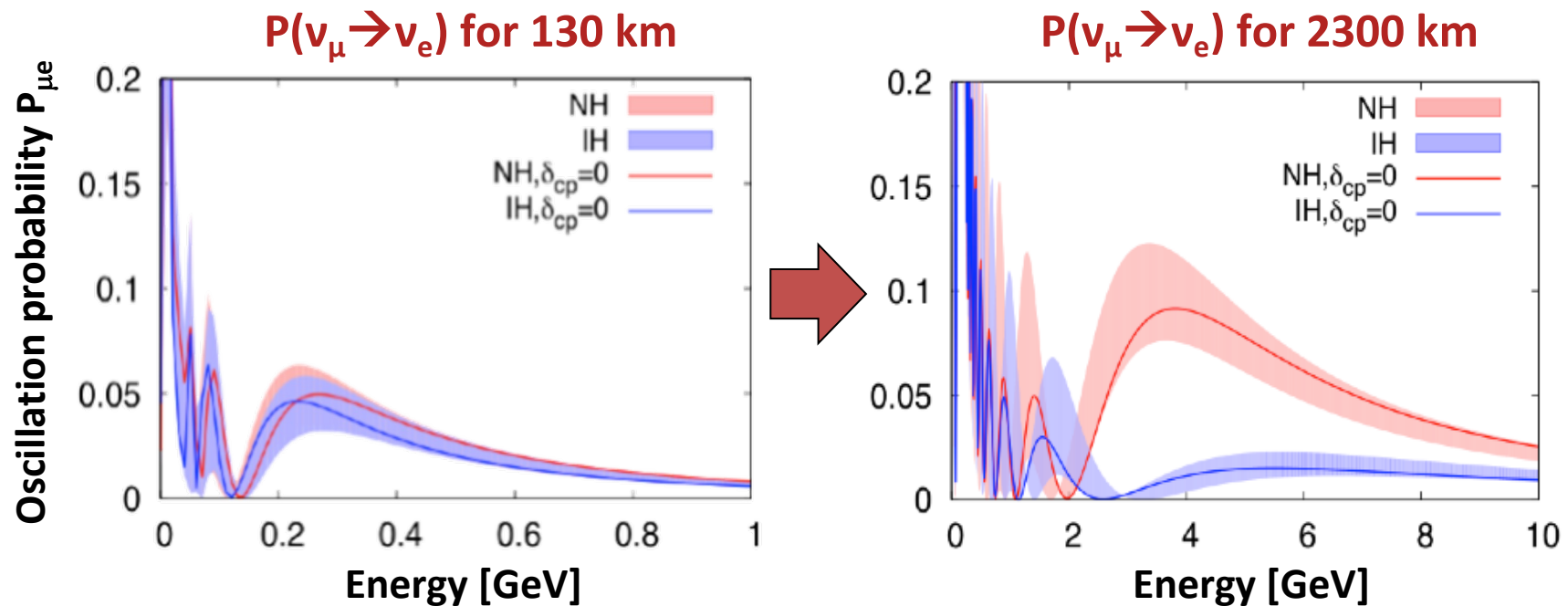


Wolfenstein



# Oscillation spectra at long baselines

- Oscillation probabilities differ for  $\nu_\mu \rightarrow \nu_e$  vs.  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$
- Enhanced electron-flavor appearance for: neutrinos  $\rightarrow$  normal hierarchy  
antineutrinos  $\rightarrow$  inverted

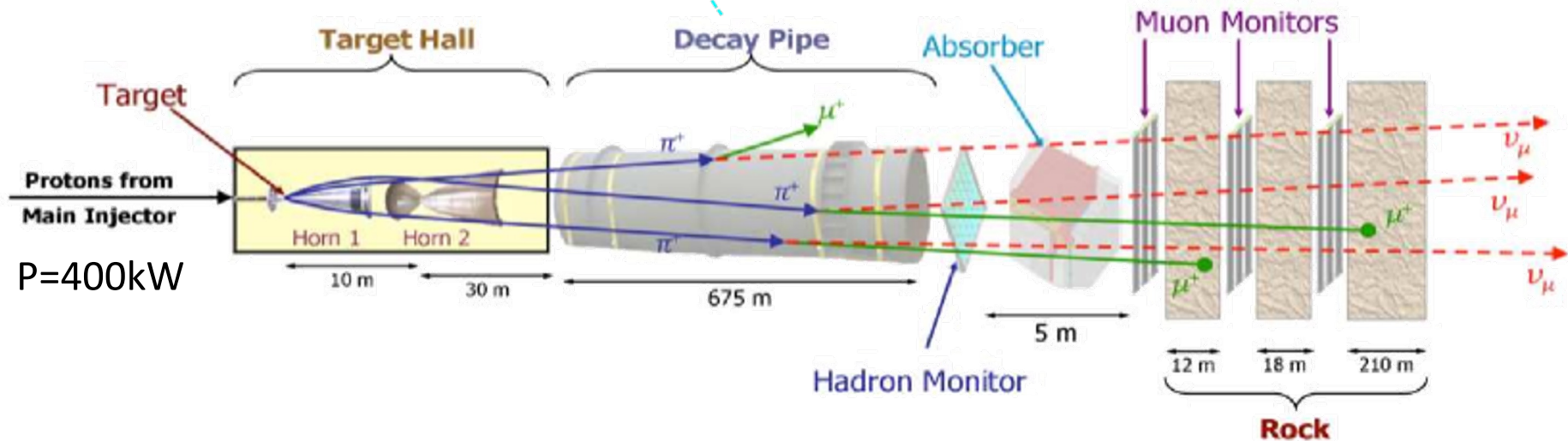
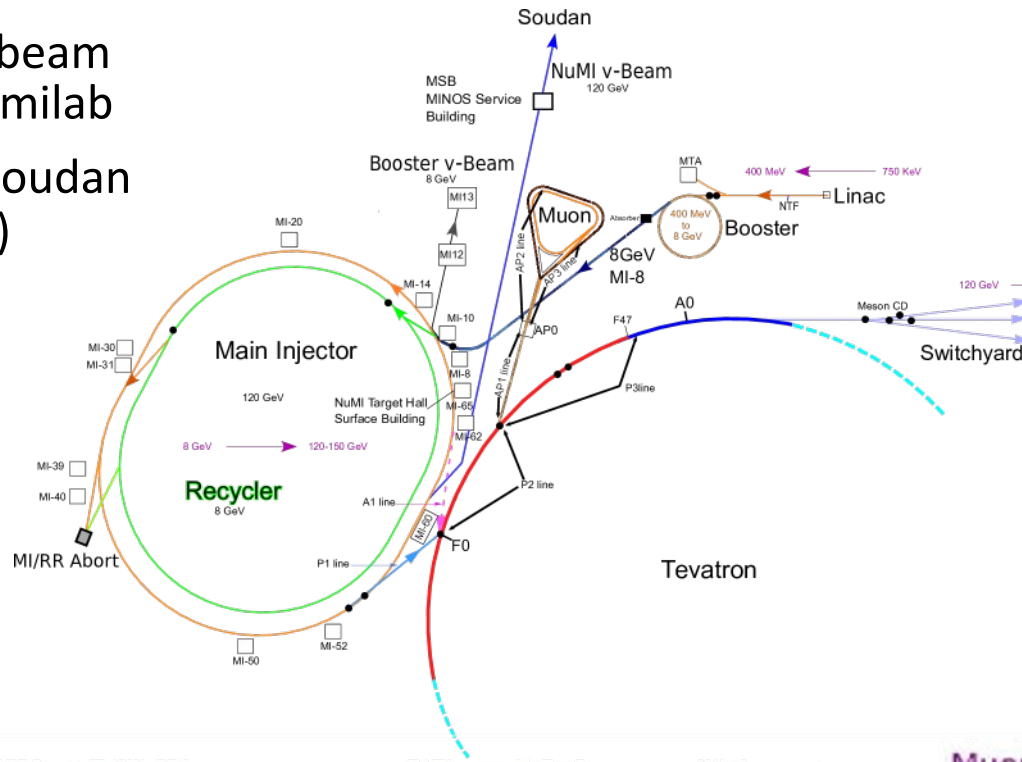


- Far detector at first atmospheric oscillation maximum:  
longer baseline  $\rightarrow$  larger energy  $\rightarrow$  larger matter effect!



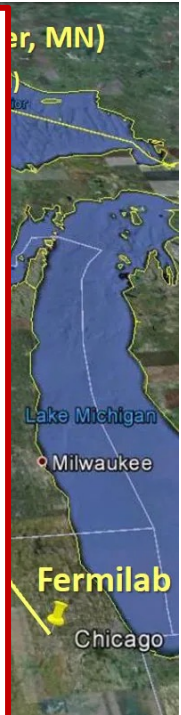
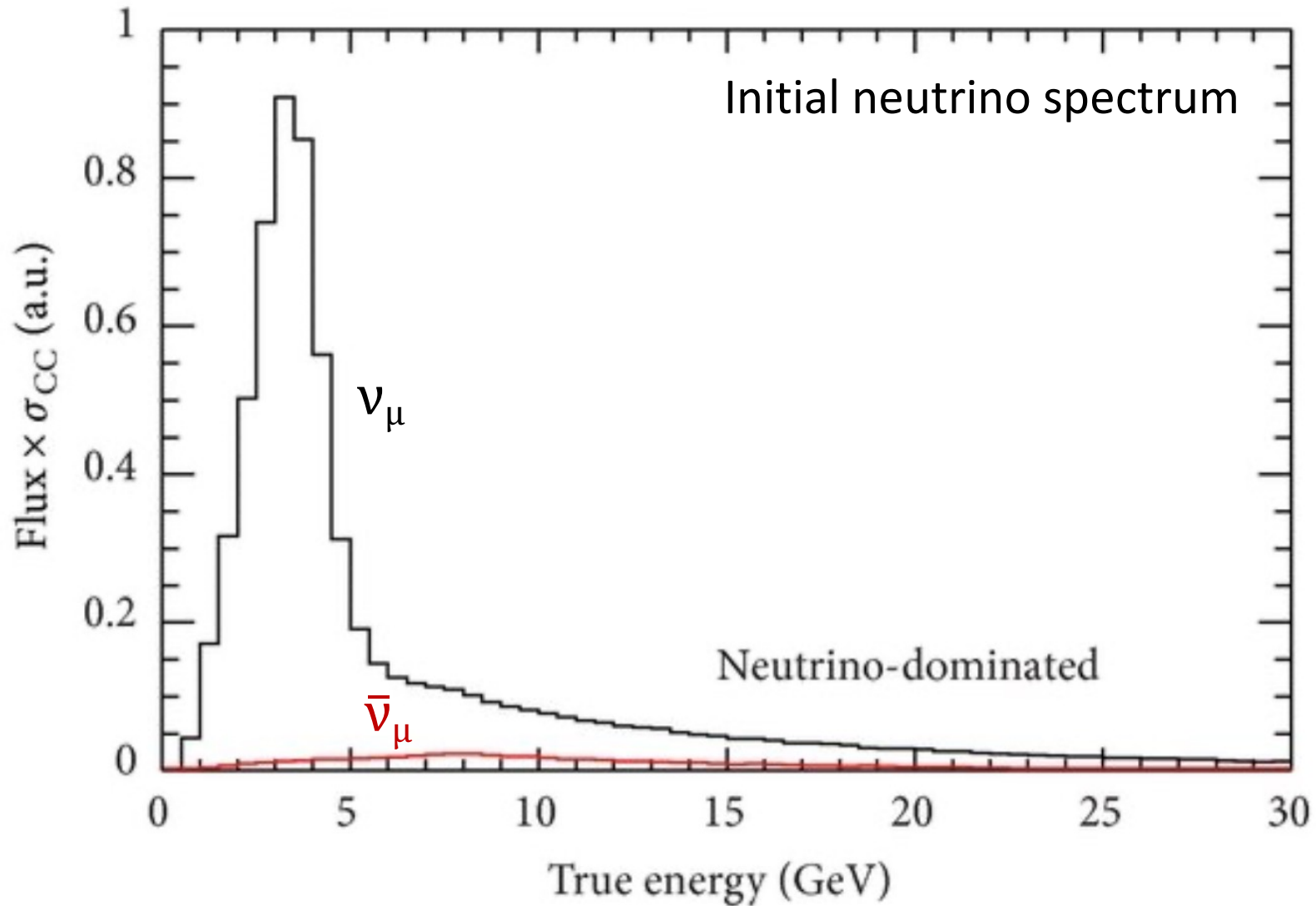
# Long-baseline oscillations with NOvA

- muon neutrino beam produced at Fermilab
- far detector in Soudan mine (Ash River)



# Long-baseline oscillations with NOvA

- muon  
produ
- far de  
mine

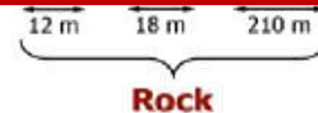


Tar

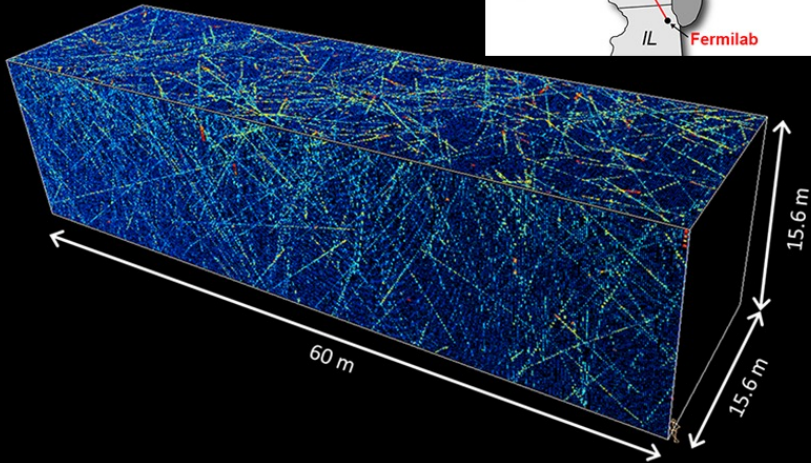
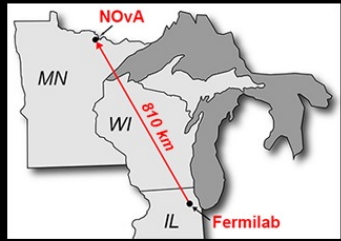
Protons fr  
Main Injec

P=400k

Hadron Monitor



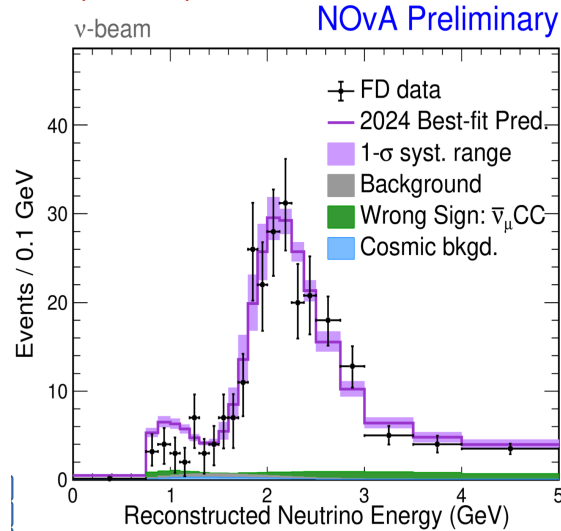
# Results from NOvA Experiment



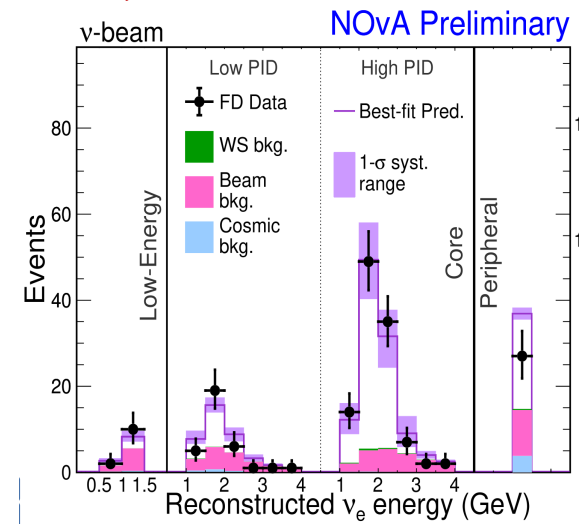
## Experimental Layout

- baseline: 810km
- alignment: 16 mrad off-axis
- spectrum:  $(2 \pm 1)$  GeV
- beam power: 400kW
- detector: 14kt of segmented scintillator
- near detector for cross-sections and spectral comparison

$\nu_\mu \rightarrow \nu_\mu$  disappearance



$\nu_\mu \rightarrow \nu_e$  appearance

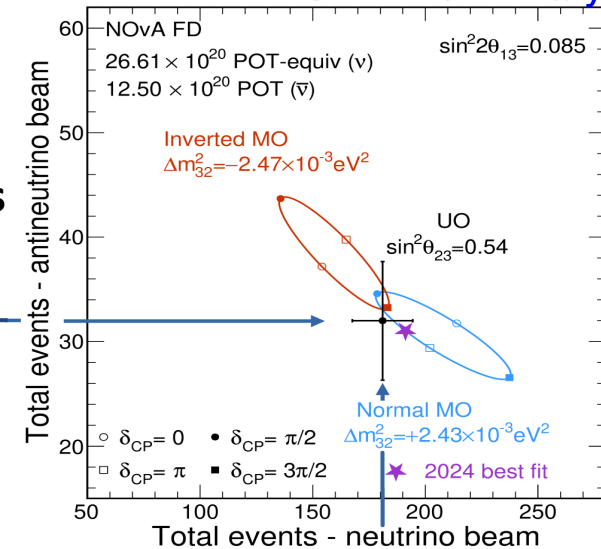


comparison of neutrino and anti-neutrino modes

$\bar{\nu}_e$  appearance: 32 ev

$\nu_e$  appearance: 181 ev

NOvA Preliminary

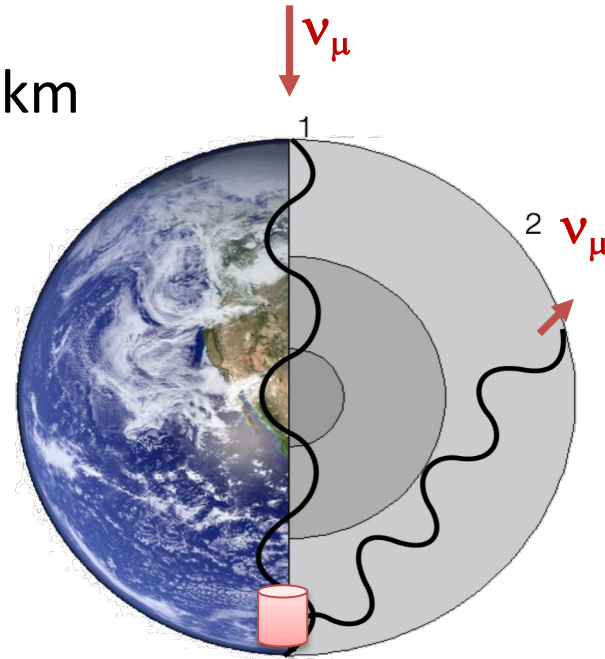




# Matter effects and atmospheric neutrinos

## Source: Atmospheric $\mu$ -neutrinos

- Energies: 2-20 GeV
- Baselines: 20-13000 km
- Matter potential: Earth core & mantle



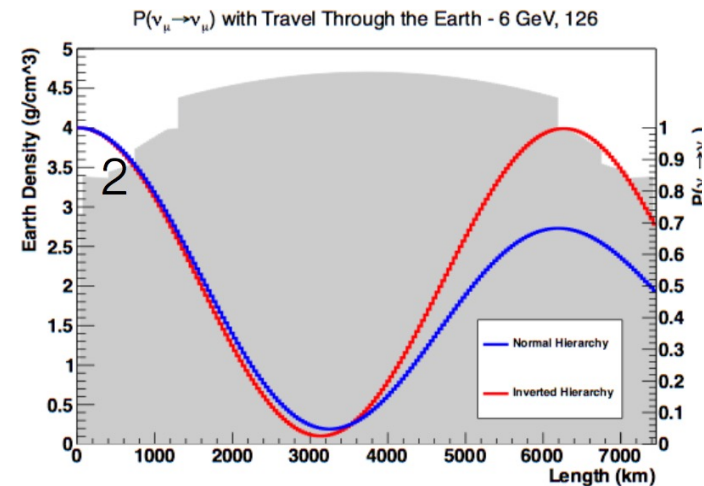
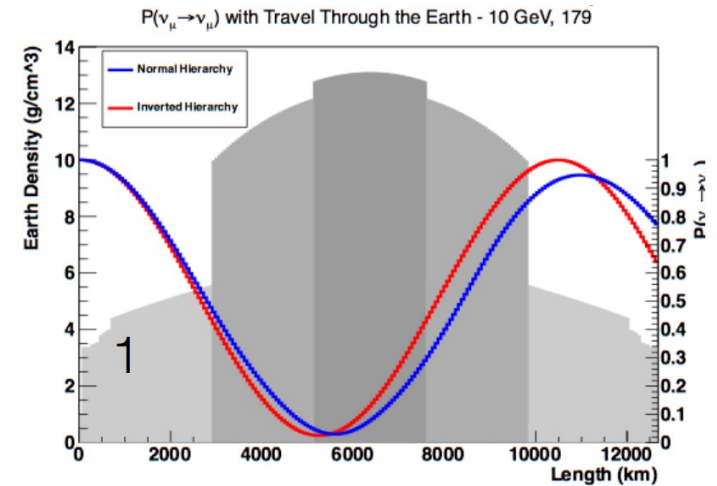
## MH signature

matter effects in

- $\nu_\mu \rightarrow \nu_\mu$  disappearance
- $\nu_\mu \rightarrow \nu_e$  appearance

## Detector requirements

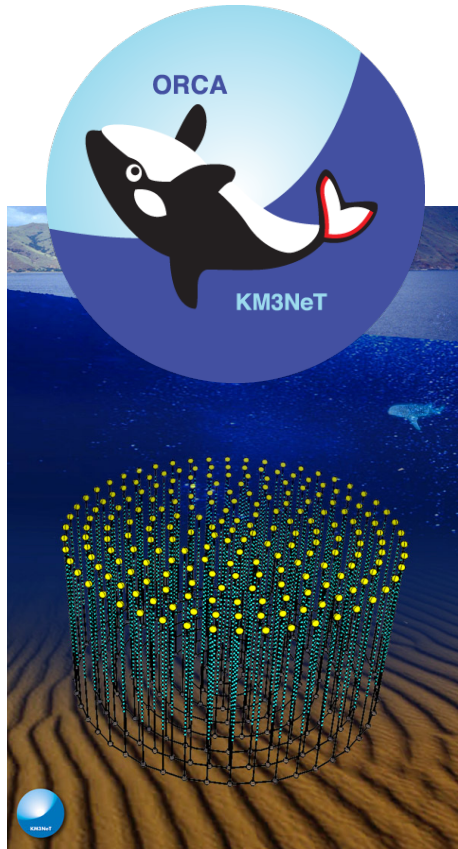
- relatively low energy threshold:  $O(1\text{GeV})$
- good angular resolution
- flavor identification
- nice to have: lepton charge ID ( $\nu/\bar{\nu}$ )



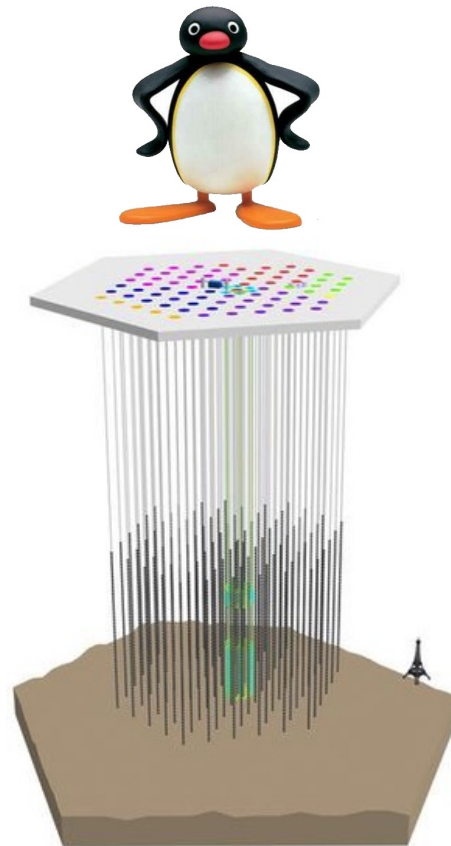


# Upcoming Detectors

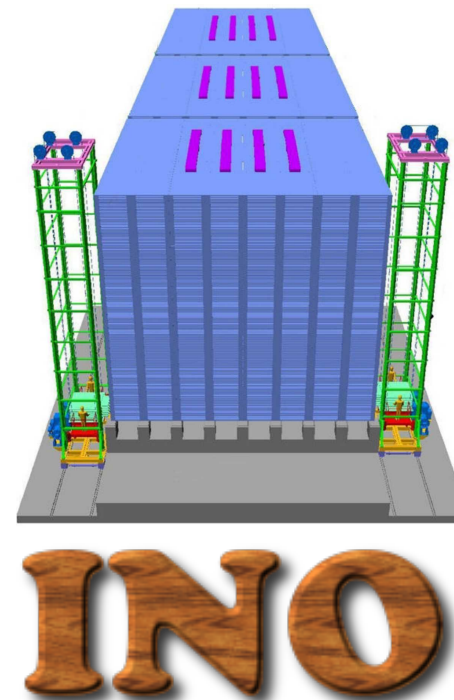
*KM3Net  
ORCA (2025)*



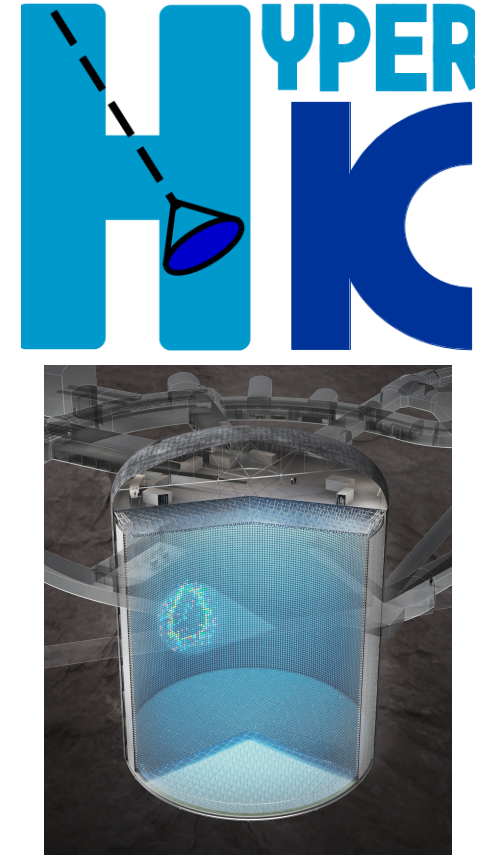
*IceCube-Upgrade  
(2026)*



*INO  
(??)*

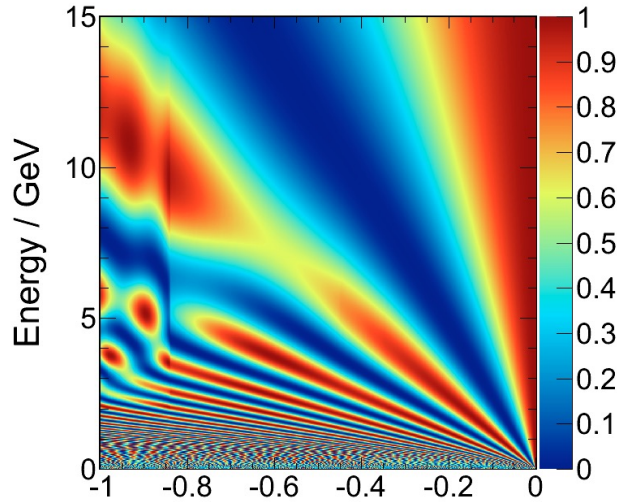


*Hyper-Kamiokande  
(2027)*

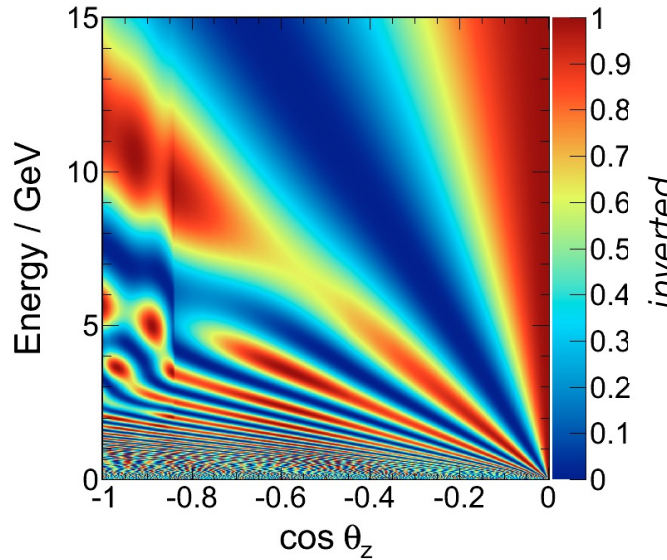
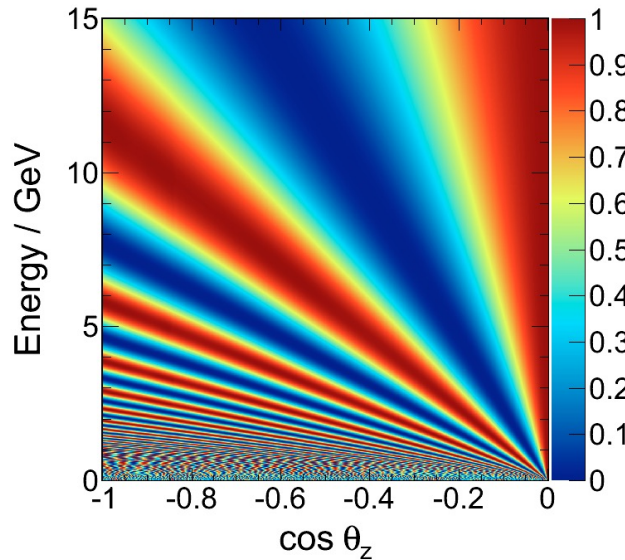
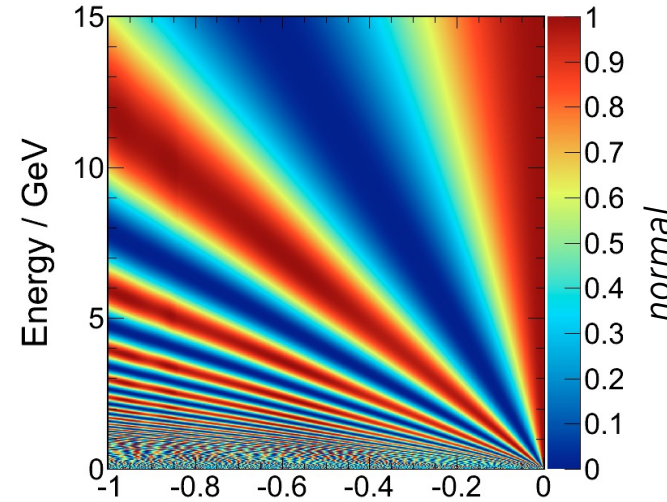


# Matter effects in atmospheric $\nu$ oscillations

neutrinos



anti-neutrinos



## Signal

- matter effects inverted for NH and IH
- **similar flux** of  $\nu$  and  $\bar{\nu}$
- detector cannot separate  $\nu$  and  $\bar{\nu}$  events!  
→ combined signal
- **but: different x-sections**  
 $\sigma(\nu N) : \sigma(\bar{\nu} N) \approx 2 : 1$

→ **few % effect**

## Requirements

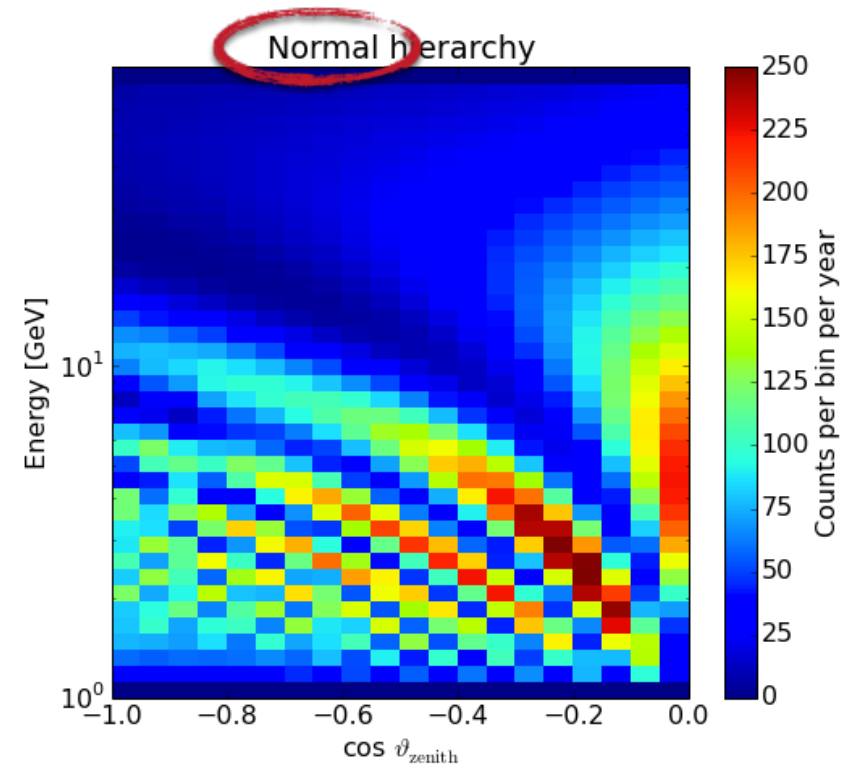
- high statistics
- very good control of systematic effects

plots by Sebastian Böser

# Expected signal in PINGU

## Event statistics

- $\nu_{\mu}$ :  $5.0 \times 10^4 \text{ yr}^{-1}$
- $\nu_e$ :  $3.8 \times 10^4 \text{ yr}^{-1}$

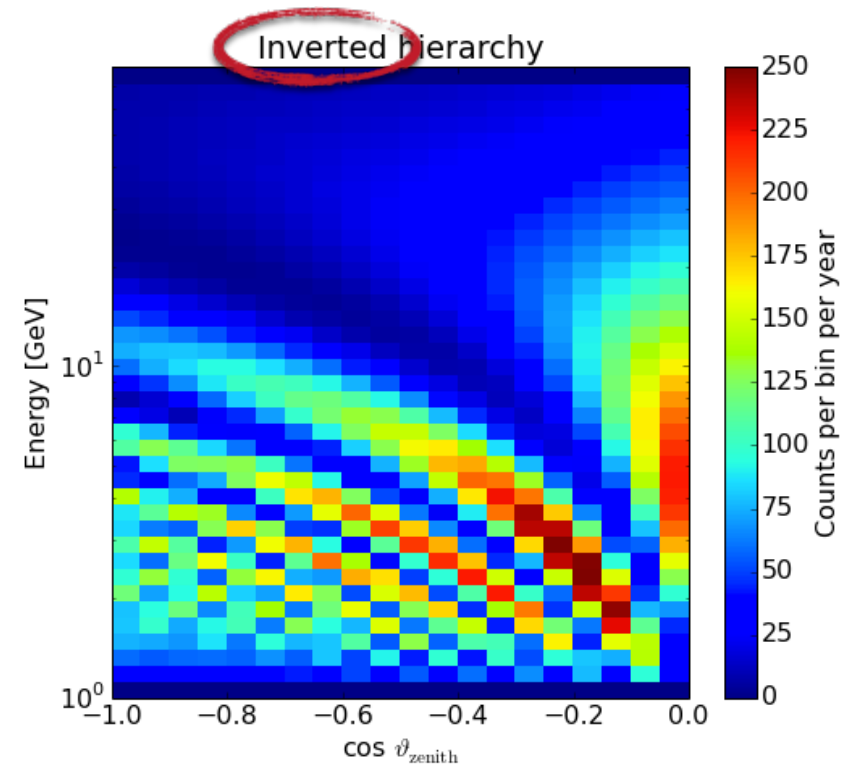


plots by Sebastian Böser

# Expected signal in PINGU

## Event statistics

- $\nu_{\mu}$ :  $5.0 \times 10^4 \text{ yr}^{-1}$
- $\nu_e$ :  $3.8 \times 10^4 \text{ yr}^{-1}$



plots by Sebastian Böser



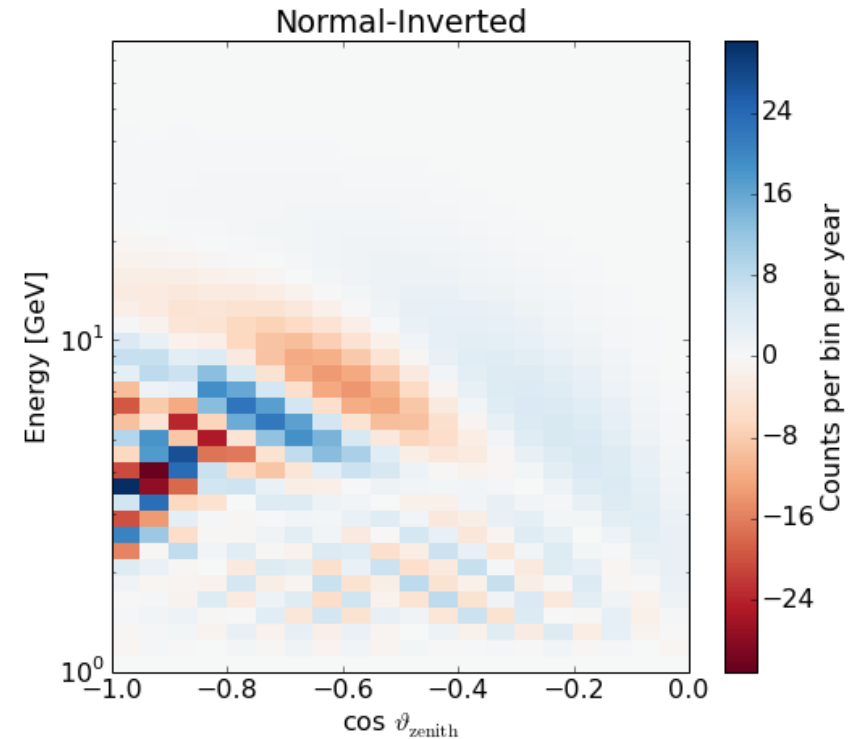
# Expected signal in PINGU

## Event statistics

■  $\nu_{\mu}$ :  $5.0 \times 10^4 \text{ yr}^{-1}$

■  $\nu_e$ :  $3.8 \times 10^4 \text{ yr}^{-1}$

→ detectable difference



plots by Sebastian Böser

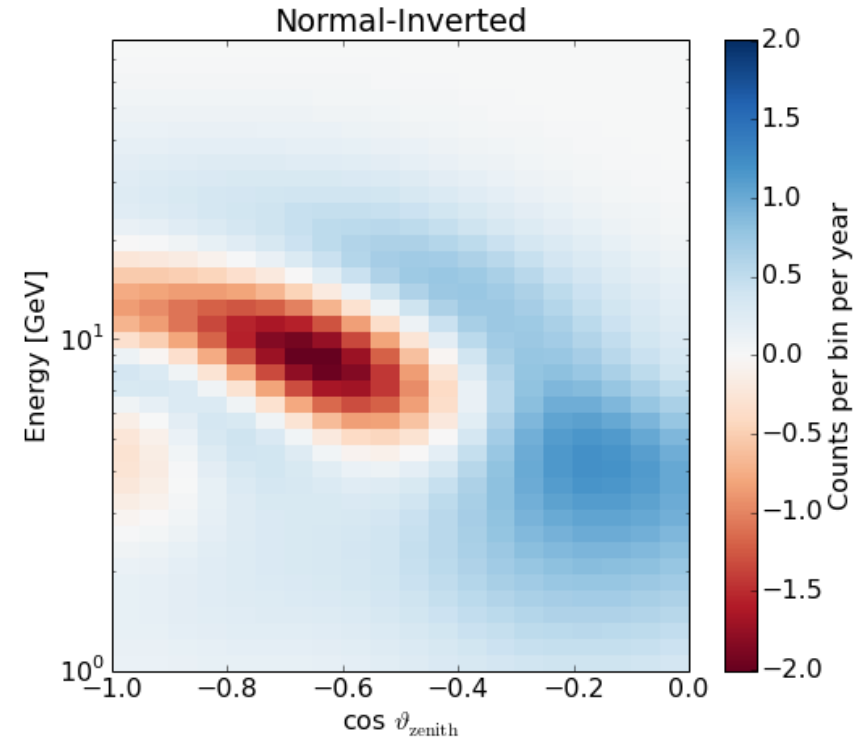
# Expected signal in PINGU

## Event statistics

- $\nu_{\mu}$ :  $5.0 \times 10^4 \text{ yr}^{-1}$
- $\nu_e$ :  $3.8 \times 10^4 \text{ yr}^{-1}$
- detectable difference

## Detector resolution

- energy resolution:  
~20% above 10 GeV
- directional resolution  
improving with energy



plots by Sebastian Böser

# Expected signal in PINGU

## Event statistics

- $\nu_{\mu}$ :  $5.0 \times 10^4 \text{ yr}^{-1}$

- $\nu_e$ :  $3.8 \times 10^4 \text{ yr}^{-1}$

→ detectable difference

## Detector resolution

- energy resolution:  
~20% above 10 GeV

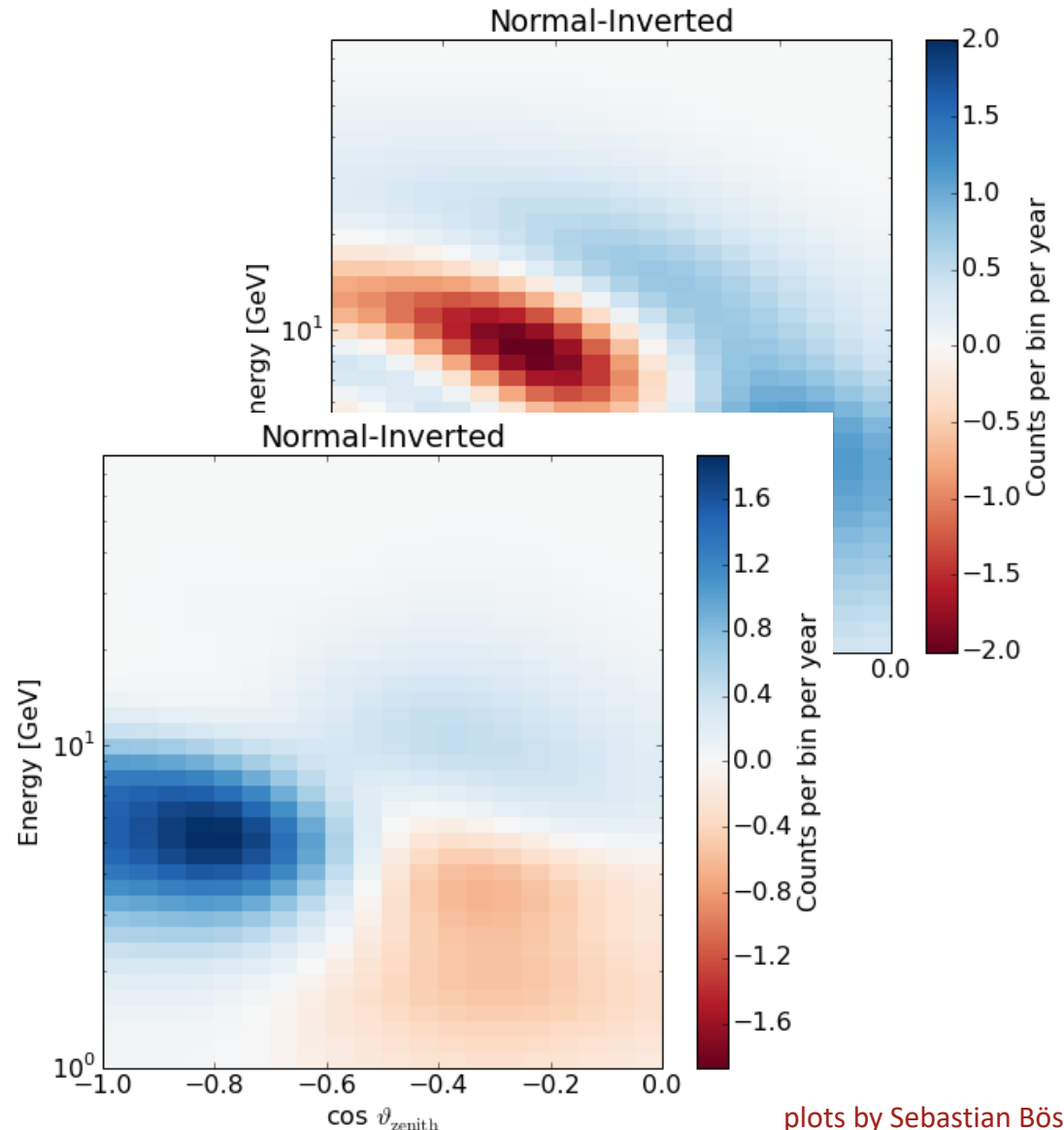
- directional resolution  
improving with energy

## Particle identification

- $\nu_{\mu}$  (CC): tracks

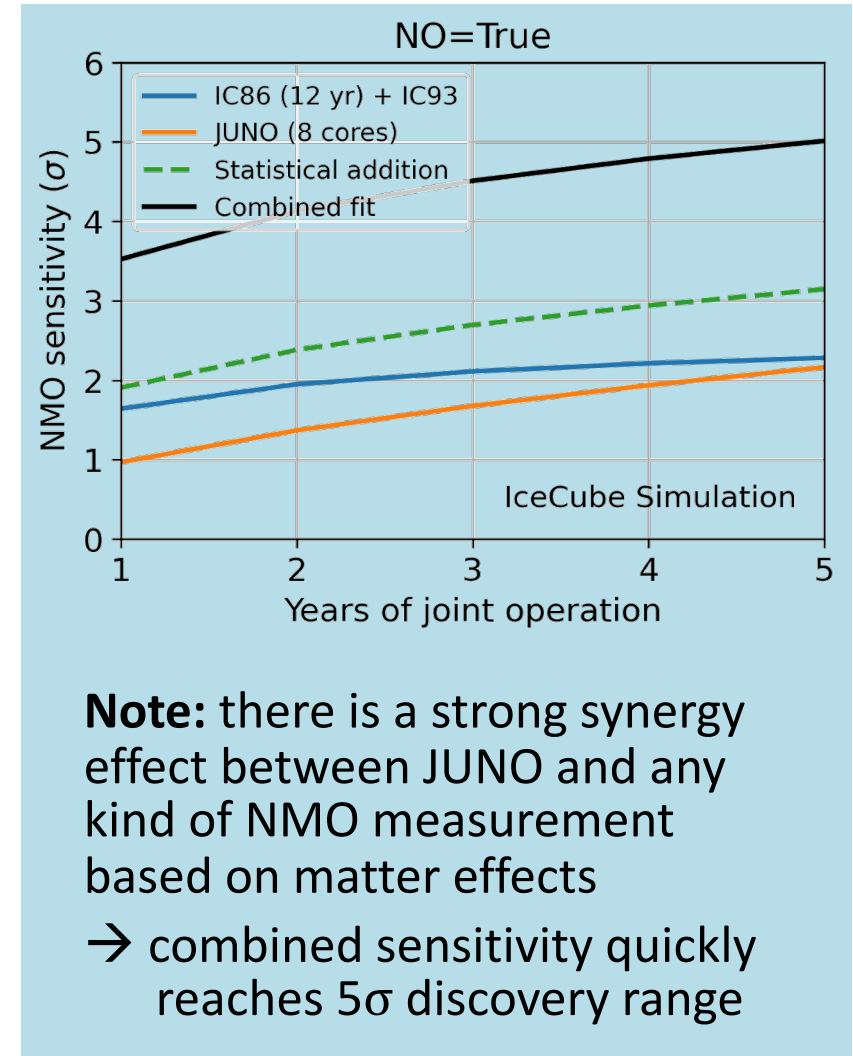
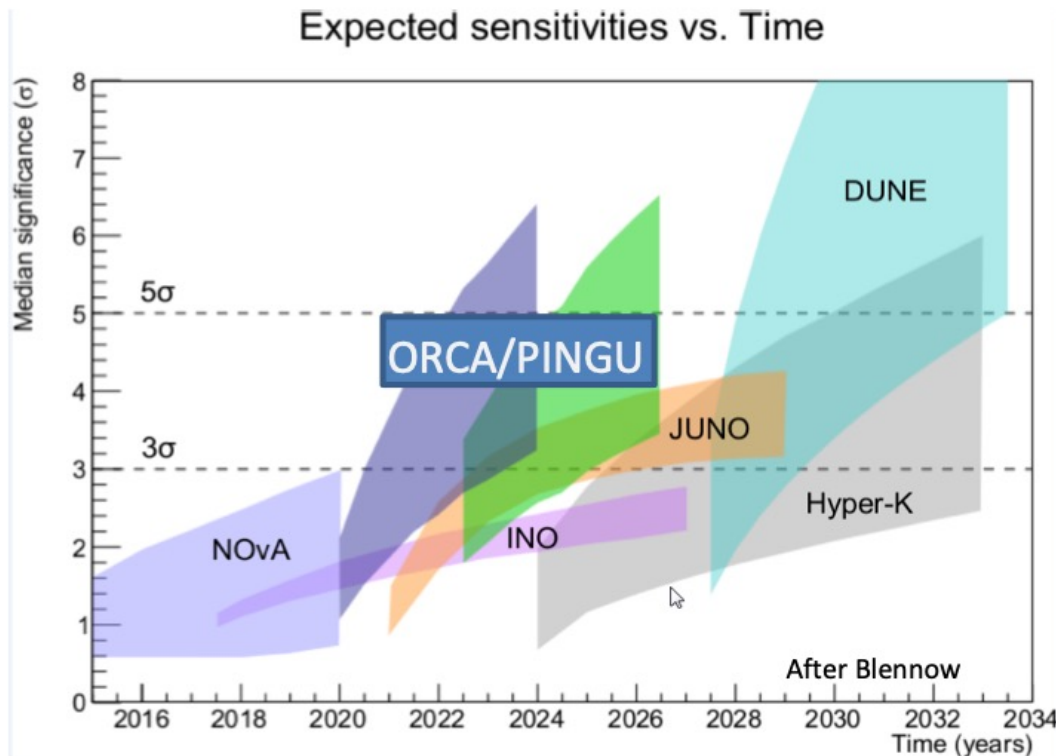
- $\nu_e$  (CC) +  $\nu_x$  (NC): cascades

→ distinction of event types



plots by Sebastian Böser

# Global NMO sensitivity vs. time



NMO sensitivity depends on

- oscillation parameters, e.g.  $\delta_{CP}$  for DUNE,  $\theta_{23}$  for atm. exp.
- detector performance, e.g. energy resolution for JUNO



# LECTURE QUIZ

## Question 5

What detector technology is used in the NOvA Far Detector?

C : Water Cherenkov Detector

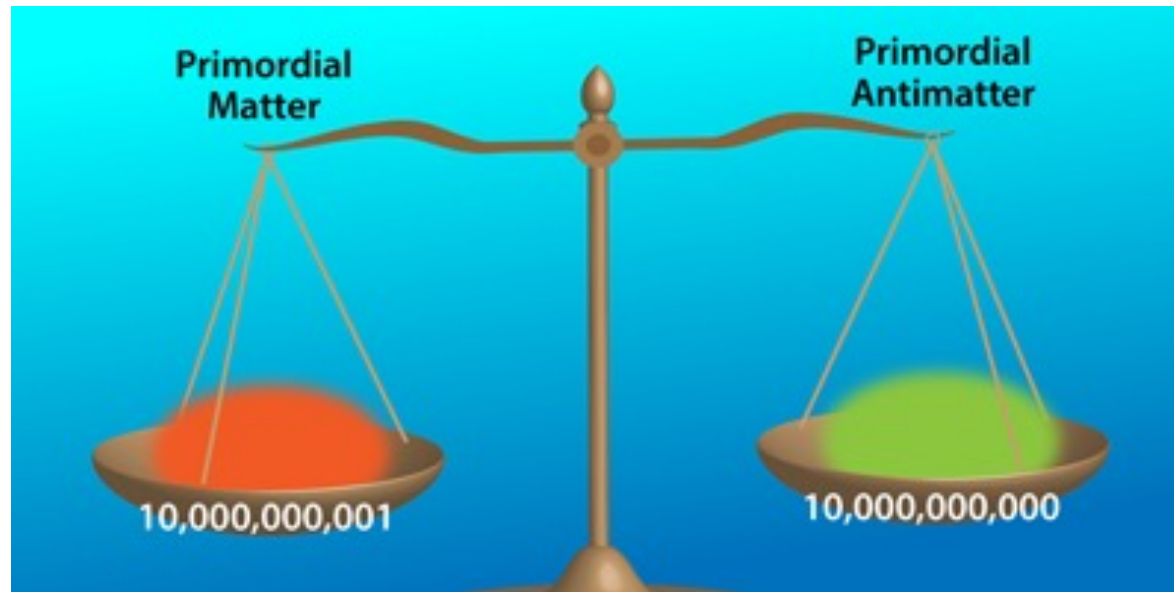
D : Liquid Argon Detector

E : Liquid Scintillator Detector



# CP violation

... is one of the three preconditions of creating **matter-antimatter asymmetry**:



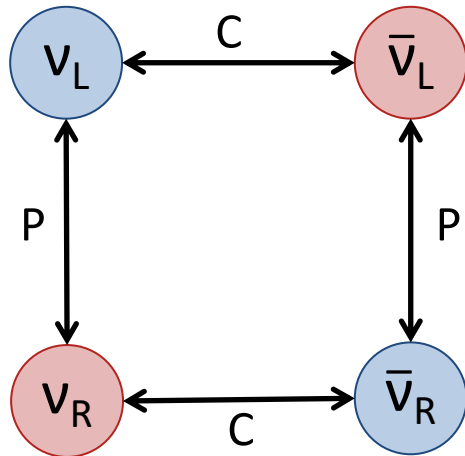
→ matter excess is tiny, but **CP violation in the quark sector is not sufficient**

CP violation in neutrino oscillations opens the door for **leptonic CP violation**

→ can still be **1000x larger than in the quark sector**

→ **Leptogenesis**: Leptonic CP asymmetry can be transferred to baryon sector

# Effects of the leptonic CP phase



→ **Neutrinos** themselves violate both P and C-parities.

→ **In oscillations:**

CP conservation:  $P(\nu_\alpha \rightarrow \nu_\beta) = P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta)$

CP violation:  $P(\nu_\alpha \rightarrow \nu_\beta) \neq P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta)$

but

$P(\nu_\alpha \rightarrow \nu_\beta) = P(\bar{\nu}_\beta \rightarrow \bar{\nu}_\alpha)$  **CPT**

Full three-flavor oscillation probability:

$$P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta}$$

$$-4 \sum_{i < j} \text{Re} [U_{\alpha i} U_{\alpha j}^* U_{\beta i}^* U_{\beta j}] \sin^2 \left[ \frac{\Delta m_{ji}^2 L}{4E} \right]$$

$$+2 \sum_{i < j} \text{Im} [U_{\alpha i} U_{\alpha j}^* U_{\beta i}^* U_{\beta j}] \sin \left[ \frac{\Delta m_{ji}^2 L}{2E} \right]$$

same for neutrinos and antineutrinos

→ **conserves CP-symmetry**

→ flavor disappearance & appearance

different for neutrinos and antineutrinos

→ **violates CP-symmetry**

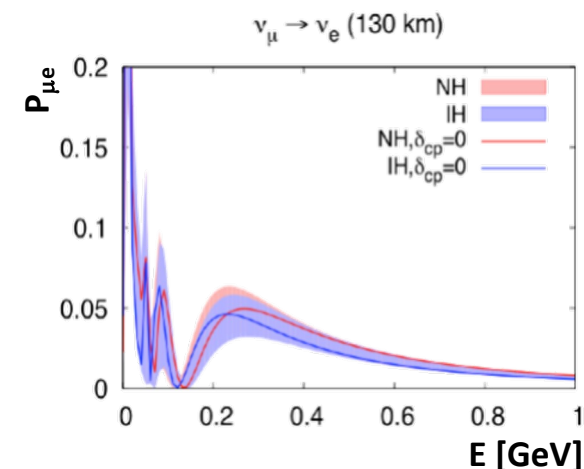
→ **only appearance oscillations!**

# $\nu_\mu \rightarrow \nu_e$ oscillation probability: $\delta_{CP}$ vs. NMO

Oscillation probability for  $\nu_e$  appearance  
in a  $\nu_\mu$  neutrino beam:

$$\begin{aligned}
 P_{\mu e(\bar{\mu} \bar{e})} = & \text{atmospheric oscillations } \rightarrow T2K \quad \sin^2 \theta_{23} \sin^2 2\theta_{13} \left( \frac{\Delta_{13}}{B_\pm} \right)^2 \sin^2 \left( \frac{B_\pm L}{2} \right) \quad \text{effects of weak matter potential} \\
 & \text{solar oscillations} \quad + \cos^2 \theta_{23} \sin^2 2\theta_{12} \left( \frac{\Delta_{12}}{A} \right)^2 \sin^2 \left( \frac{AL}{2} \right) \approx 0 \quad \text{leptonic CP violation} \\
 & + J \frac{\Delta_{12}}{A} \frac{\Delta_{13}}{B_\pm} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{B_\pm L}{2} \right) \cos \left( \mp \delta - \frac{\Delta_{13} L}{2} \right) \quad \text{neutrino-ant } P(\nu_\mu \rightarrow \nu_e) \text{ for } 130 \text{ km } m
 \end{aligned}$$

- matter effects and  $\delta_{CP}$  both lead to differences in neutrino/antineutrino oscillation probabilities
- $\delta_{CP}$  best measured over short baselines where impact of matter effects is small!





# T2K: Tokai-to-Kamioka Experiment

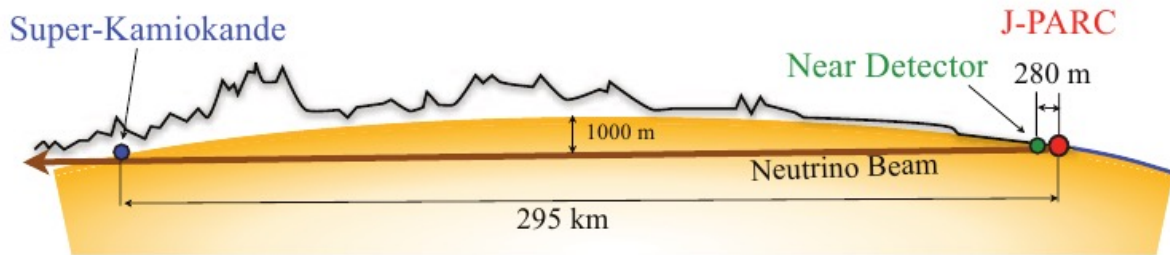
## T2K Experiment



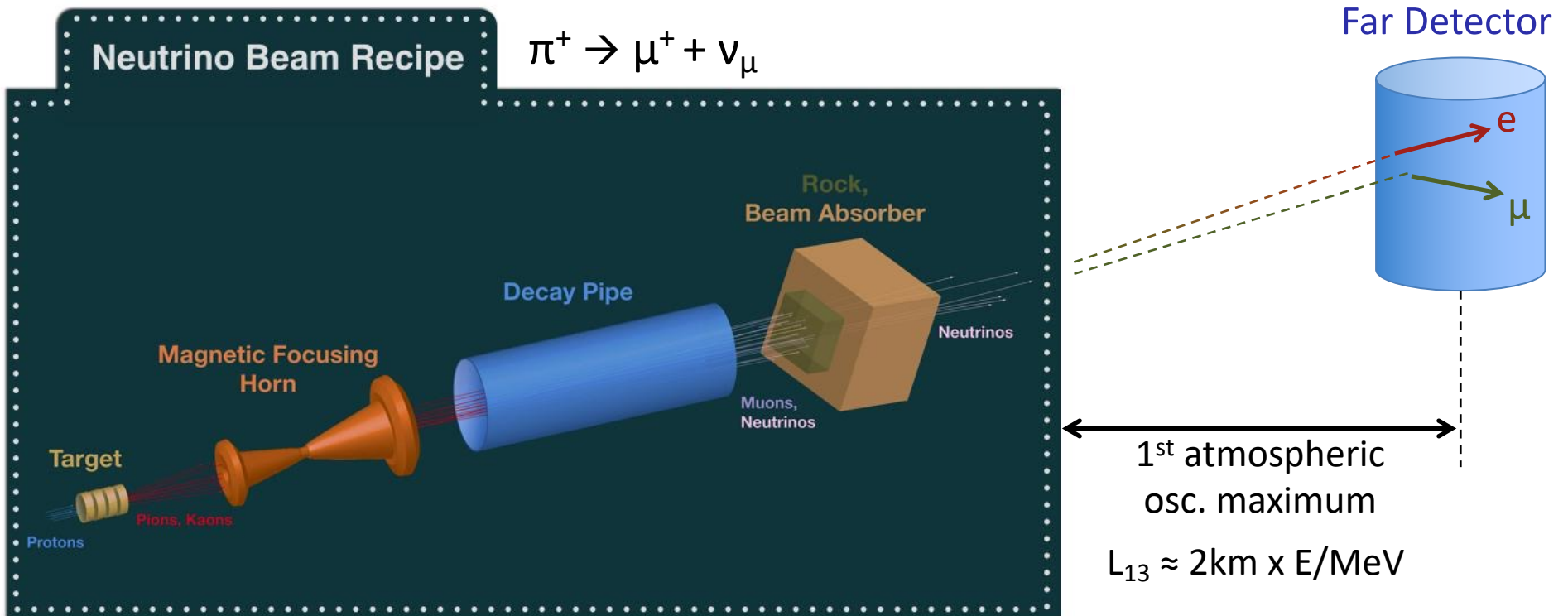
Super-Kamiokande  
(ICRR, Univ. Tokyo)



J-PARC Main Ring  
(KEK-JAEA, Tokai)



# Long-baseline $\nu_\mu$ beam experiments

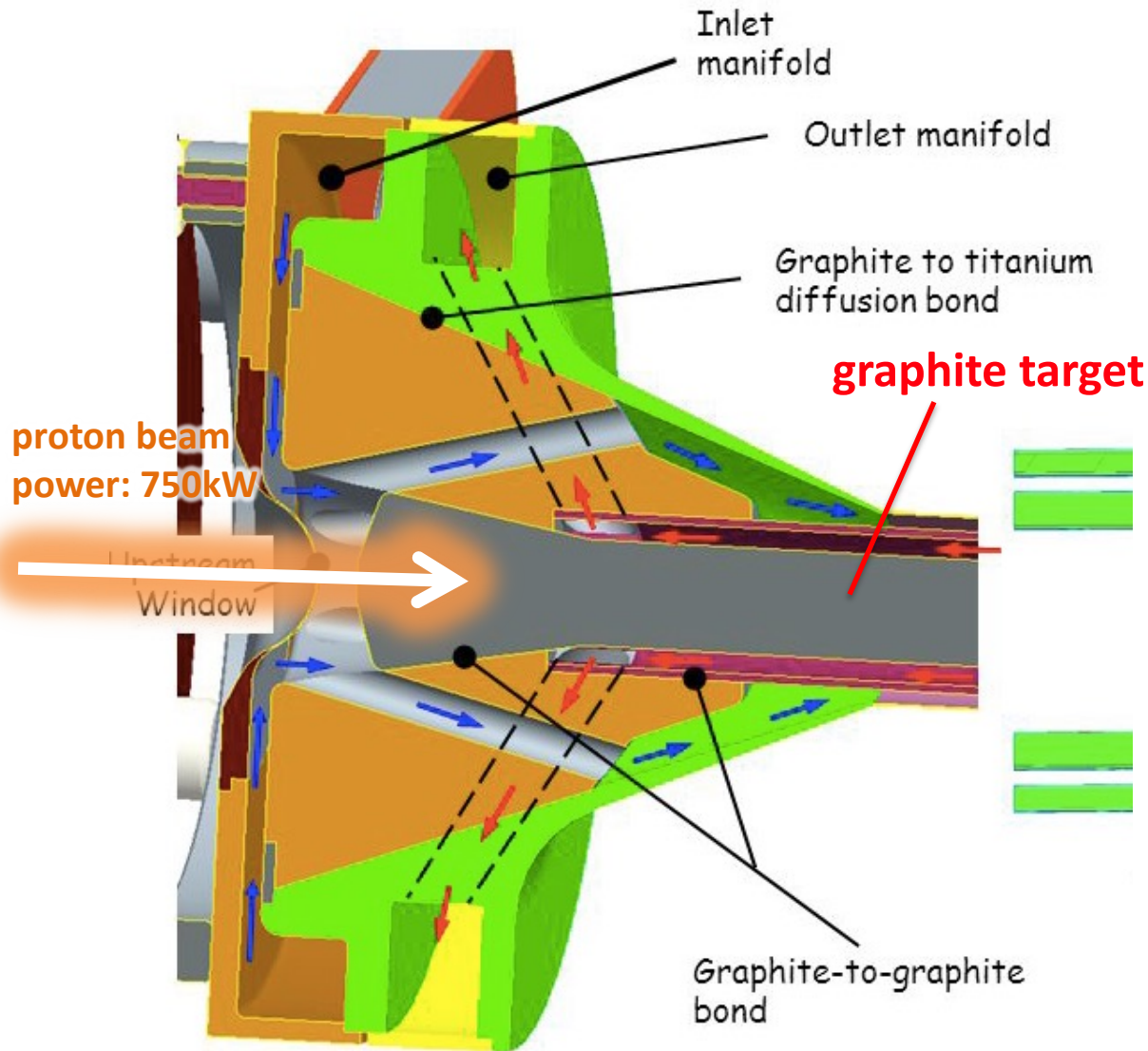


**Search modes:** ■ Disappearance oscillations:  $\nu_\mu \rightarrow \nu_\mu \rightarrow \theta_{23}, \Delta m_{32}^2$

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2 2\theta_{23} \sin^2 \left( \frac{\Delta m_{32}^2}{4E} \right)$$

■ Appearance oscillations:  $\nu_\mu \rightarrow \nu_e \rightarrow \theta_{13}, \delta_{CP}$

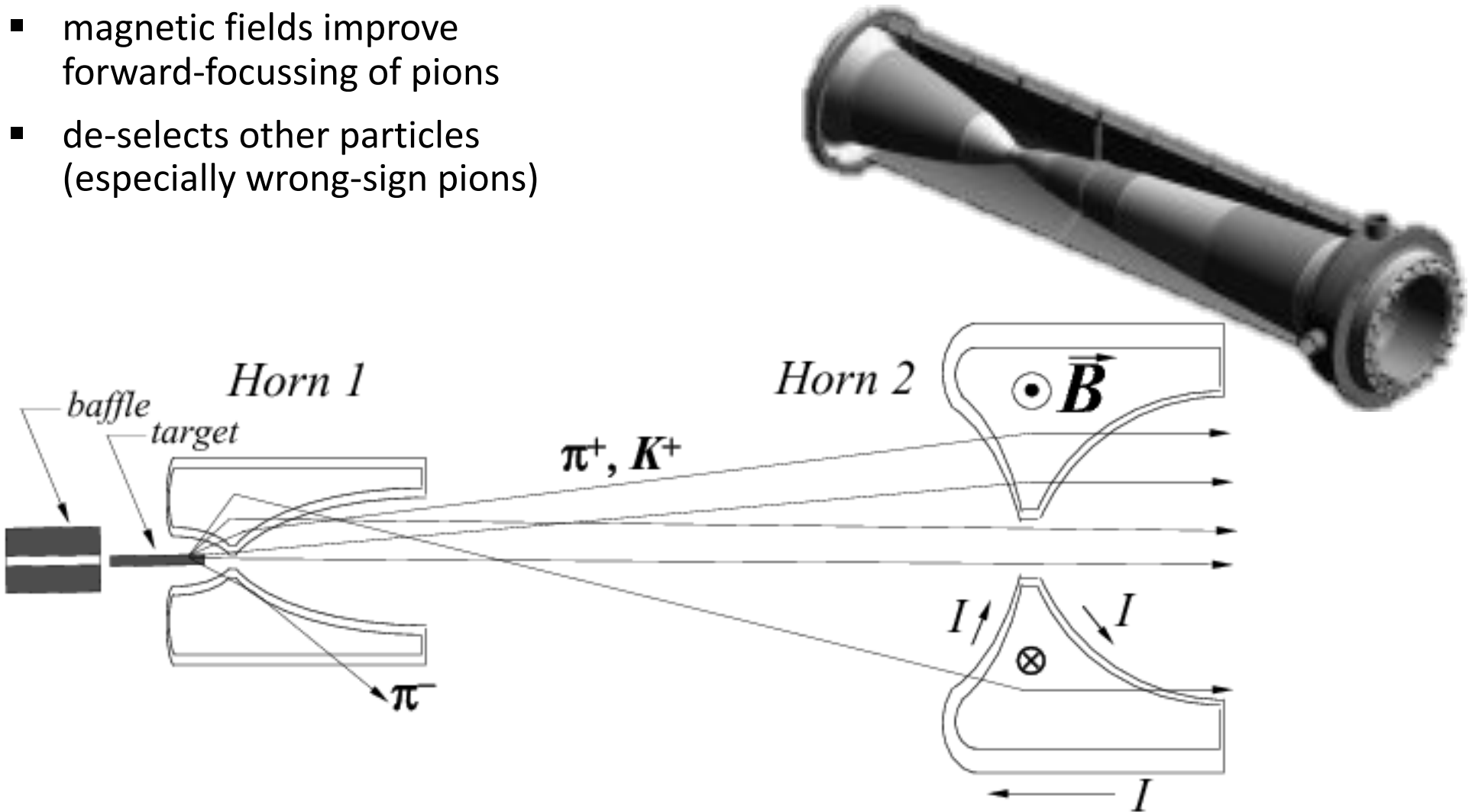
# Neutrino target



- production of charged pions (and kaons) by interactions of protons on carbon
- light material favors higher-energy pions
- pions are beamed in forward direction
- beams are typically pulsed  
→ BG reduction

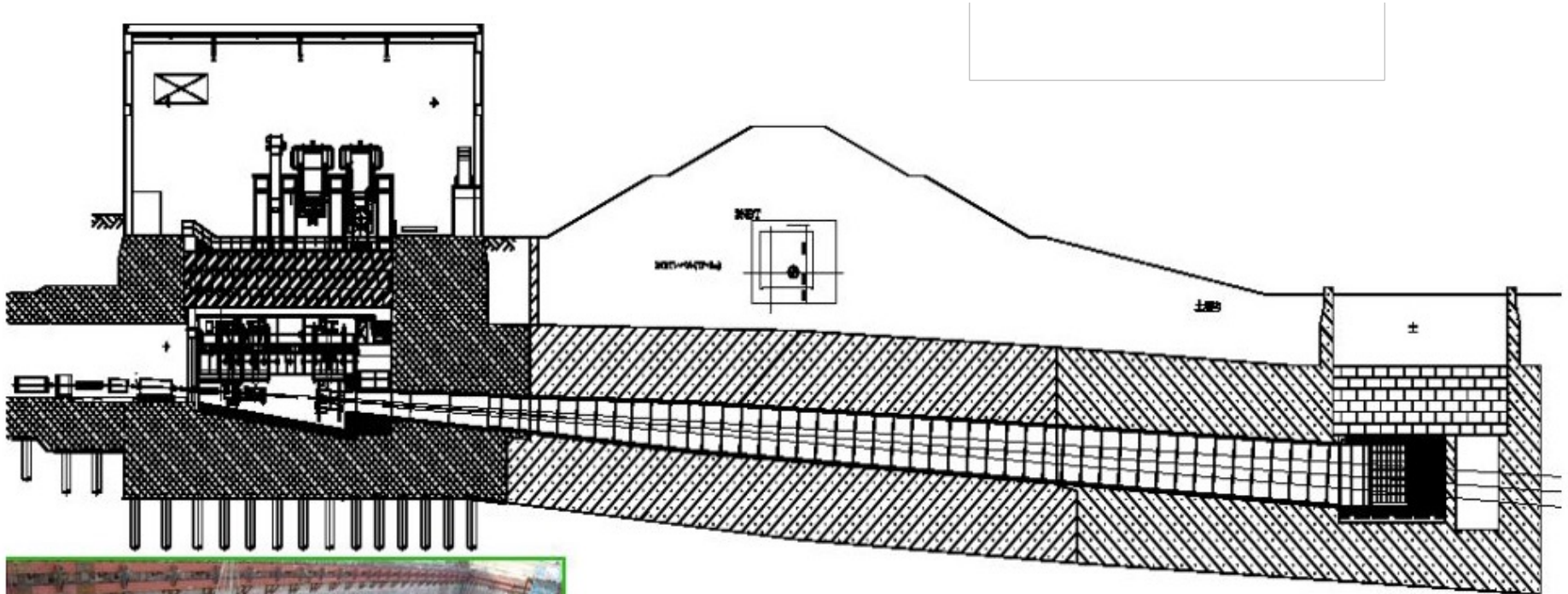
# Focussing horns

- magnetic fields improve forward-focussing of pions
- de-selects other particles (especially wrong-sign pions)





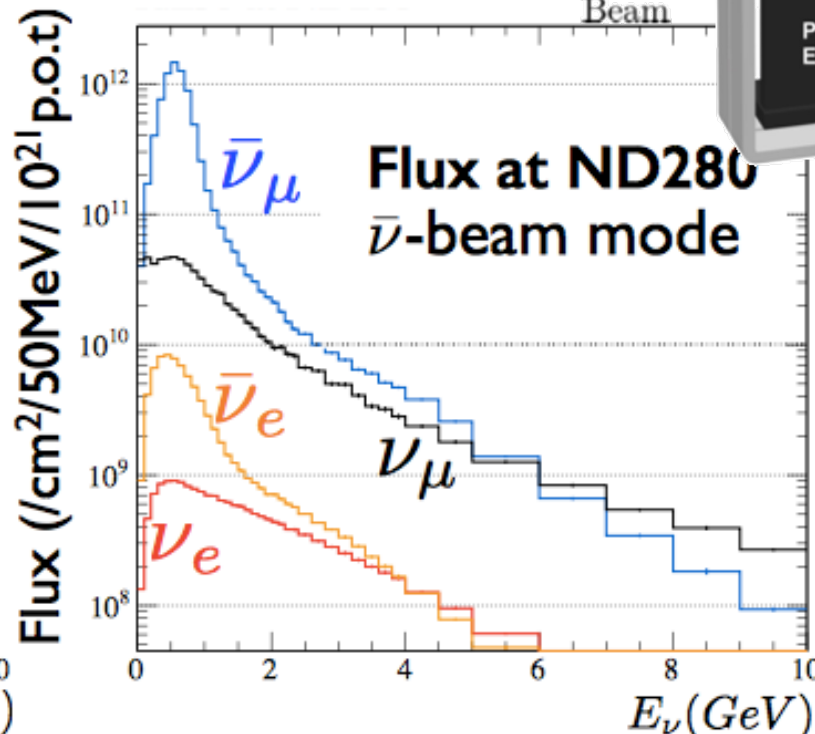
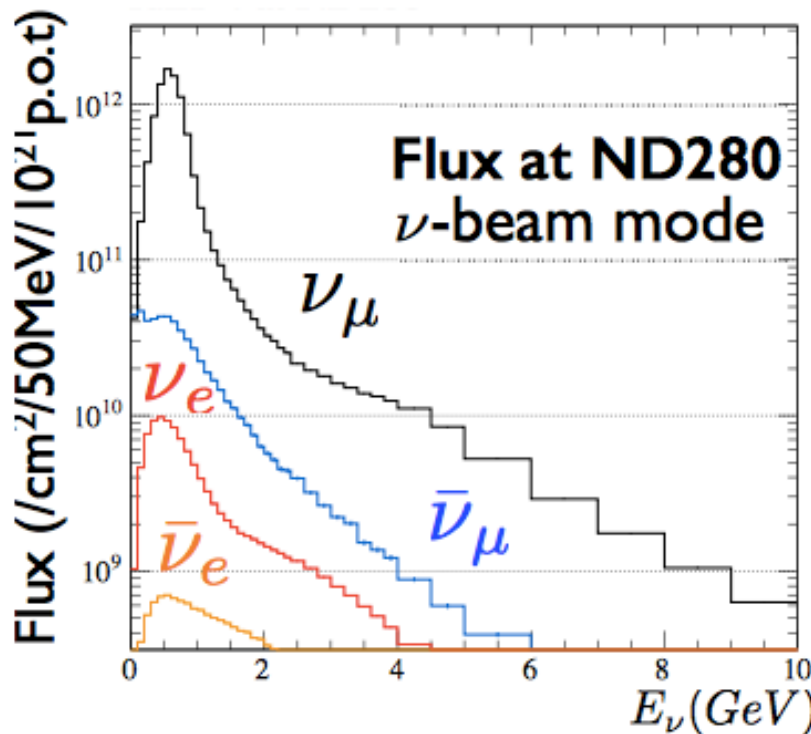
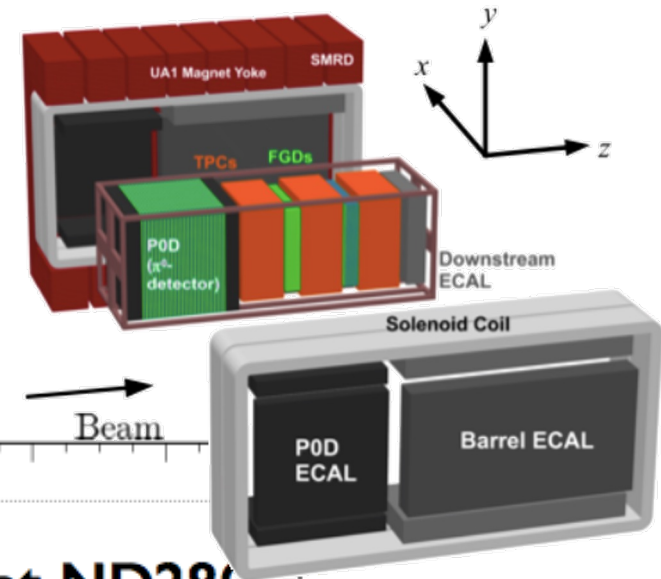
# Inclined decay pipe



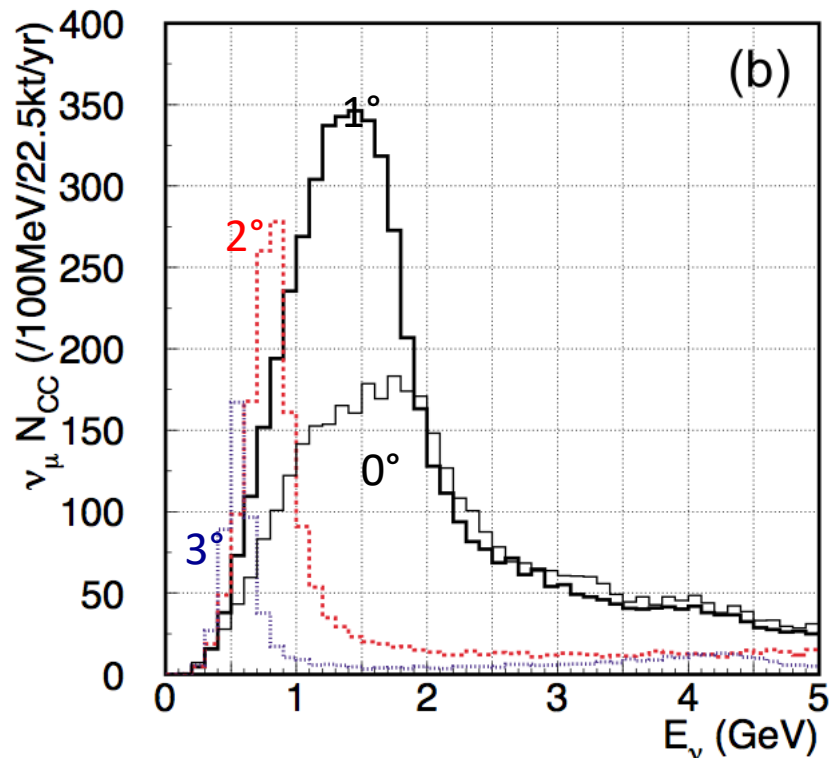
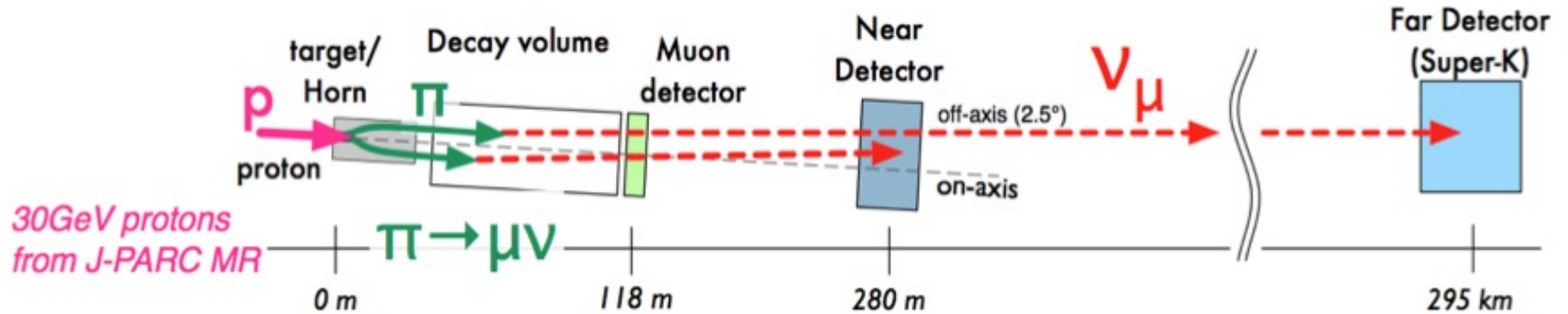
- evacuated pipe for  $\pi^+ \rightarrow \mu^+ + \nu_\mu$  (*neutrino mode*)
- try to balance pion and muon decay  
not wanted:  $\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$
- tunnel has to be inclined to compensate curvature of Earth surface  $\rightarrow$  expensive!!

# T2K Near Detectors for $\nu$ spectrum

- some **intrinsic beam contamination** with  $\nu_e$  flavor
- polarity of beam horn switched to obtain  $\bar{\nu}_\mu$ -beam
- near detector (ND280) to measure beam direction and composition, cross-sections ... (reduce systematics)



# T2K: Off-axis beam



## $\nu_\mu$ -beam energy spectrum

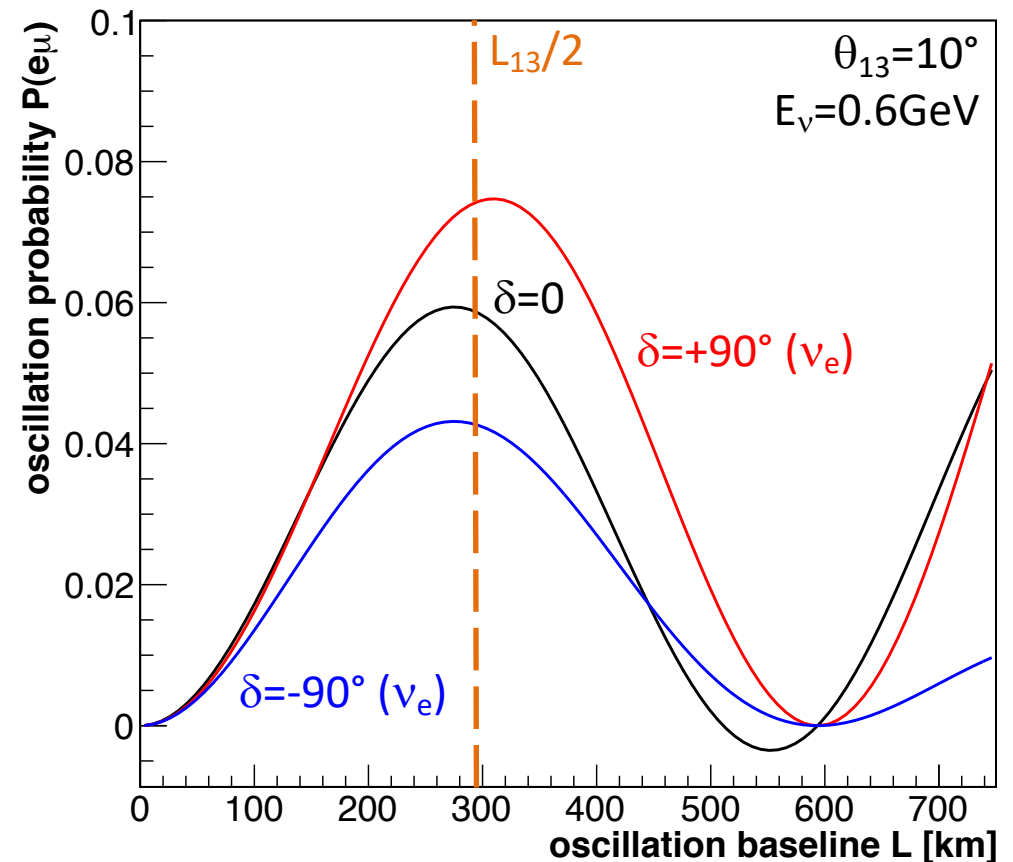
- on-axis: wide-band beam
  - off-axis: narrower beam spectrum, increased peak intensity
- increased event rate at correct L/E
- less high-energy background

# Short-baseline $\nu_e$ appearance probability

## Effective oscillation probability

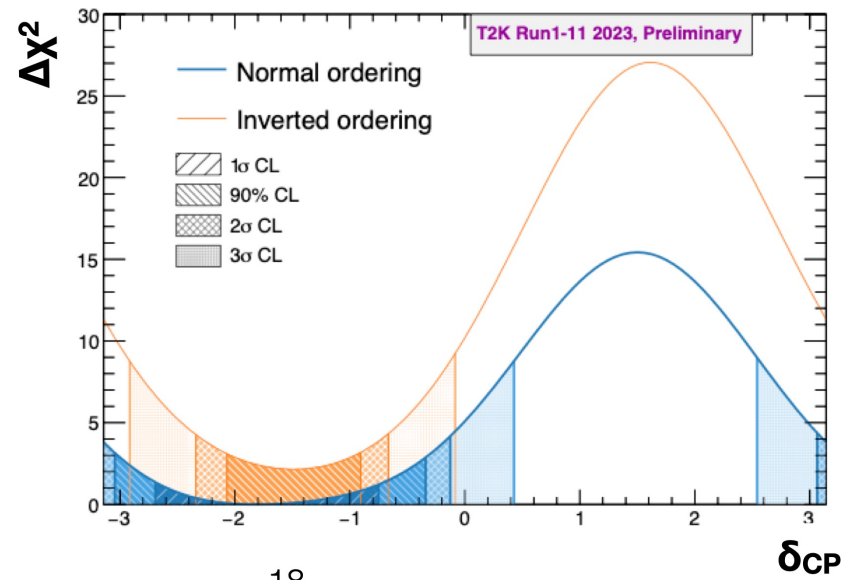
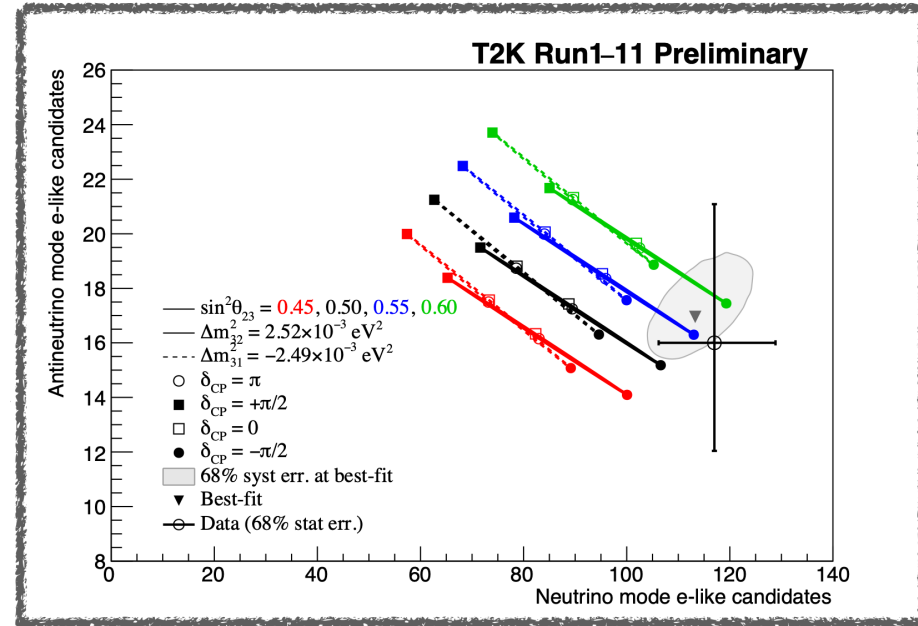
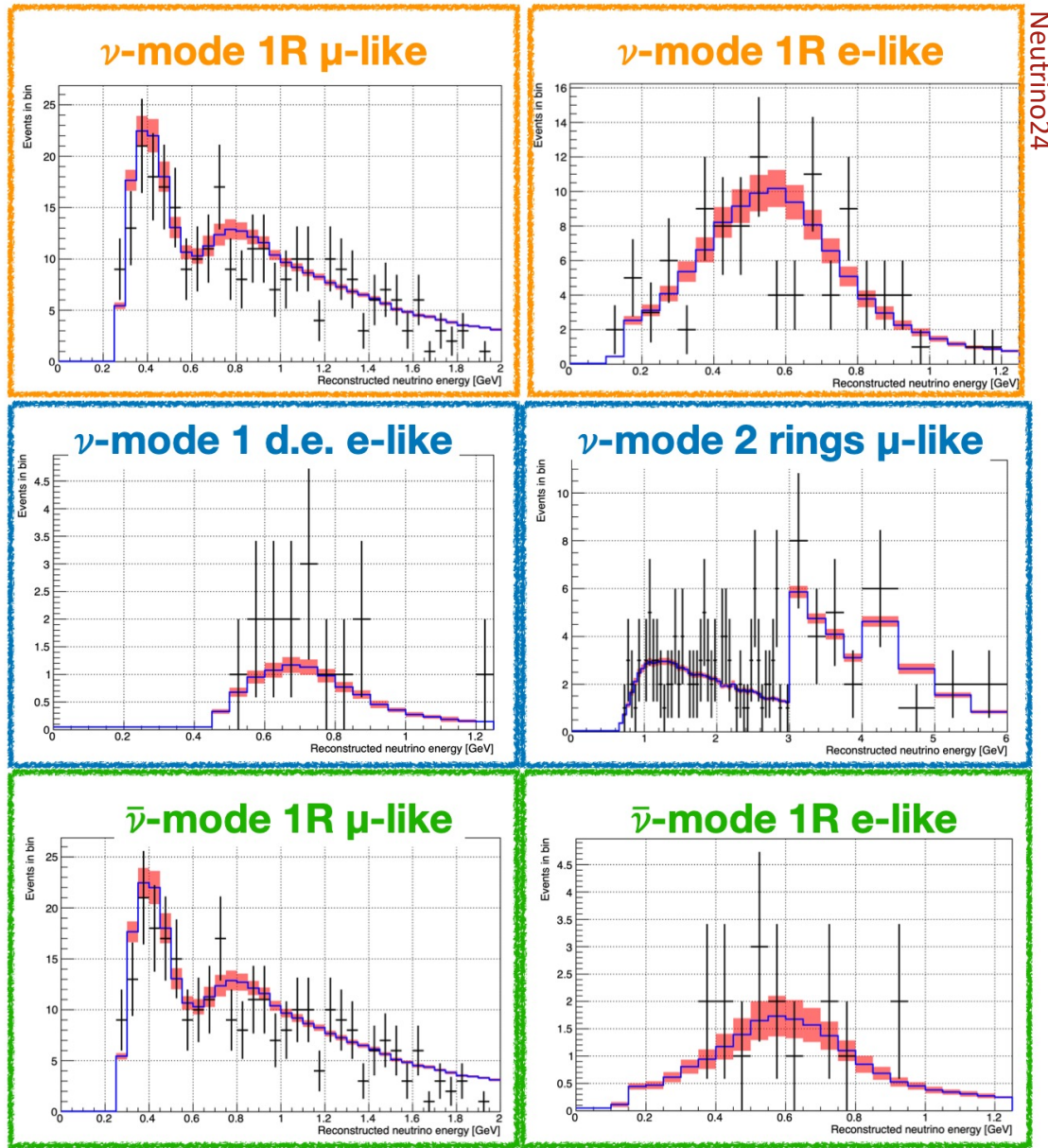
$$P_{\mu e} = \sin^2 \theta_{23} \sin^2 2\theta_{13} \sin^2 \left( \frac{\Delta m_{31}^2 L}{4E} \right) + h.o.f.(\theta_{ij}, \Delta m_{ij}^2) \cdot \cos(\mp \delta)$$

- term with CP phase shifts amplitude and position of 1<sup>st</sup> oscillation maximum
- neutrinos and antineutrino shifts are inverted



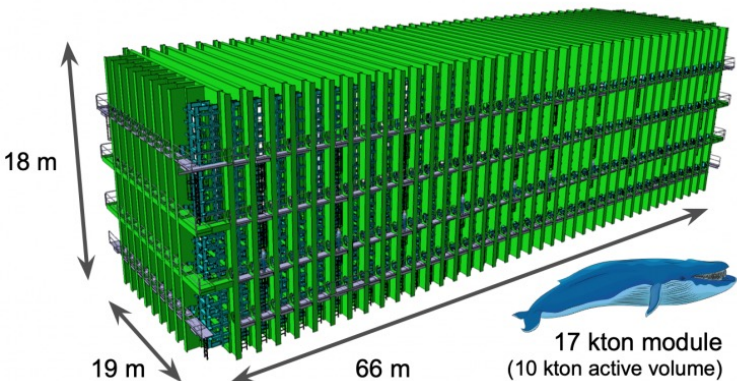
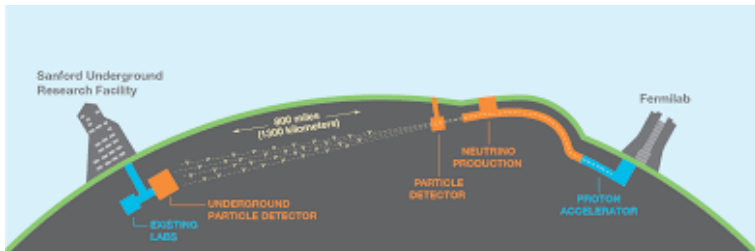
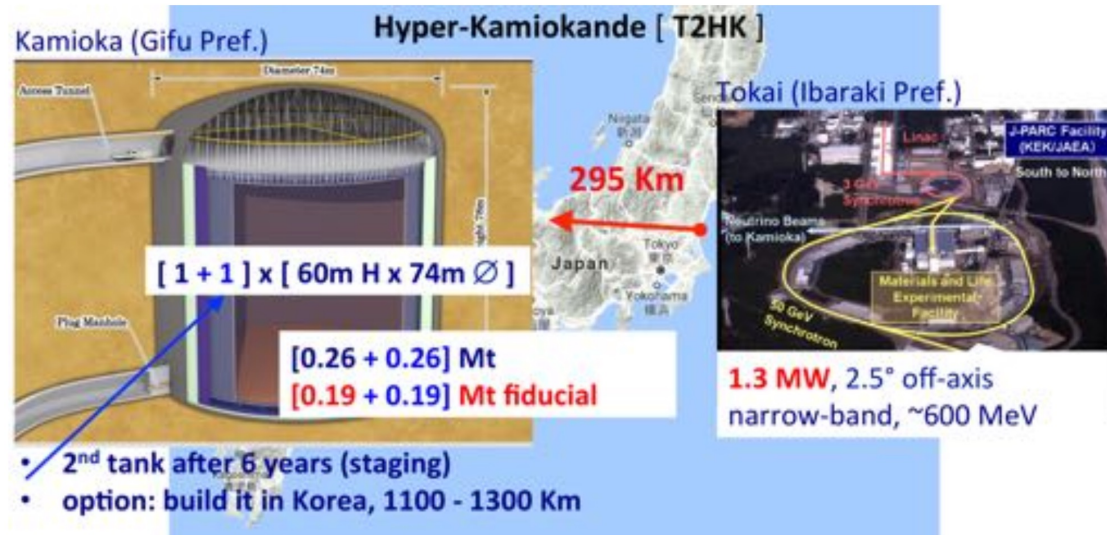


# T2K $\nu_\mu \rightarrow \nu_e$ appearance results for $\delta_{CP}$

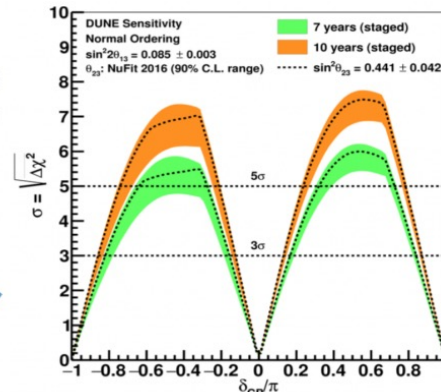


# Future experiments for CP-phase

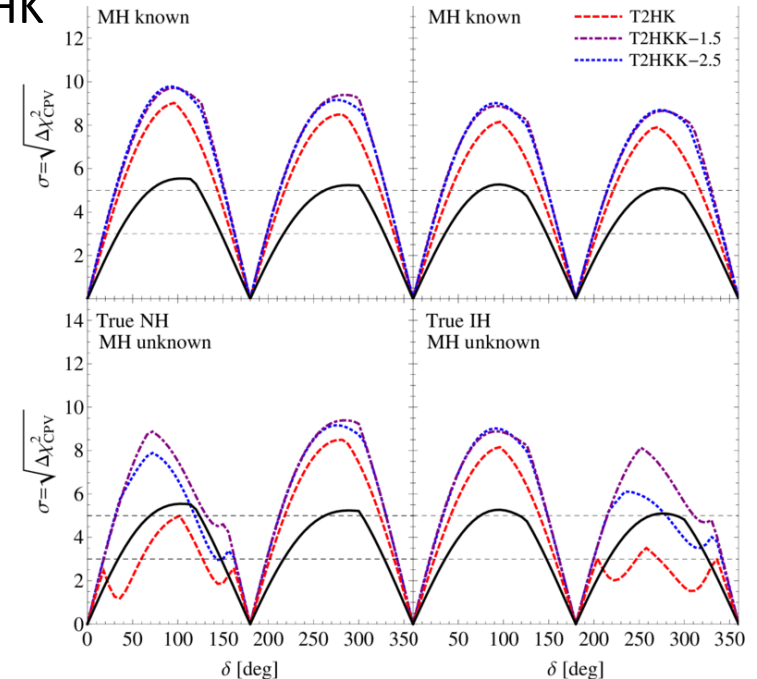
- **DUNE:** Fermilab → Homestake (1300 km)
- **T2HK:** Tokai → Kamioka (285 km)
- **ESSvSB:** Lund → ? (360/450 km)



DUNE



T2HK



# LECTURE QUIZ

## Question 6

What device is used in the T2K beam?

Q : Berillium target

R : Magnetic horn

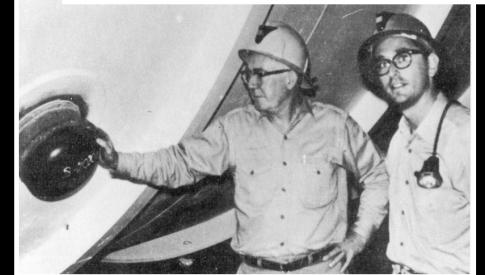
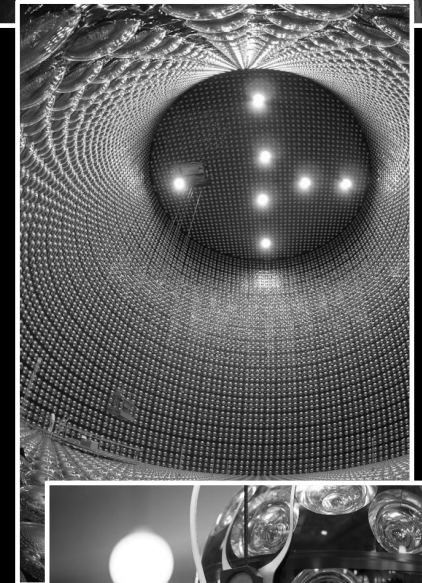
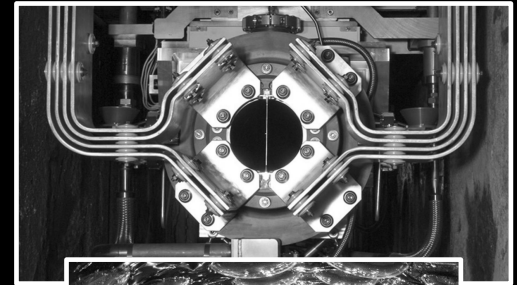
S : Neutrino lense





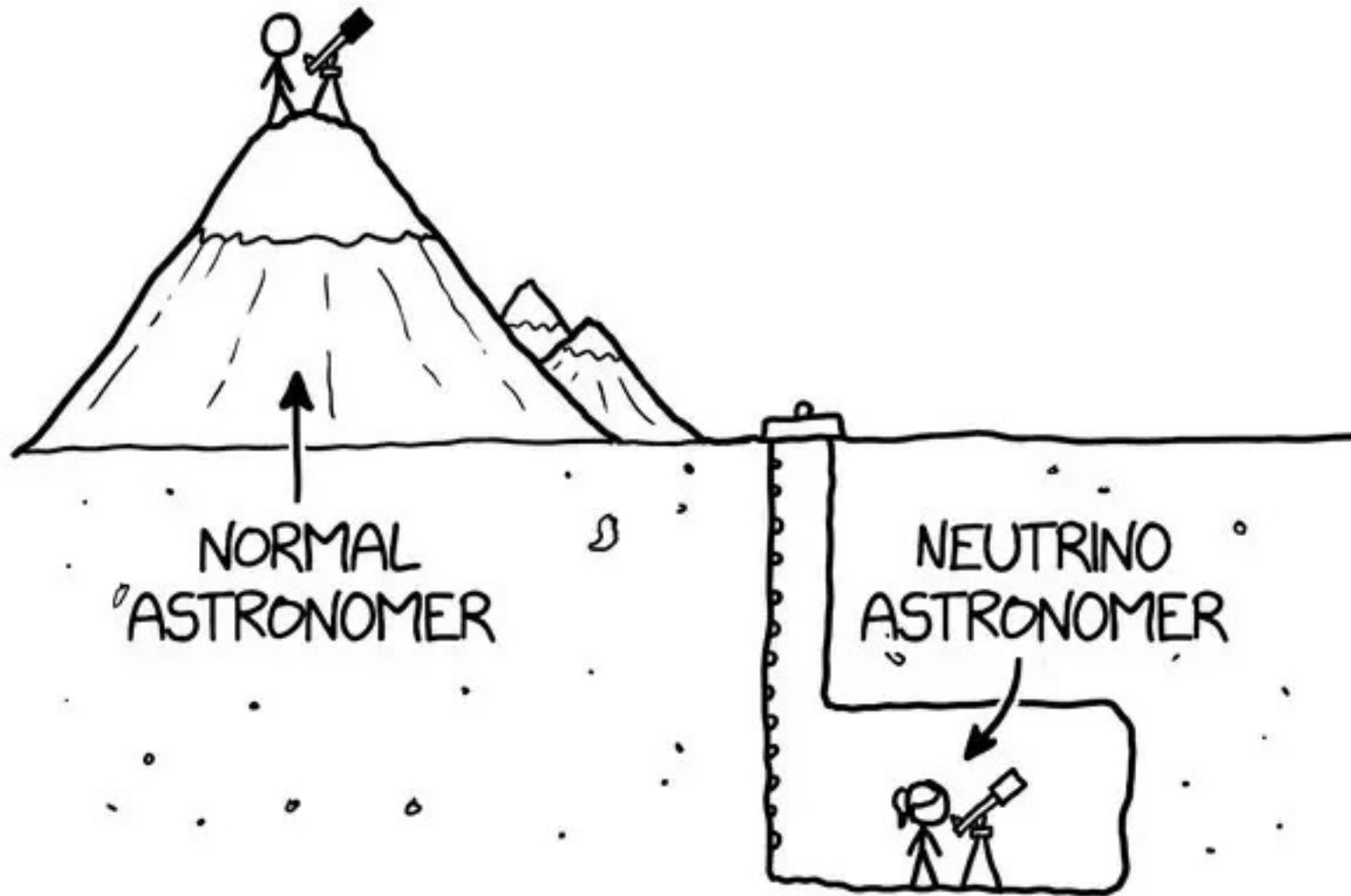
# Summary

- The discovery of **neutrino flavor oscillations** is the 1<sup>st</sup> evidence of physics beyond the original Standard Model.
- Historically, **natural neutrino sources** (e.g. atmospheric, solar  $\nu$ 's) have played a large role in their exploration. Precision experiments often use **reactors or beams**.
- **Basic oscillation parameters** (mixing angles, mass splittings) have been **measured on few %-level** but important ingredients are still missing.
- Upcoming oscillation experiments investigate the **neutrino mass ordering** (JUNO, ORCA, IC-Upgrade) and **CP phase  $\delta_{CP}$**  (T2HK, NovA, DUNE)
- Note: **Complementary searches** for non-standard oscillations (eV sterile neutrinos) are on-going.





# Thanks for your attention!



## Questions? Or is it time for \_\_\_\_\_?