



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



Direct Dark Matter Searches: Part I

Principles of direct detection: nuclear recoil

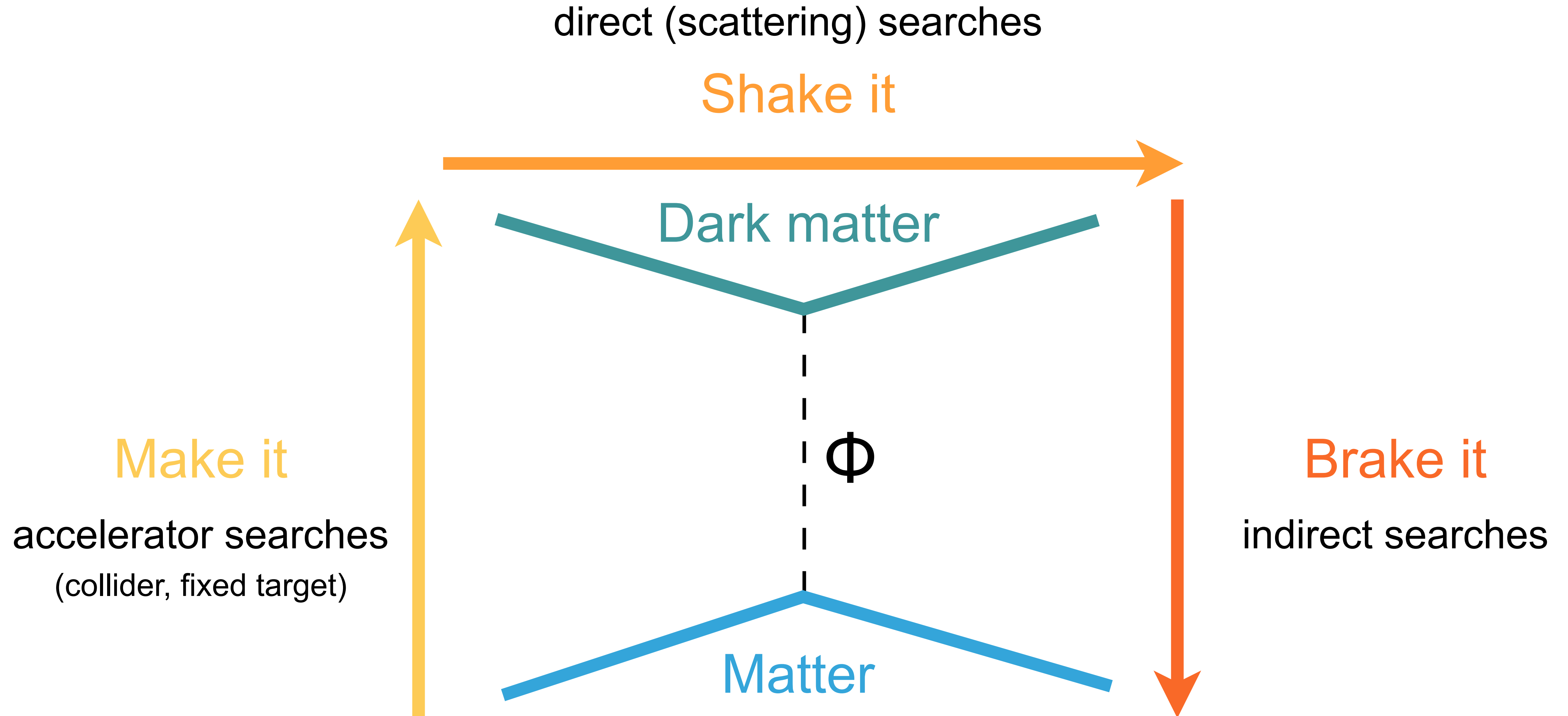
ISAPP School „Neutrinos and Dark Matter – in the lab and in the Universe“, 24.09.2024

Belina VON KROSIGK (bkrosigk@kip.uni-heidelberg.de)



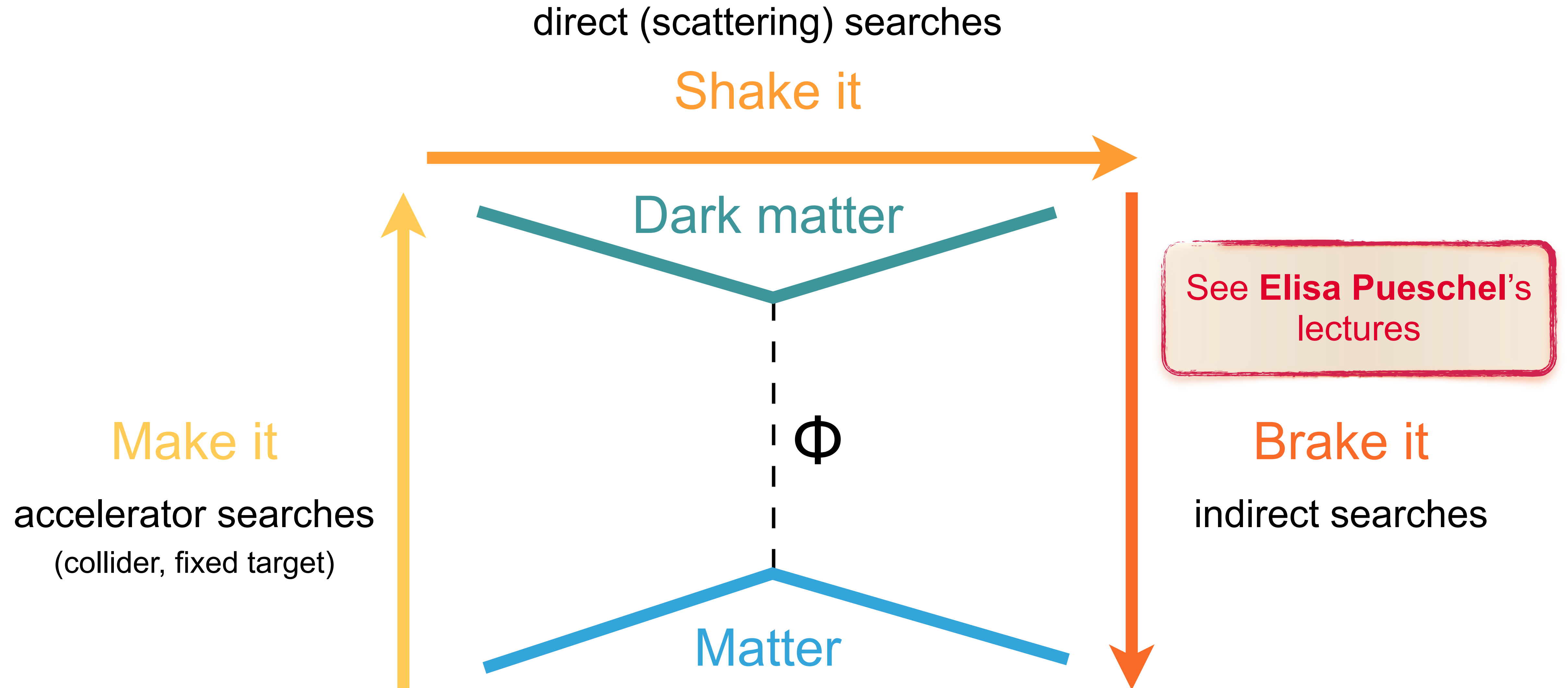


Ways to detect dark matter particles





Ways to detect dark matter particles



Ways to detect dark matter particles

direct (scattering) searches

Shake it

Dark matter

Matter

Φ

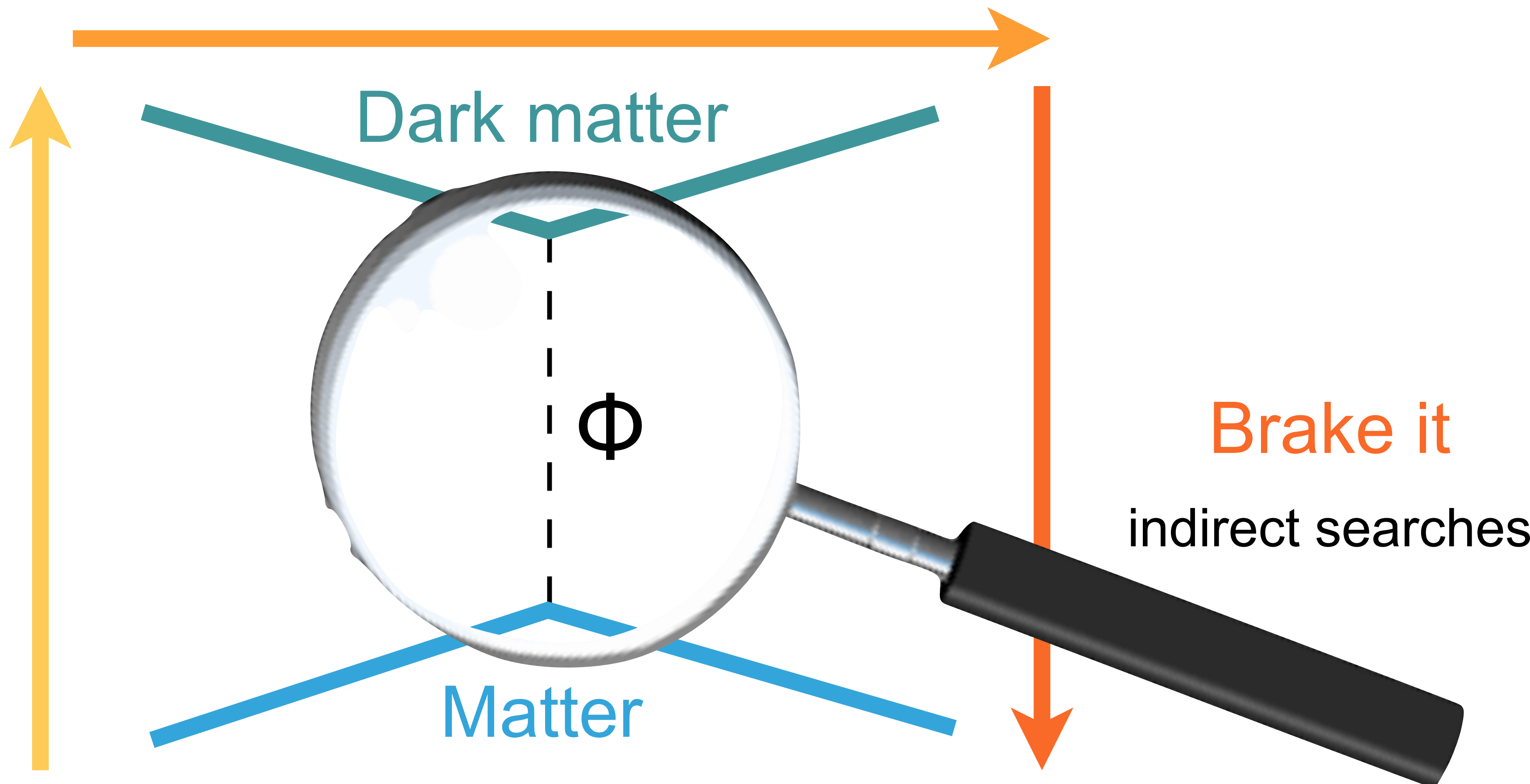
Brake it

indirect searches

See Jan Heisig's lectures

Make it

accelerator searches
(collider, fixed target)



Ways to detect dark matter particles

Subject of these lectures

direct (scattering) searches

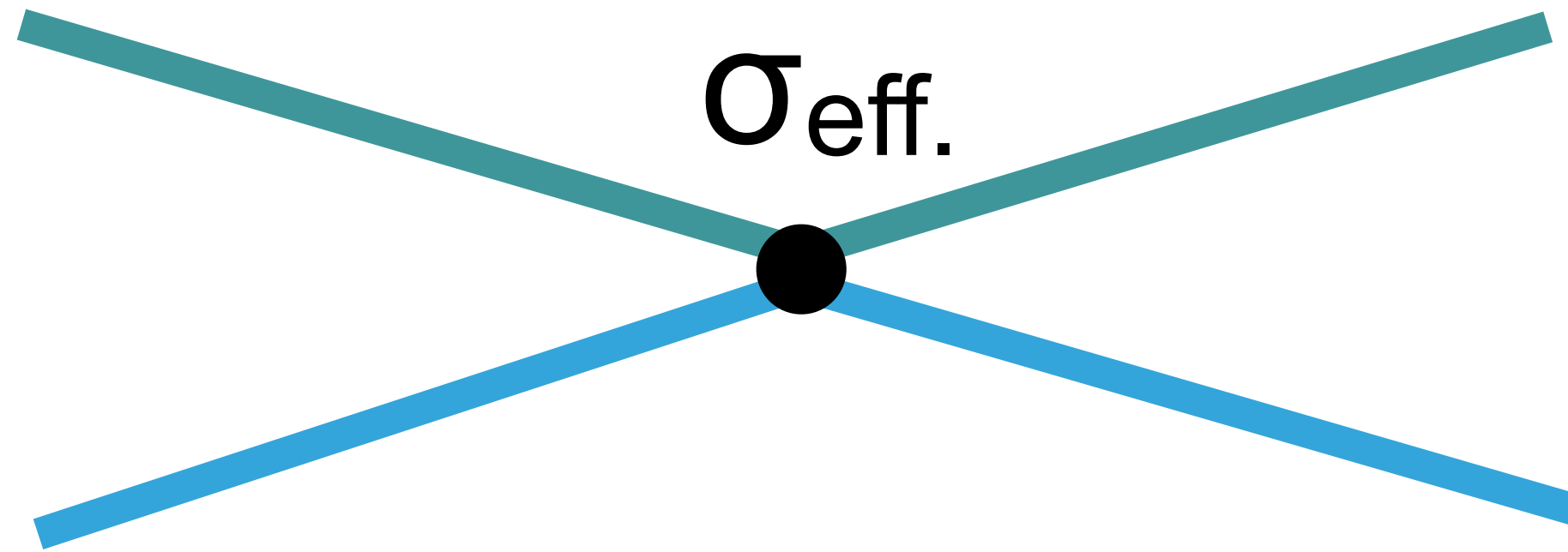
Shake it



Dark matter



$\sigma_{\text{eff.}}$



Matter

Make it

accelerator searches
(collider, fixed target)

Brake it

indirect searches





Ways to detect dark matter particles

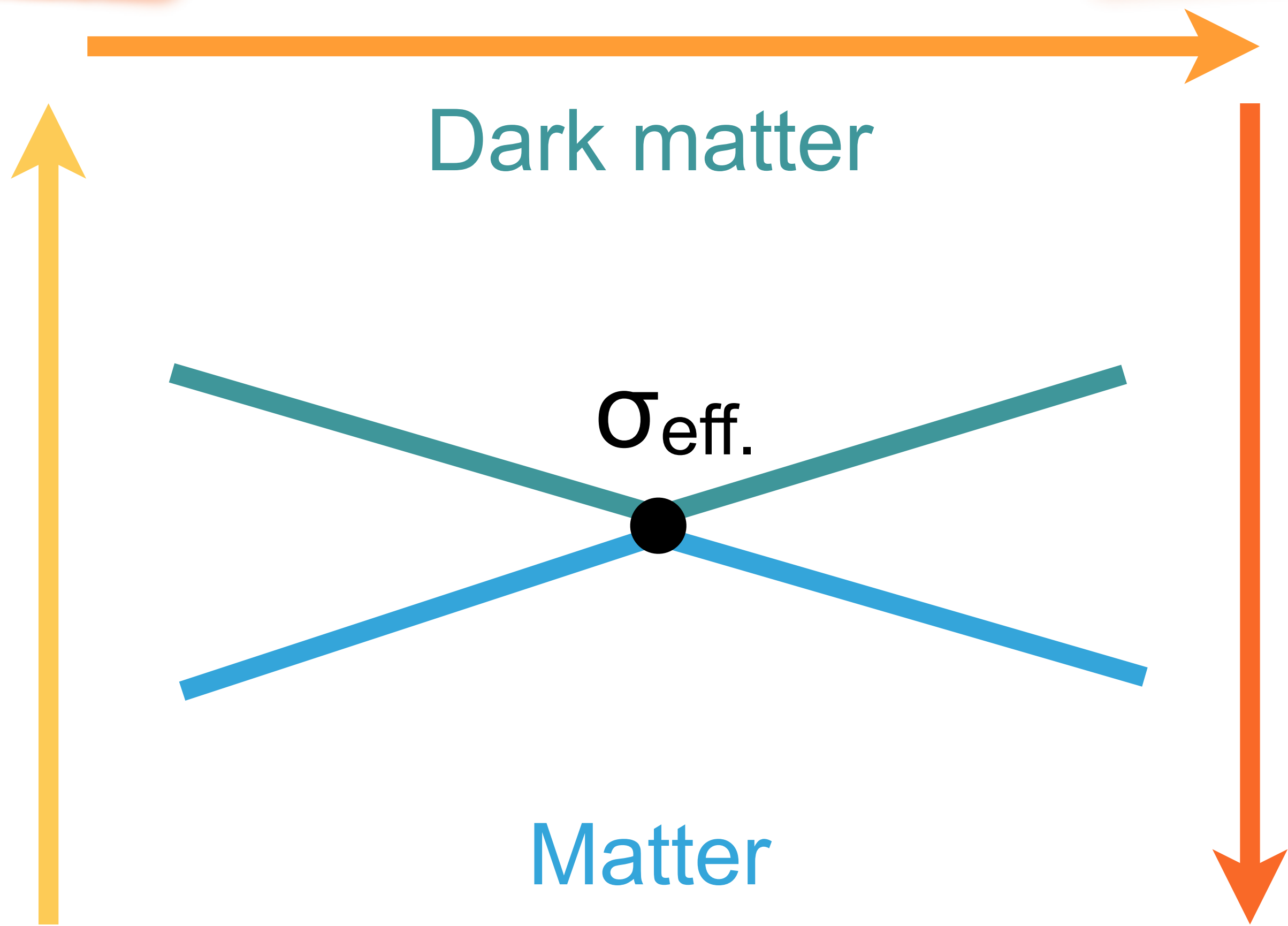
Subject of these lectures

direct (scattering) searches

Shake it

Non-scattering searches:
See **Béla Majorovits**' lectures

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Brake it
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Direct dark matter detection

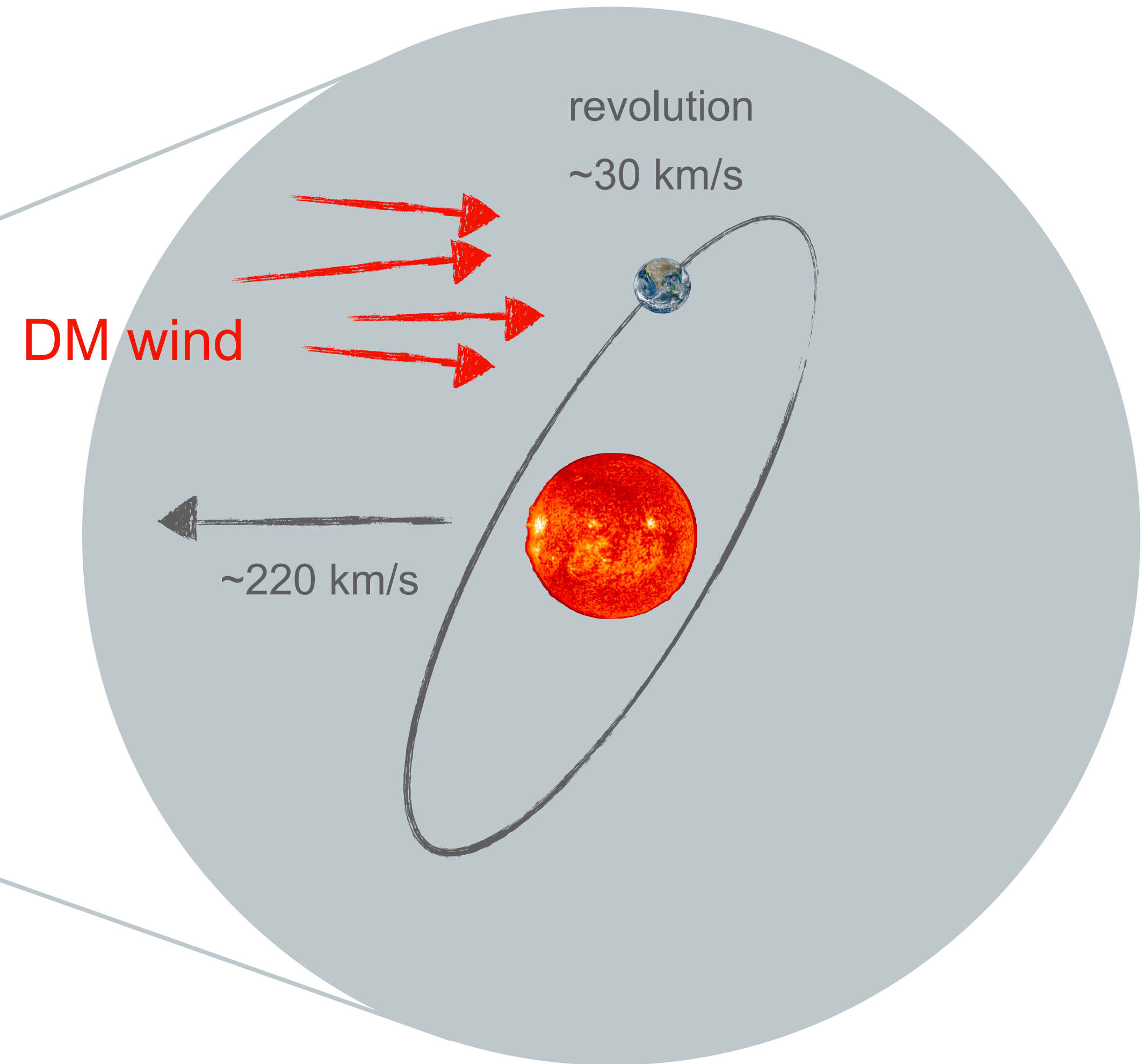
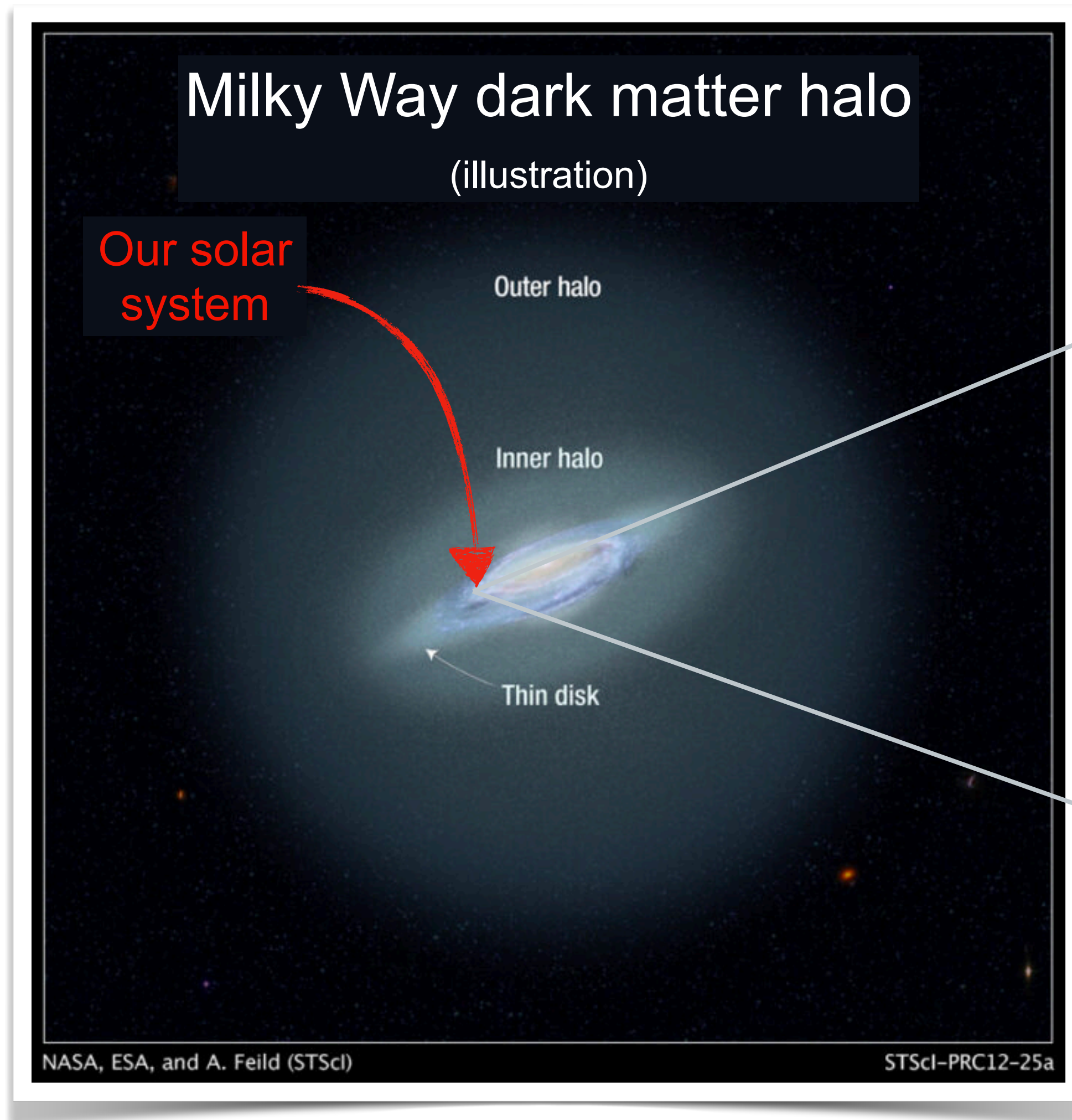
How to build a dark matter detector



Direct dark matter detection

How to build a *relic* **dark matter detector**

Taking advantage of galactic dark matter halo



Taking advantage of galactic dark matter halo

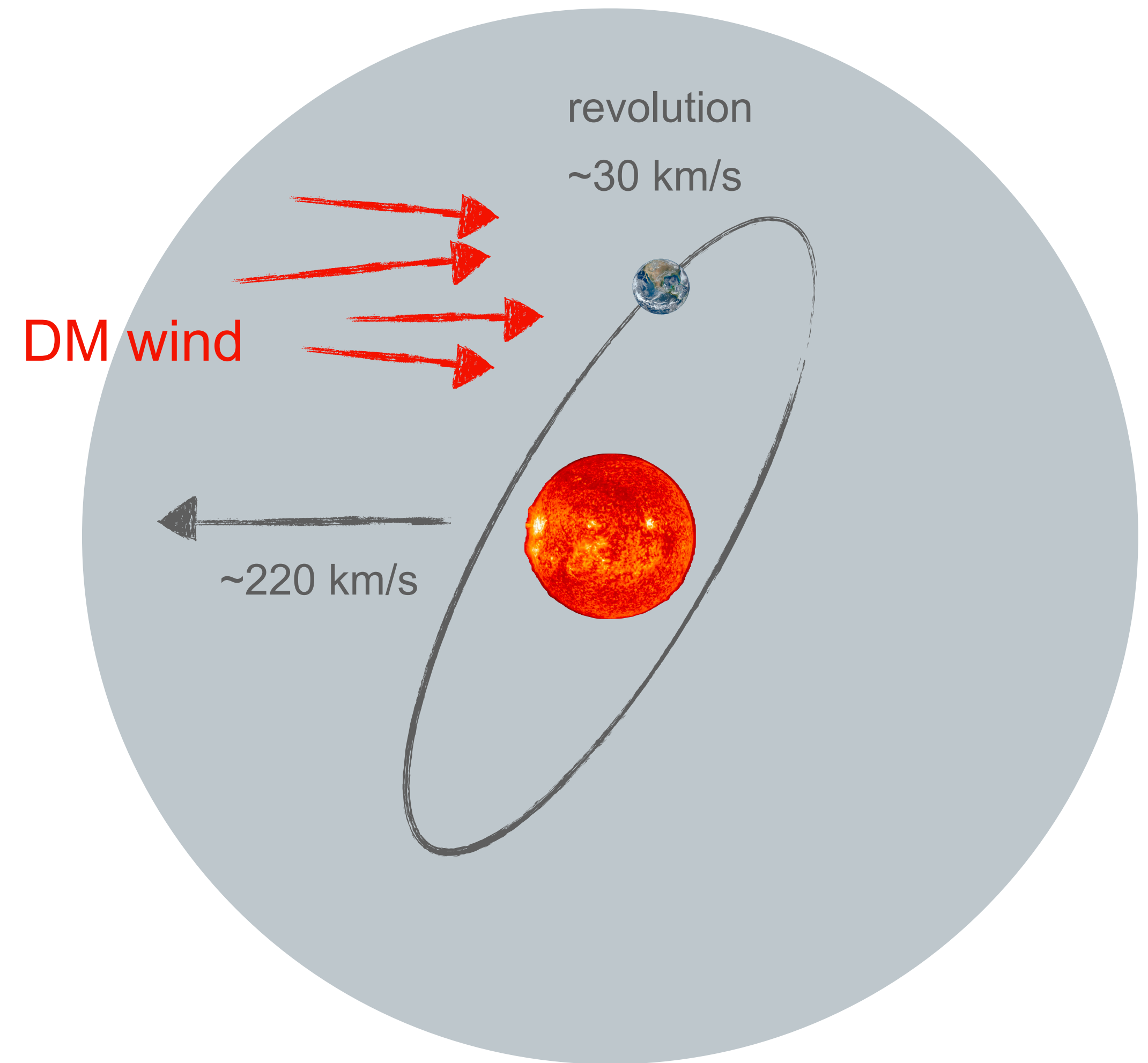
Place detector on Earth.



DM particles will permanently cross detector.



Search for interactions of DM particles with detector material.



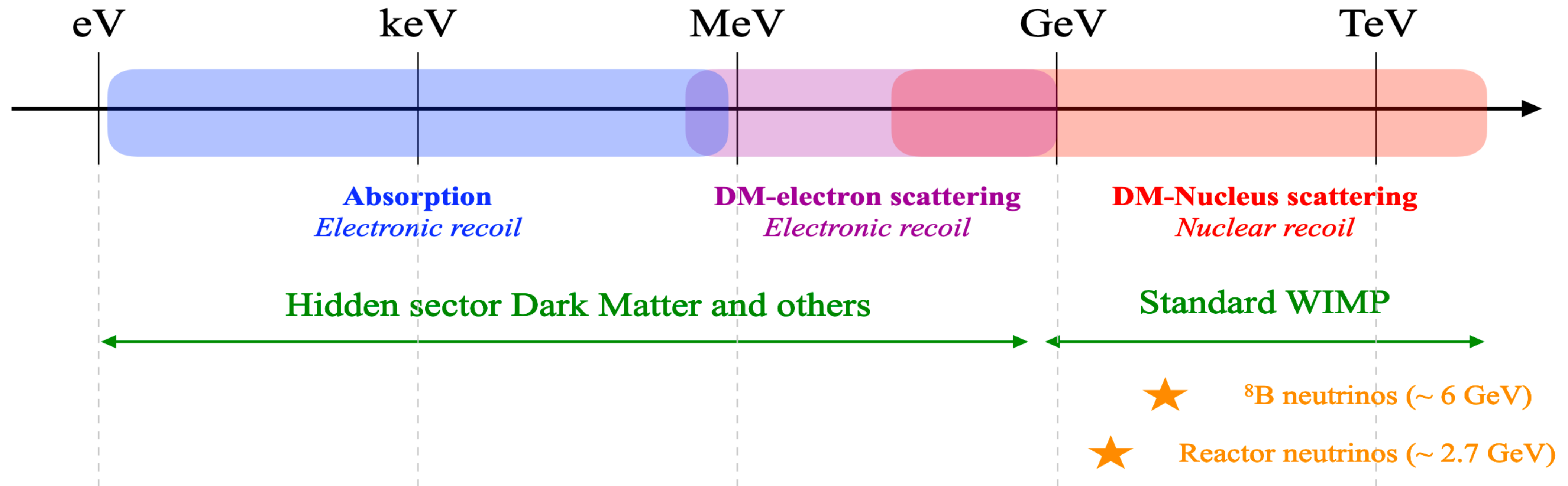


How to design a dark matter detector

- Expected candidates, interactions, and rates
- Background considerations
- Experimental signatures

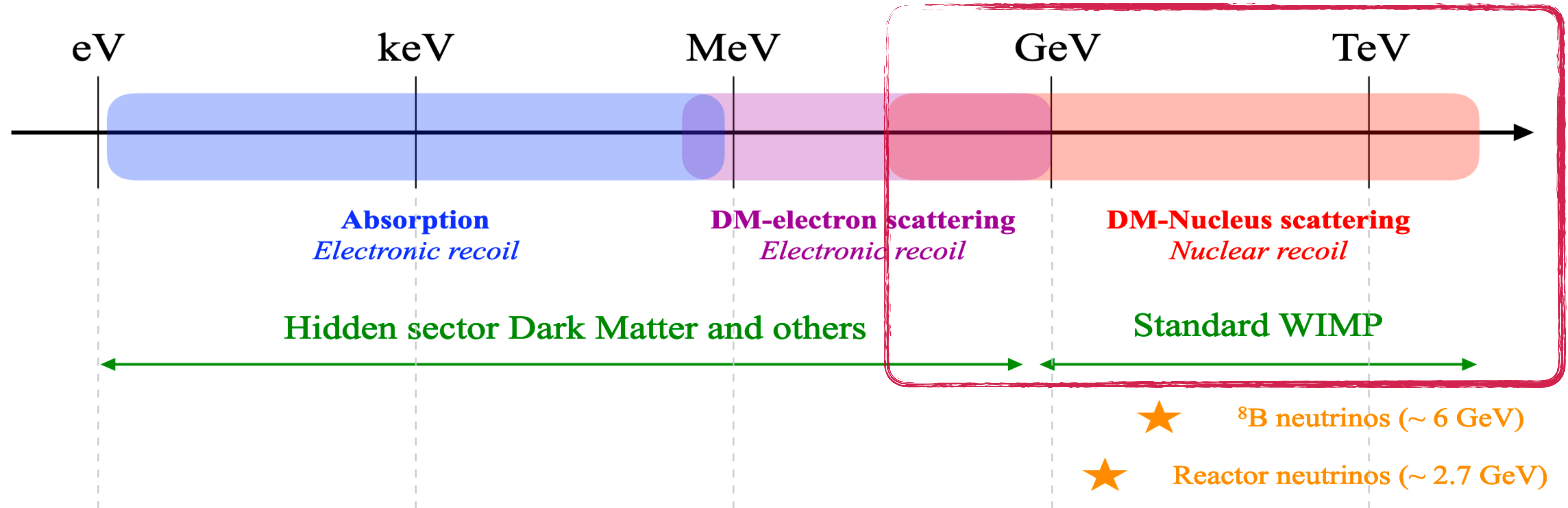
How to design a dark matter detector

■ Expected candidates, interactions, and rates



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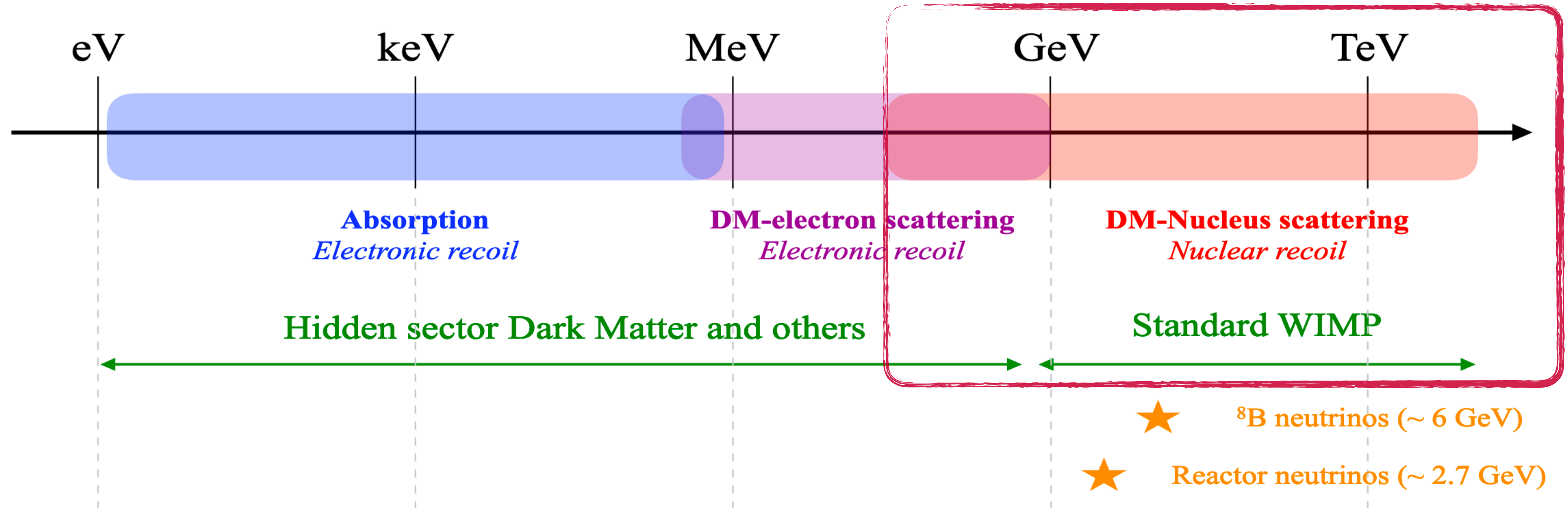
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How to design a dark matter detector

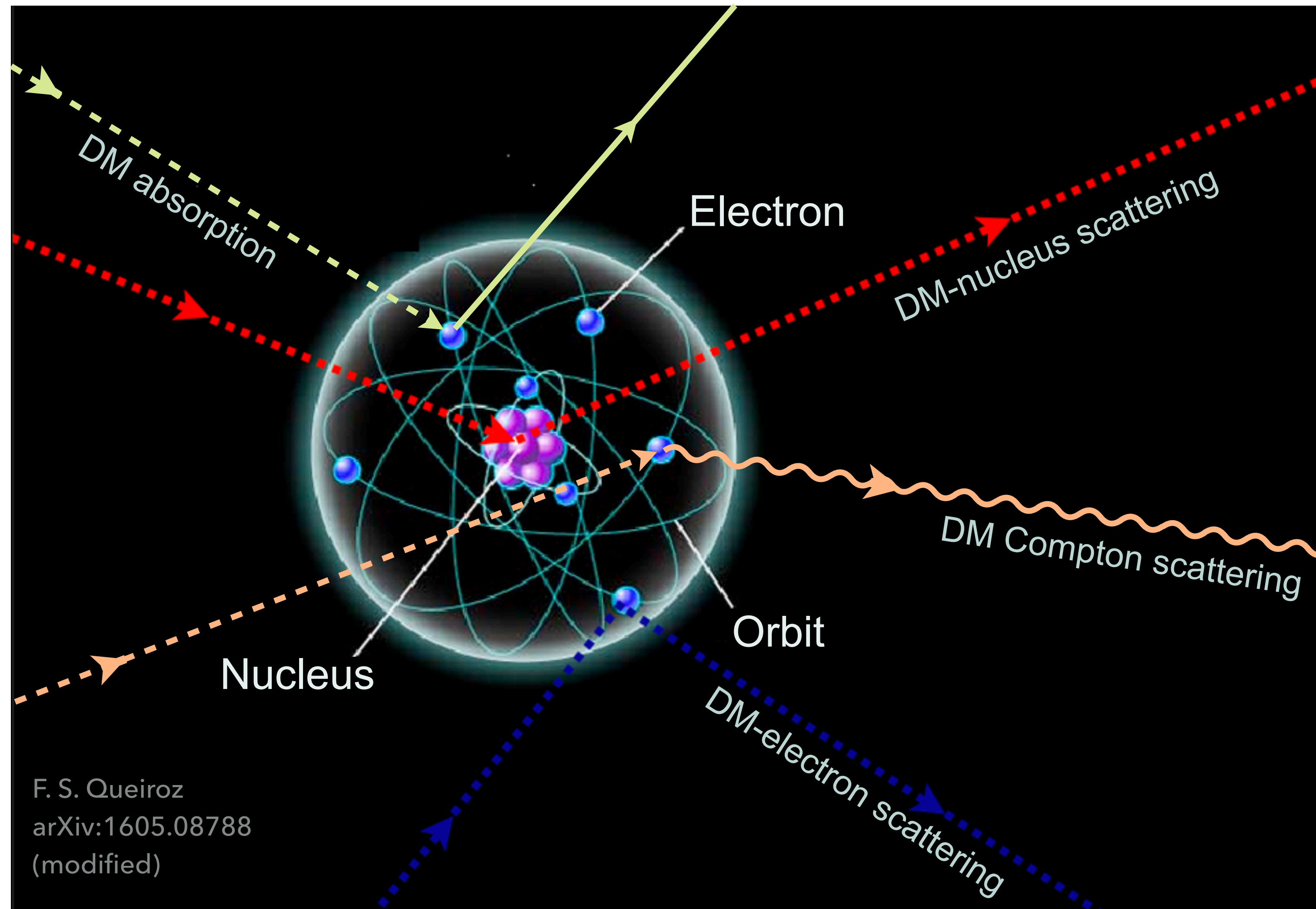
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See Marco Cirelli's
lectures

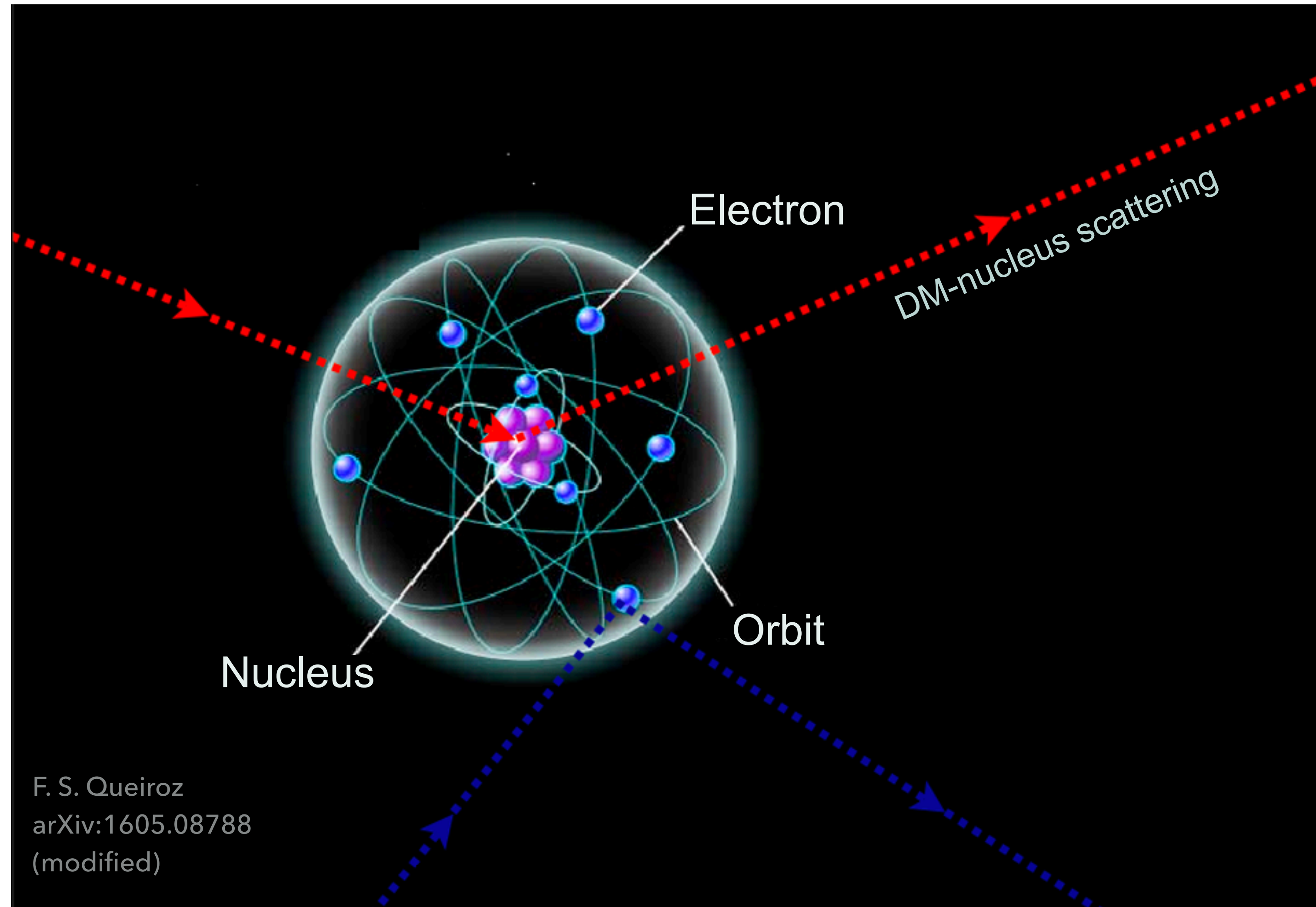
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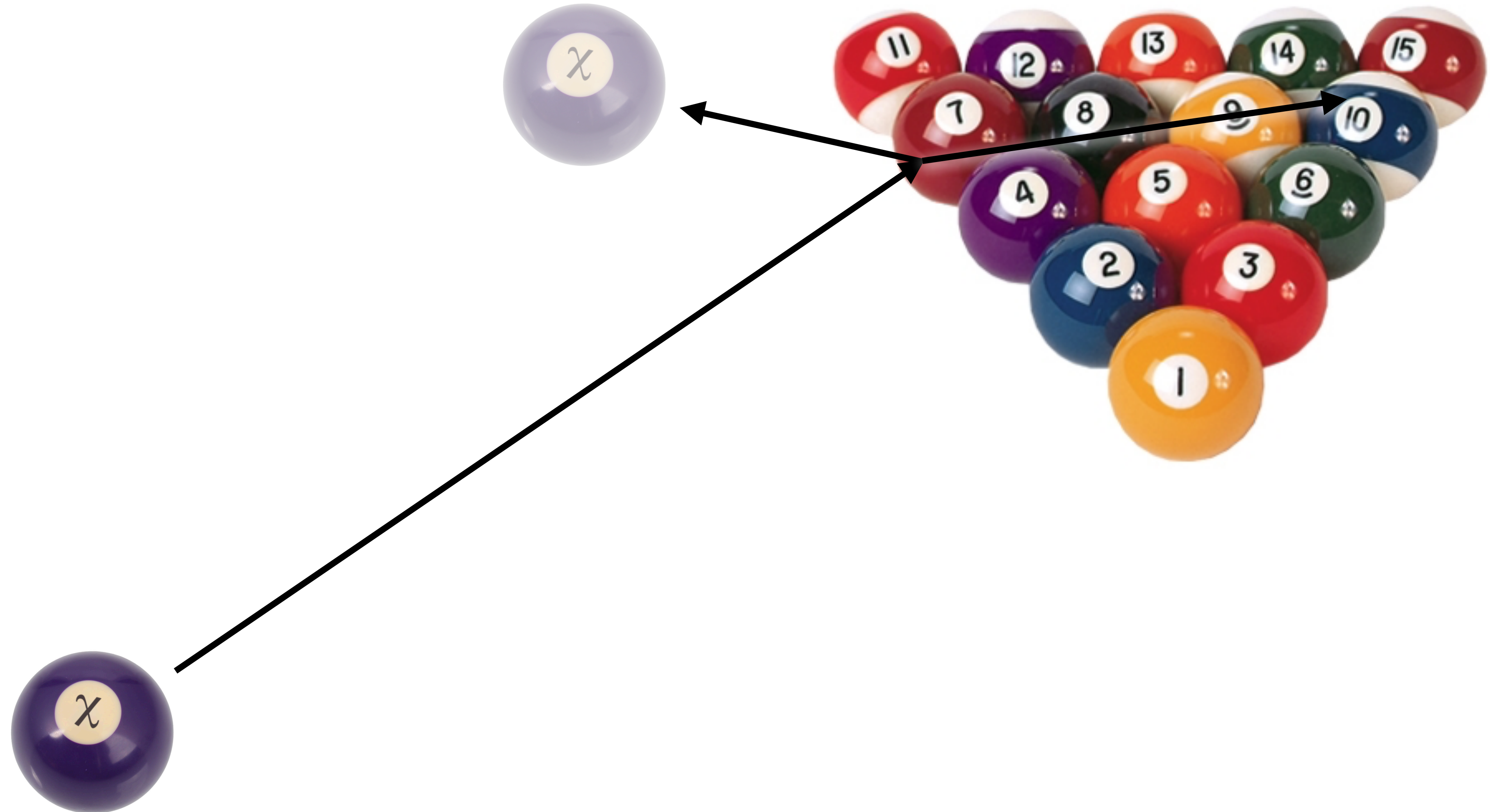


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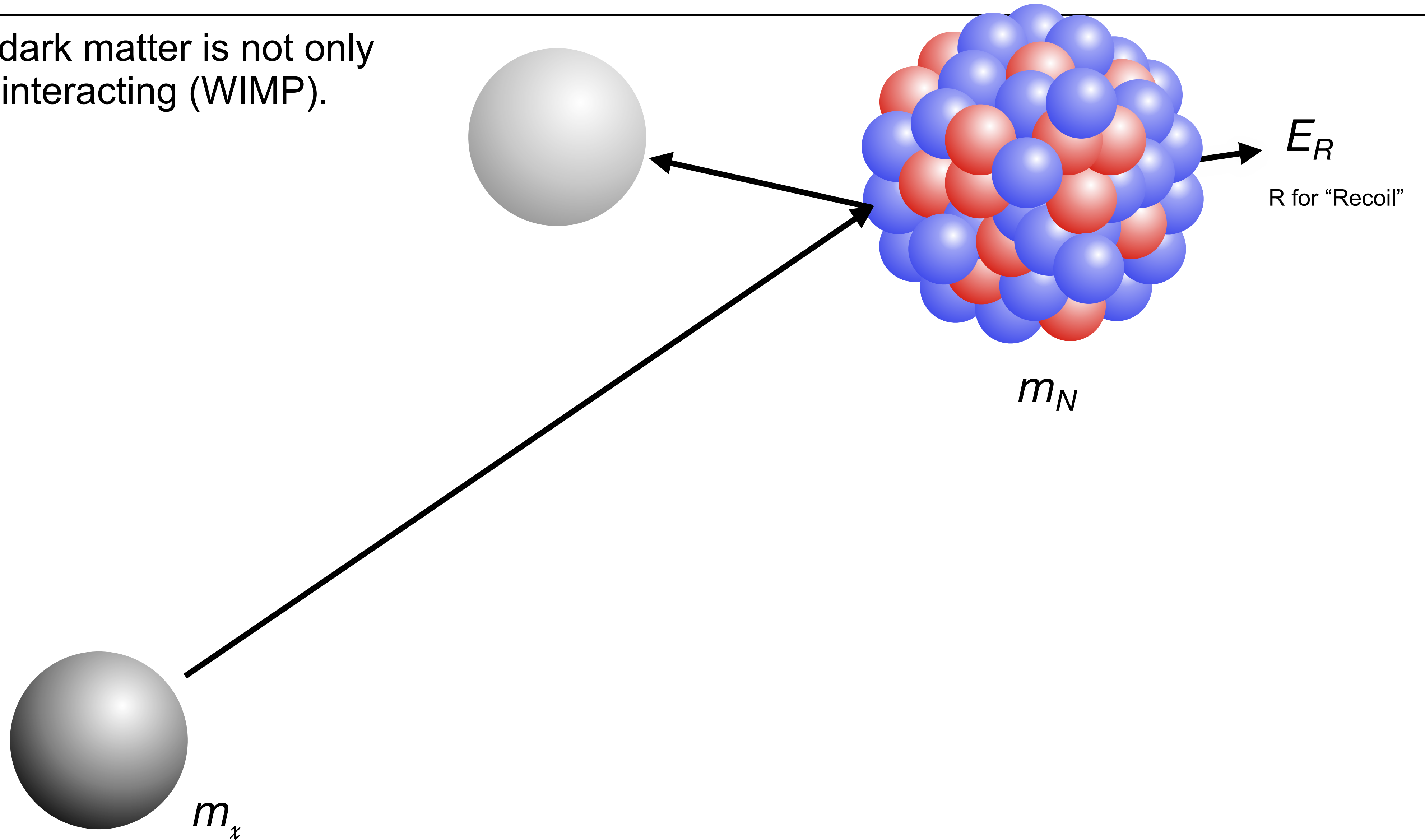


Elastic dark matter-nucleus scattering



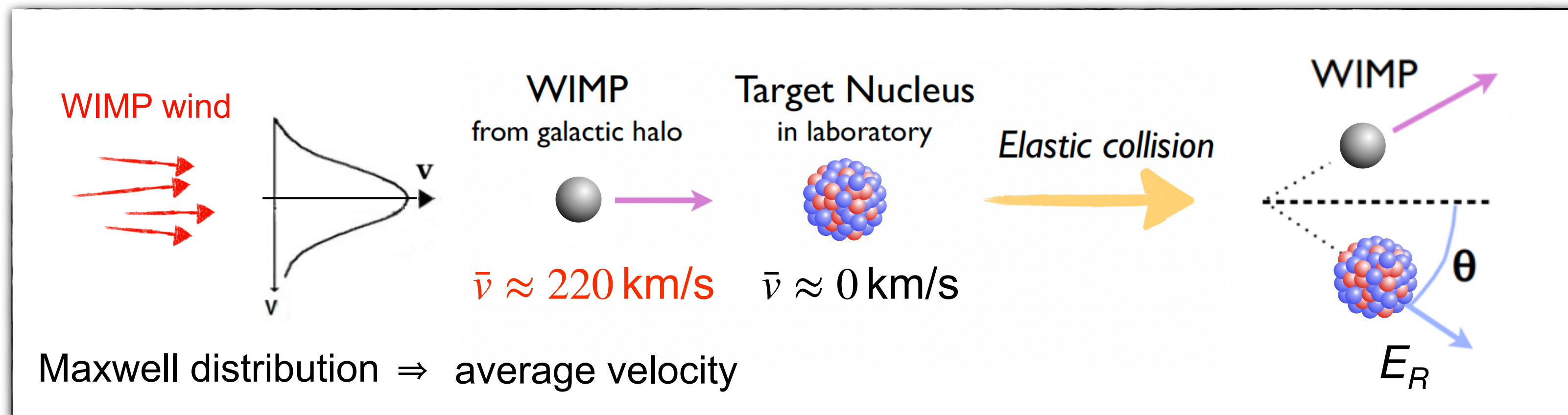
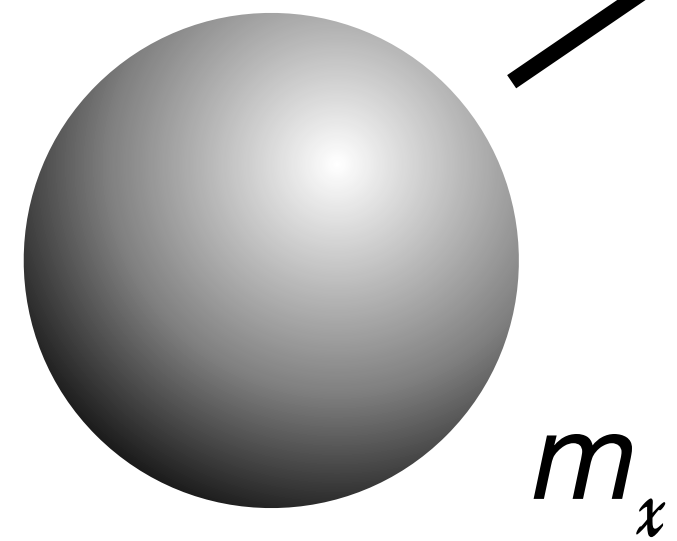
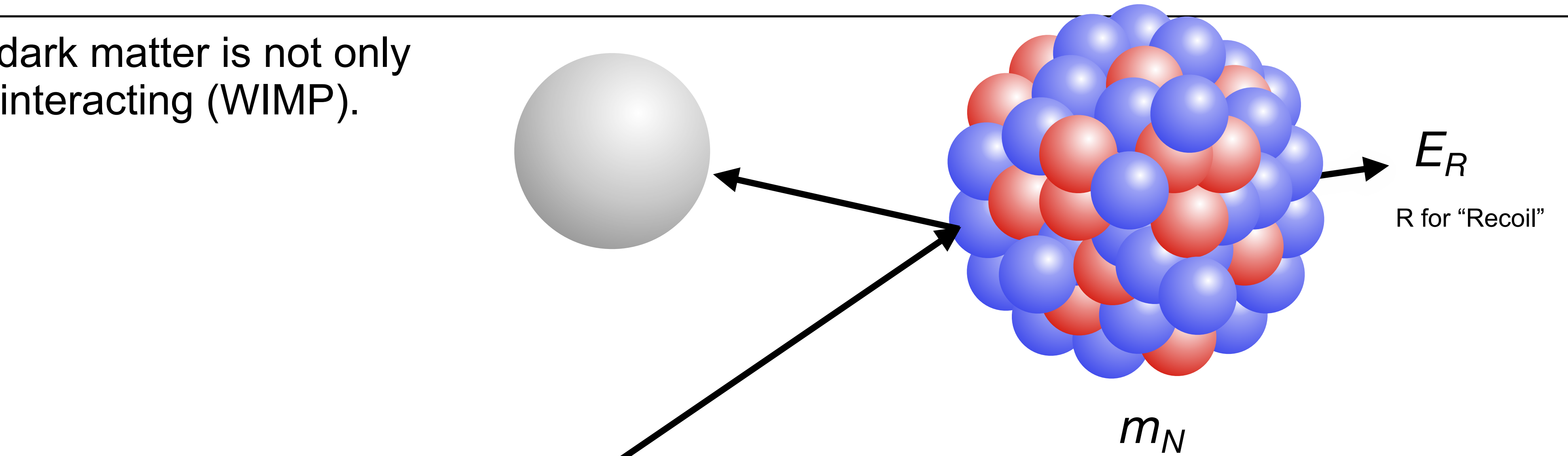
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Assume that the dark matter is not only gravitationally interacting (WIMP).



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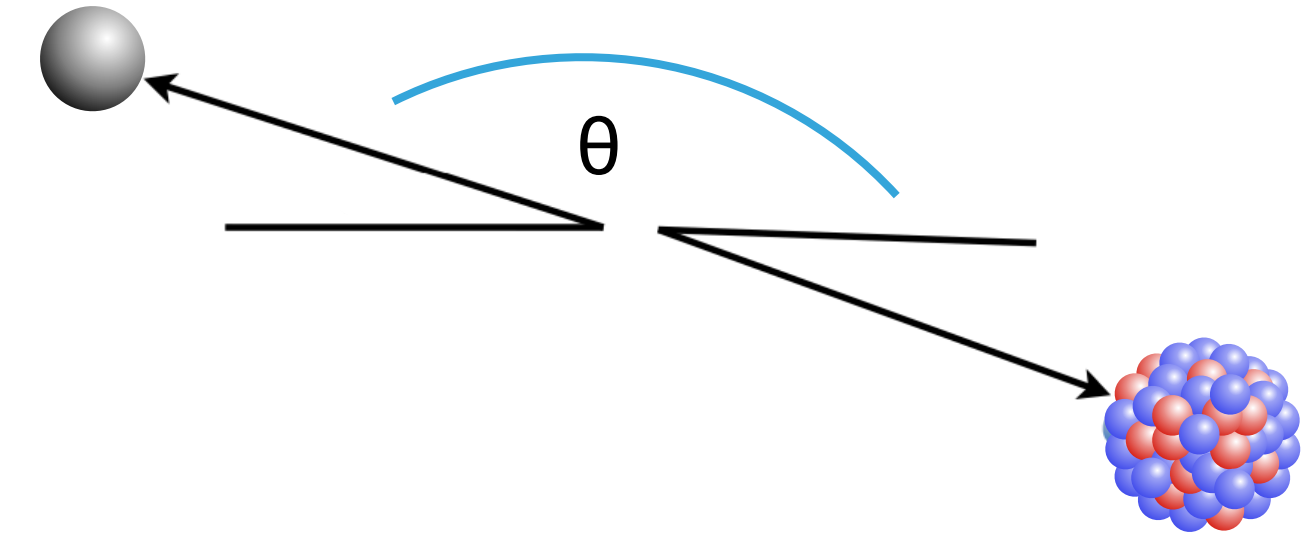
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Dive-in: kinematics

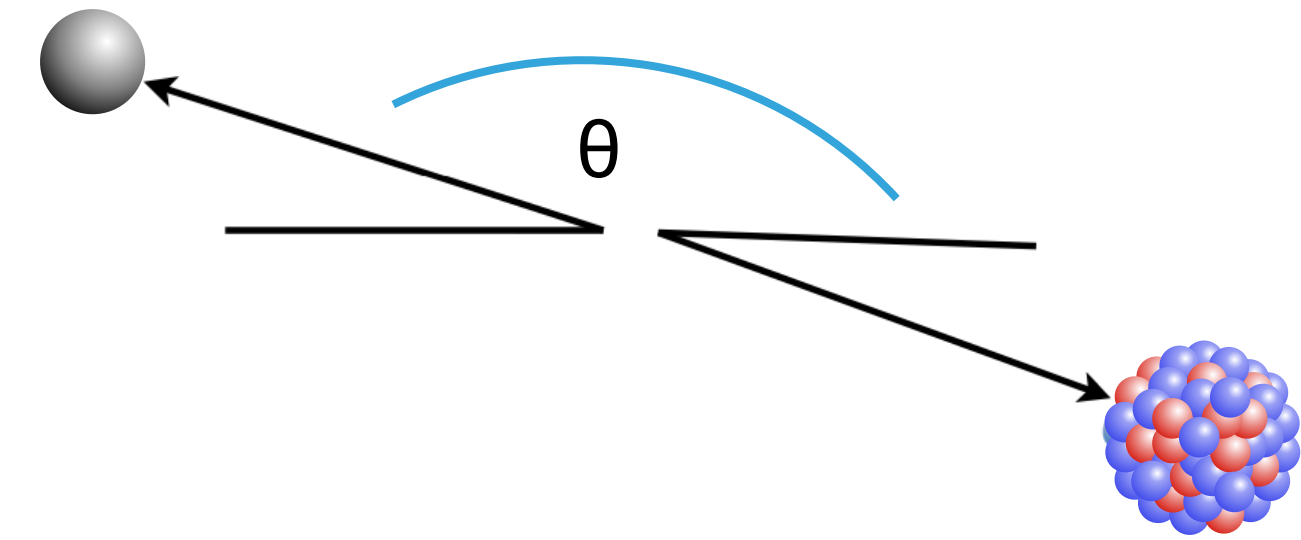
Calculate E_R , i.e. the recoil energy of a nucleus, in the center of mass frame:



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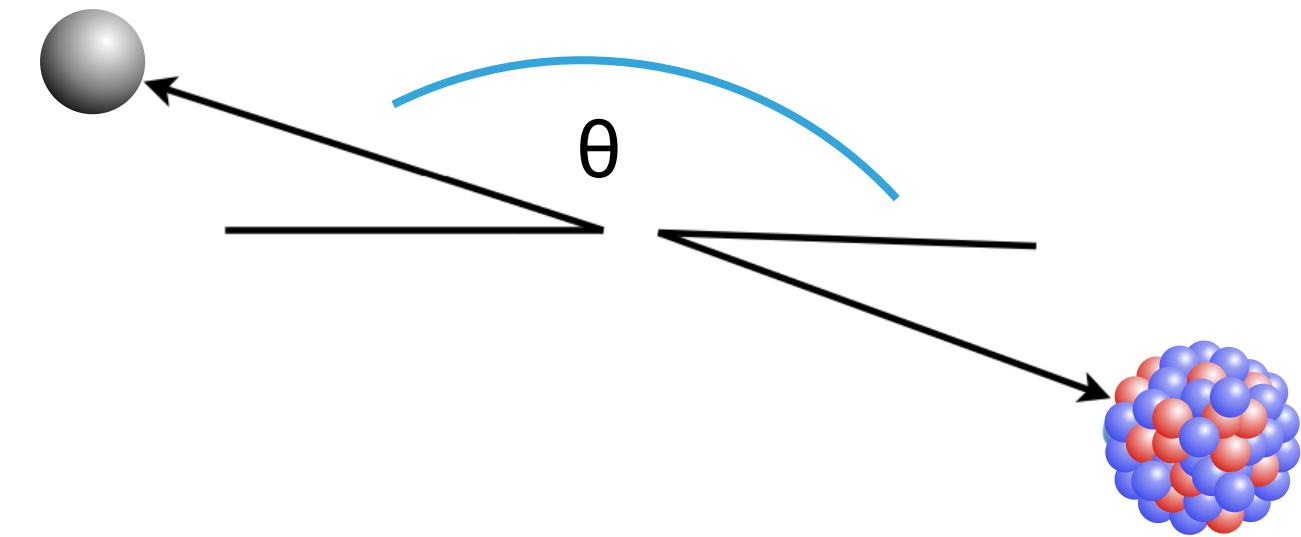


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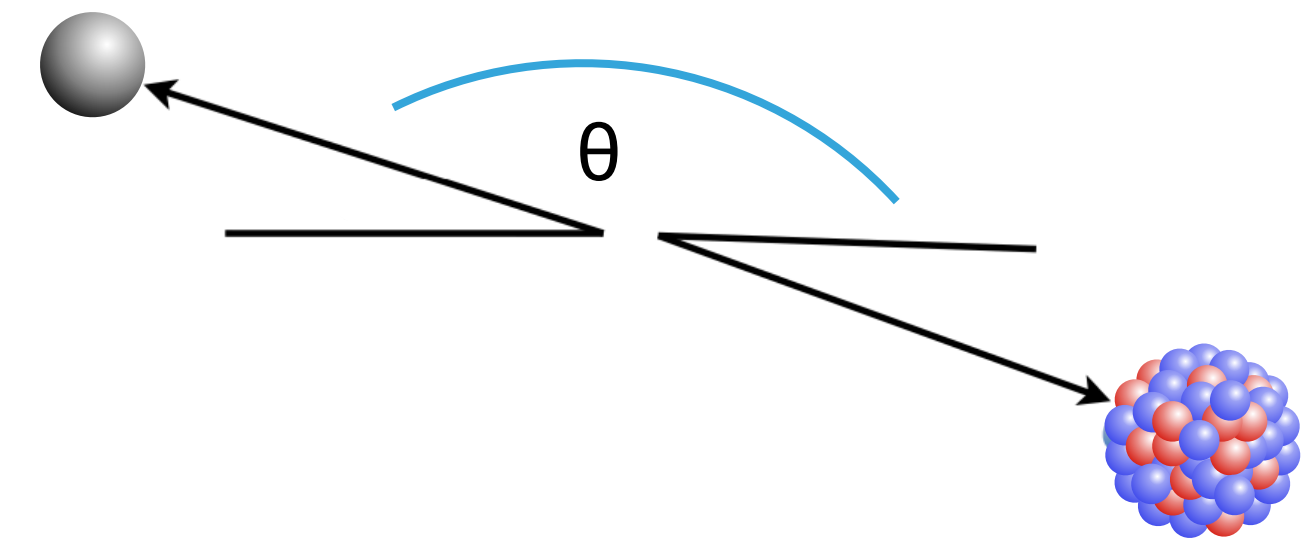
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\bar{v} : mean DM speed relative to target

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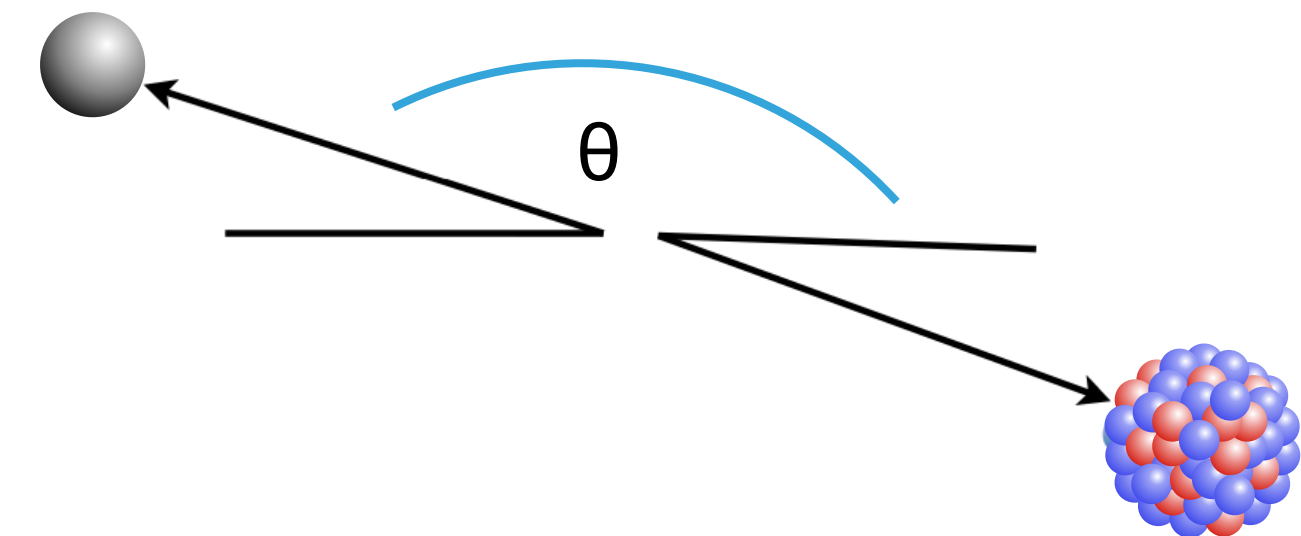
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Dive-in: kinematics

Minimum DM particle speed v_{\min}
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■ Implications

- Lighter dark matter particles ($m_\chi \ll m_N$) require a larger minimum speed for a given E_R
- Inelastic scattering can further increase the minimum speed needed



What recoil energies do we expect?

$$E_R^{\max} = 2 \frac{\mu^2 \bar{v}^2}{m_N} = \left(\frac{1}{2} m_\chi \bar{v}^2 \right) \left(\frac{4 m_\chi m_N}{(m_\chi + m_N)^2} \right)$$

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→ assuming $m_N = m_\chi = 100 \text{ GeV}/c^2$ and $\bar{v} \approx 220 \text{ km/s} = 0.75 \times 10^{-3} c$

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But what about rates?



Expected rates in a detector

number of observed DM particles

DM number density • DM velocity

$$N = t \cdot \overbrace{n \cdot v}^{\text{DM number density} \cdot \text{DM velocity}} \cdot \underbrace{N_T \cdot \sigma}_{\text{number of targets} \cdot \text{scattering cross section}}$$

observation time

number of targets • scattering cross section

Spectrum of DM recoils, i.e. the energy dependence of the number of detected DM particles:

$$\frac{dN}{dE_R} = t \cdot n \cdot v \cdot N_T \cdot \frac{d\sigma}{dE_R}$$



Expected rates in a detector - the laundry list

DM velocity
distribution

Effective
movement of
Earth

DM-nucleus
spin interaction

Size of nucleus
(form factor)

Signal
efficiency

...

Both theoretical and experimental aspects need to be carefully evaluated for a sound rate prediction.

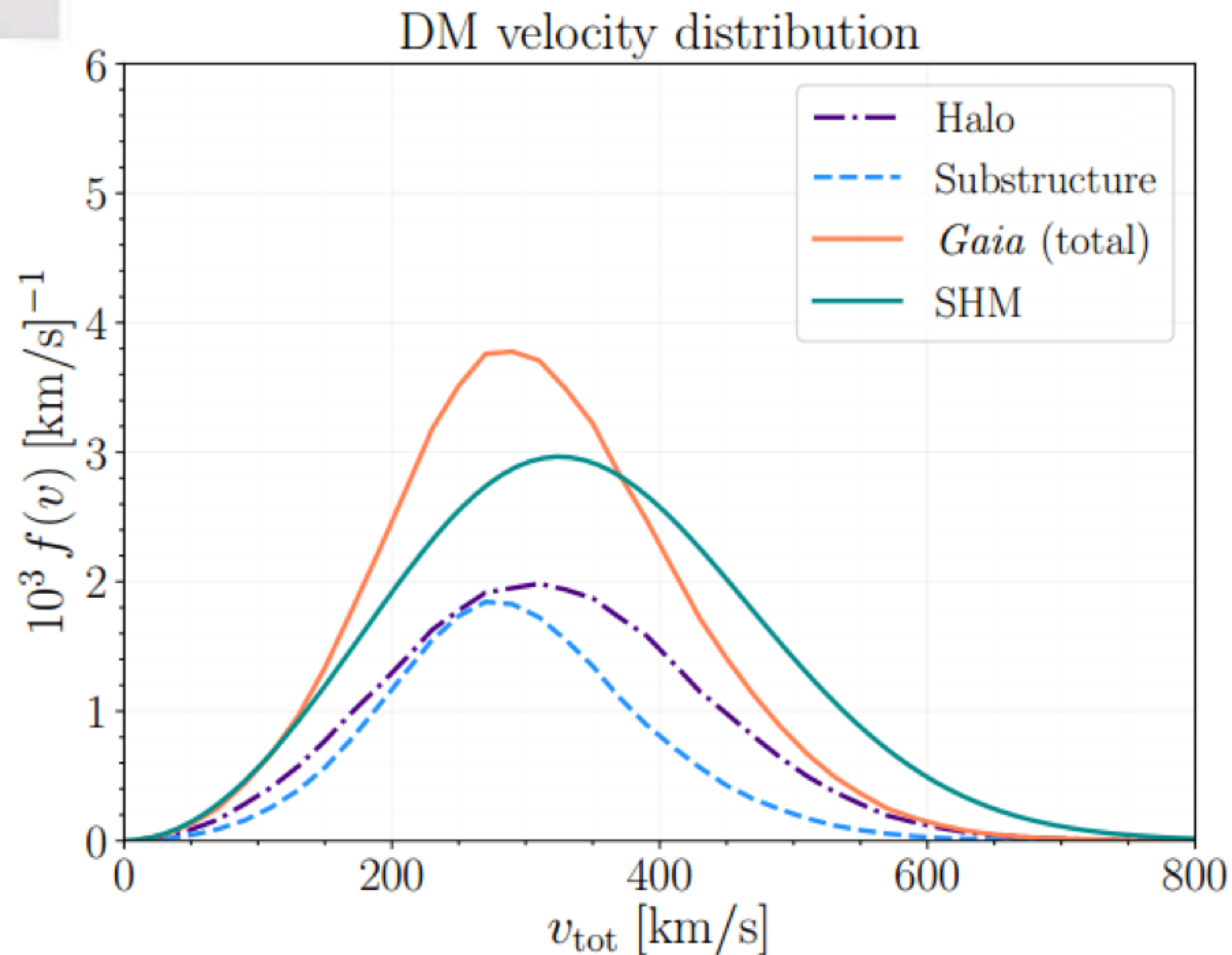
Local velocity distribution

DM velocity
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Need to consider the **local velocity distribution**, $f(\vec{v})$, of DM particles where \vec{v} is the **DM velocity in the reference frame of the detector**.

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$$v_{\min} = \sqrt{\frac{m_N E_R}{2\mu^2}} = \frac{q}{2\mu}$$



SHM: Standard Halo model
(truncated Maxwell distribution)

$$f(\vec{v}) = \frac{1}{N_{\text{esc.}}} \frac{1}{(2\pi\sigma^2)^{3/2}} e^{-\frac{|\vec{v}|^2}{2\sigma^2}} \Theta(v_{\text{esc.}} - v)$$

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local DM mass density

Note that:

$$n = \frac{\rho_0}{m_\chi}$$

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$$\varepsilon = t \cdot M_T$$

exposure

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The DM-nucleon scattering cross section

DM-nucleus
spin interaction

$$\frac{dR}{dE_R} = \frac{\rho_0}{m_\chi m_N} \int_{v_{\min.}}^{\infty} v f(\vec{v}) \frac{d\sigma}{dE_R} d\vec{v}$$

$$E_R = \frac{\mu^2 v^2}{m_N} (1 - \cos \theta)$$

$$= \frac{E_R^{\max}}{2} (1 - \cos \theta)$$

The DM-nucleon cross section can be separated:

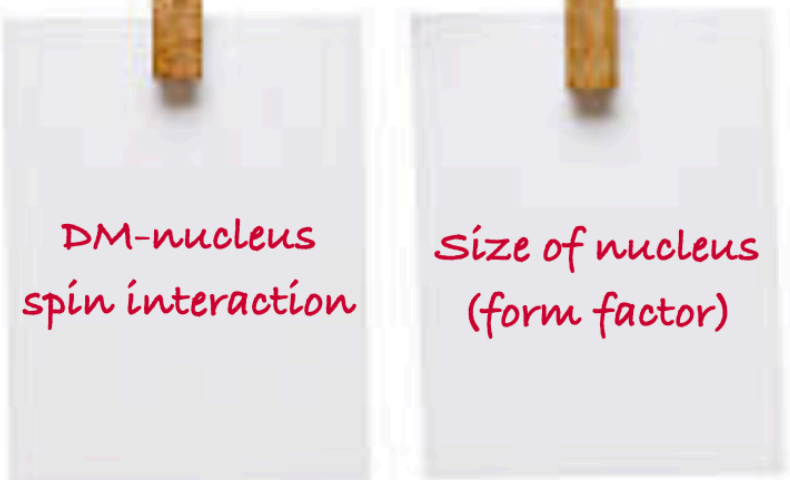
$$\frac{d\sigma}{dE_R} = \left[\left(\frac{d\sigma}{dE_R} \right)_{\text{SI}} + \left(\frac{d\sigma}{dE_R} \right)_{\text{SD}} \right]$$

arises from scalar
or vector couplings
to quarks

Spin Independent Spin Dependent

arises from axial-
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F : nuclear form factor

The DM-nucleon scattering cross section

particle theory

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nuclear form factors:
quantum mechanics of interaction with nucleus

DM-nucleus
spin interaction

Size of nucleus
(form factor)

The DM-nucleon scattering cross section

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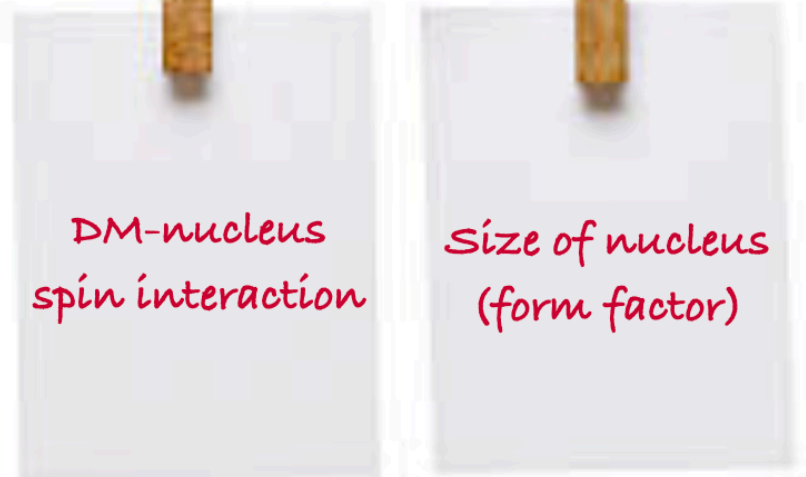
$$\sigma_0^{\text{SD}} = \frac{32 G_F^2 \mu^2}{\pi} \frac{J+1}{J} \left[a_p \langle S_p \rangle + a_n \langle S_n \rangle \right]^2$$

Fermi constant \downarrow $32 G_F^2 \mu^2$
 nuclear angular momentum \nearrow J
 expectation value of proton/neutron spin within nucleus \downarrow $\langle S_p \rangle$ and $\langle S_n \rangle$
 effective couplings to protons and neutrons \uparrow a_p and a_n

DM-nucleus
spin interactionSize of nucleus
(form factor)



The DM-nucleon scattering cross section



$$\frac{d\sigma}{dE_R} = \frac{m_N}{2\mu^2 v^2} \left[\sigma_0^{\text{SI}} F_{\text{SI}}^2(E_R) + \sigma_0^{\text{SD}} F_{\text{SD}}^2(E_R) \right]$$

particle theory

nuclear form factors:
quantum mechanics of interaction with nucleus

Spin-Independent (SI)

$$\sigma_0^{\text{SI}} = \frac{4\mu^2}{\pi} \left[Zf_p + (A - Z)f_n \right]^2$$

scalar couplings to protons and neutrons

Spin-Dependent (SD)

$$\sigma_0^{\text{SD}} = \frac{32G_F^2 \mu^2}{\pi} \frac{J+1}{J} \left[a_p \langle S_p \rangle + a_n \langle S_n \rangle \right]^2$$

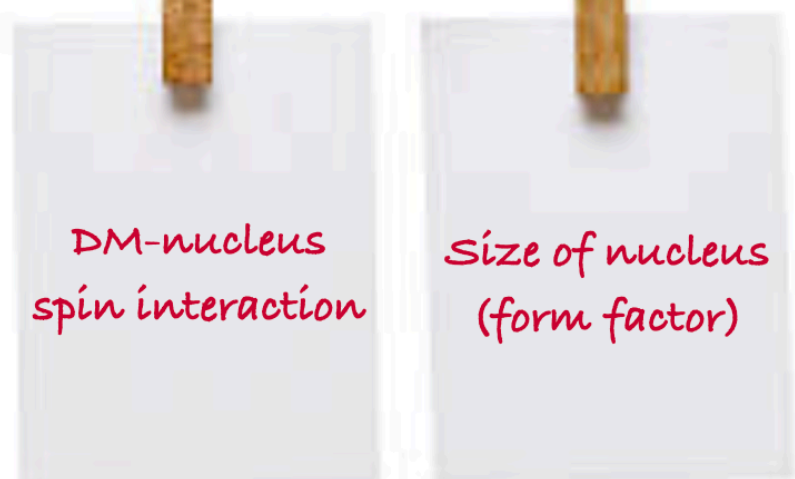
Fermi constant

nuclear angular momentum

expectation value of proton/neutron spin within nucleus

effective couplings to protons and neutrons

The DM-nucleon scattering cross section



$$\frac{d\sigma}{dE_R} = \frac{m_N}{2\mu^2 v^2} \left[\sigma_0^{\text{SI}} F_{\text{SI}}^2(E_R) + \sigma_0^{\text{SD}} F_{\text{SD}}^2(E_R) \right]$$

particle theory

nuclear form factors:
quantum mechanics of interaction with nucleus

Spin-Independent (SI)

$$\sigma_0^{\text{SI}} = \frac{4\mu^2}{\pi} \left[Zf_p + (A - Z)f_n \right]^2 \propto A^2$$

↑ scalar couplings to protons and neutrons

In most models $f_p \approx f_n$.

⇒ Scattering adds coherently with A^2 enhancement.

Spin-Dependent (SD)

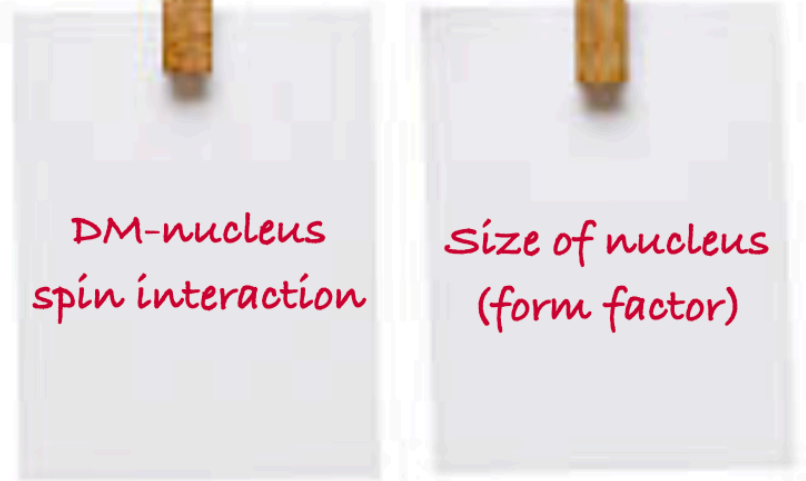
$$\sigma_0^{\text{SD}} = \frac{32G_F^2 \mu^2}{\pi} \frac{J+1}{J} \left[a_p \langle S_p \rangle + a_n \langle S_n \rangle \right]^2$$

Fermi constant ↓ expectation value of proton/neutron spin within nucleus ↓
 nuclear angular momentum ↑ effective couplings to protons and neutrons ↑

Nuclei with non-zero angular momentum required.

No coherence effect!

The DM-nucleon scattering cross section



$$\frac{d\sigma}{dE_R} = \frac{m_N}{2\mu^2 v^2} \left[\sigma_0^{\text{SI}} F_{\text{SI}}^2(E_R) + \sigma_0^{\text{SD}} F_{\text{SD}}^2(E_R) \right]$$

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Fermi constant

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expectation value of proton/neutron spin within nucleus

effective couplings to protons and neutrons

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Finally... the dark matter direct detection master formula

$$\left(\frac{dR}{dE_R} \right)_{\chi N}^{\text{SI}} = \frac{\sigma_0^{\text{SI}}}{m_\chi} \cdot \frac{\rho_0 T(\vec{v})}{v\sqrt{\pi}} \cdot \frac{F_{\text{SI}}^2(E_R)}{\mu^2}$$

$$\frac{dR}{dE_R} = \frac{\rho_0}{m_\chi m_N} \int_{v_{\text{min.}}}^{\infty} v f(\vec{v}) \frac{d\sigma}{dE_R} d\vec{v}$$

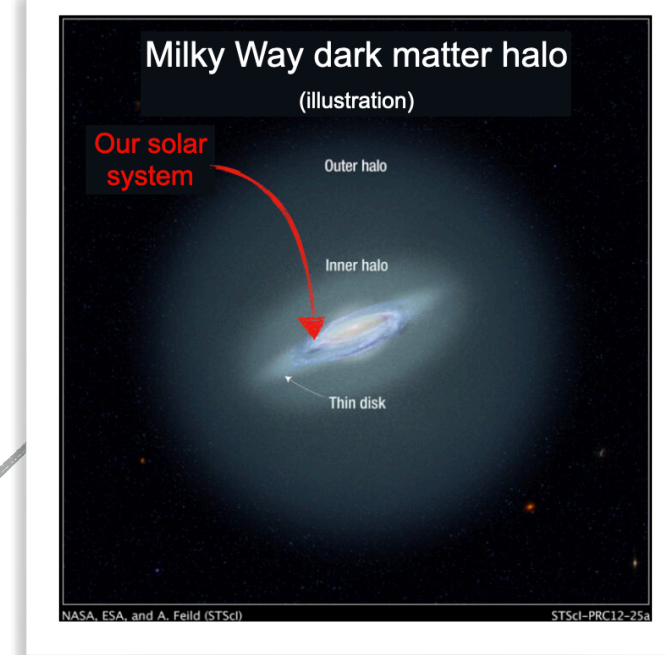
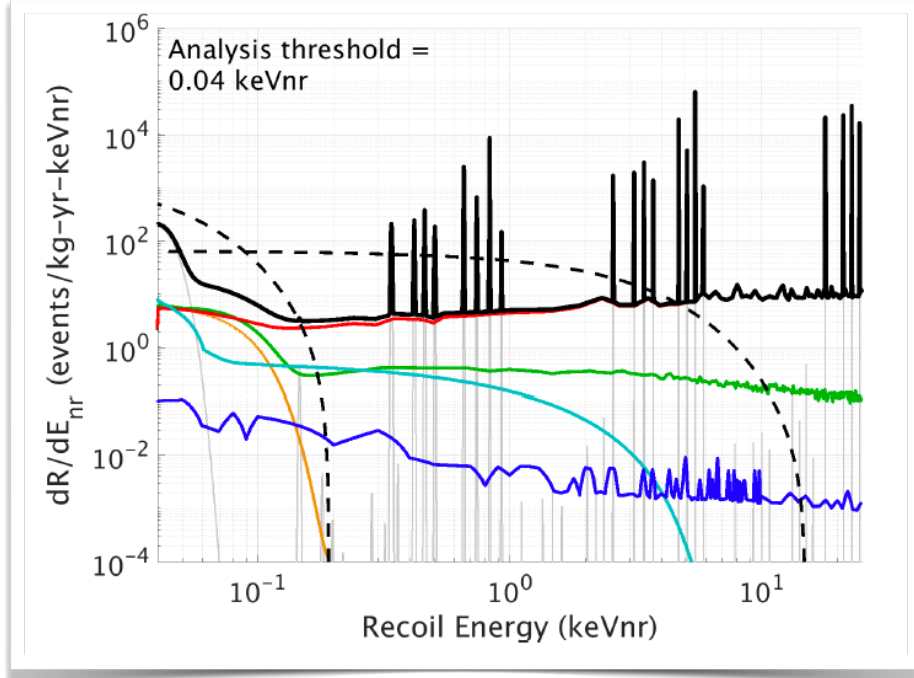
$$\frac{d\sigma^{\text{SI}}}{dE_R} = \frac{m_N}{2\mu^2 v^2} \sigma_0^{\text{SI}} F_{\text{SI}}^2(E_R)$$

$$f(\vec{v}) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{|\vec{v}|^2}{2\sigma^2}}$$

$$\rho(r) \propto r^{-2} \quad \text{and} \quad \rho_0 \approx 0.3 \text{ GeV cm}^{-3}$$



Finally... the dark matter direct detection master formula



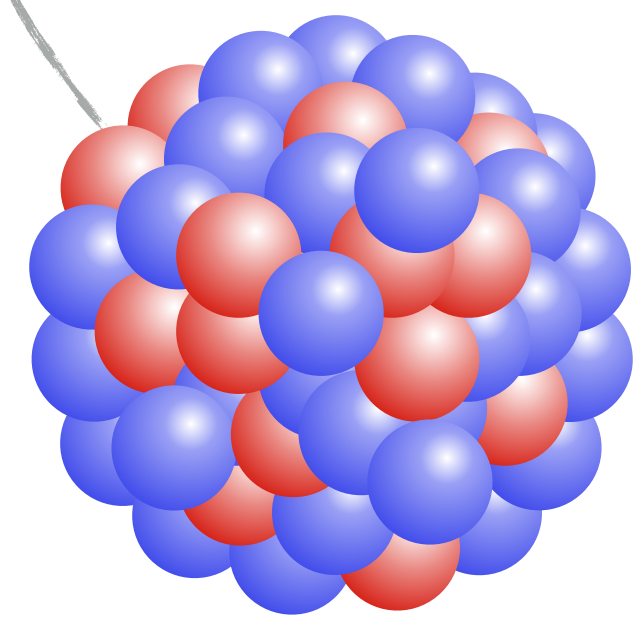
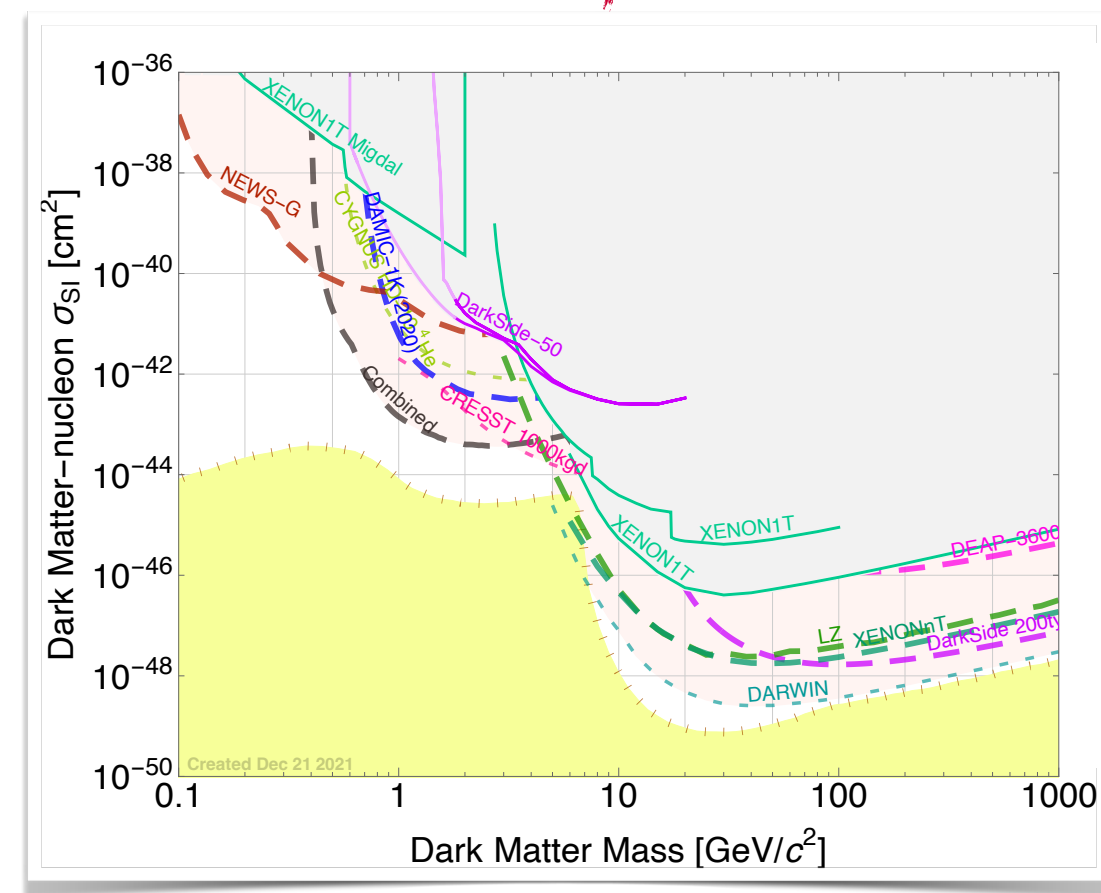
$$\frac{dR}{dE_R} = \frac{\rho_0}{m_\chi m_N} \int_{v_{\min.}}^{\infty} v f(\vec{v}) \frac{d\sigma}{dE_R} d\vec{v}$$

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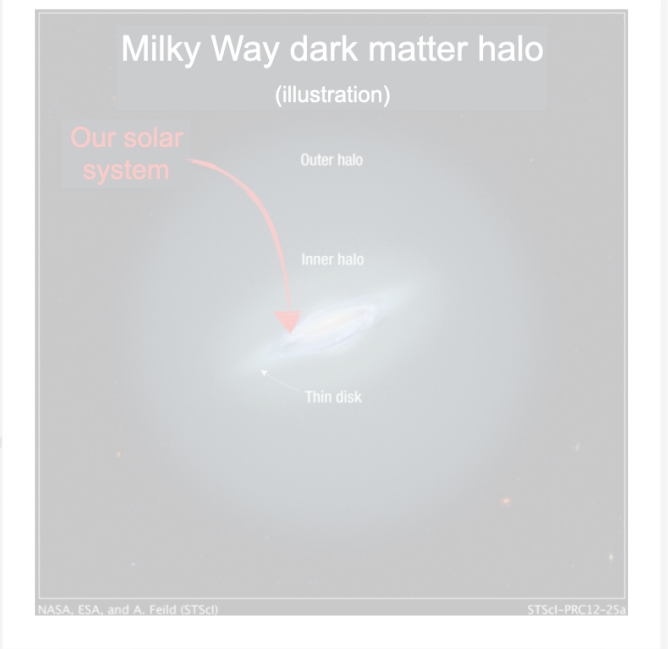
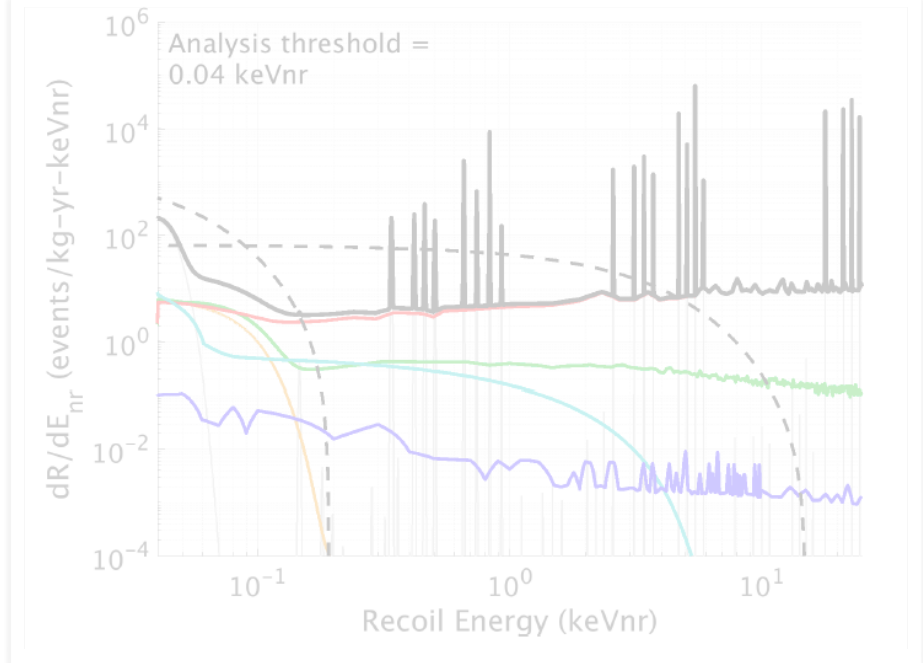
$$\rho(r) \propto r^{-2} \quad \text{and} \quad \rho_0 \approx 0.3 \text{ GeV cm}^{-3}$$

$$\left(\frac{dR}{dE_R} \right)_{\chi N}^{\text{SI}} = \frac{\sigma_0^{\text{SI}}}{m_\chi} \cdot \frac{\rho_0 T(\vec{v})}{v \sqrt{\pi}} \cdot \frac{F_{\text{SI}}^2(E_R)}{\mu^2}$$





Finally... the dark matter direct detection master formula



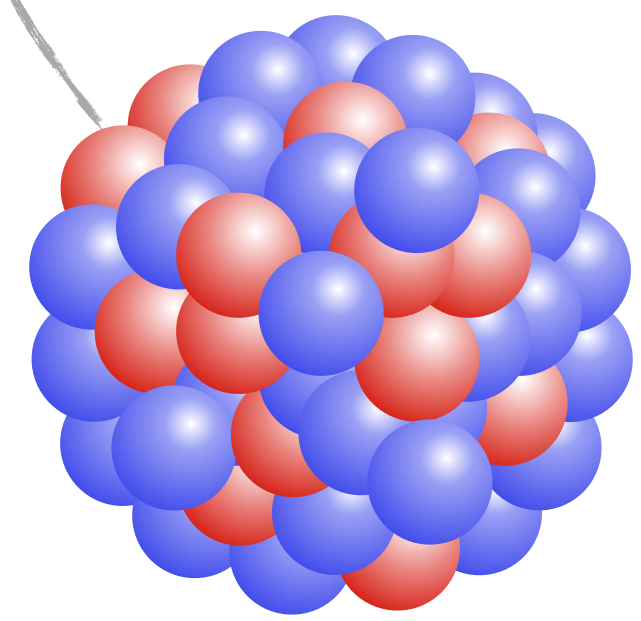
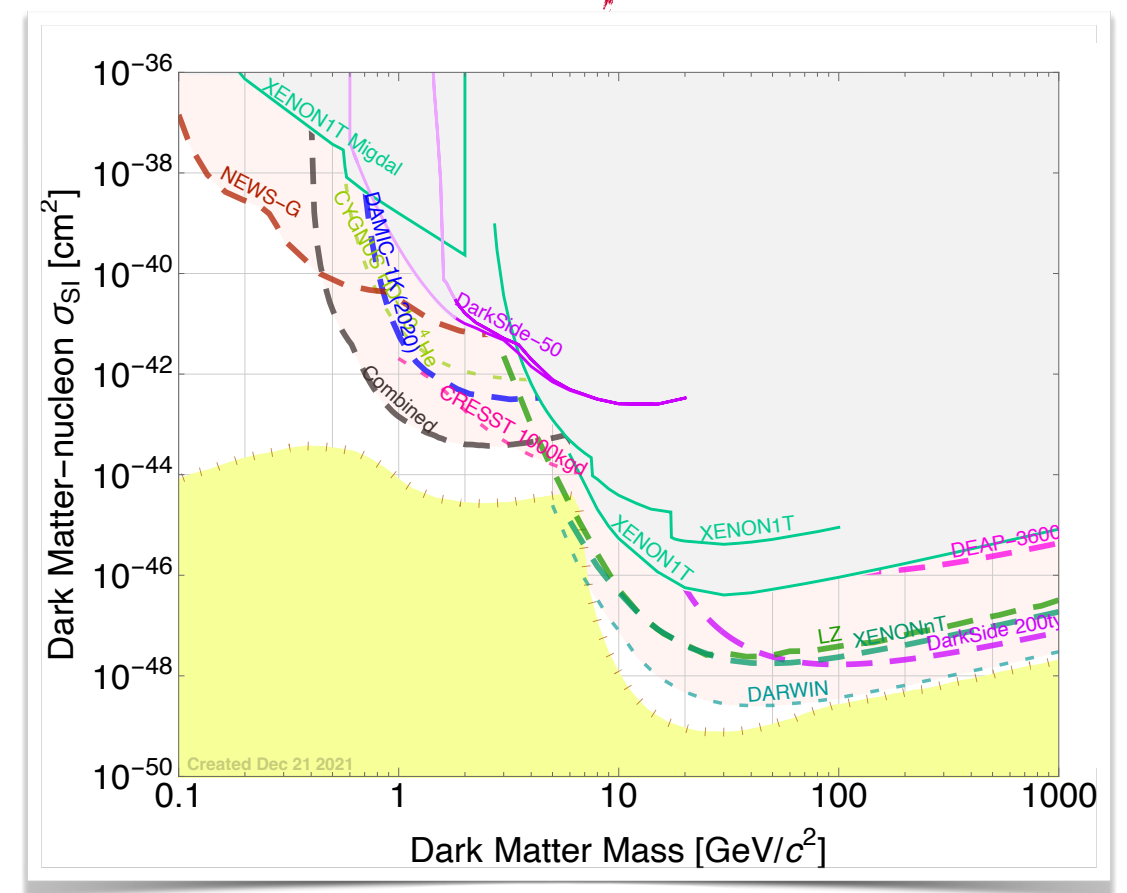
$$\frac{dR}{dE_R} = \frac{\rho_0}{m_\chi m_N} \int_{v_{\min.}}^{\infty} v f(\vec{v}) \frac{d\sigma}{dE_R} d\vec{v}$$

$$\frac{d\sigma^{\text{SI}}}{dE_R} = \frac{m_N}{2\mu^2 v^2} \sigma_0^{\text{SI}} F_{\text{SI}}^2(E_R)$$

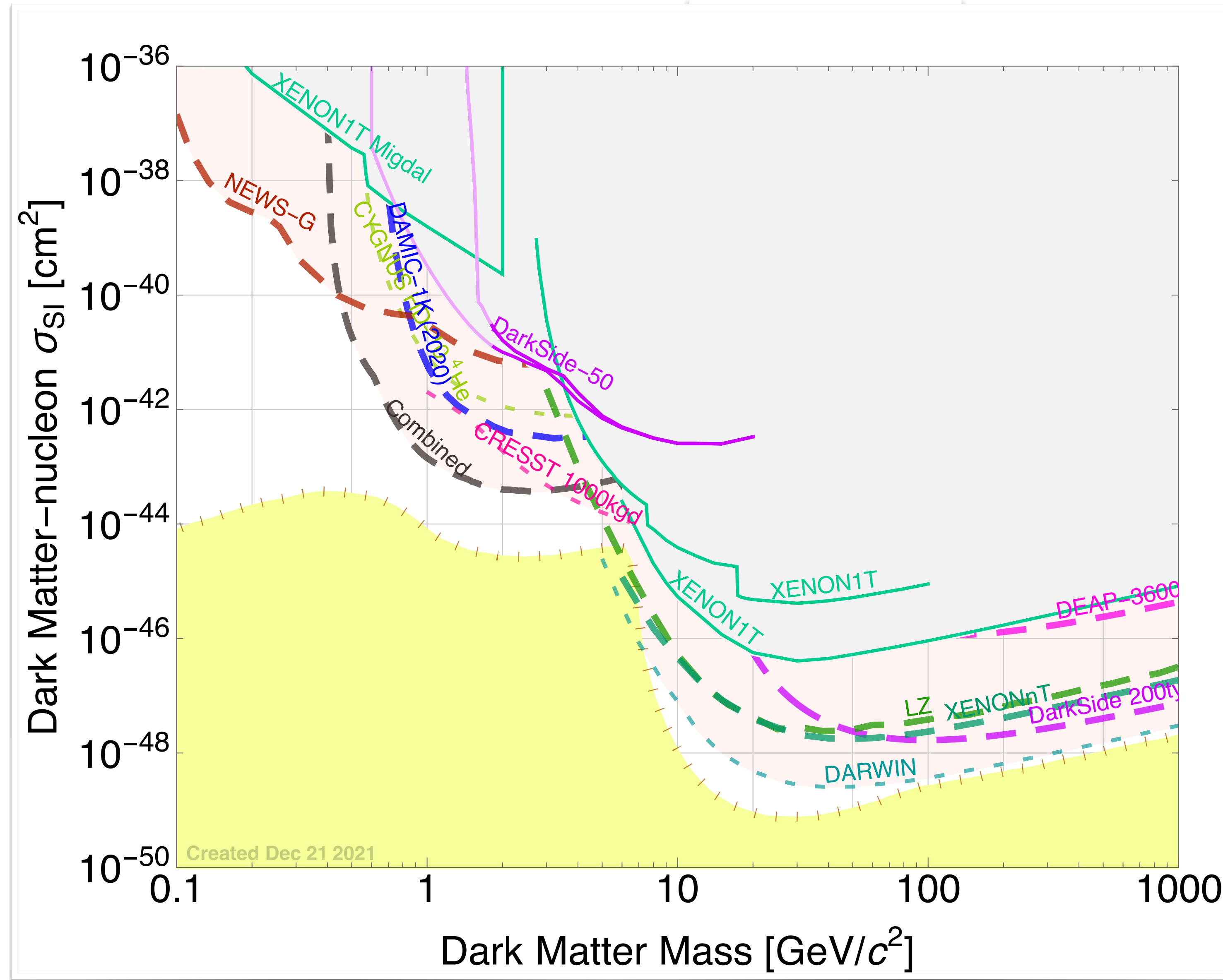
$$f(\vec{v}) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{|\vec{v}|^2}{2\sigma^2}}$$

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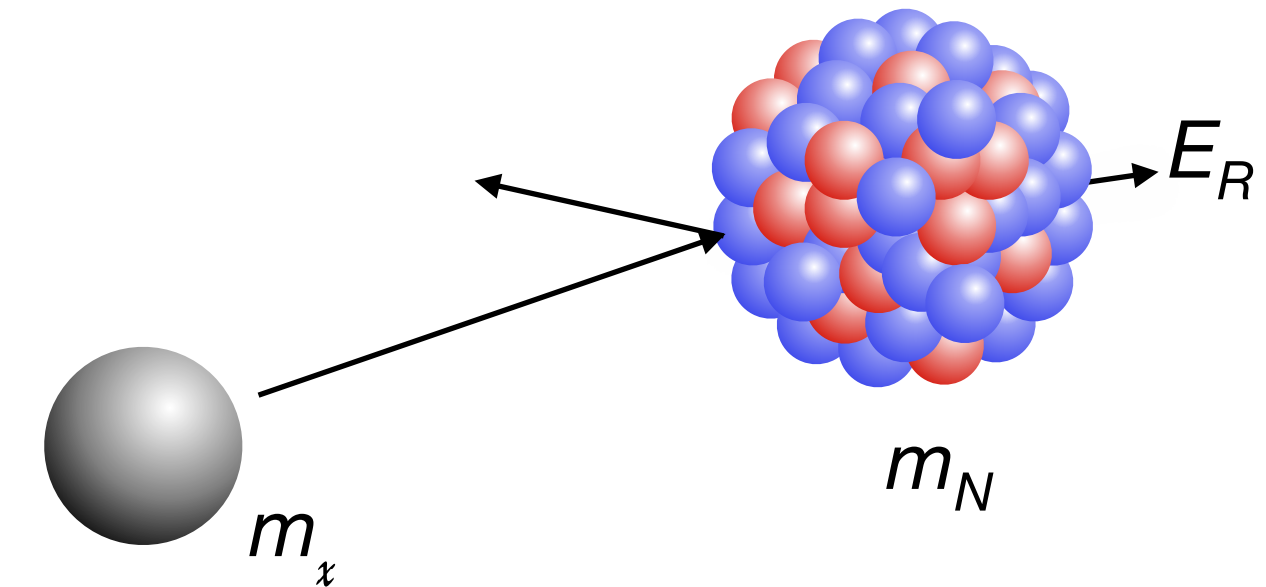
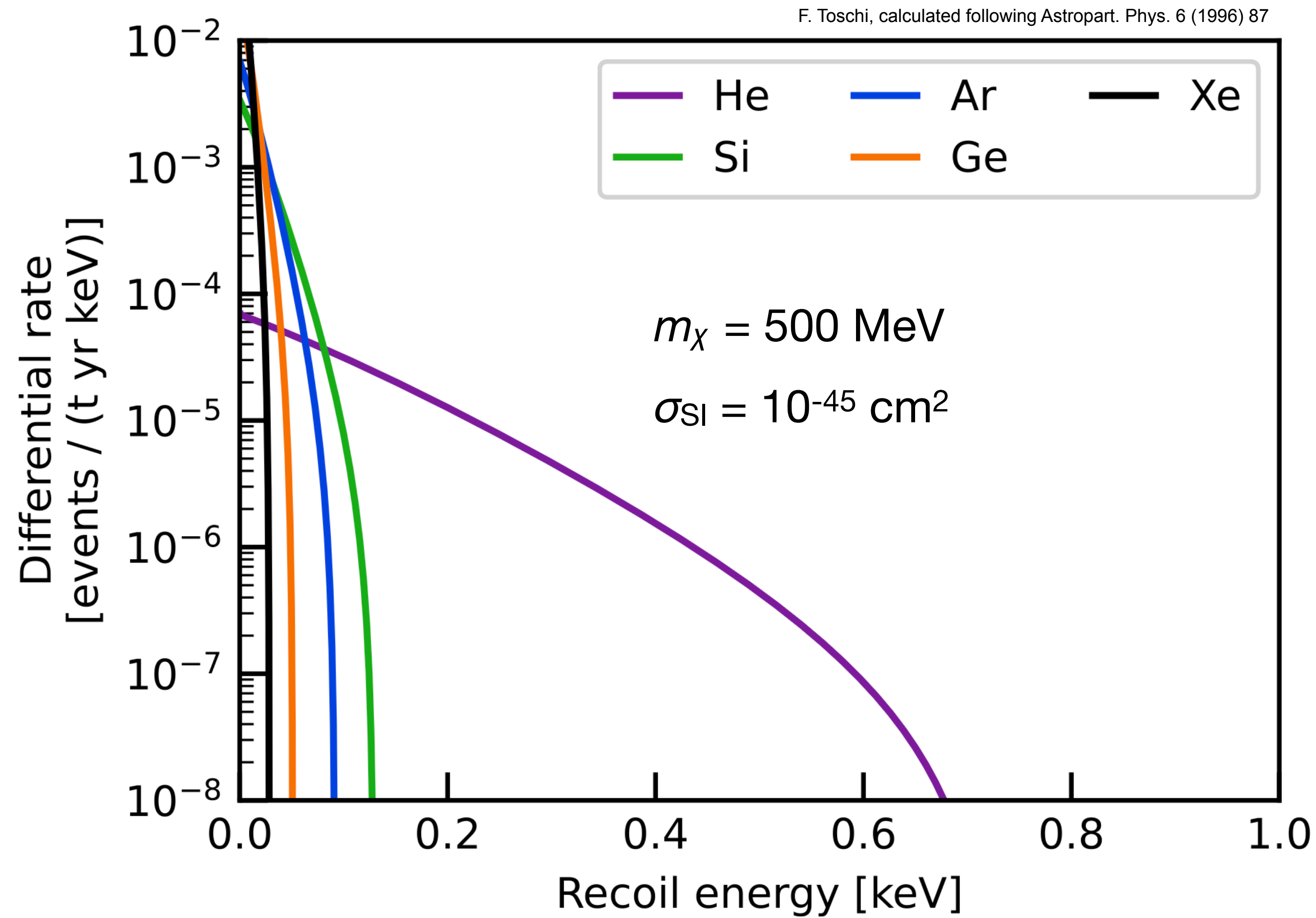
$$\left(\frac{dR}{dE_R} \right)_{\chi N}^{\text{SI}} = \frac{\sigma_0^{\text{SI}}}{m_\chi} \cdot \frac{\rho_0 T(\vec{v})}{v \sqrt{\pi}} \cdot \frac{F_{\text{SI}}^2(E_R)}{\mu^2}$$



Finally... the dark matter direct detection master formula

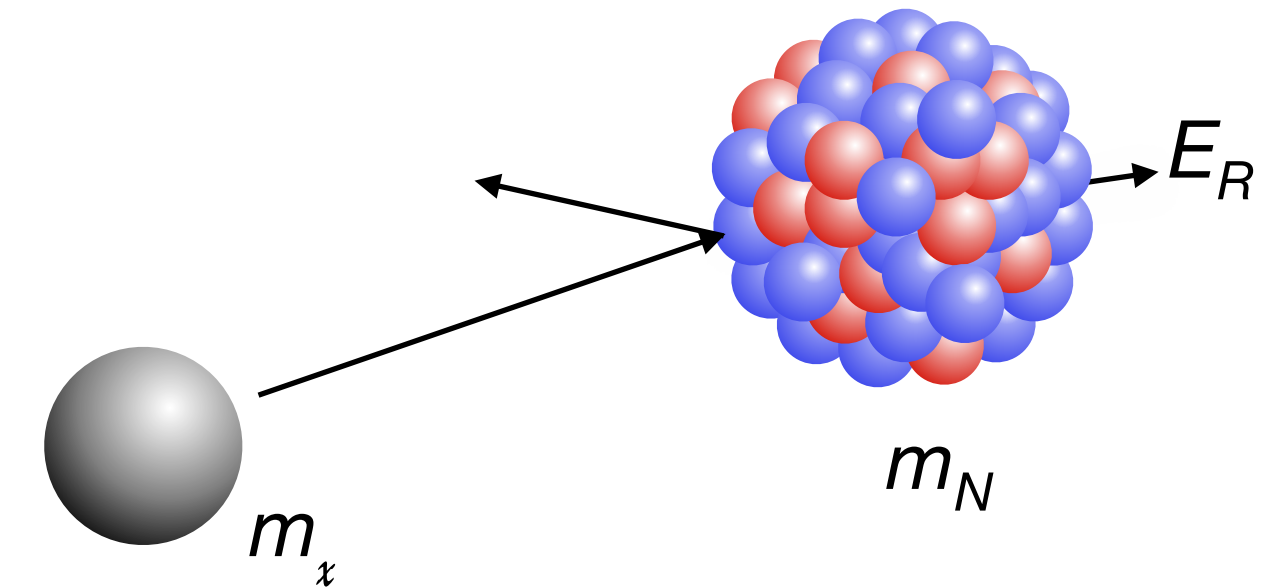
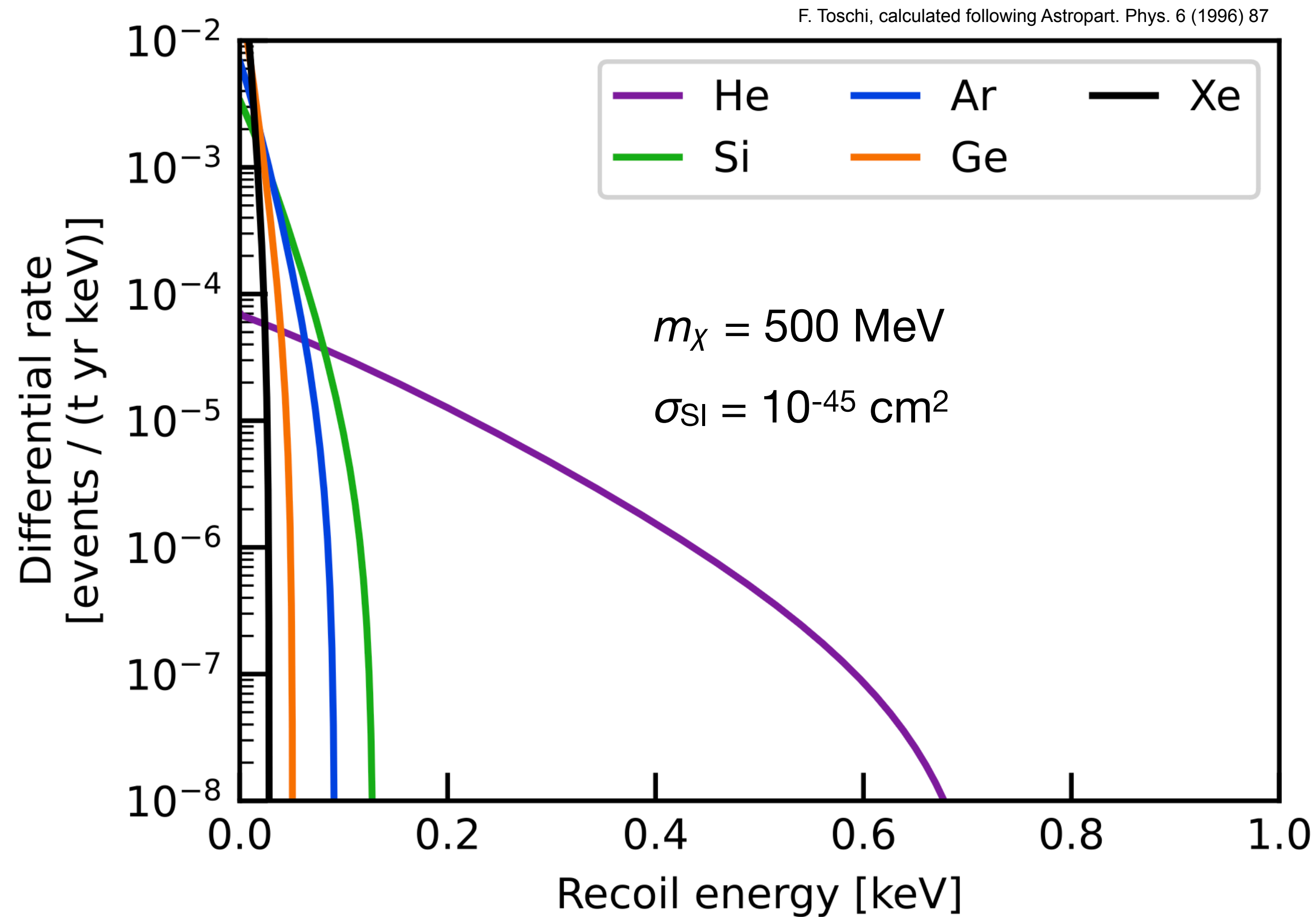


What nucleus (i.e. target) to pick?



$$E_R = \frac{1}{2} \frac{q^2}{m_N} \approx \frac{2 m_\chi^2 v^2}{m_N}$$

What nucleus (i.e. target) to pick?

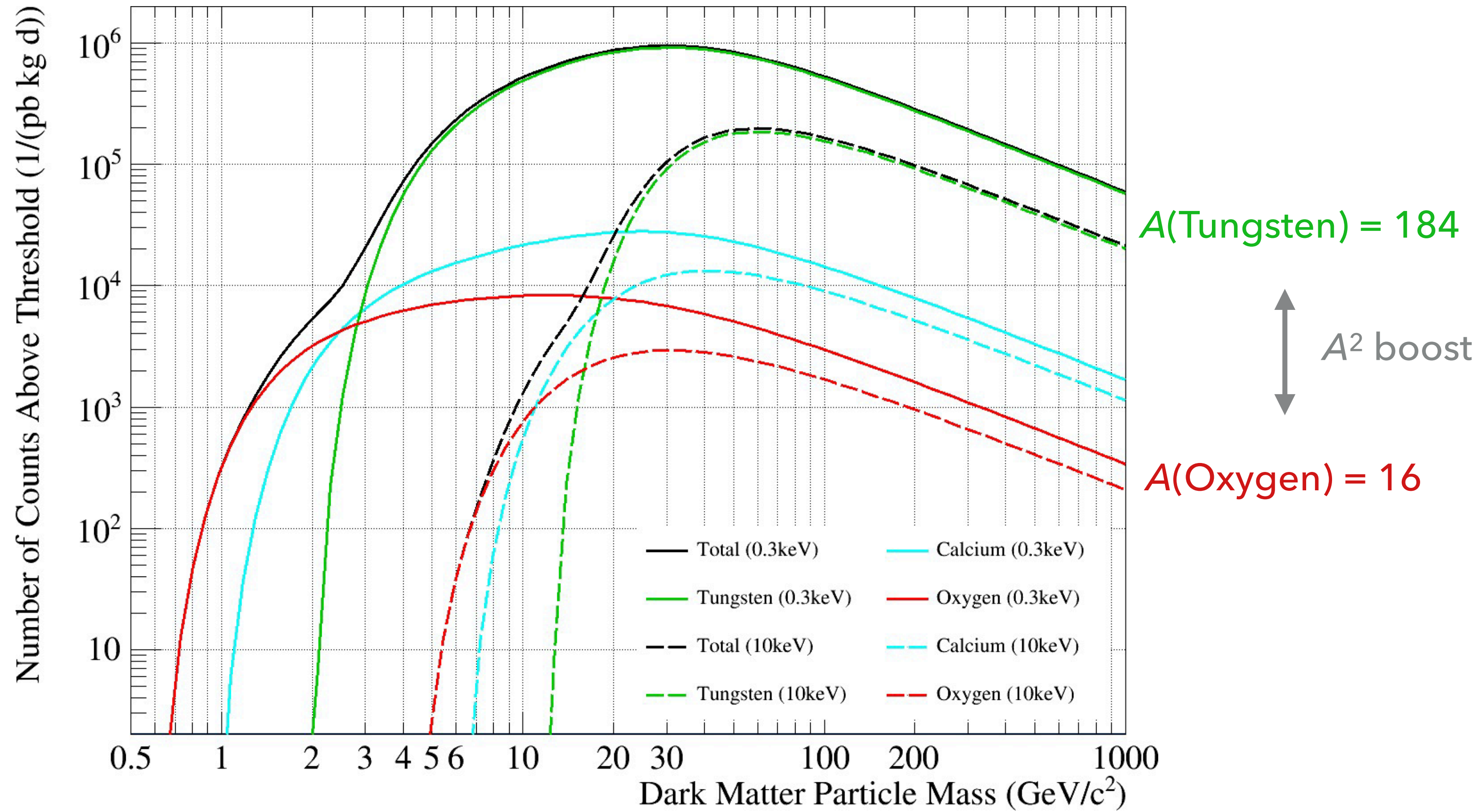


$$E_R = \frac{1}{2} \frac{q^2}{m_N} \approx \frac{2 m_\chi^2 v^2}{m_N}$$

Light target nuclei are favorable!

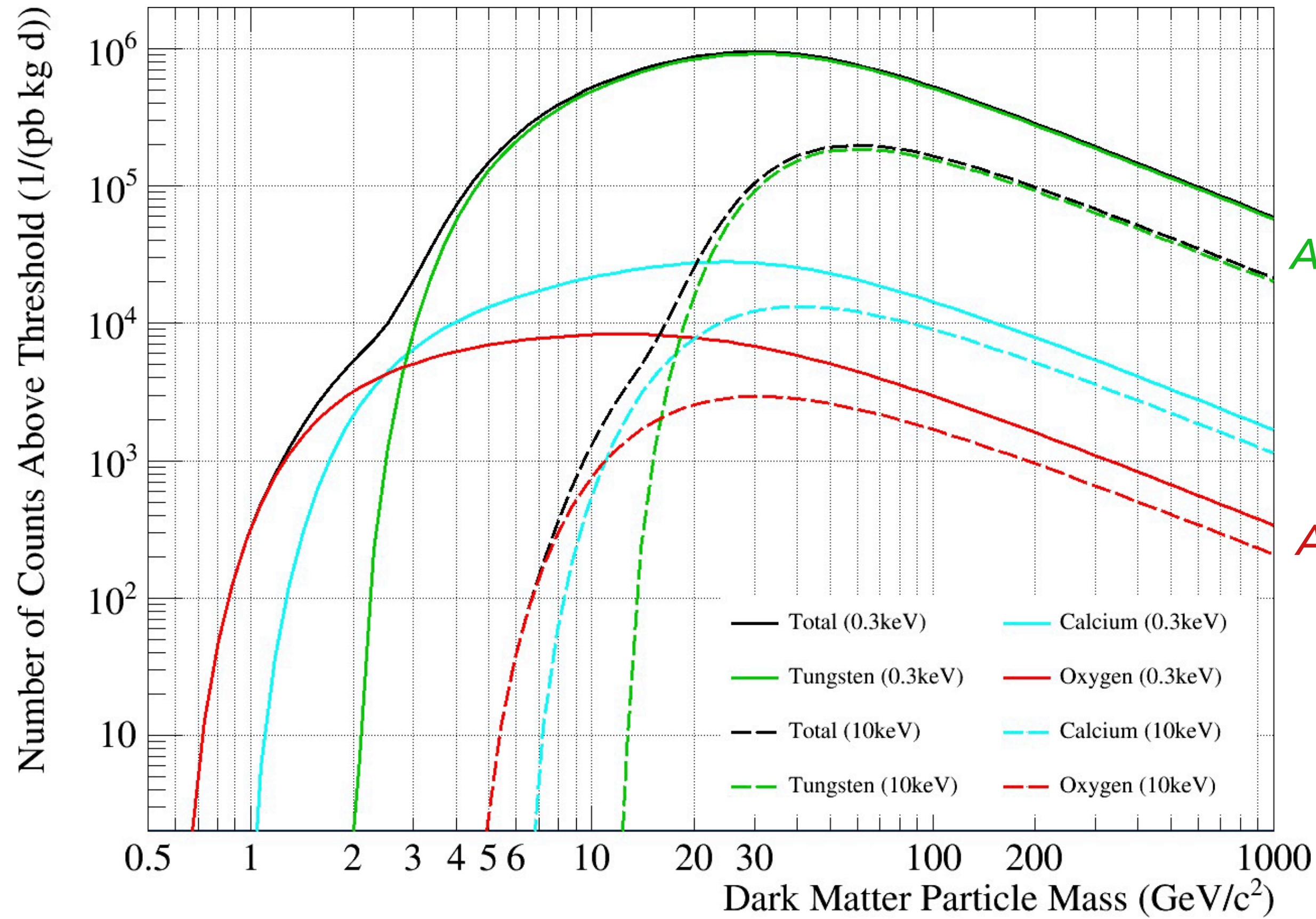


What nucleus (i.e. target) to pick?





What nucleus (i.e. target) to pick?



$A(\text{Tungsten}) = 184$

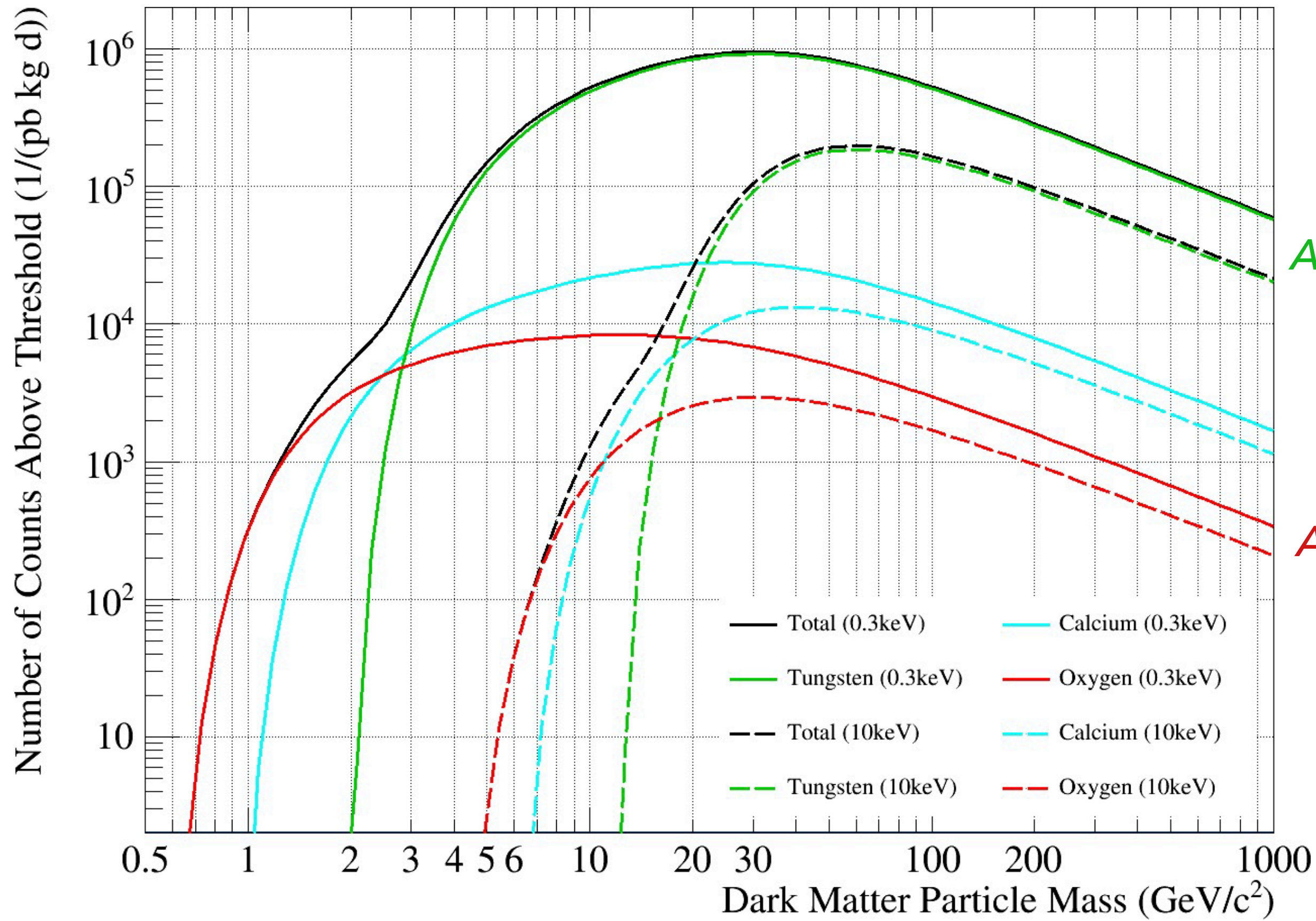
A^2 boost

$A(\text{Oxygen}) = 16$

Heavy target nuclei are favorable!



What nucleus (i.e. target) to pick?



$A(\text{Tungsten}) = 184$

A^2 boost

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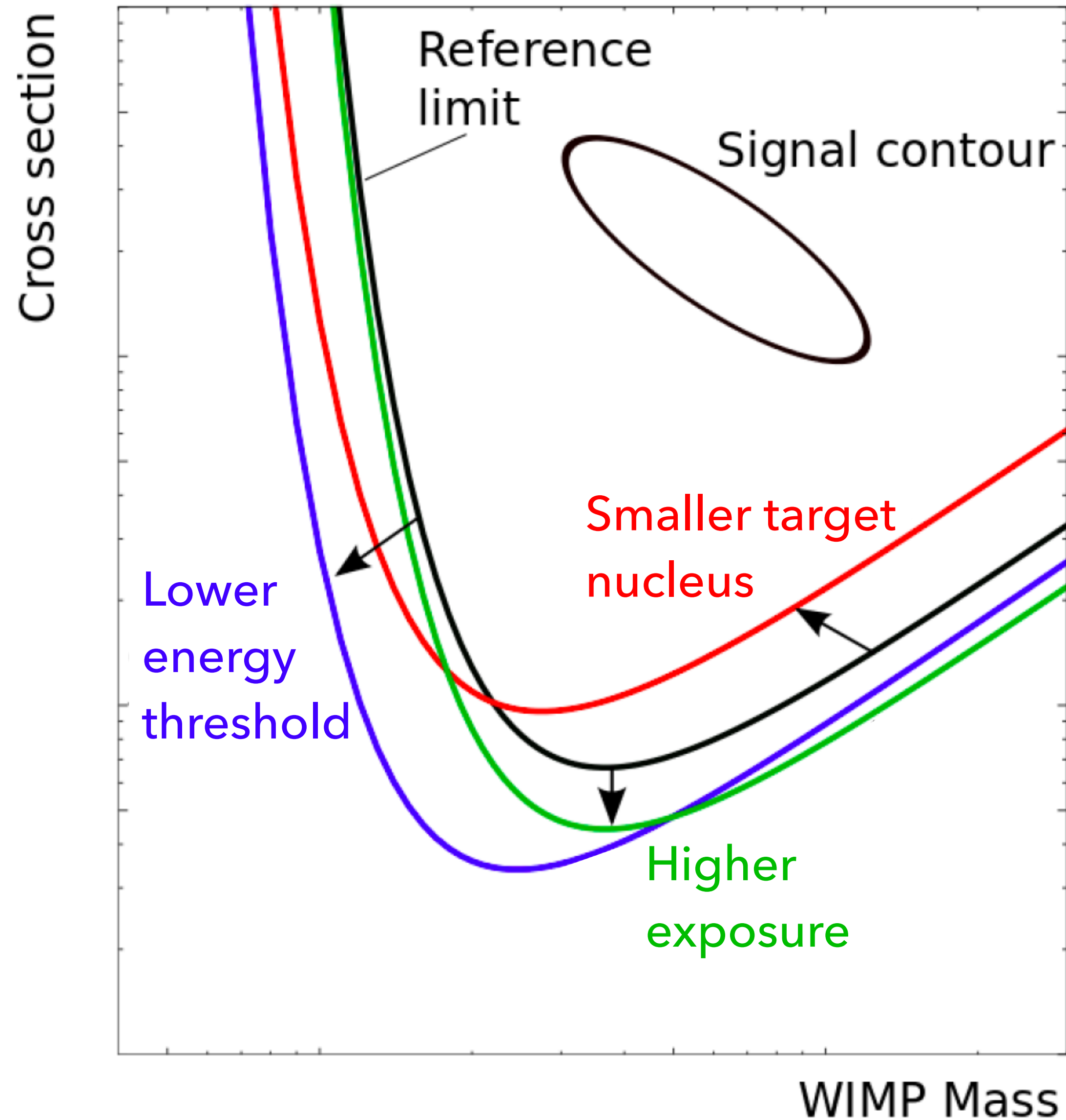
Heavy target nuclei are favorable!

Wait... what?



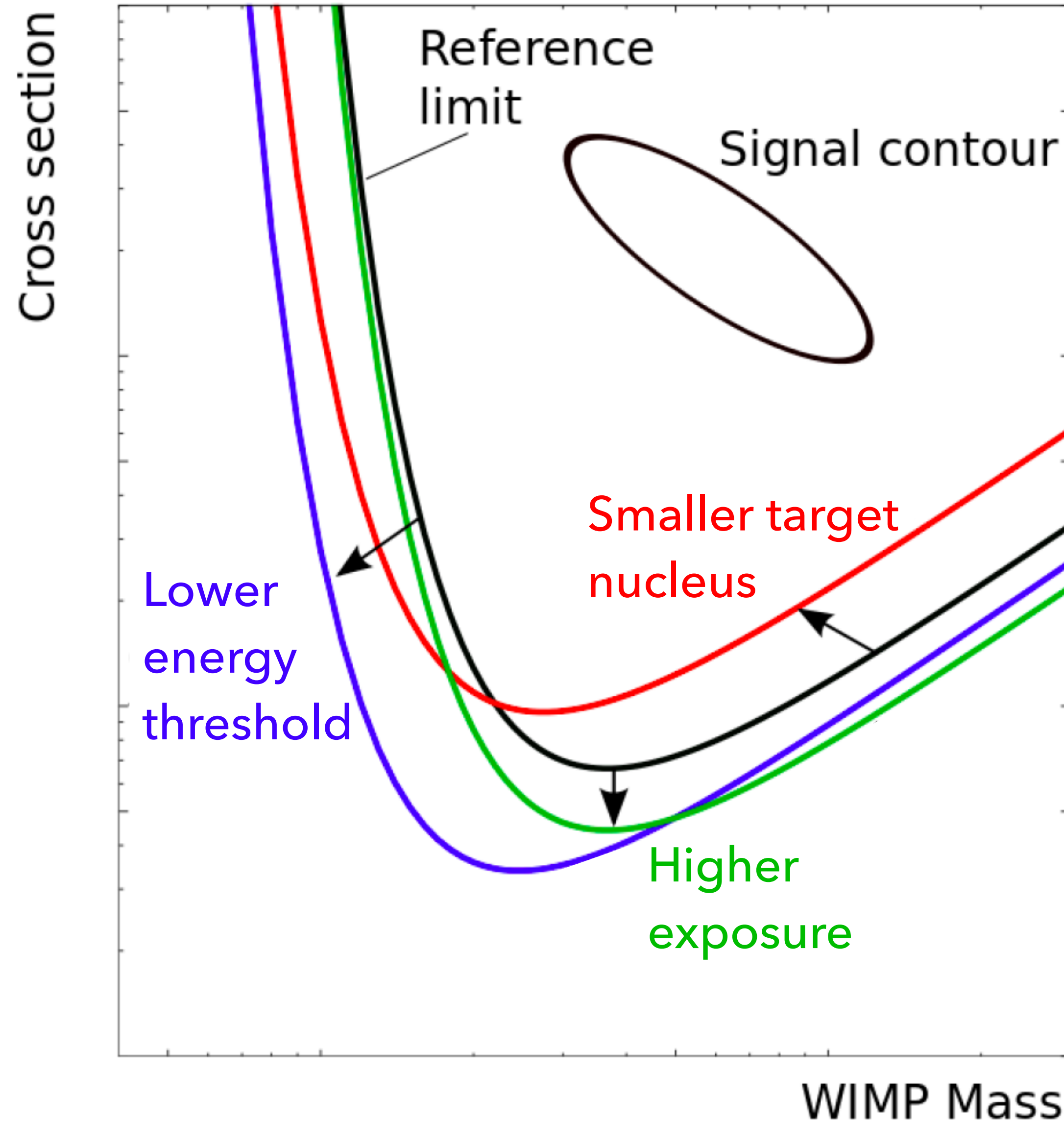
What nucleus (i.e. target) to pick?

J. Phys. G43 (2016) 1, 013001

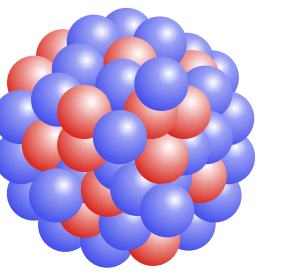
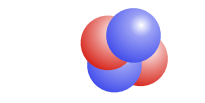


What nucleus (i.e. target) to pick?

J. Phys. G43 (2016) 1, 013001



| Group | | | | | |
|-----------------|-----------------|-----------------|-----------------|----------------|---------------|
| 13 | 14 | 15 | 16 | 17 | 18 |
| | | | | | He Helium |
| B Boron | C Carbon | N Nitrogen | O Oxygen | F Fluorine | Ne Neon |
| Al Aluminium | Si Silicon | P Phosphorus | S Sulfur | Cl Chlorine | Ar Argon |
| Ga Gallium | Ge Germanium | As Arsenic | Se Selenium | Br Bromine | Kr Krypton |
| In Indium | Sn Tin | Sb Antimony | Te Tellurium | I Iodine | Xe Xenon |



It depends on the parameter space you are interested in!

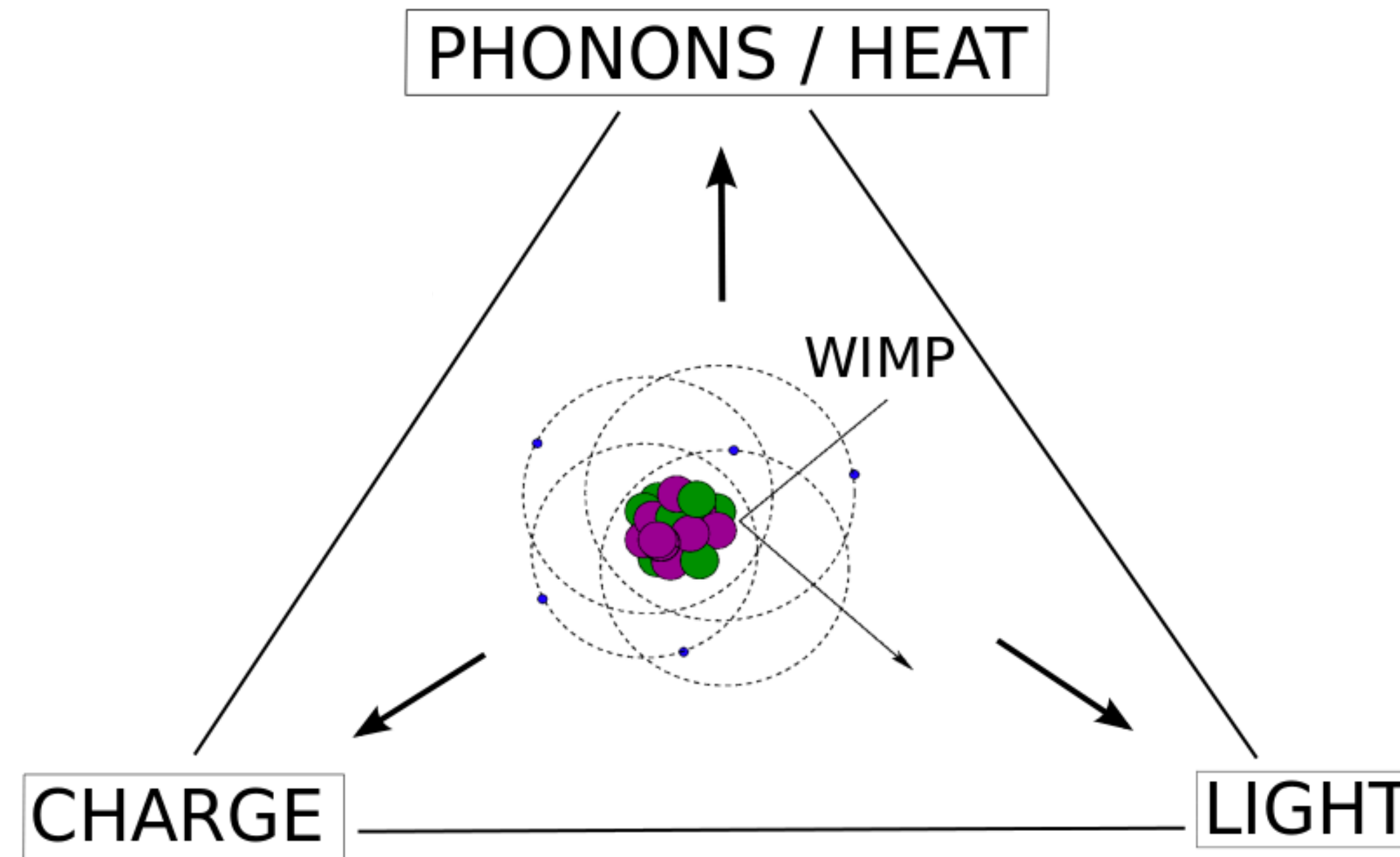


Direct dark matter detection

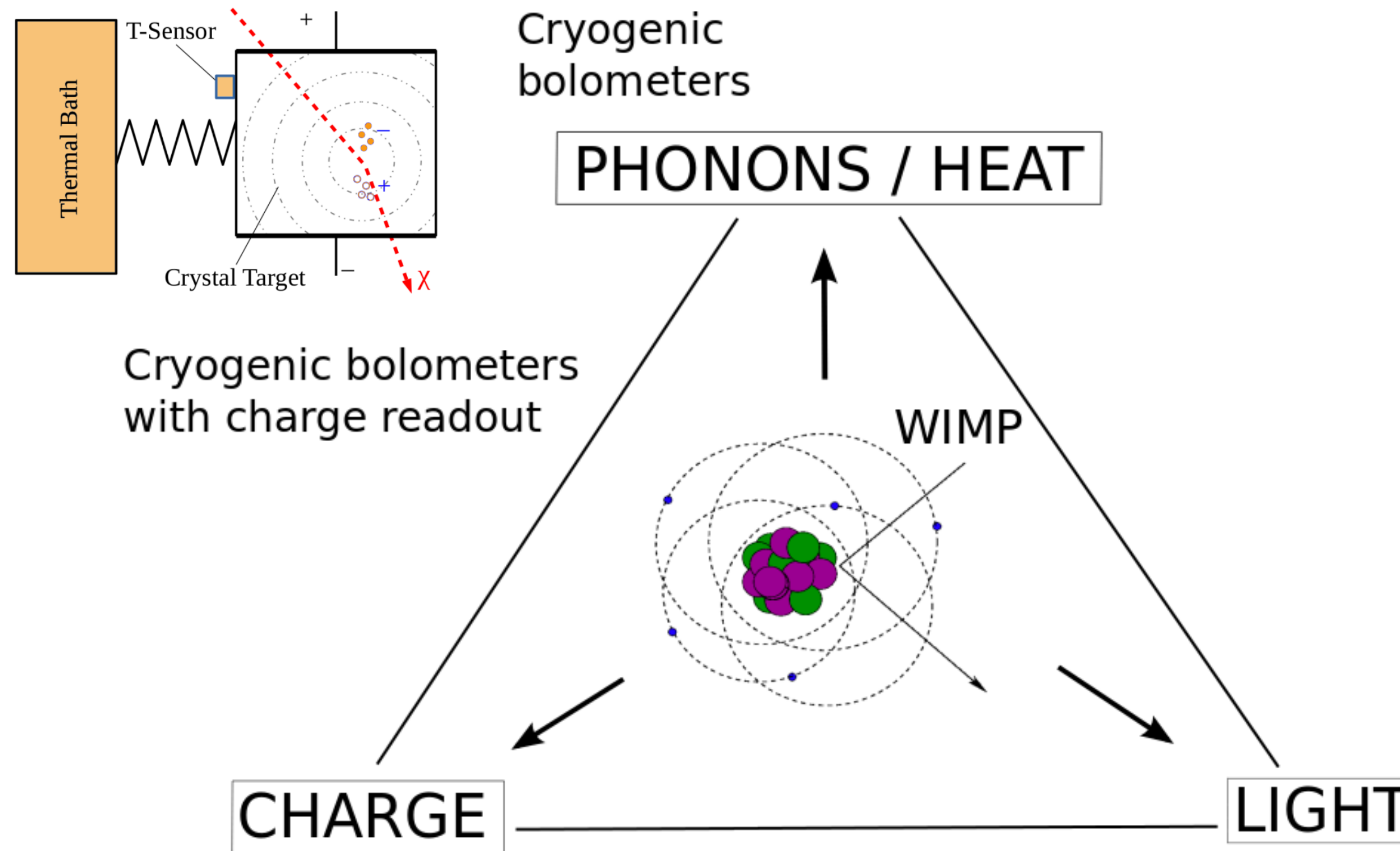
Detector concepts



How to design a dark matter detector

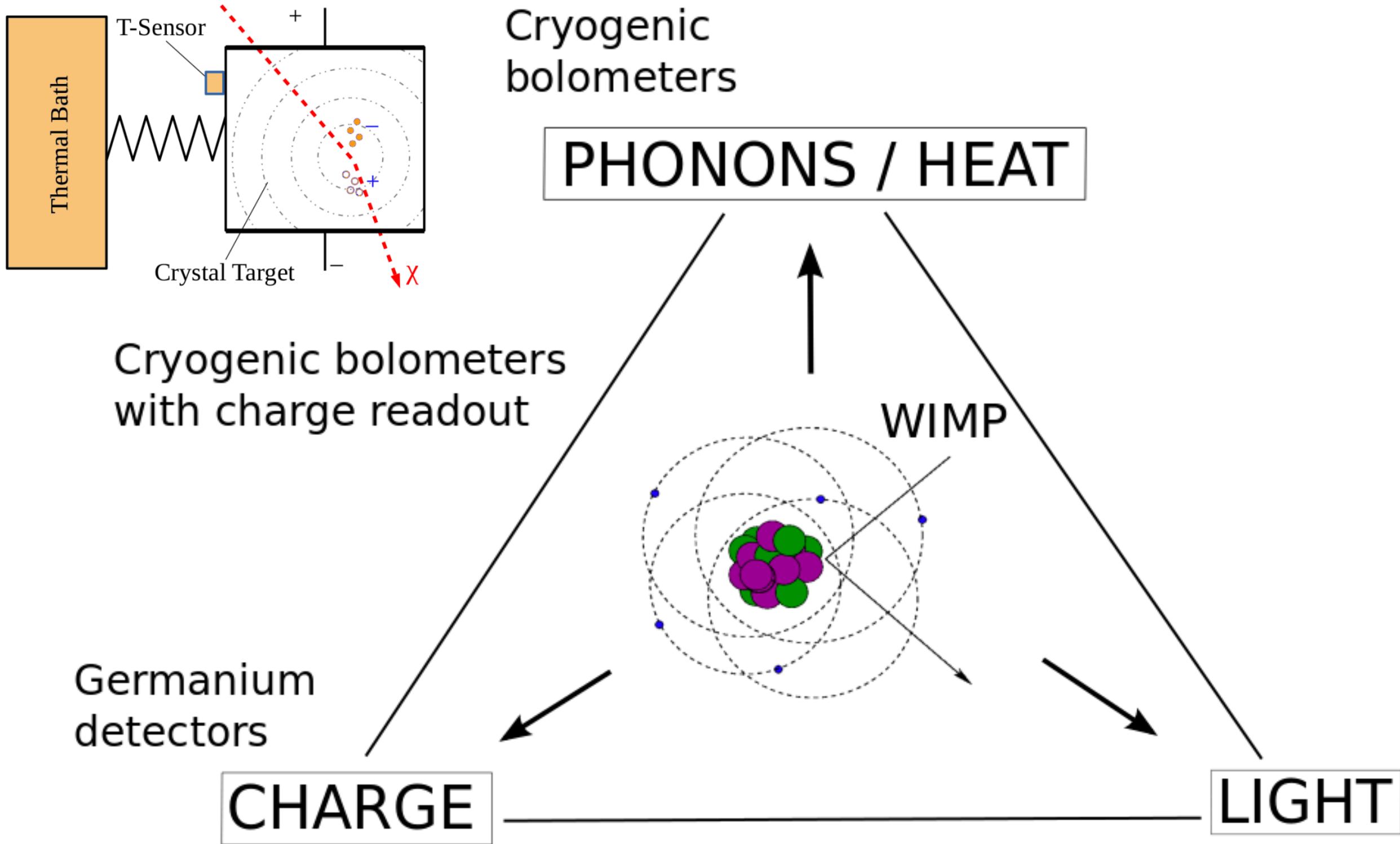


How to design a dark matter detector

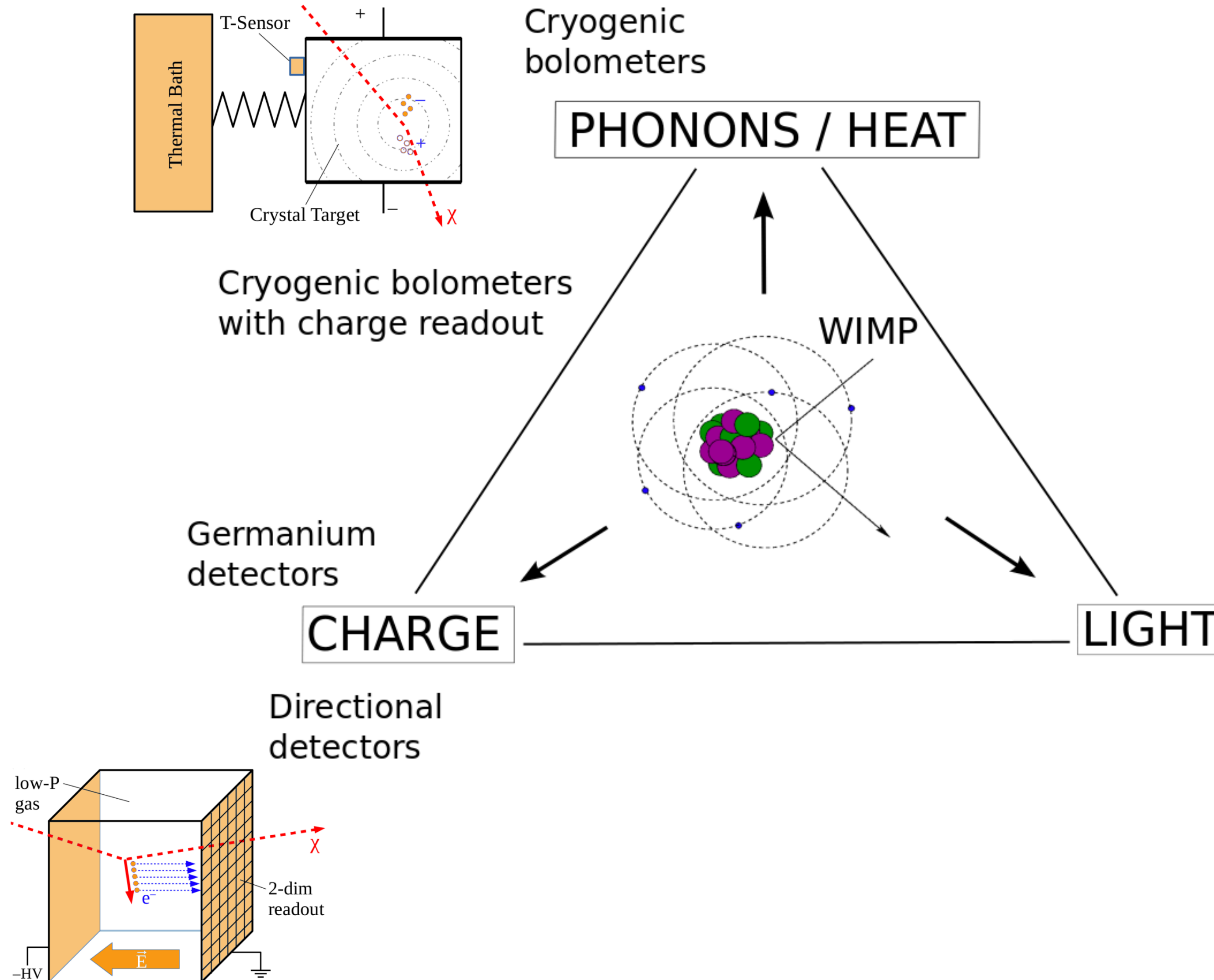




How to design a dark matter detector

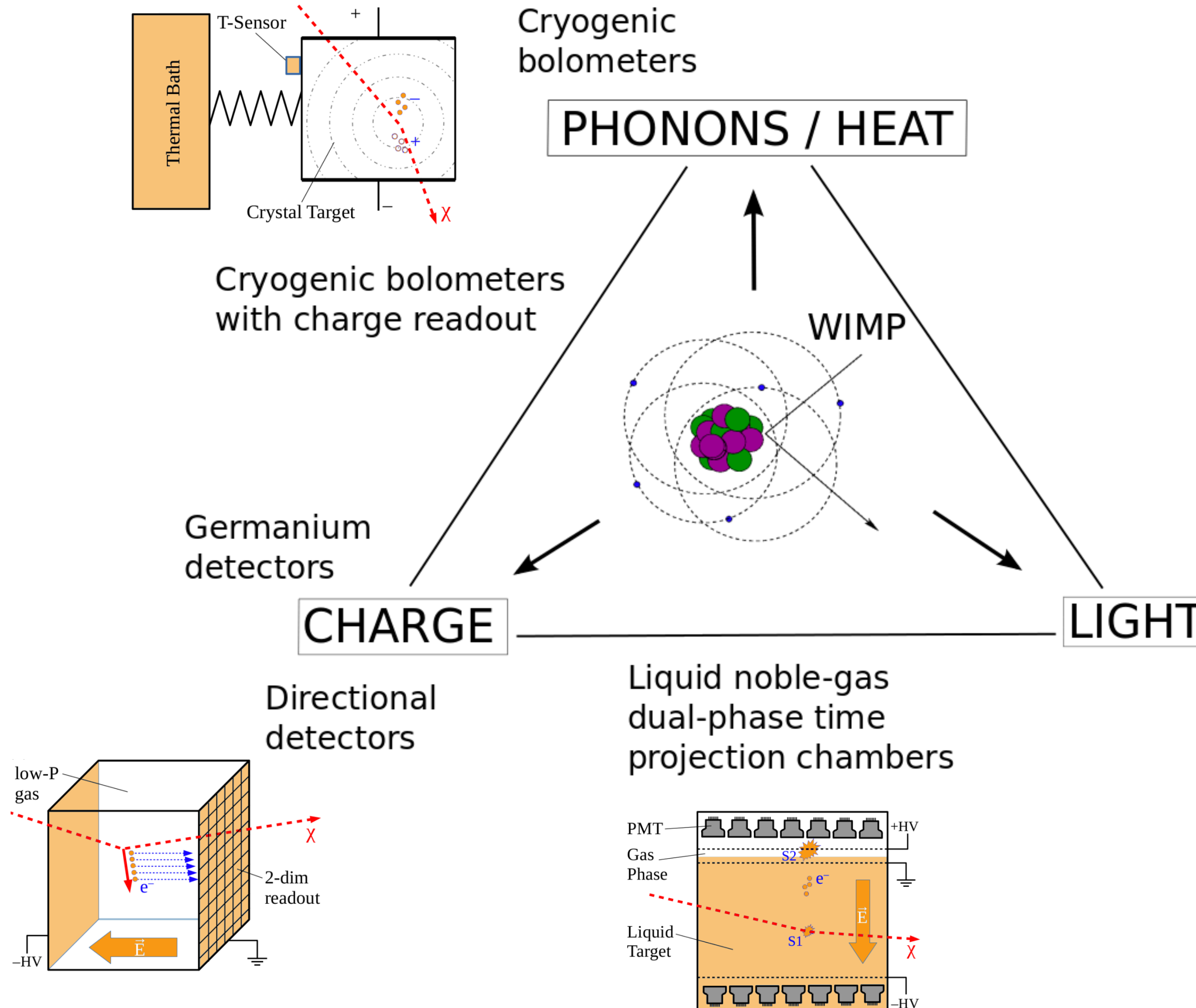


How to design a dark matter detector

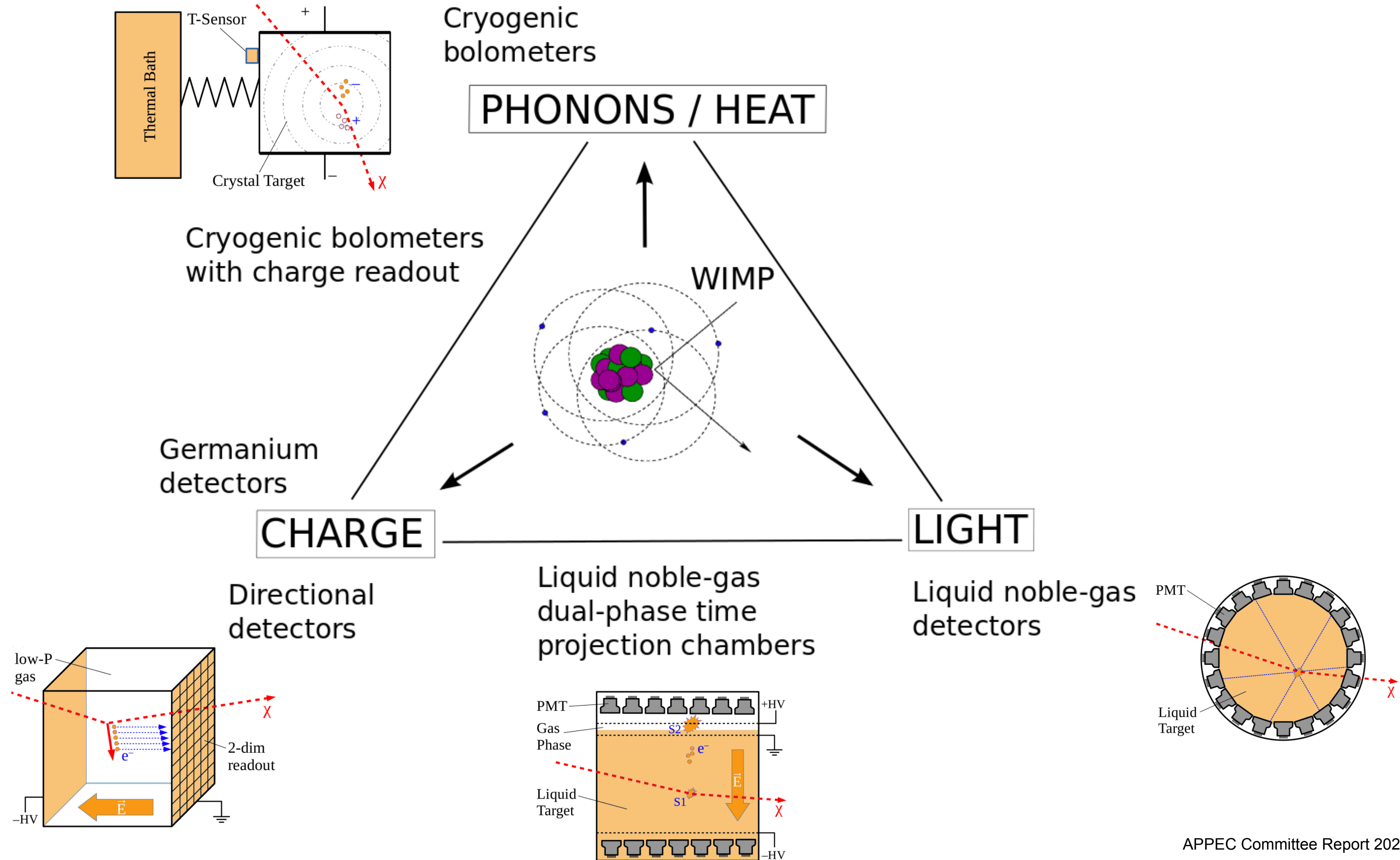




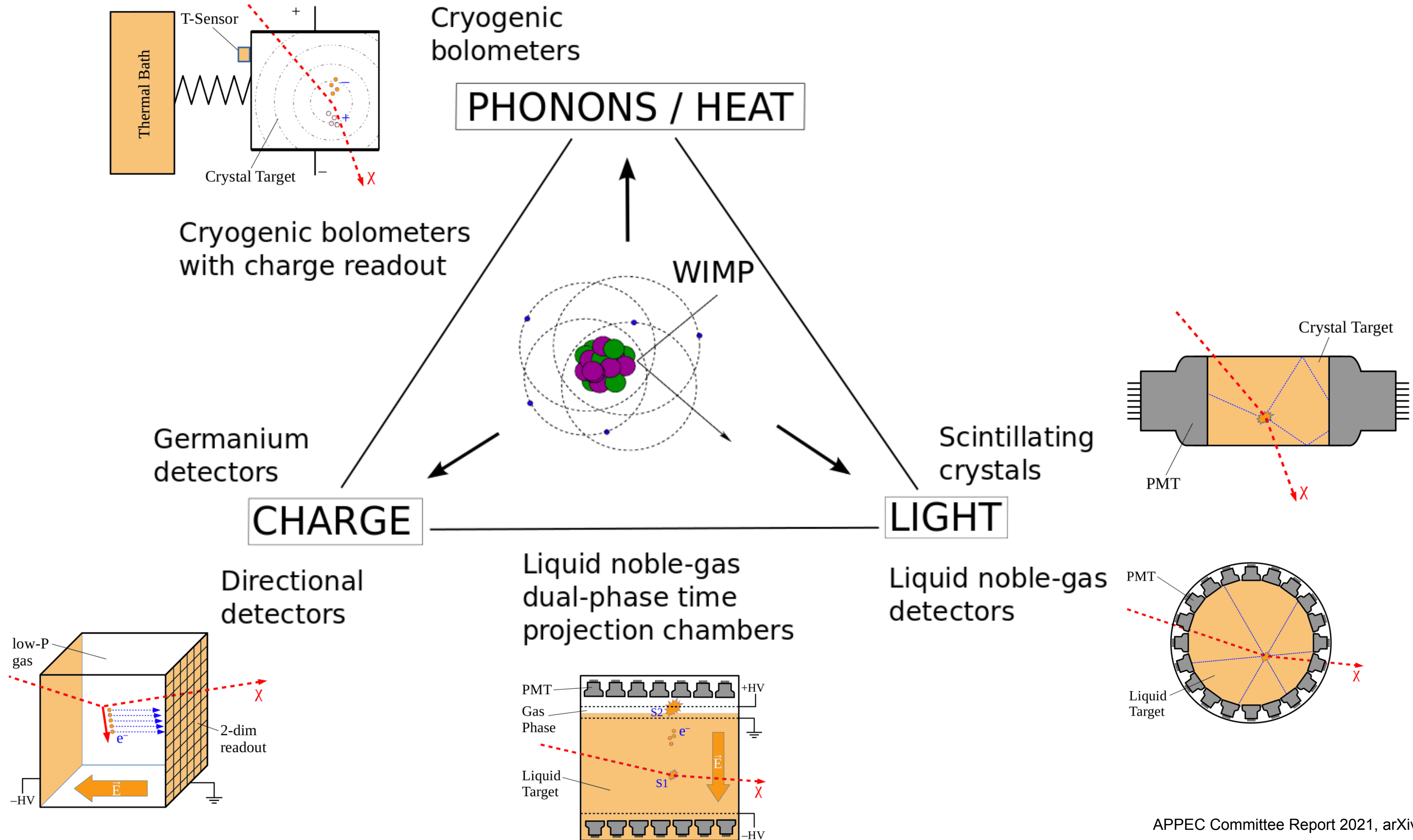
How to design a dark matter detector



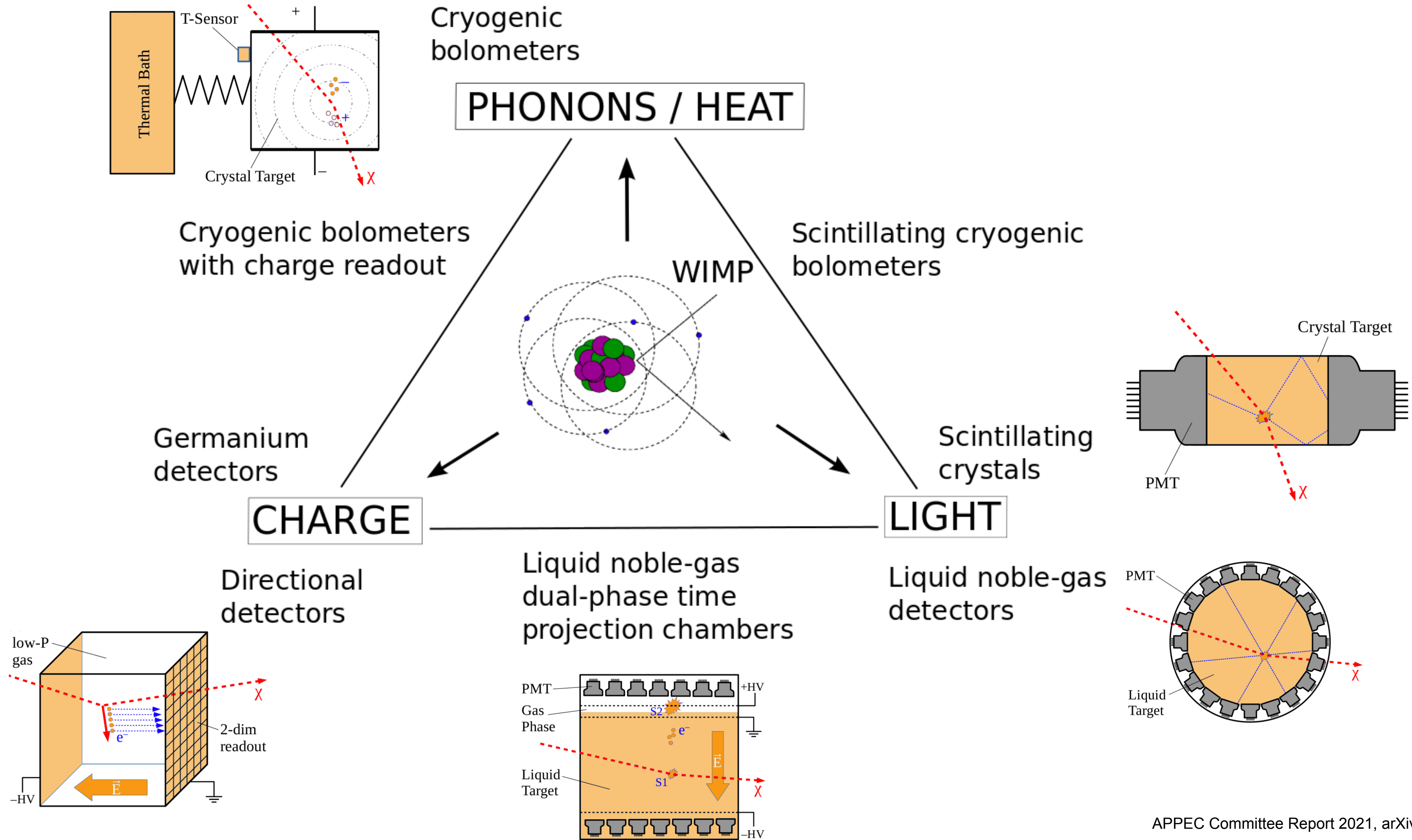
How to design a dark matter detector



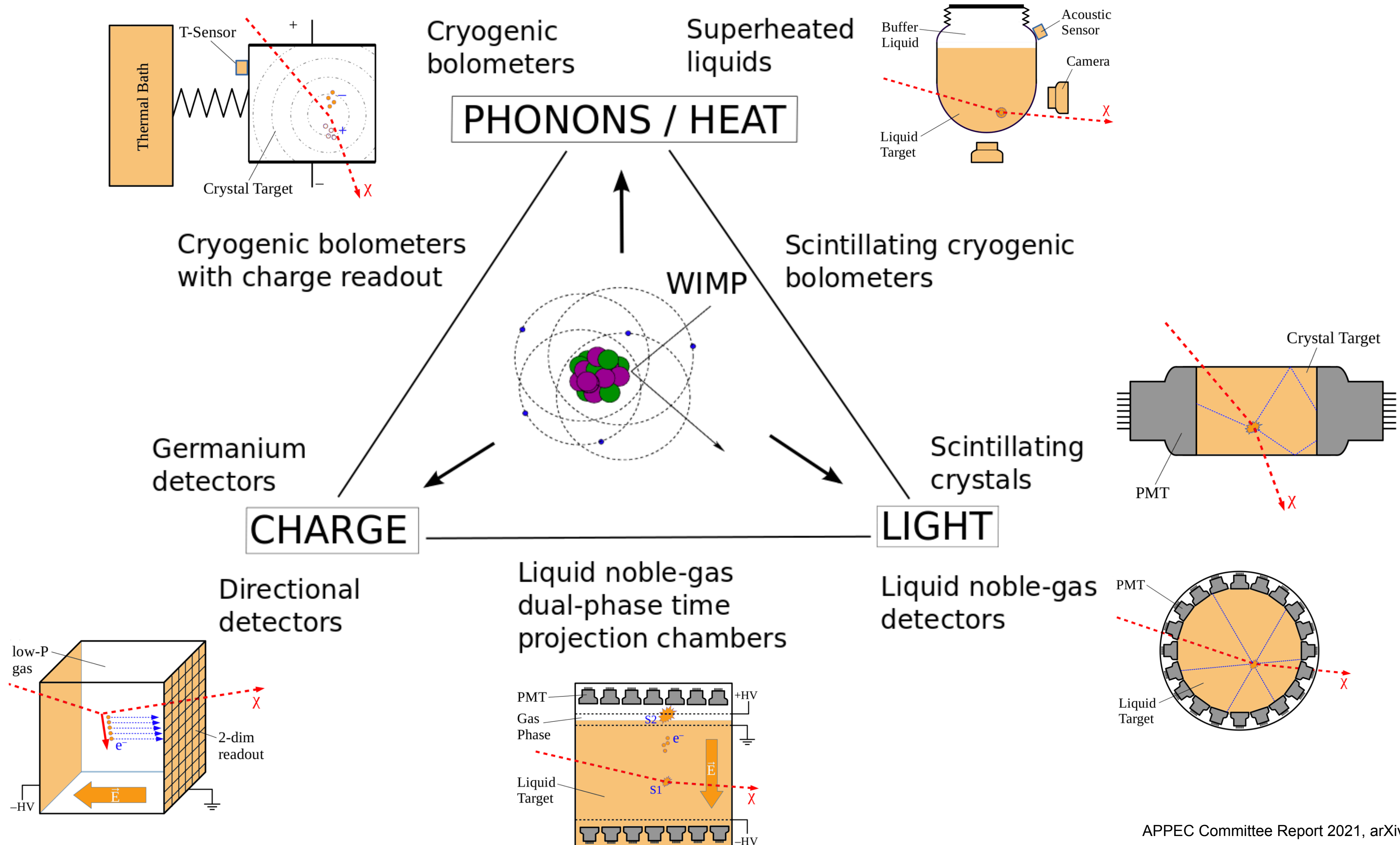
How to design a dark matter detector



How to design a dark matter detector



How to design a dark matter detector





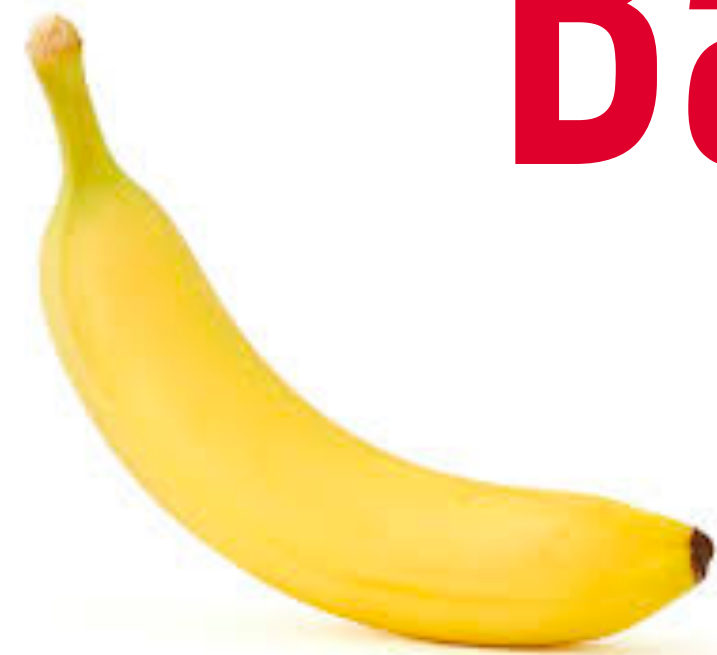
Direct dark matter detection

Why combining two signals?



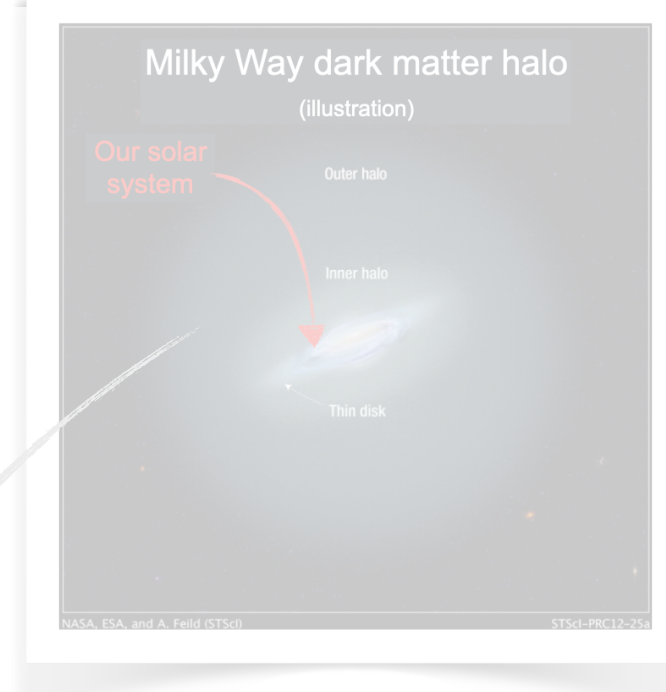
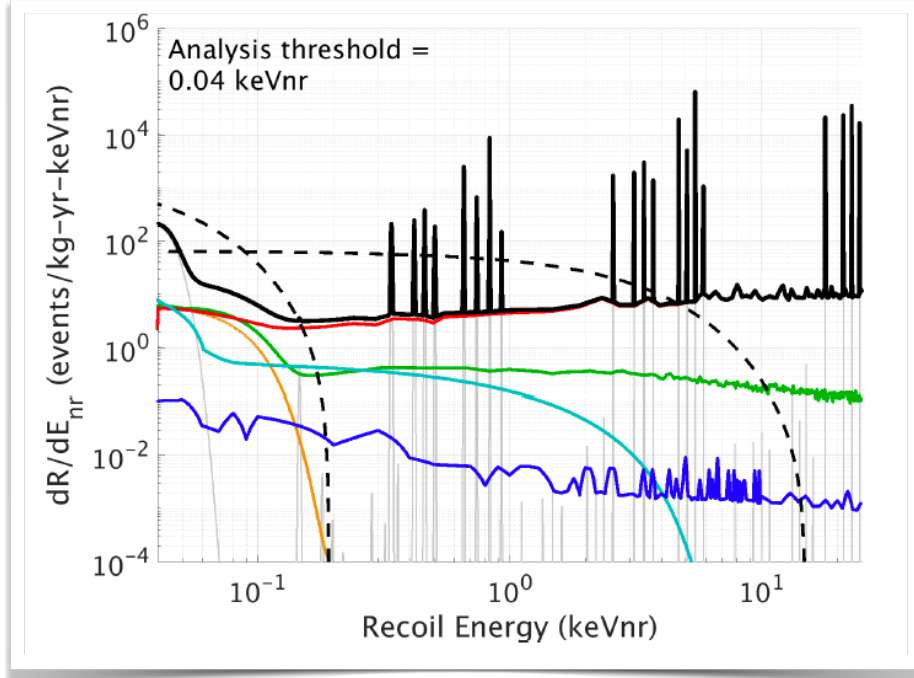
Direct dark matter detection

Backgrounds...





The dark matter direct detection master formula



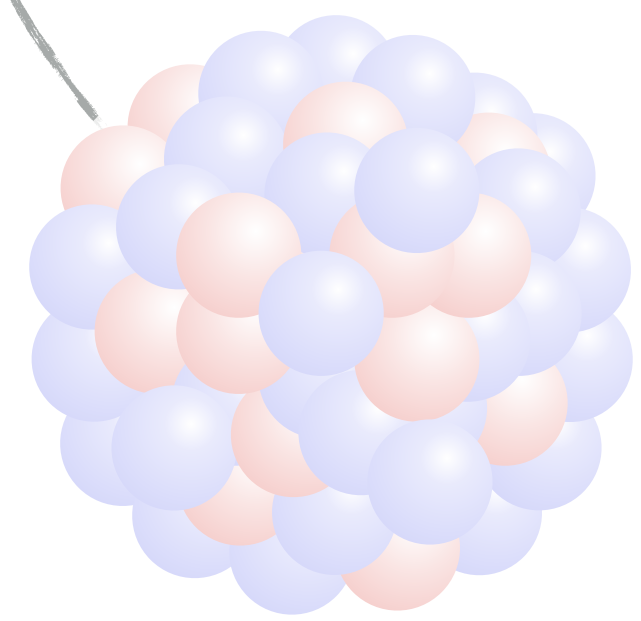
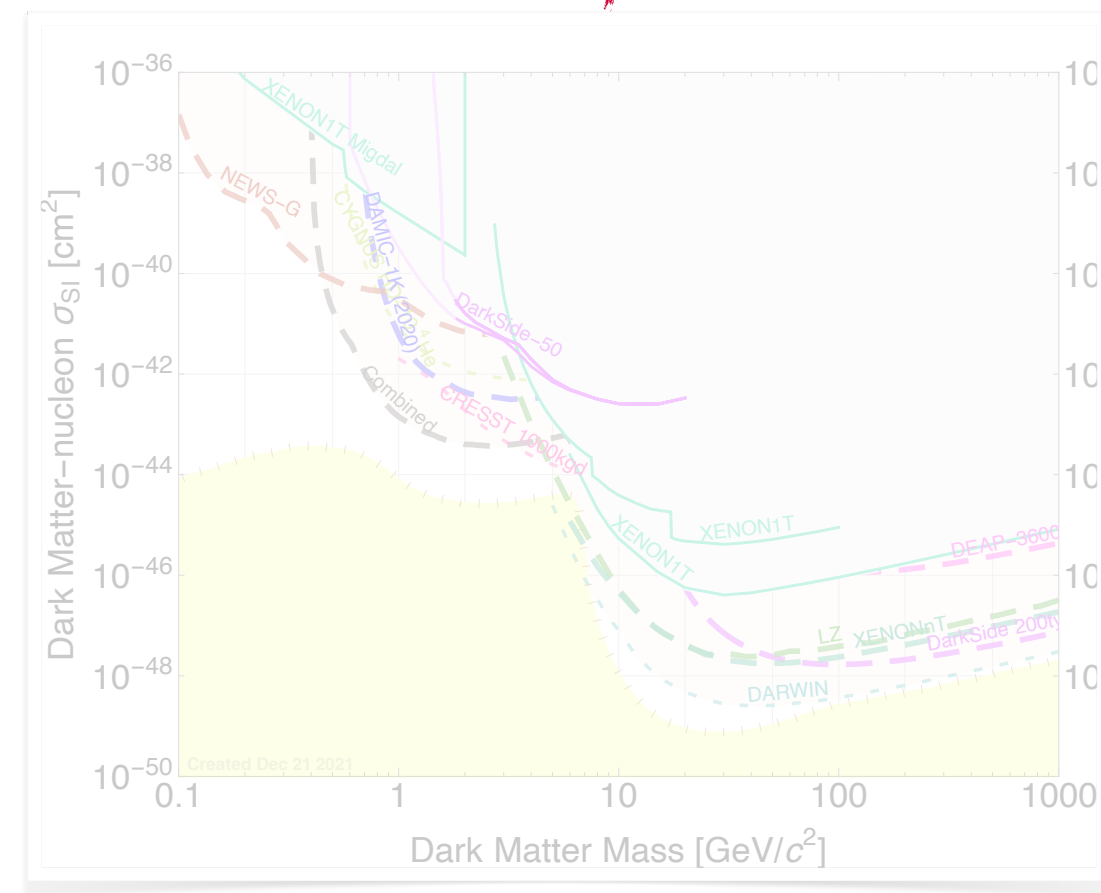
$$\left(\frac{dR}{dE_R} \right)_{\chi N}^{\text{SI}} = \frac{\sigma_0^{\text{SI}}}{m_\chi} \cdot \frac{\rho_0 T(\vec{v})}{v \sqrt{\pi}} \cdot \frac{F_{\text{SI}}^2(E_R)}{\mu^2}$$

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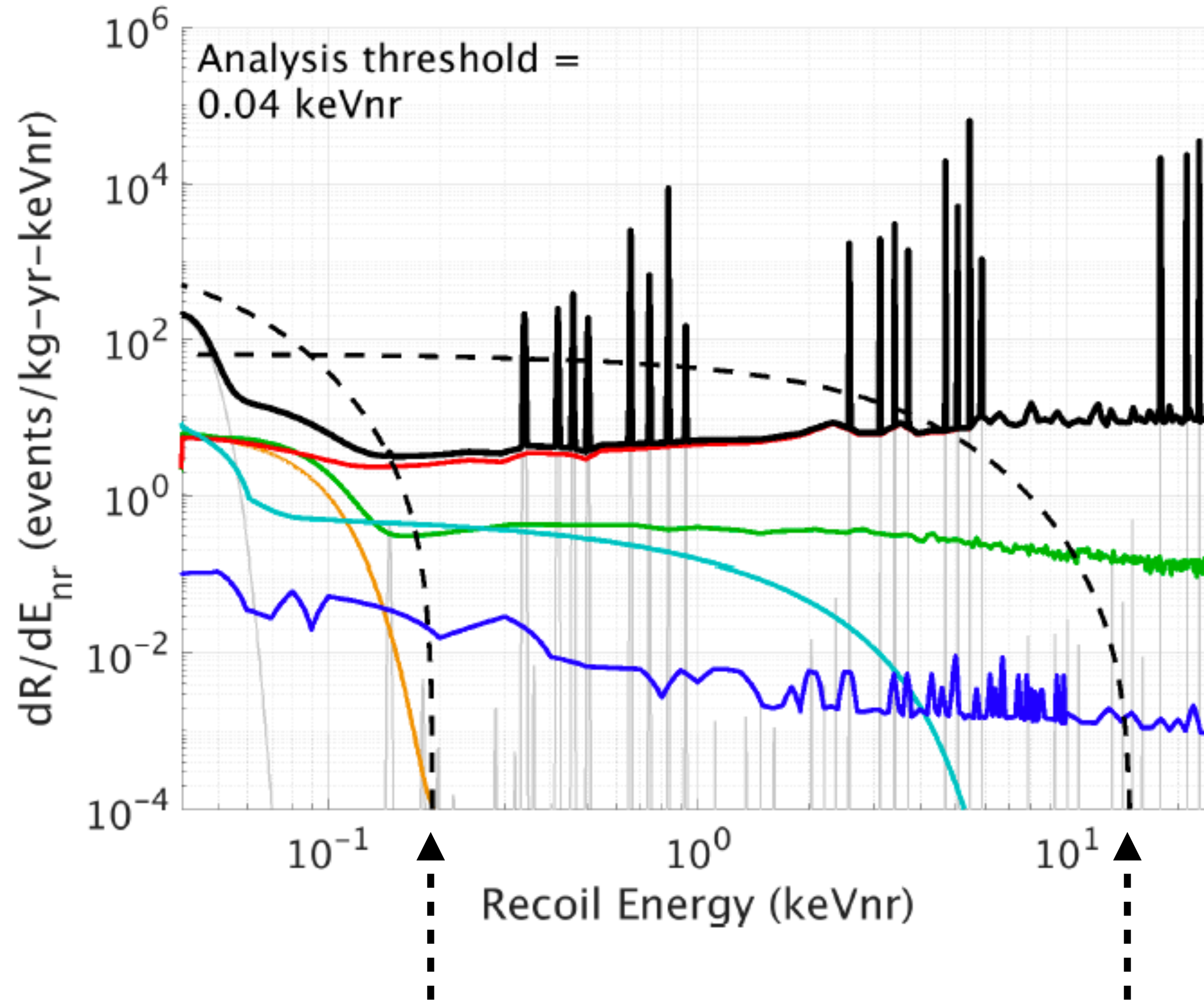




DM-nucleus scattering spectrum and backgrounds

Example:

Prediction for
SuperCDMS SNOLAB
(Ge HV detectors)



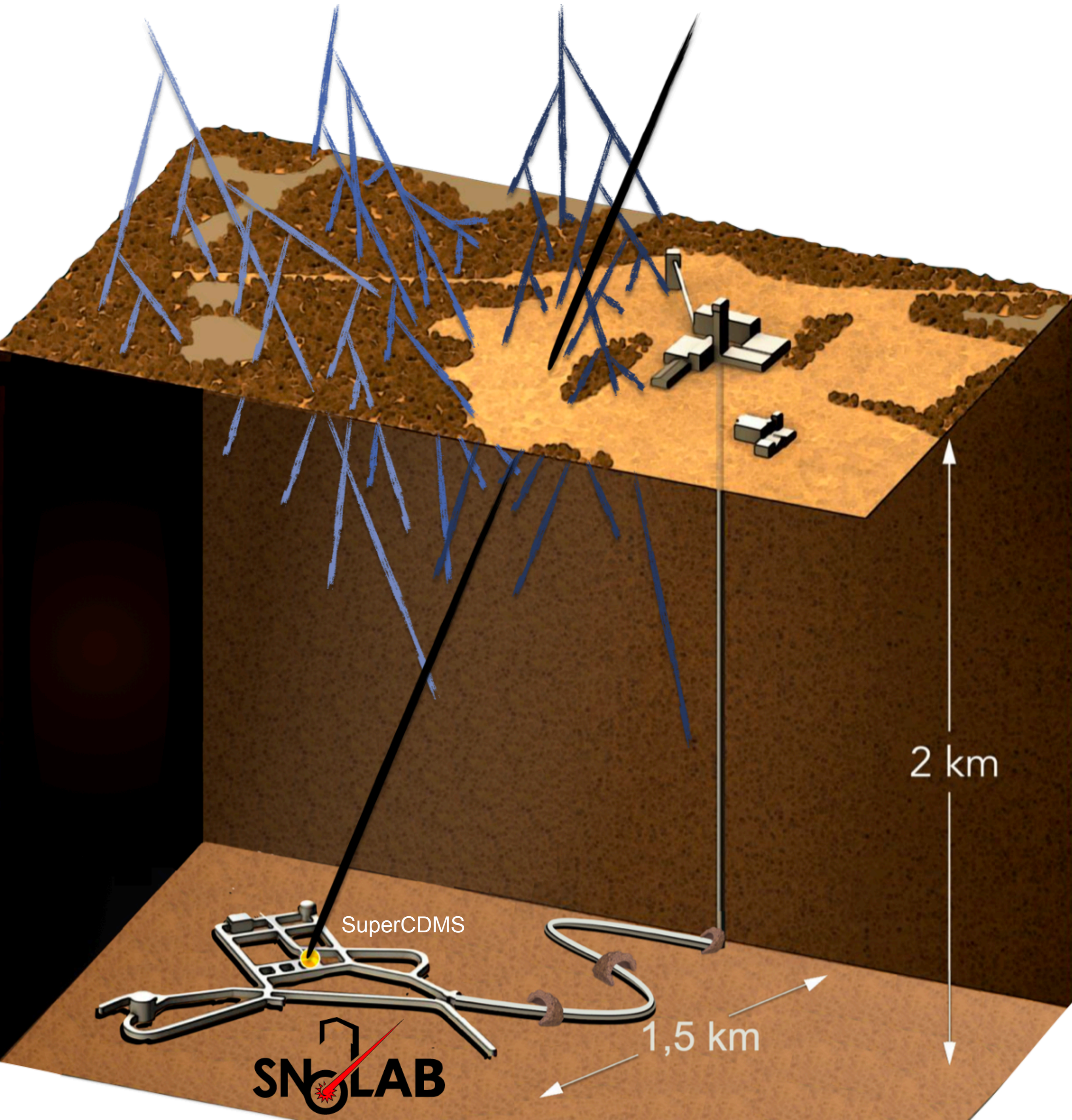
Total
³H and Comptons
 Ge activation
 Surface betas
 Surface ²⁰⁶Pb
 Coherent neutrinos
 Neutrons

1 GeV/c² WIMP

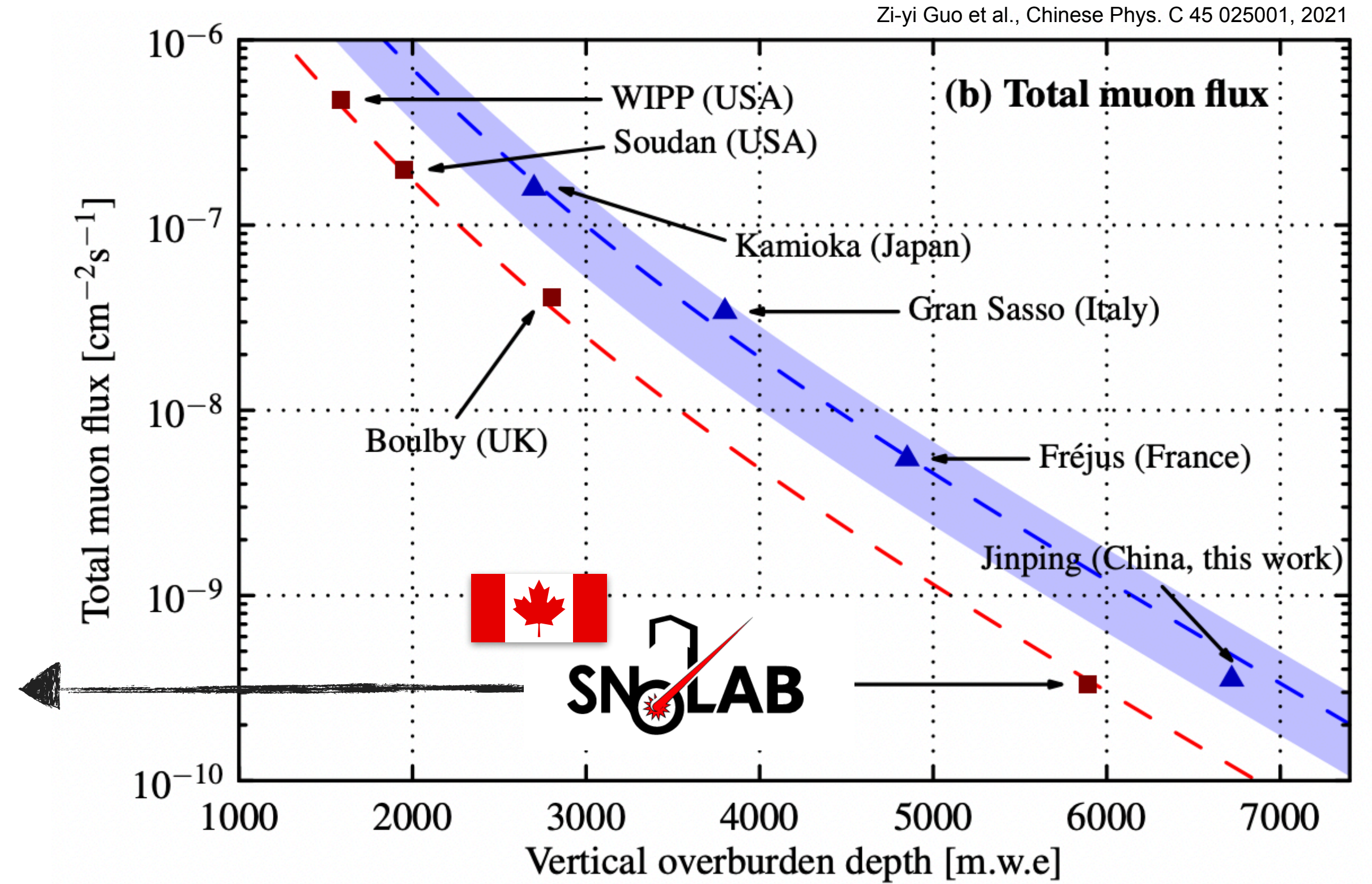
10 GeV/c² WIMP

with $\sigma = 10^{-42} \text{ cm}^2$

Backgrounds: cosmic rays



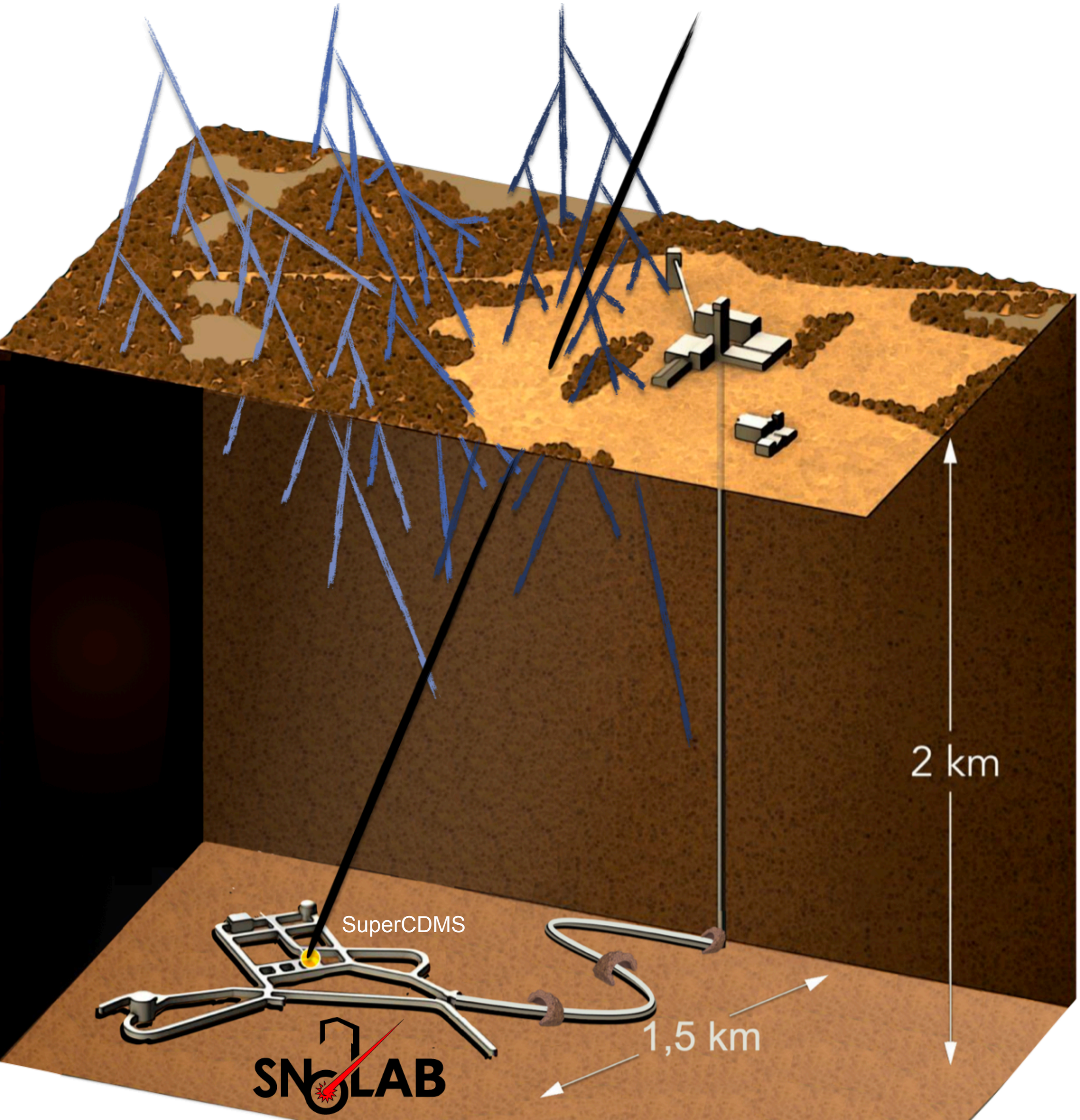
Going underground to mitigate cosmic and cosmogenic backgrounds



At SNOLAB: ~0.3 muons per m^2 per day.



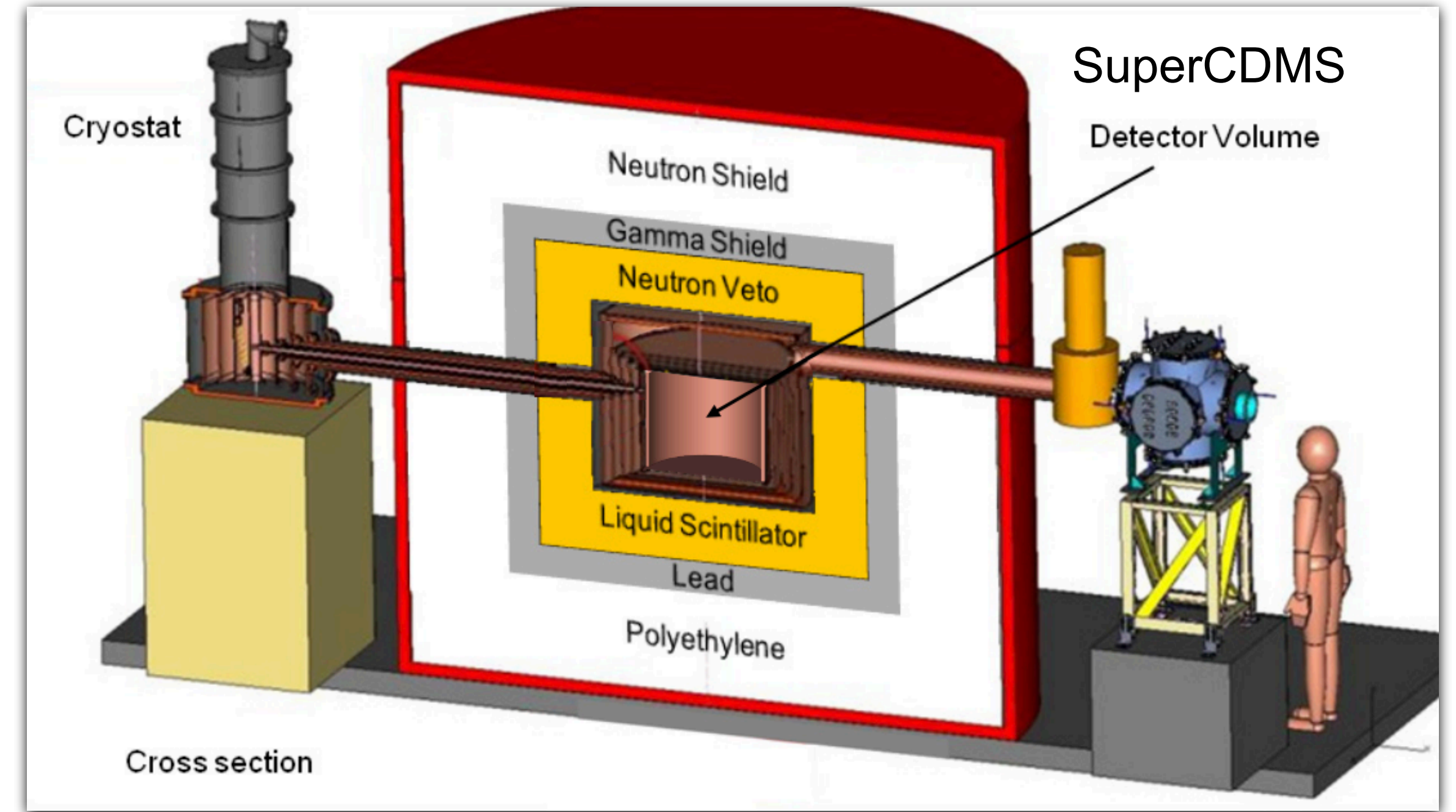
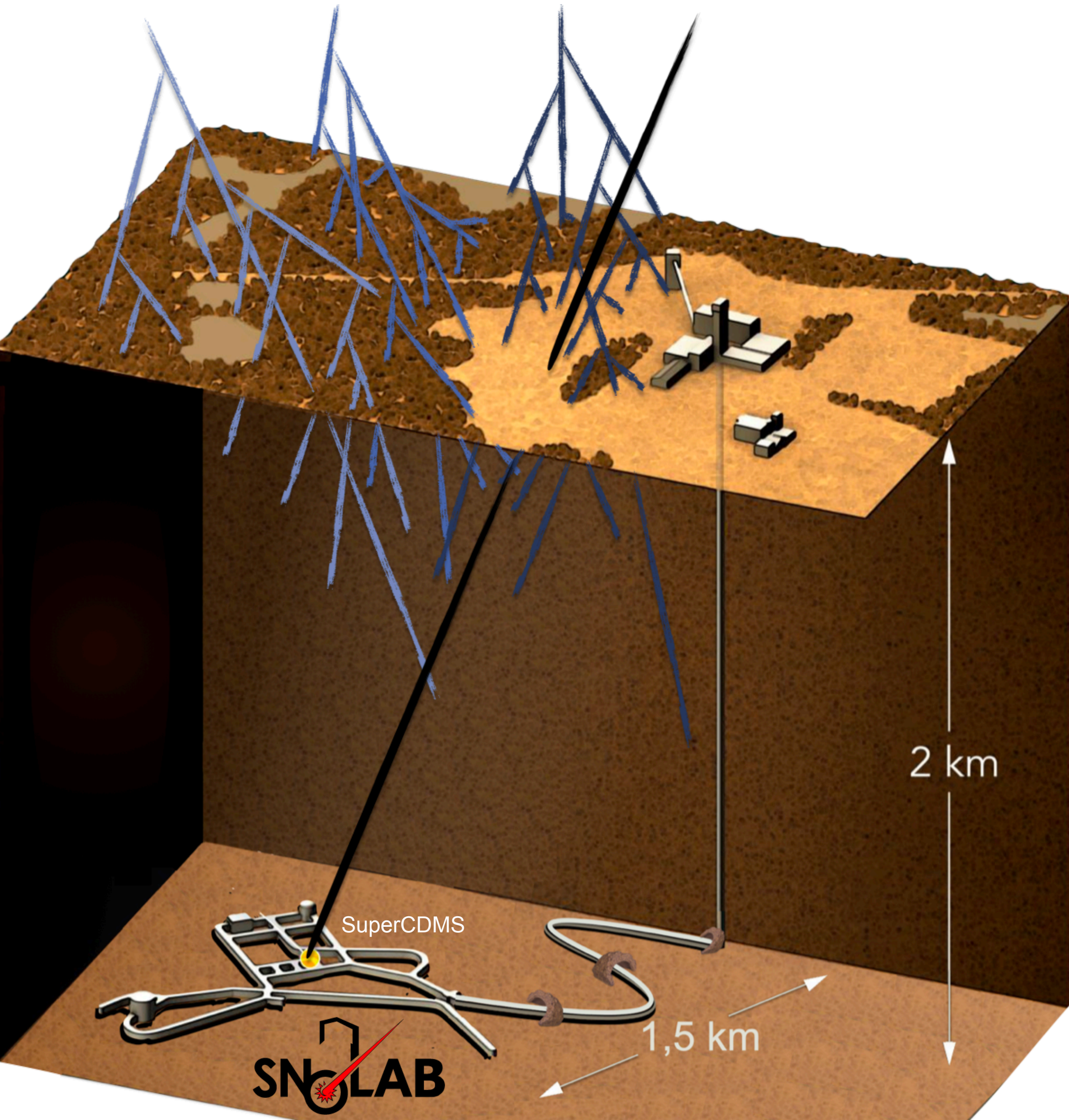
Backgrounds: cosmic rays



Credit: SuperCDMS Collaboration / SNOLAB / M. Wilson



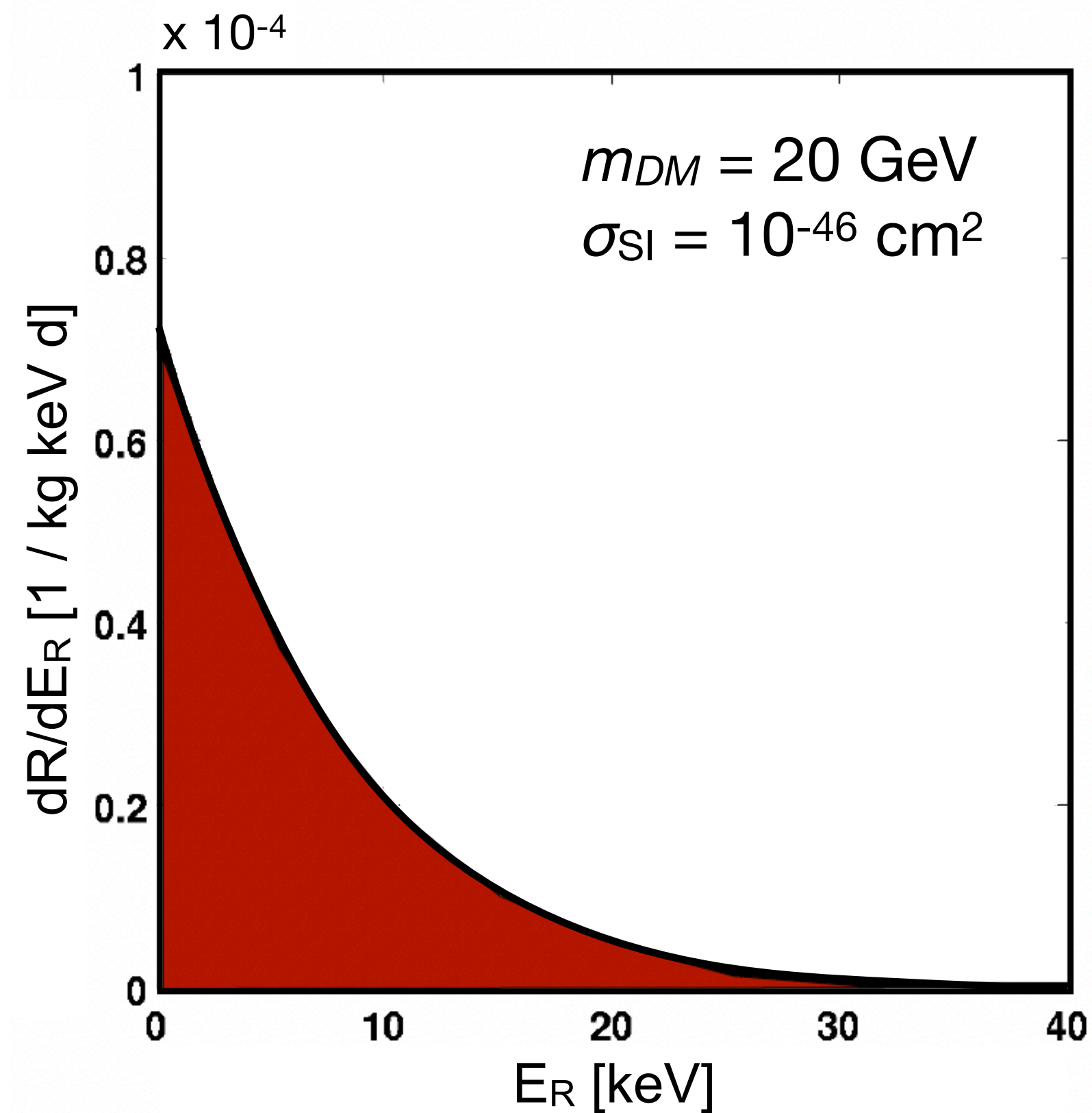
Backgrounds: cosmic rays



Additional active and passive shielding against cosmogenic secondaries

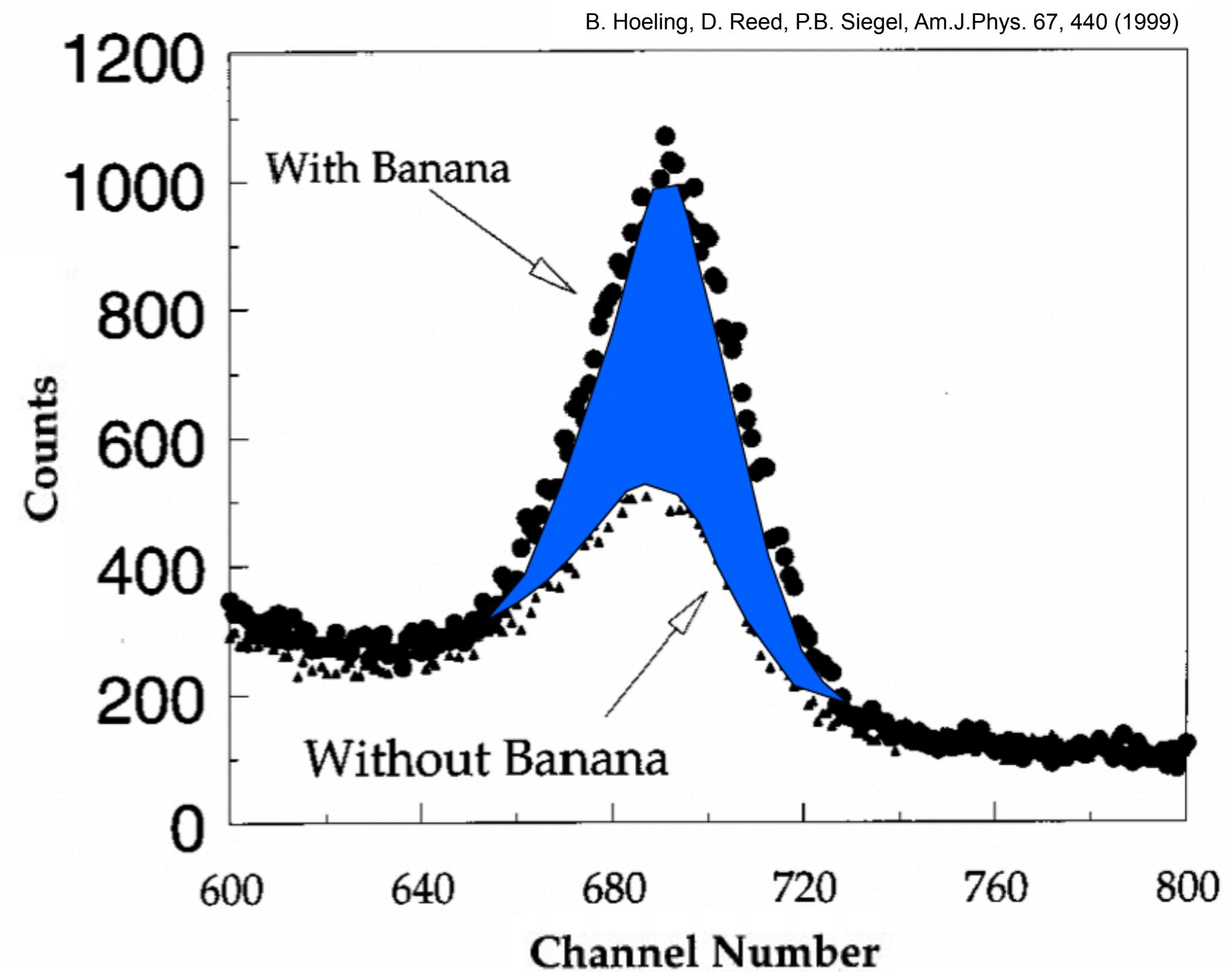
Backgrounds: radioactive decays

Expected DM spectrum



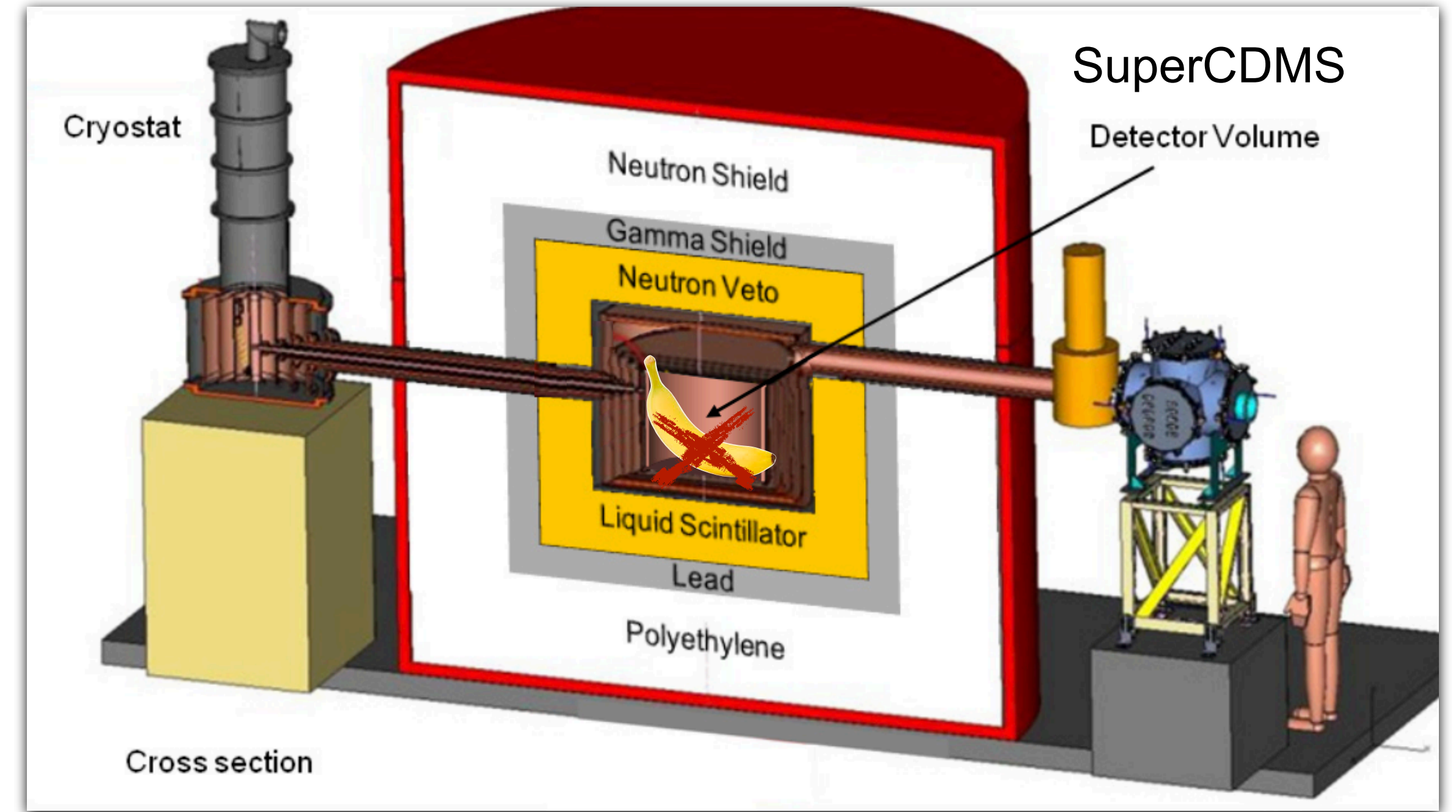
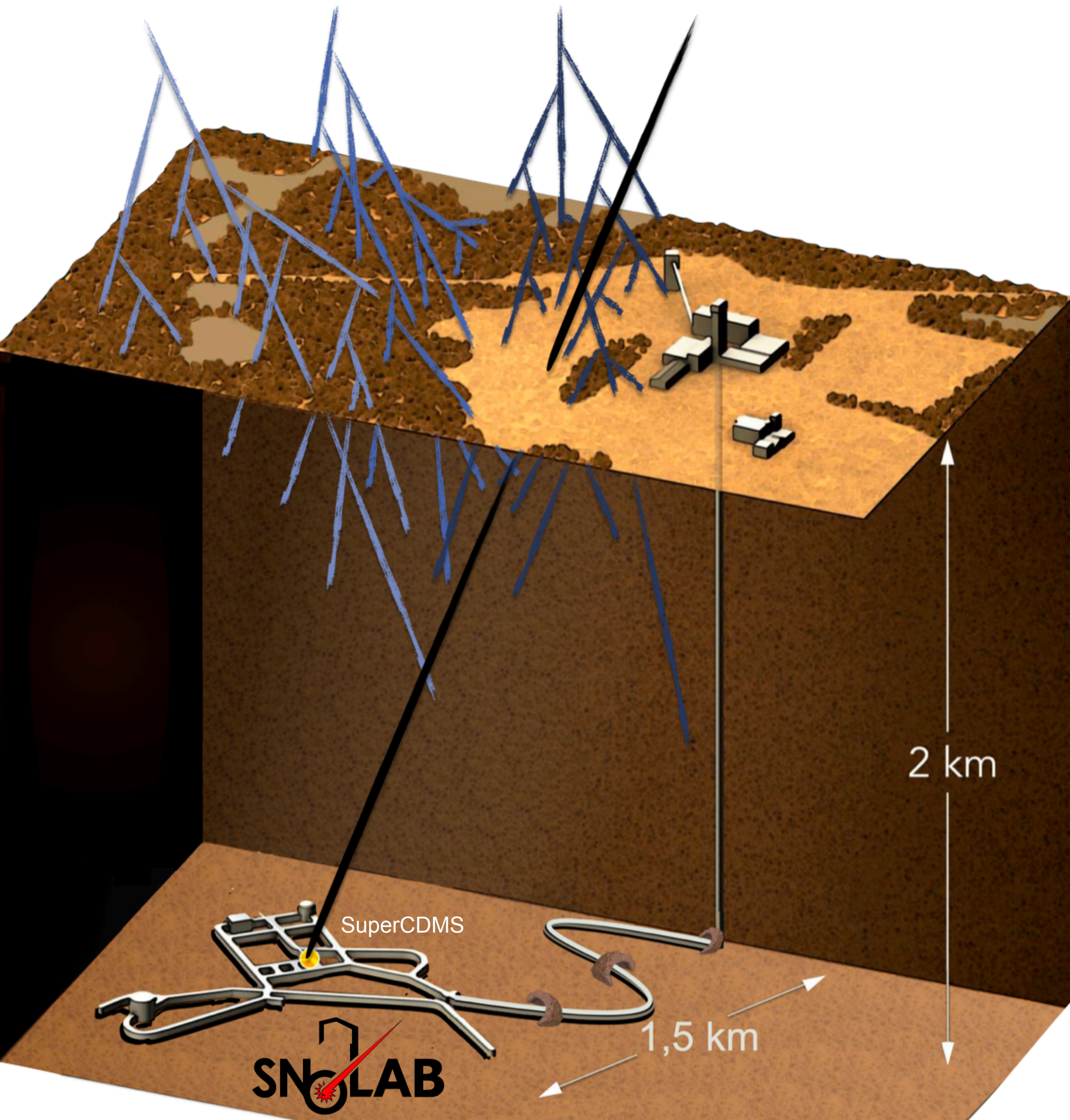
<0.1 event per kg per year
→ nuclear recoils

Measured banana spectrum



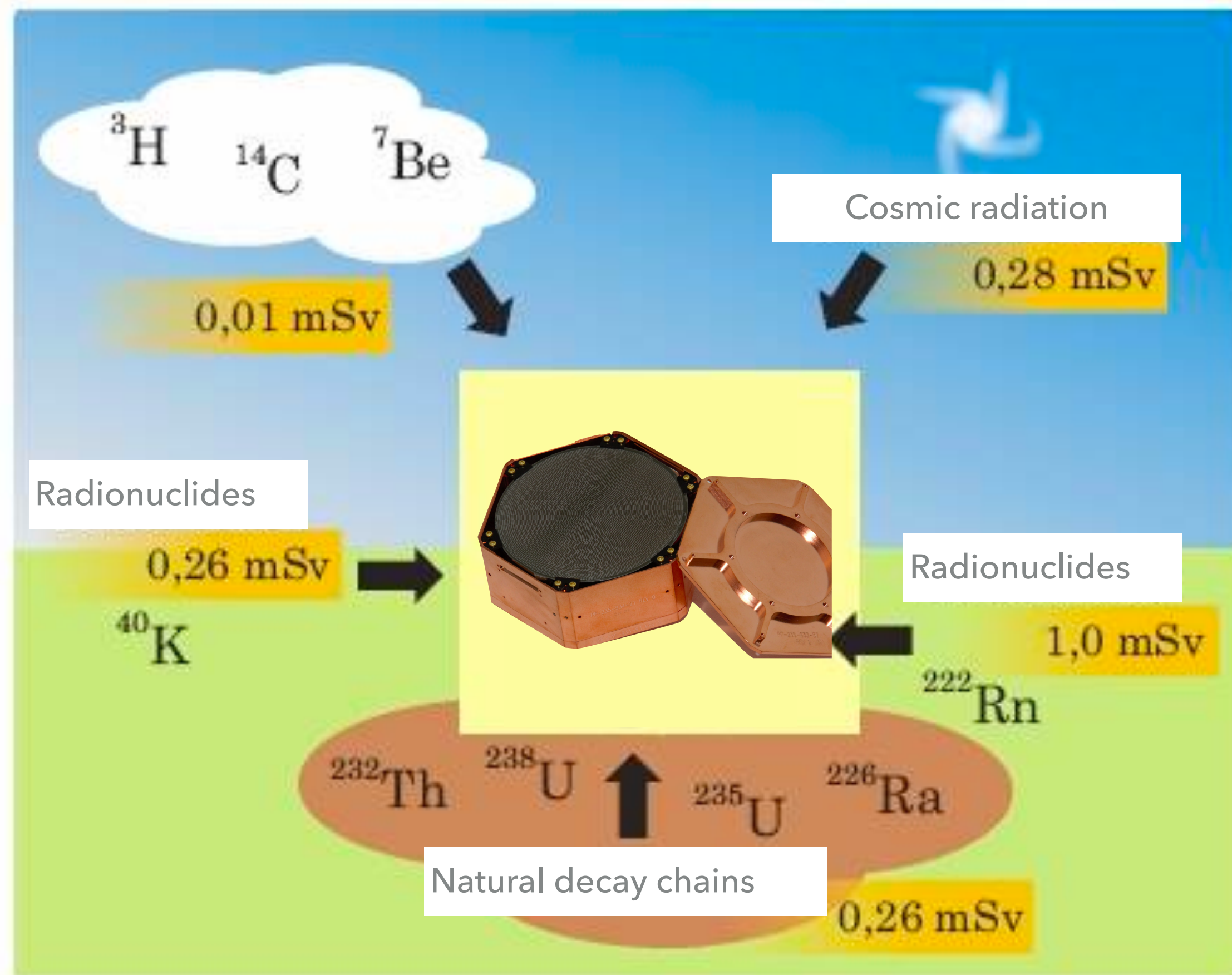
>100 000 events per banana per year
→ electron recoils

Backgrounds: cosmic rays and radioactive decays



Additional active and passive shielding against cosmogenic secondaries

Backgrounds: cosmic rays and radioactive decays



<http://www.goerudio.com/izpratnes-lapa/radioaktivitate>
(modified)

Mitigation strategies

- going underground
- storing materials underground
- passive and active shielding
- Radon mitigation
- use of materials with high purity
- characterize the background
- ...



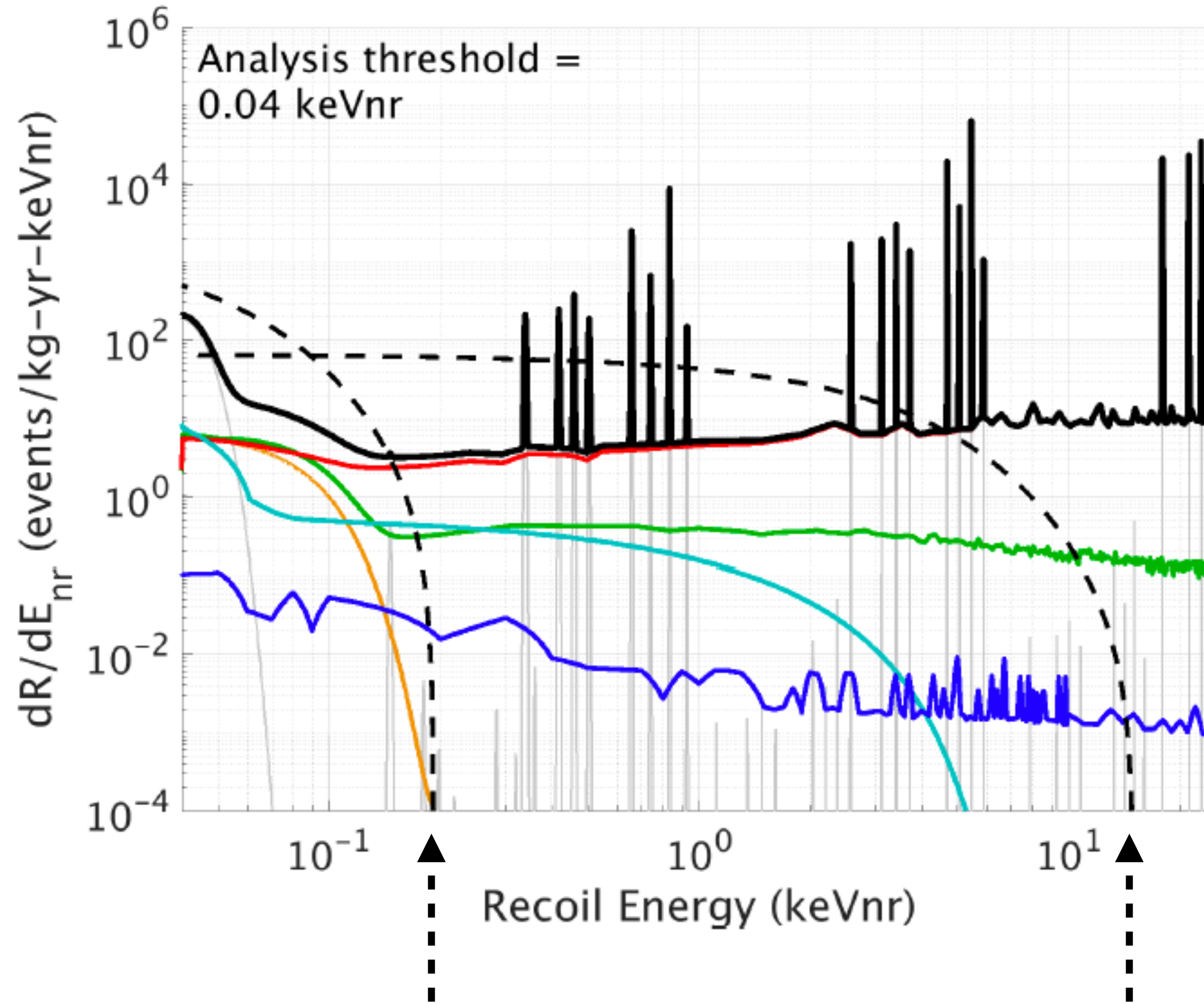


DM-nucleus scattering spectrum and backgrounds

Example:

Prediction for
SuperCDMS SNOLAB
(Ge HV detectors)

Still not
background
free!



Total

³H and Comptons

Ge activation

Surface betas

Surface ²⁰⁶Pb

Coherent neutrinos

Neutrons

1 GeV/c² WIMP

10 GeV/c² WIMP

with $\sigma = 10^{-42}$ cm²

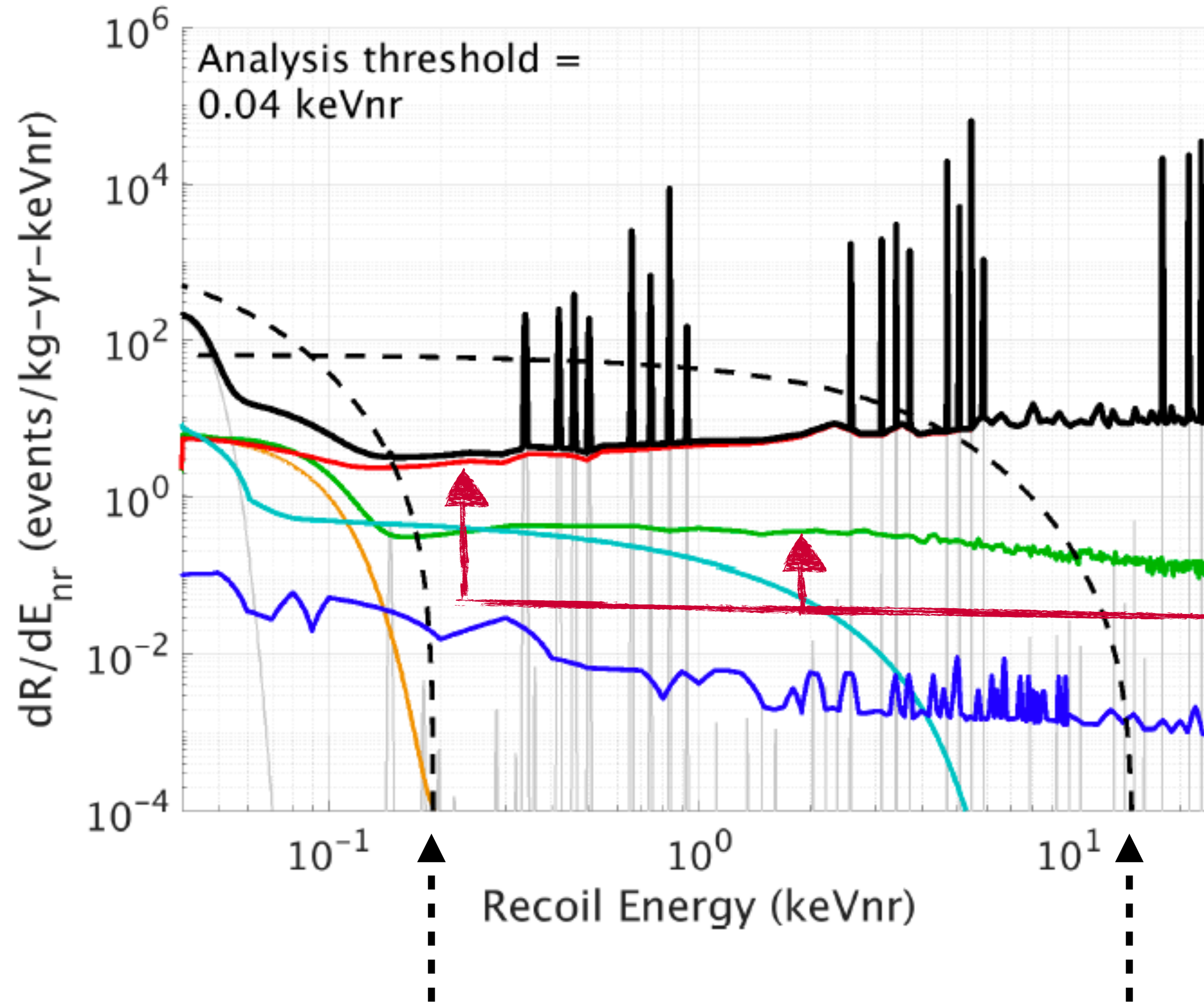


DM-nucleus scattering spectrum and backgrounds

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 Neutrons

Electron recoils!

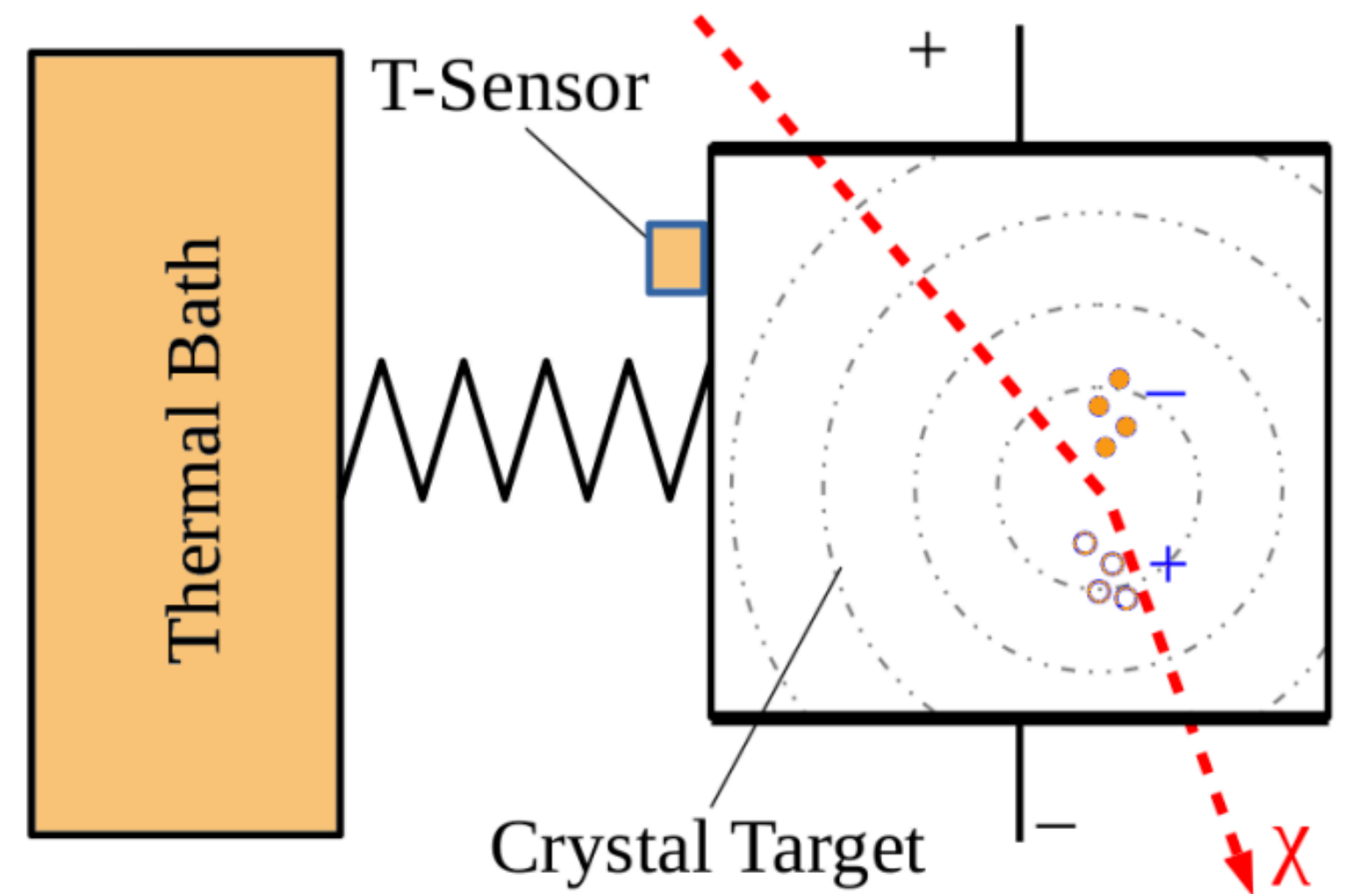
1 GeV/c² WIMP

10 GeV/c² WIMP

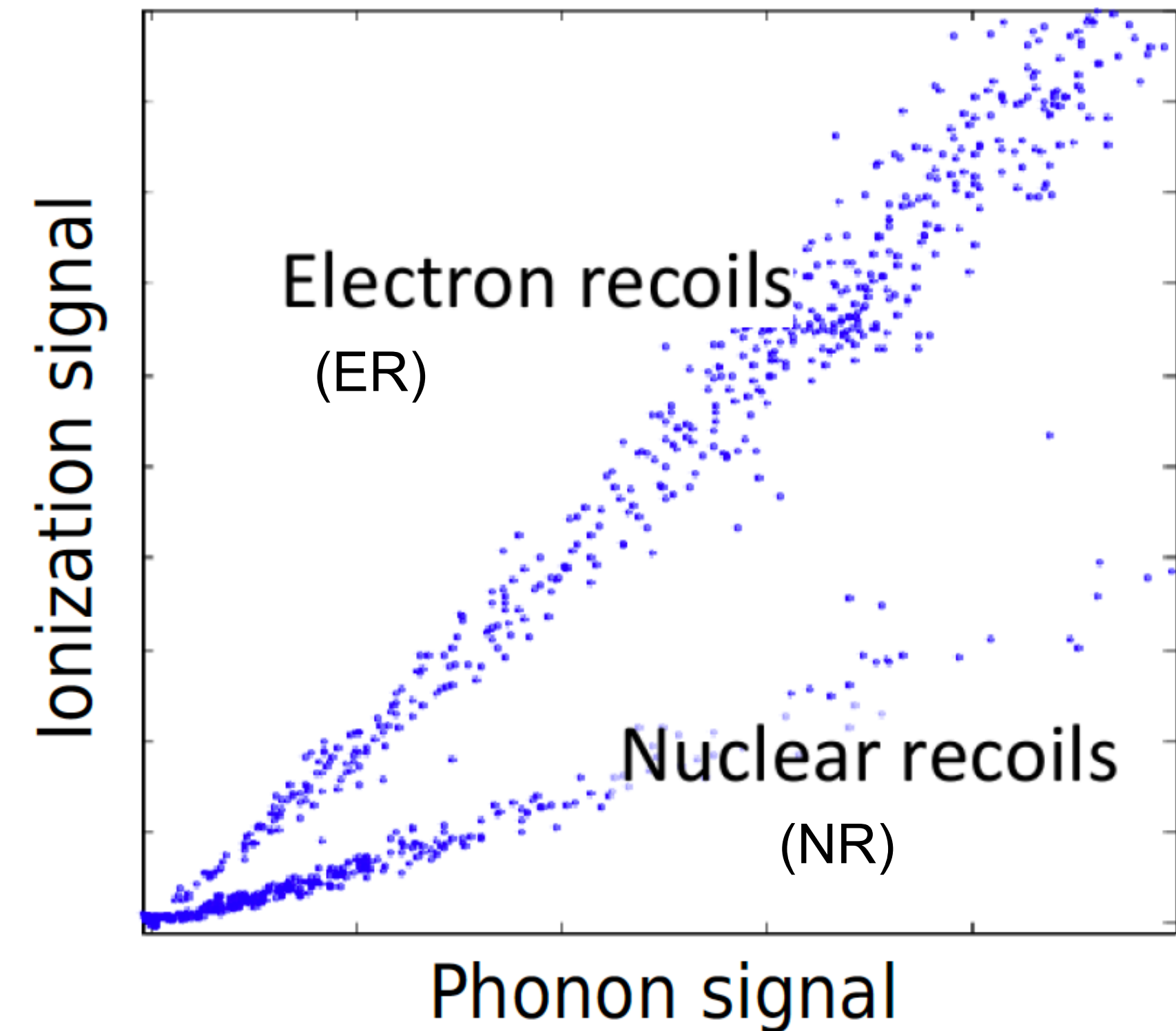
with $\sigma = 10^{-42} \text{ cm}^2$

Background discrimination using two signals

Example: measurement of PHONON/HEAT and IONIZATION signals



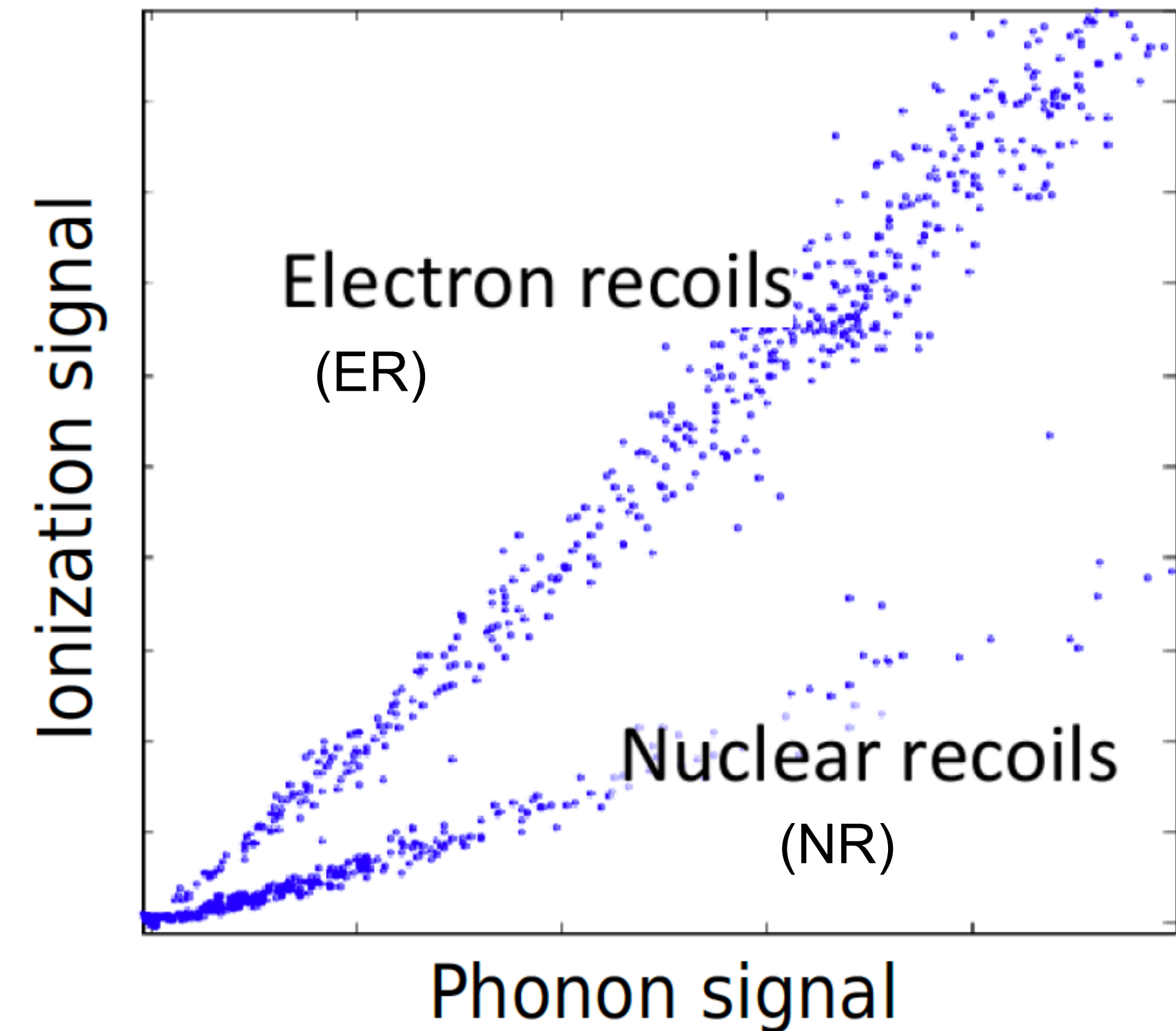
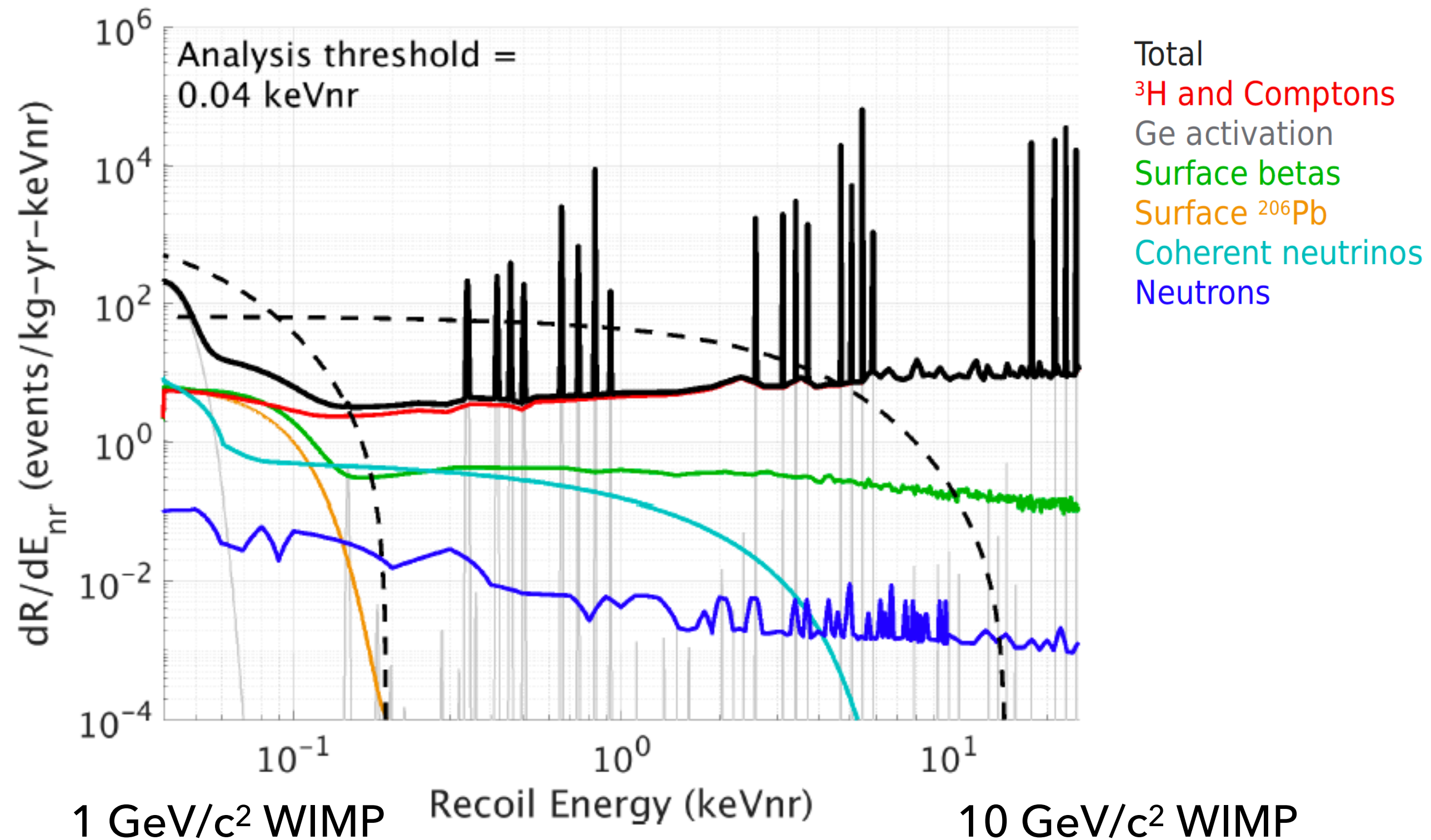
Cryogenic bolometers with charge readout



Two signals offer strong discrimination power between WIMP NR signals and backgrounds with ER signatures!

Background discrimination using two signals

Example: measurement of PHONON/HEAT and IONIZATION signals



Two signals offer strong discrimination power between WIMP NR signals and backgrounds with ER signatures!

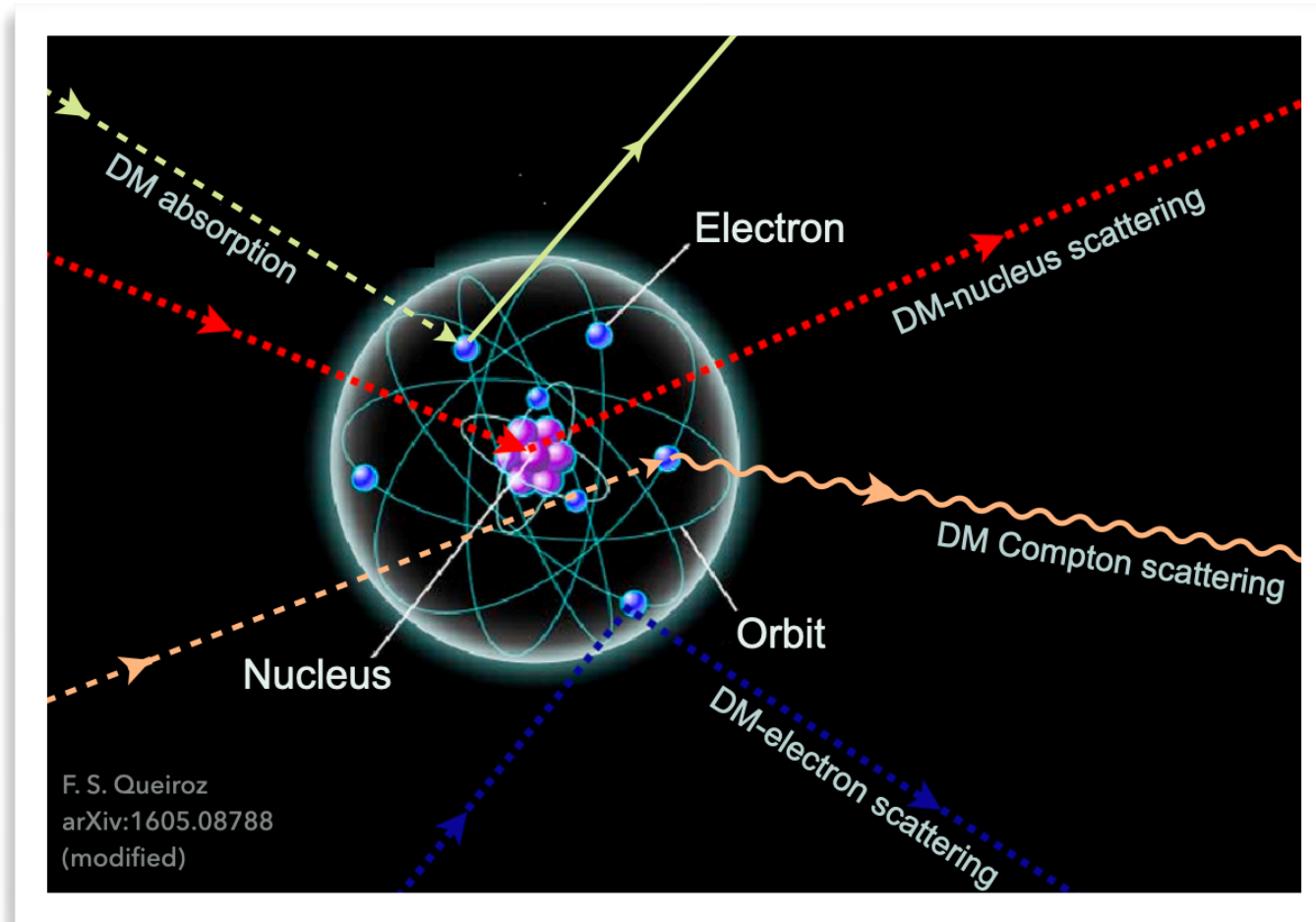


Summary



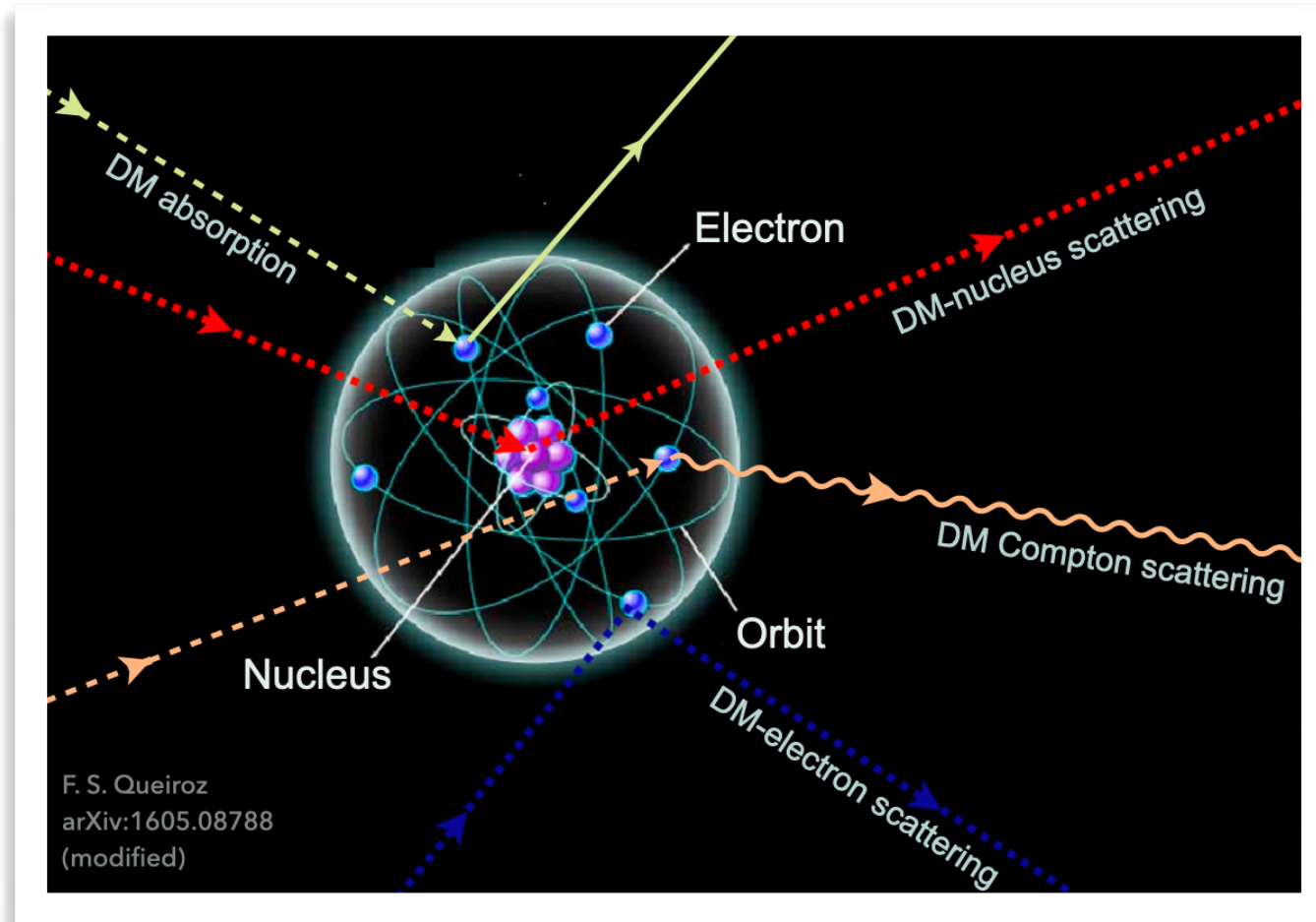
How to build a dark matter detector

1. pick your interaction

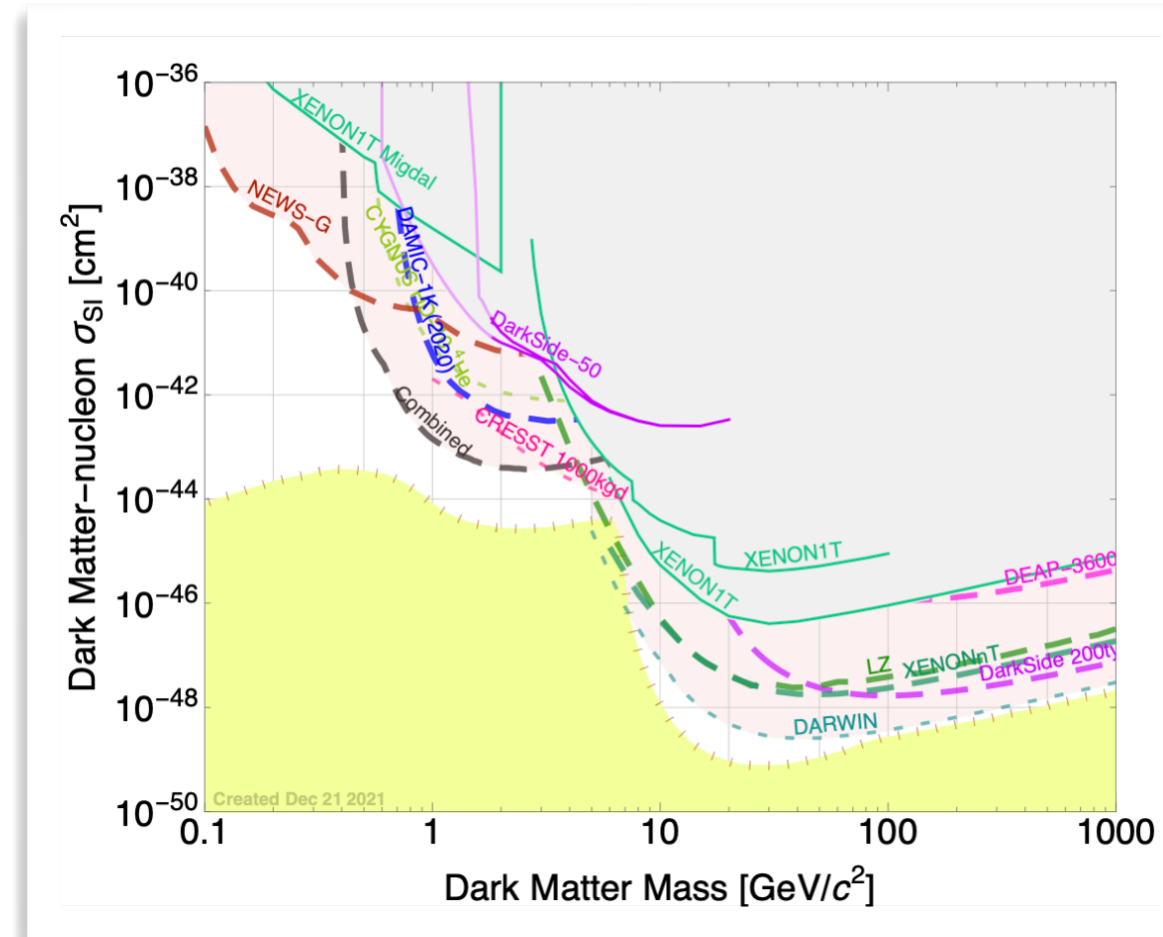


How to build a dark matter detector

1. pick your interaction



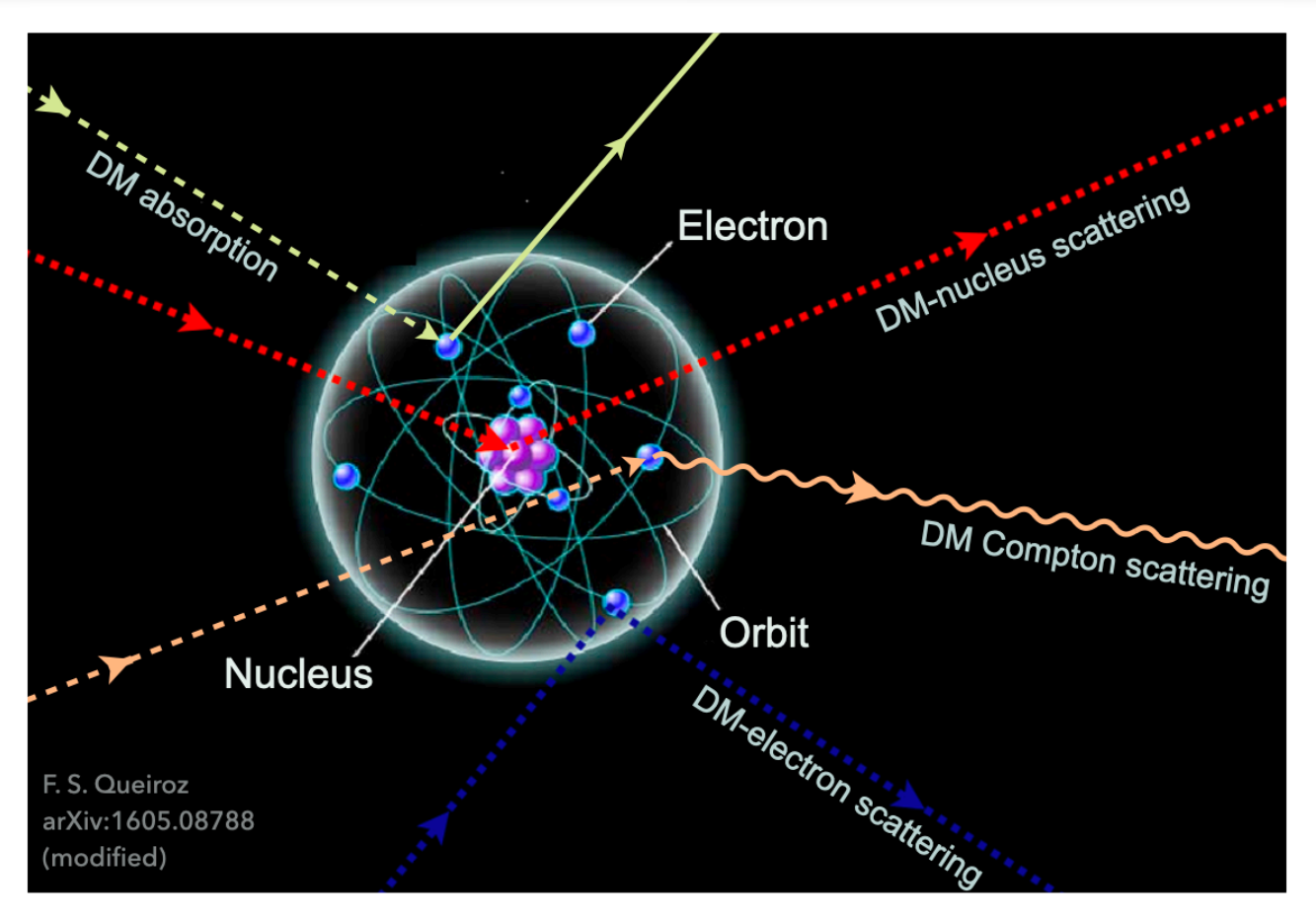
2. pick your parameter space



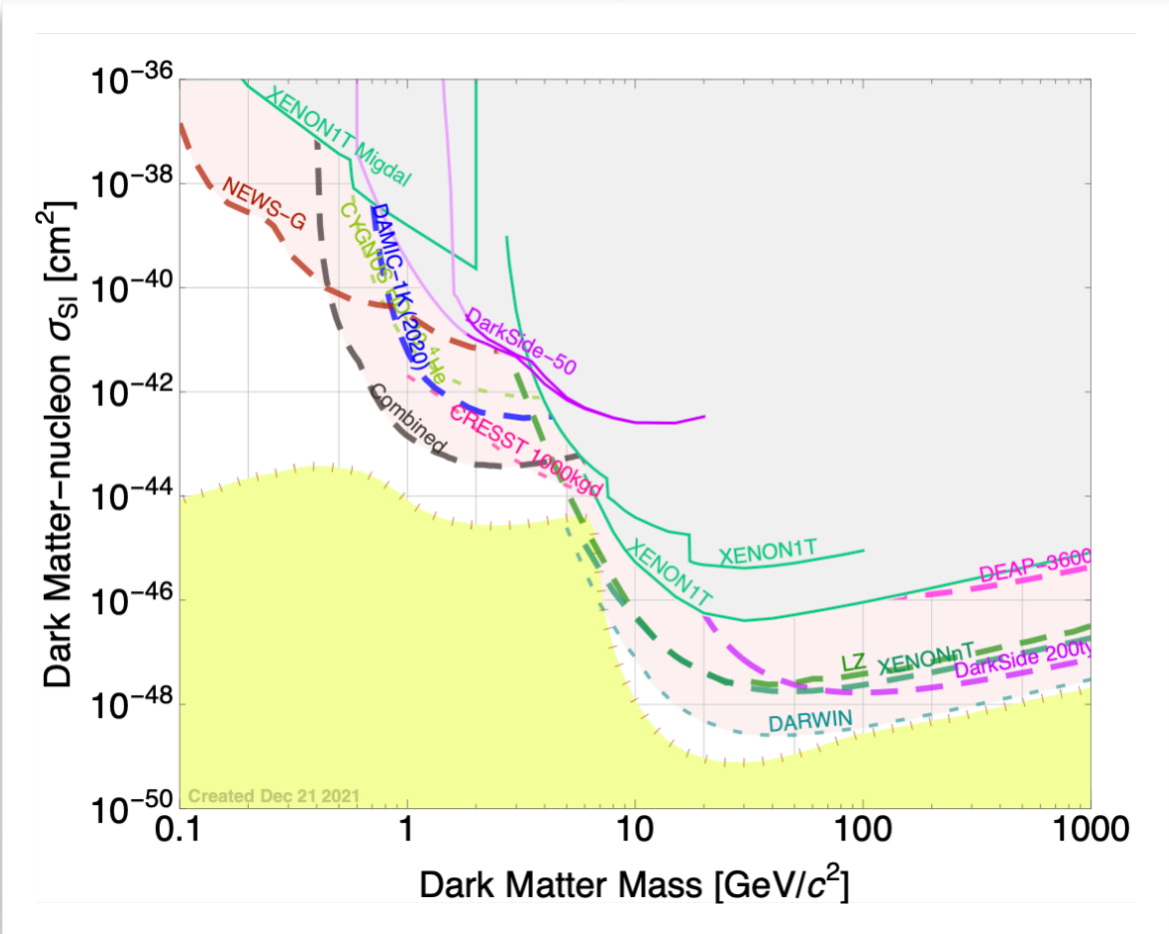


How to build a dark matter detector

1. pick your interaction



2. pick your parameter space

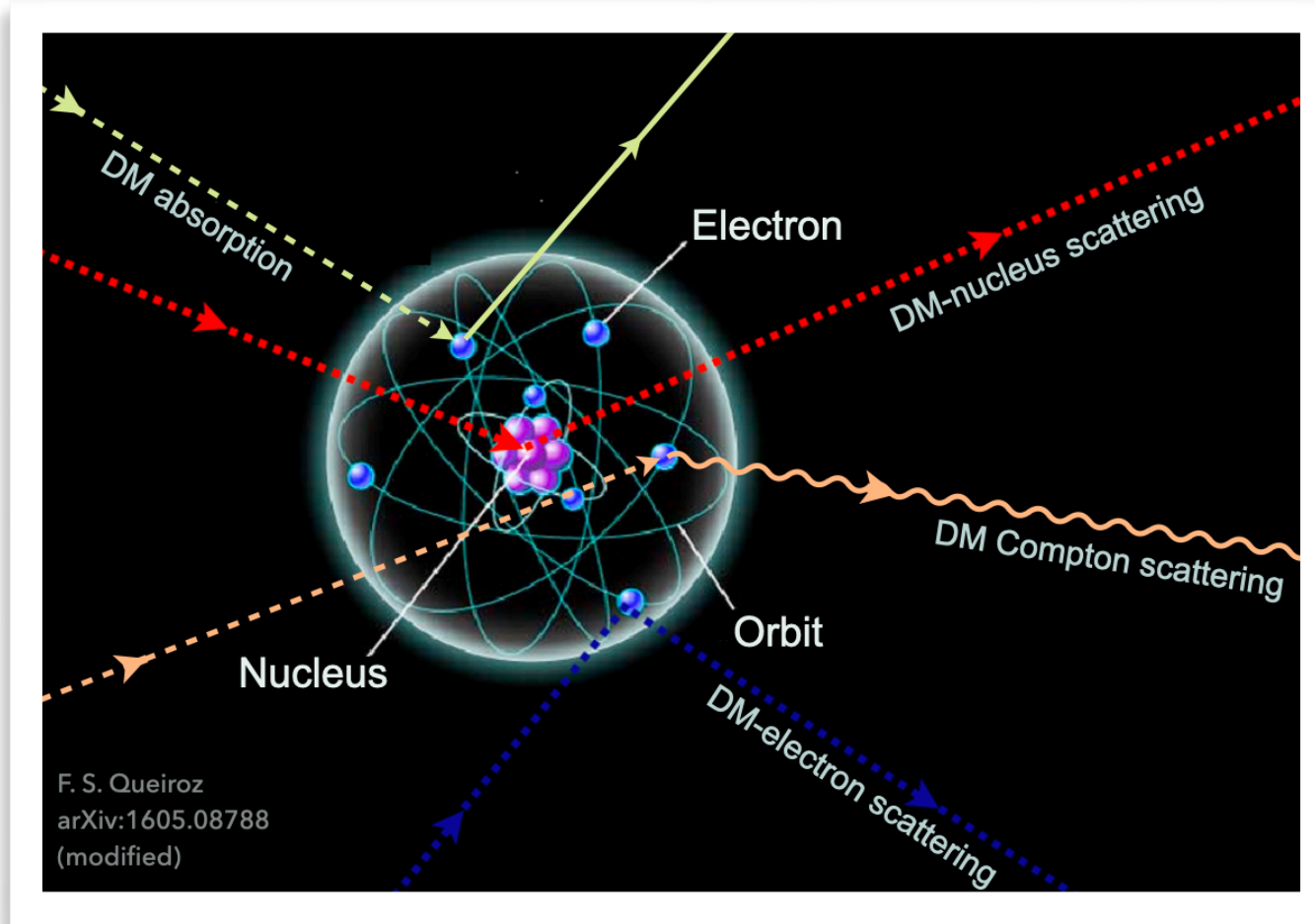


3. pick your target material

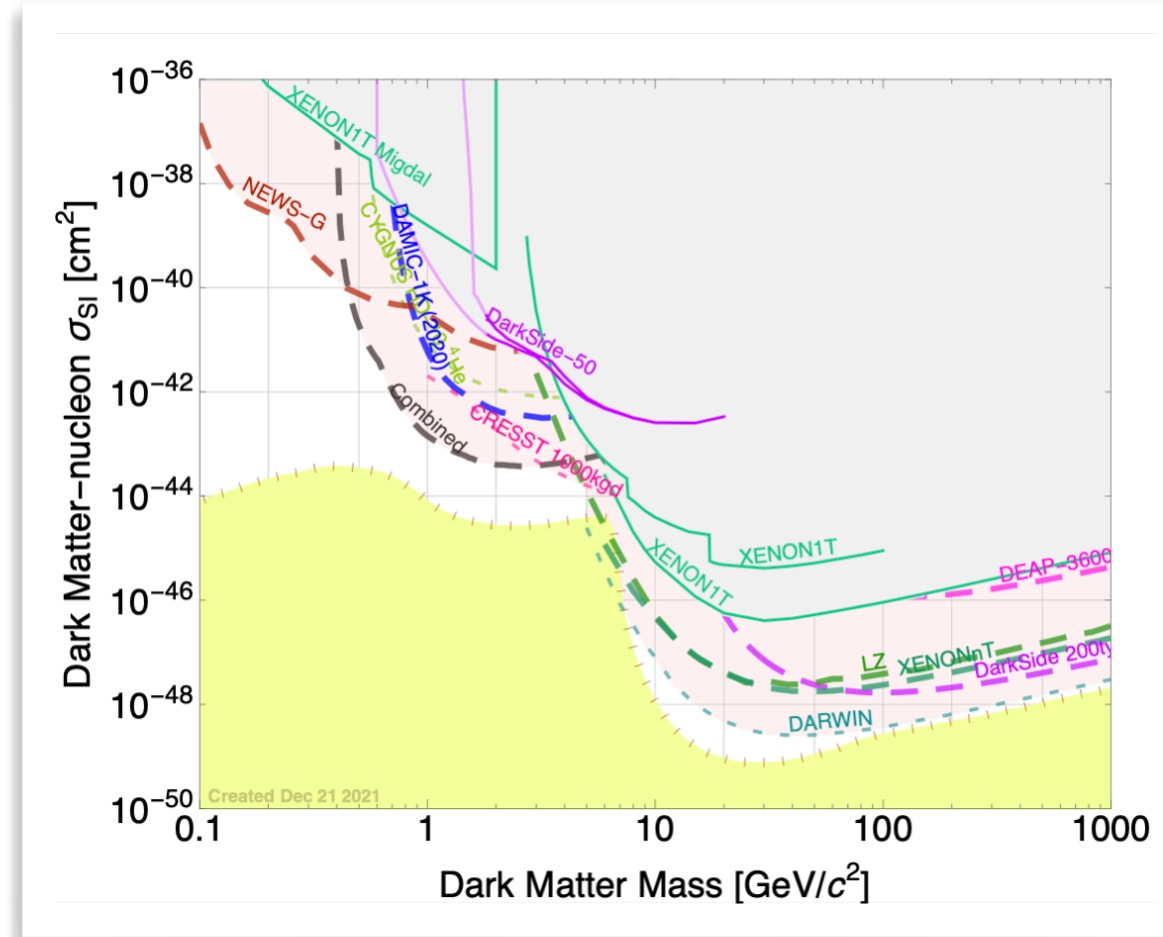
| Group | | | | | |
|-----------------|-----------------|-----------------|-----------------|----------------|---------------|
| 13 | 14 | 15 | 16 | 17 | 18 |
| | | | | | He Helium |
| B Boron | C Carbon | N Nitrogen | O Oxygen | F Fluorine | Ne Neon |
| Al Aluminium | Si Silicon | P Phosphorus | S Sulfur | Cl Chlorine | Ar Argon |
| Ga Gallium | Ge Germanium | As Arsenic | Se Selenium | Br Bromine | Kr Krypton |
| In Indium | Sn Tin | Sb Antimony | Te Tellurium | I Iodine | Xe Xenon |

How to build a dark matter detector

1. pick your interaction



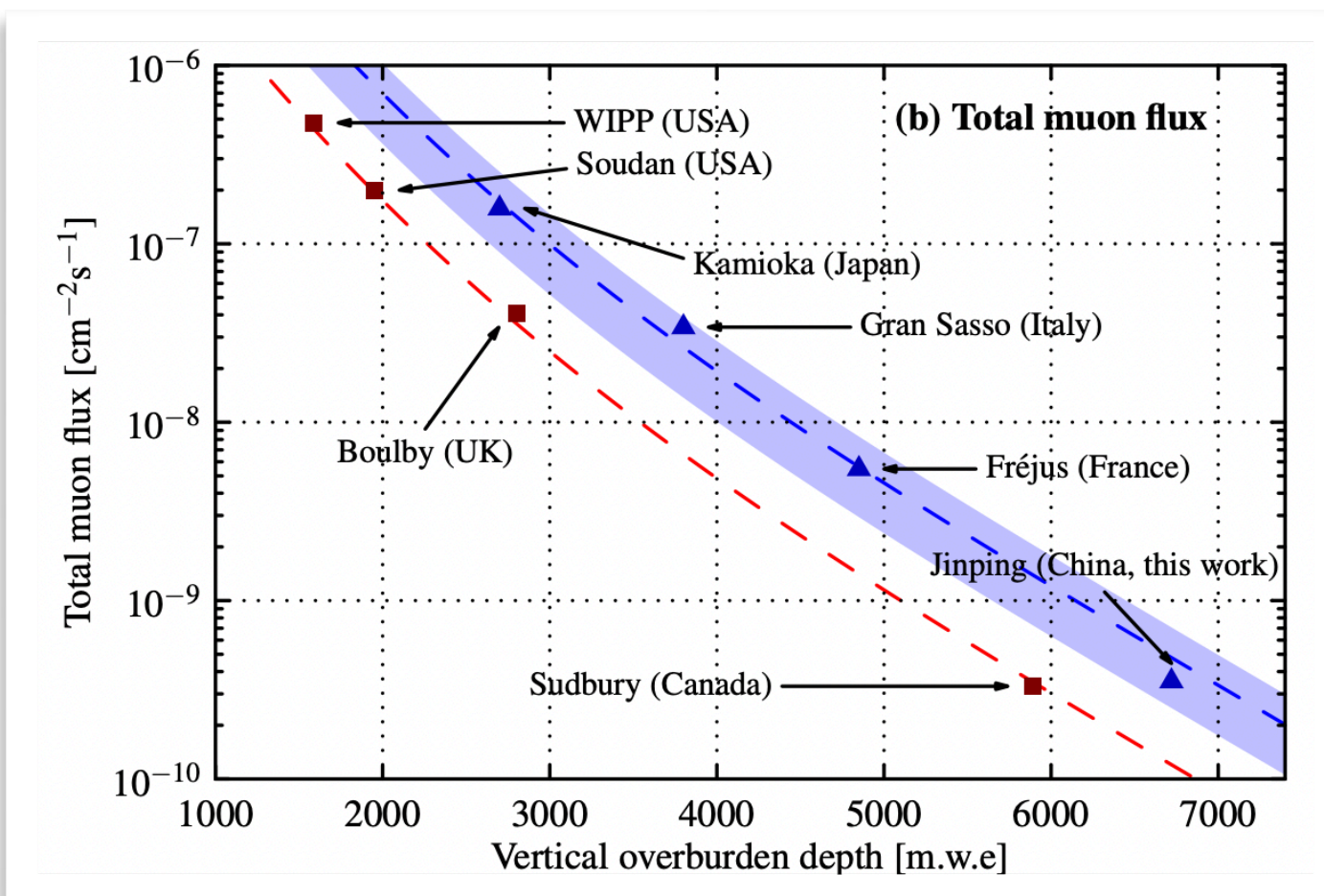
2. pick your parameter space



3. pick your target material

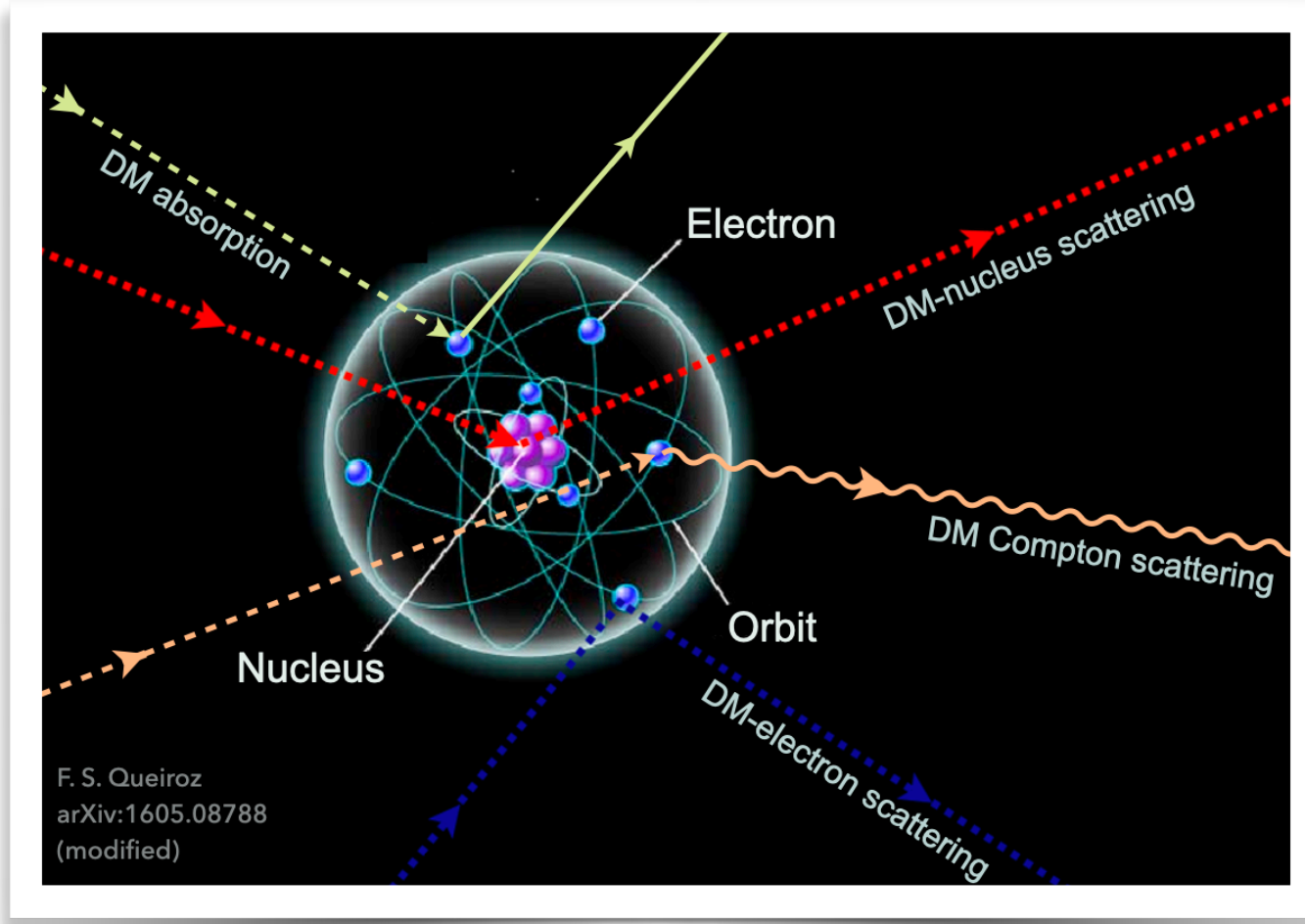
| Group | | | | | |
|-----------------|-----------------|-----------------|-----------------|----------------|---------------|
| 13 | 14 | 15 | 16 | 17 | 18 |
| | | | | | He Helium |
| B Boron | C Carbon | N Nitrogen | O Oxygen | F Fluorine | Ne Neon |
| Al Aluminium | Si Silicon | P Phosphorus | S Sulfur | Cl Chlorine | Ar Argon |
| Ga Gallium | Ge Germanium | As Arsenic | Se Selenium | Br Bromine | Kr Krypton |
| In Indium | Sn Tin | Sb Antimony | Te Tellurium | I Iodine | Xe Xenon |

4. pick your underground lab

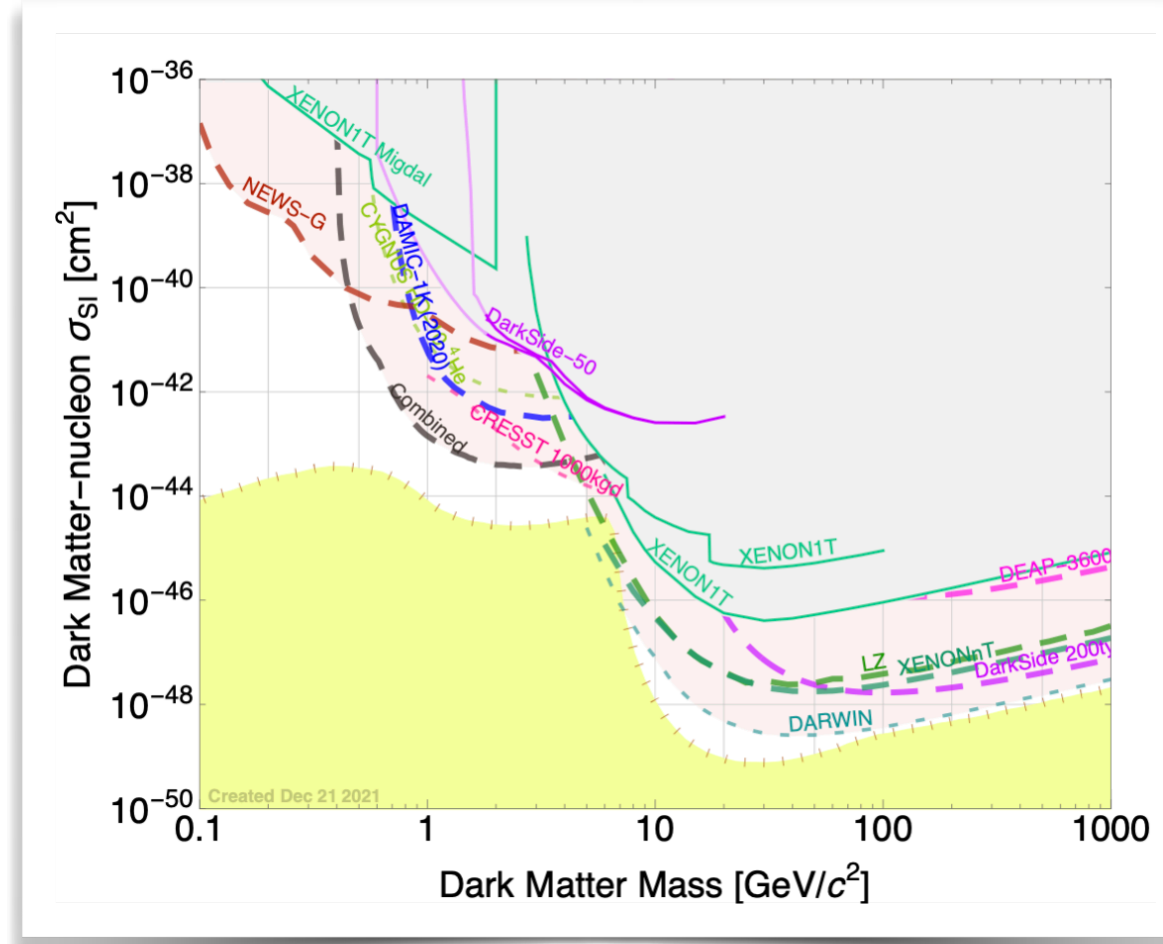


How to build a dark matter detector

1. pick your interaction



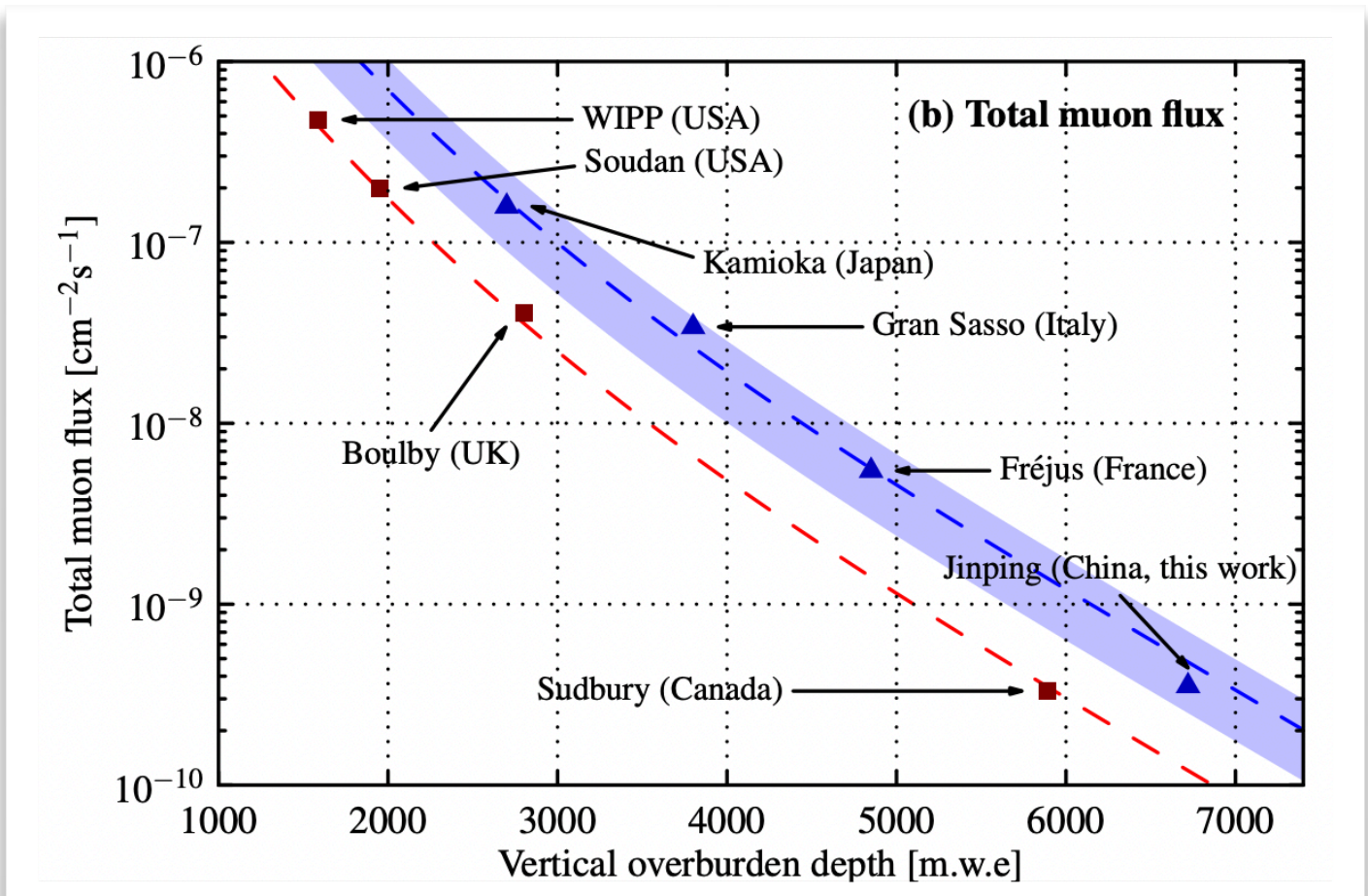
2. pick your parameter space



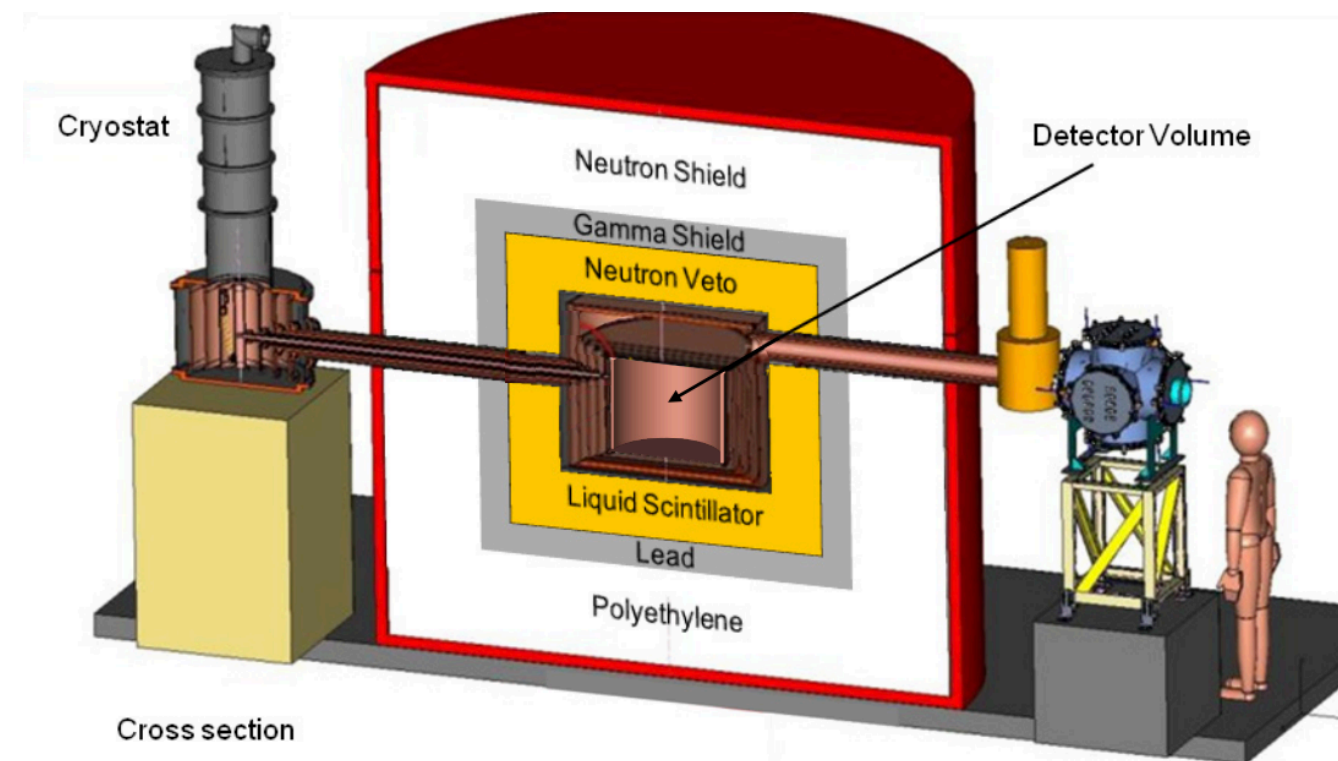
3. pick your target material

| Group | | | | | |
|-----------------|-----------------|-----------------|-----------------|----------------|---------------|
| 13 | 14 | 15 | 16 | 17 | 18 |
| | | | | | He Helium |
| B Boron | C Carbon | N Nitrogen | O Oxygen | F Fluorine | Ne Neon |
| Al Aluminium | Si Silicon | P Phosphorus | S Sulfur | Cl Chlorine | Ar Argon |
| Ga Gallium | Ge Germanium | As Arsenic | Se Selenium | Br Bromine | Kr Krypton |
| In Indium | Sn Tin | Sb Antimony | Te Tellurium | I Iodine | Xe Xenon |

4. pick your underground lab

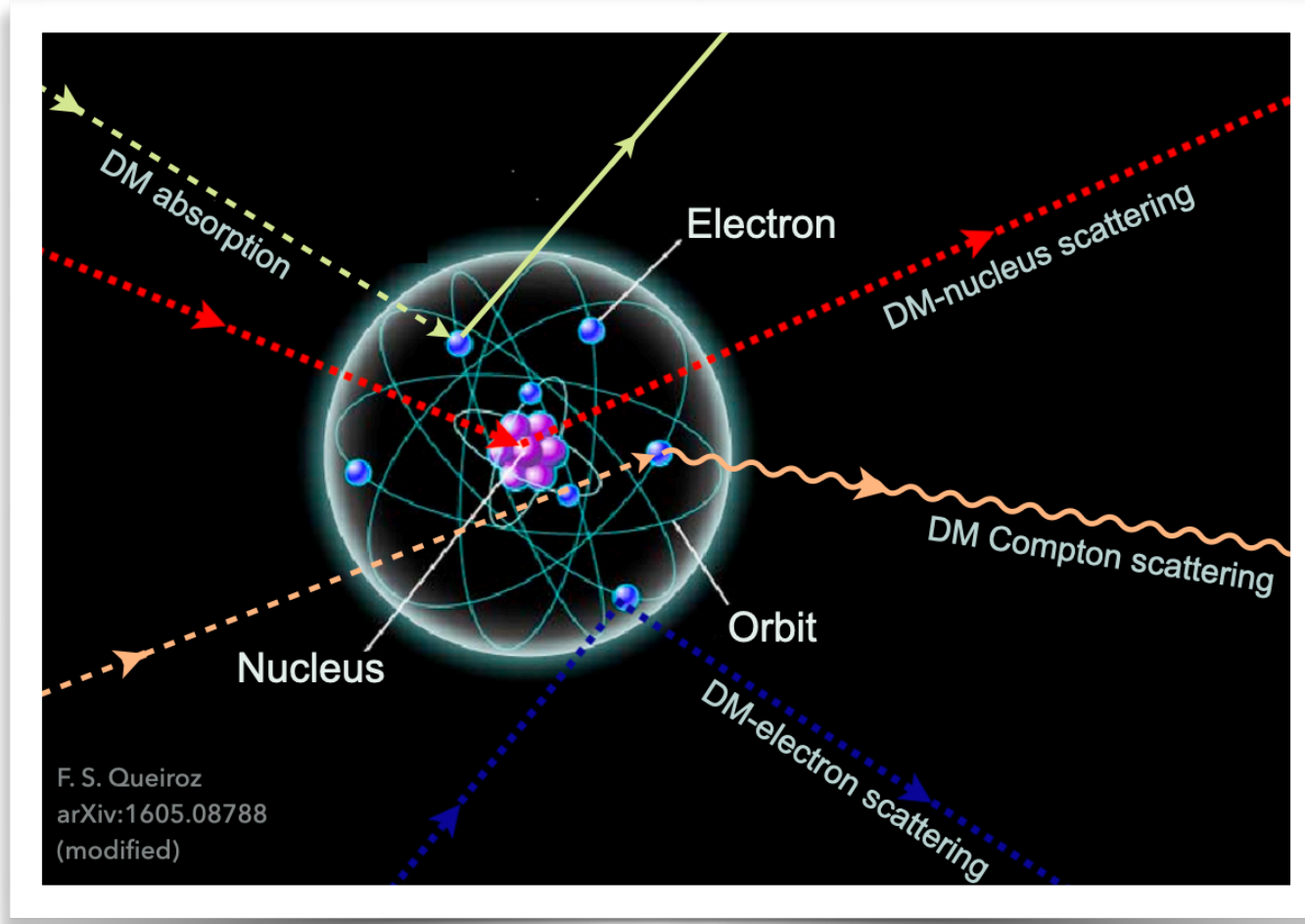


5. design your shielding

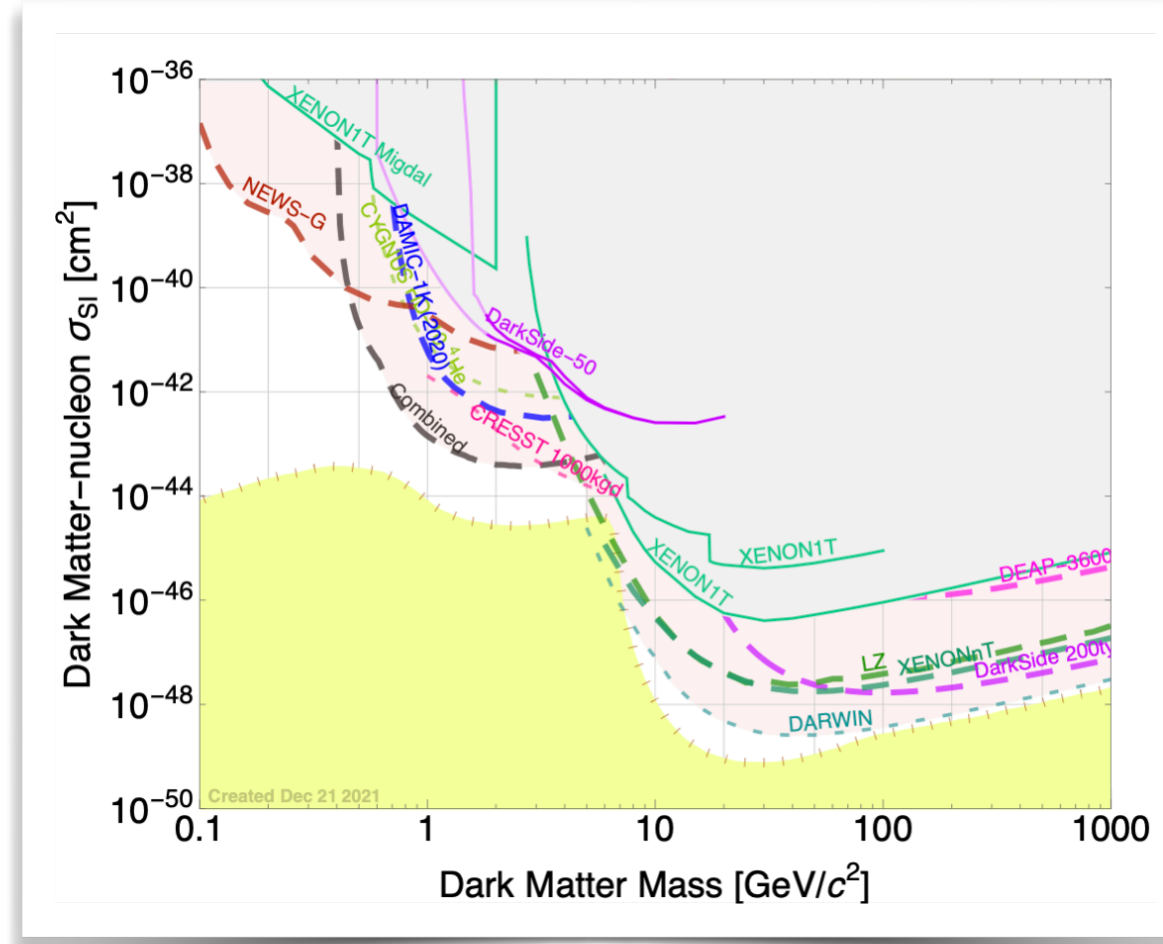


How to build a dark matter detector

1. pick your interaction



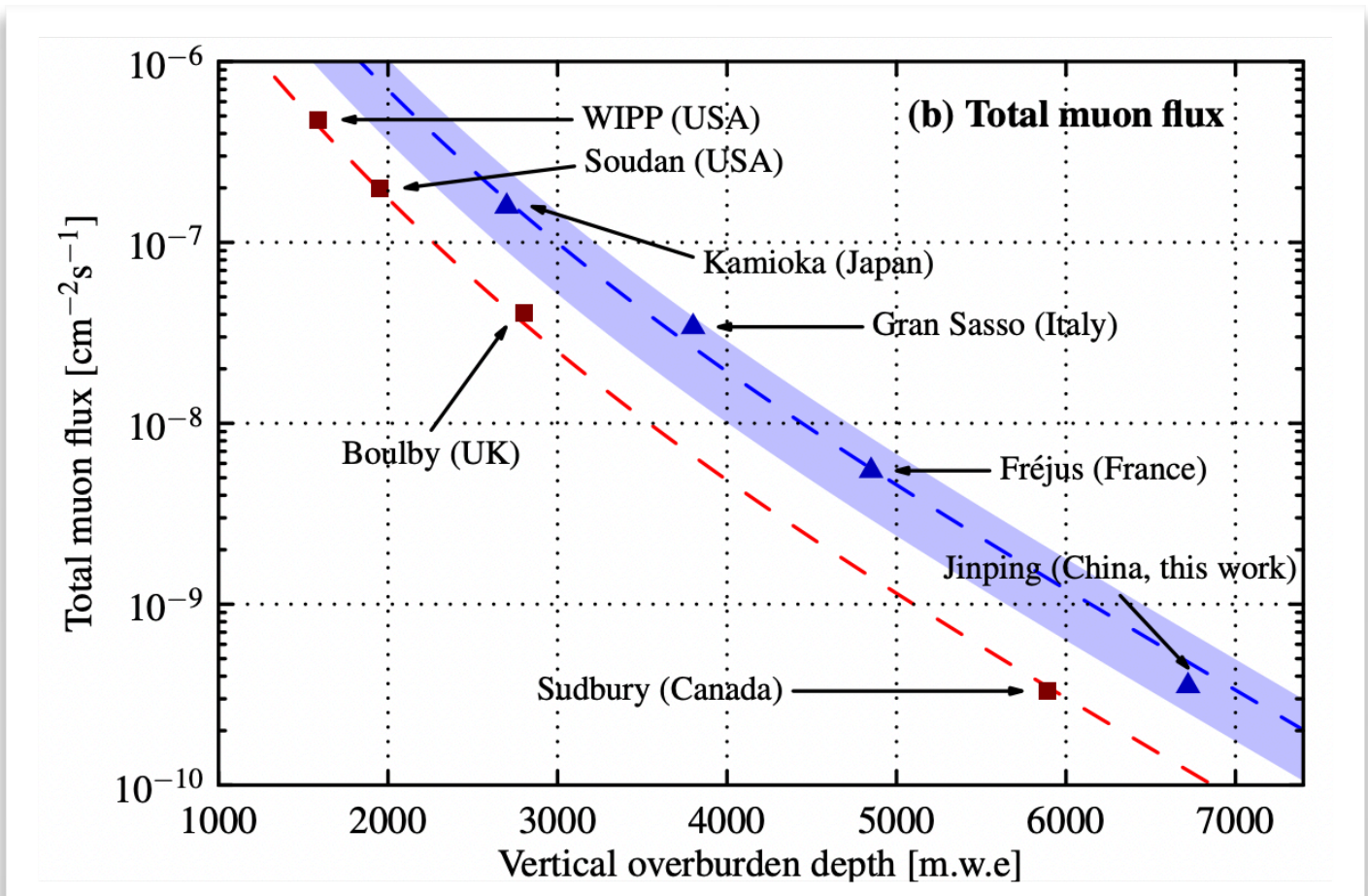
2. pick your parameter space



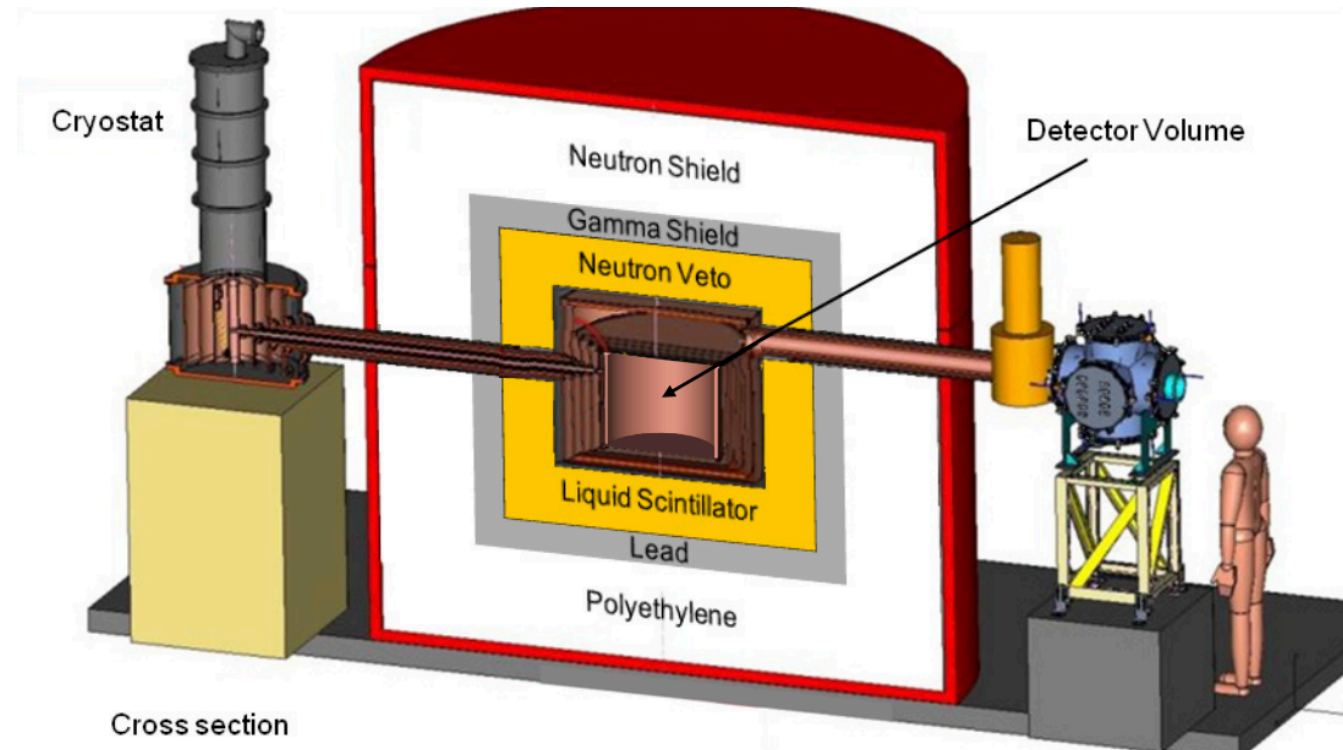
3. pick your target material

| Group | | | | | |
|-----------------|-----------------|-----------------|-----------------|----------------|---------------|
| 13 | 14 | 15 | 16 | 17 | 18 |
| | | | | | He Helium |
| B Boron | C Carbon | N Nitrogen | O Oxygen | F Fluorine | Ne Neon |
| Al Aluminium | Si Silicon | P Phosphorus | S Sulfur | Cl Chlorine | Ar Argon |
| Ga Gallium | Ge Germanium | As Arsenic | Se Selenium | Br Bromine | Kr Krypton |
| In Indium | Sn Tin | Sb Antimony | Te Tellurium | I Iodine | Xe Xenon |

4. pick your underground lab



5. design your shielding



6. select and characterize your material



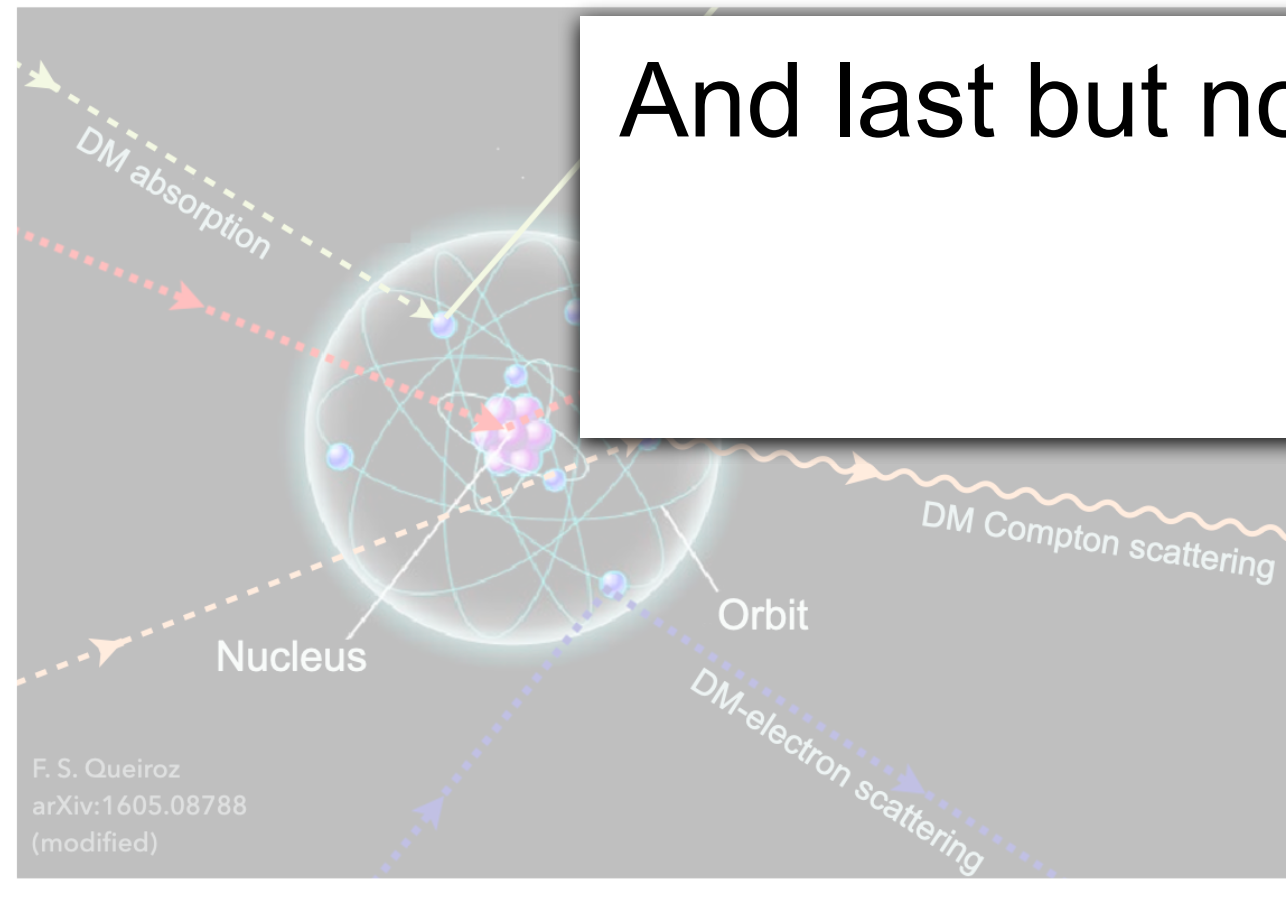


How to build a dark matter detector

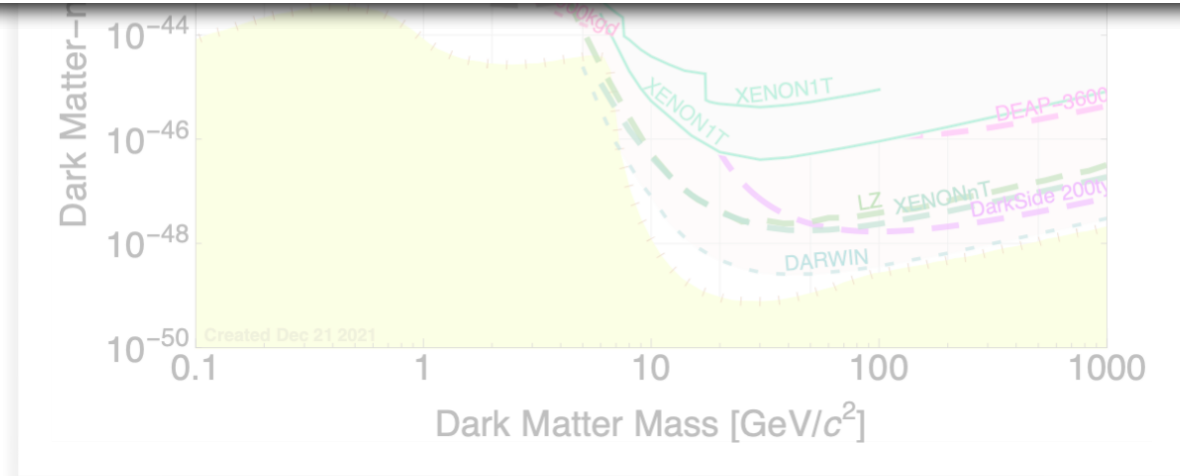
1. pick your interaction

2. pick your parameter space

3. pick your target material



And last but not least...



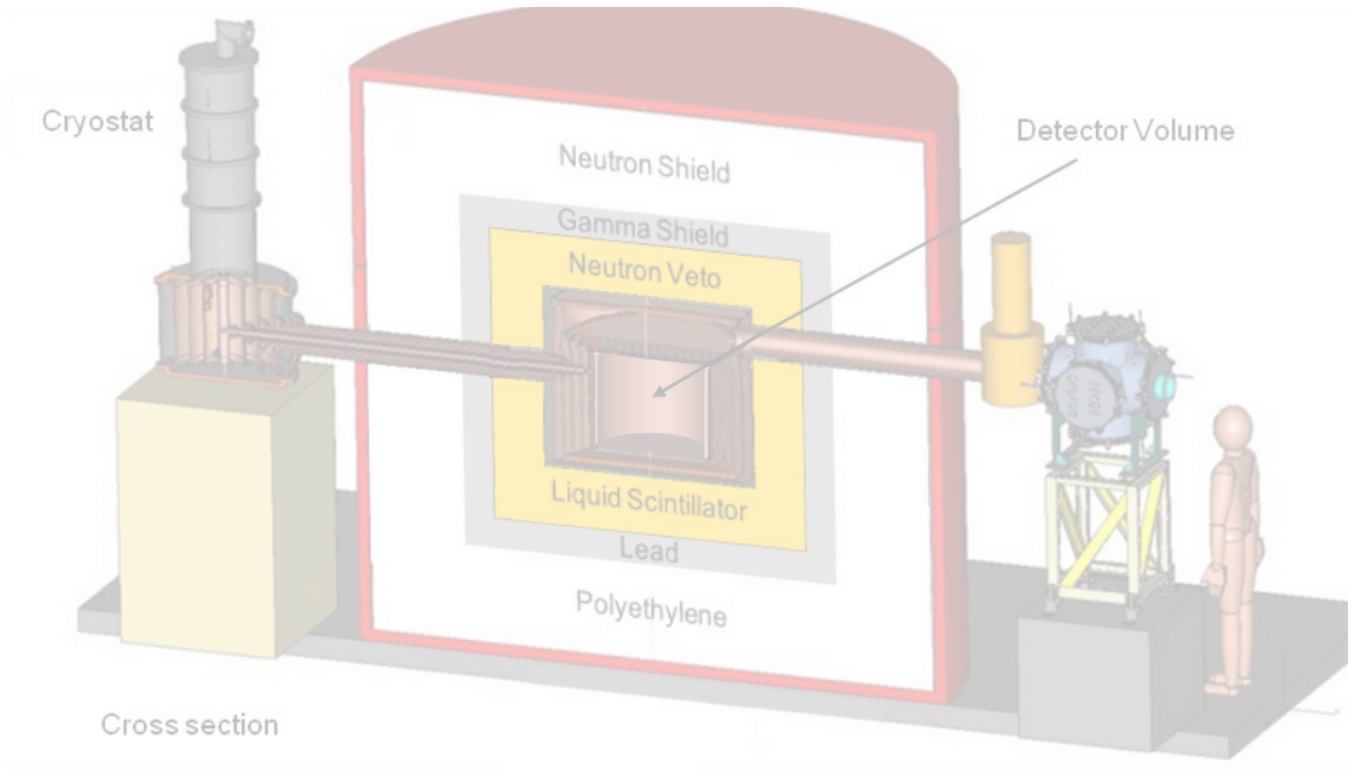
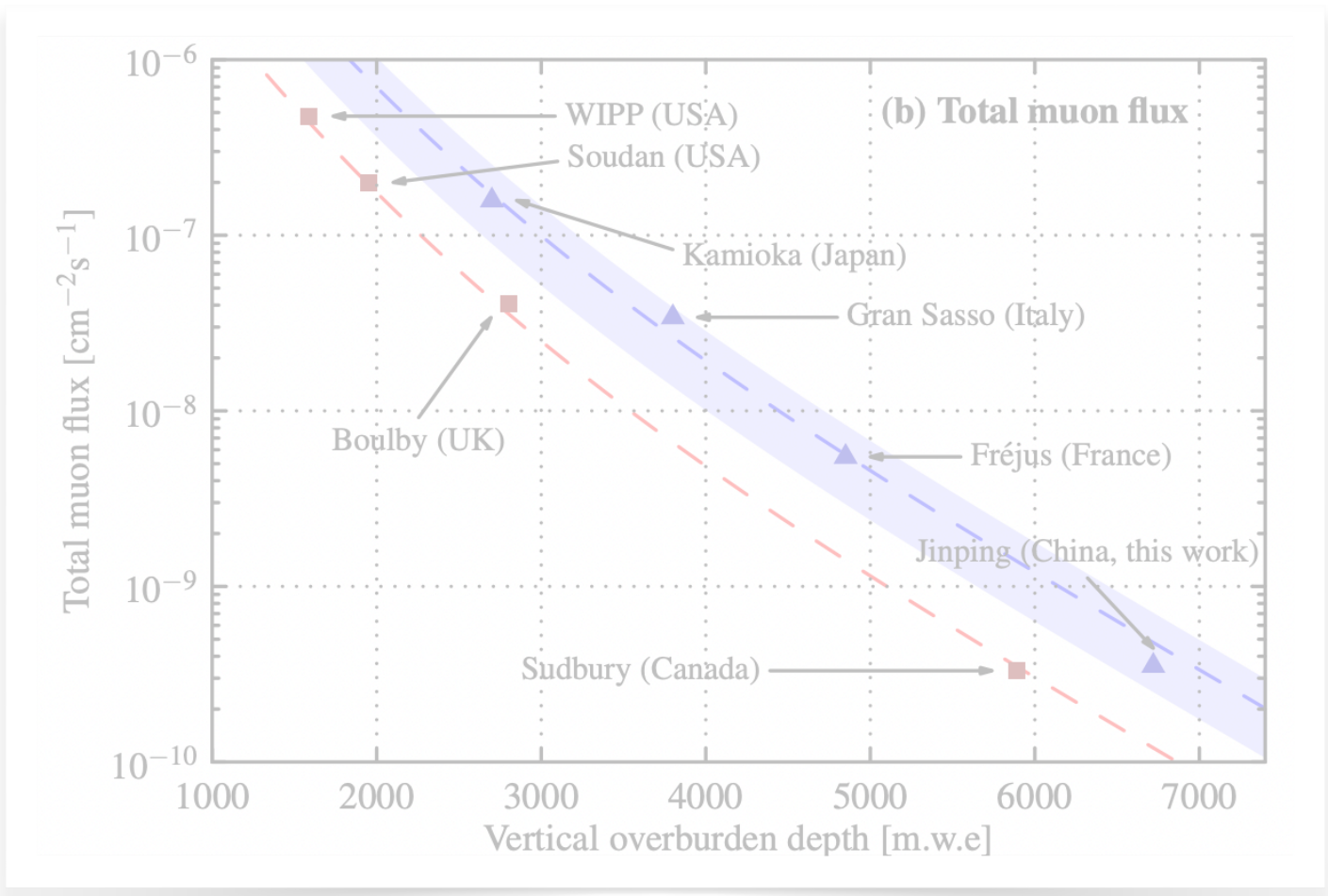
| | | | | | |
|-----------|-----------|------------|-----------|----------|---------|
| Al | Si | P | S | Cl | Ar |
| Aluminium | Silicon | Phosphorus | Sulfur | Chlorine | Argon |
| Ga | Ge | As | Se | Br | Kr |
| Gallium | Germanium | Arsenic | Selenium | Bromine | Krypton |
| In | Sn | Sb | Te | I | Xe |
| Indium | Tin | Antimony | Tellurium | Iodine | Xenon |

18
He
Helium
Ne
Neon

4. pick your underground lab

5. design your shielding

6. select and characterize your material





How to build a dark matter detector

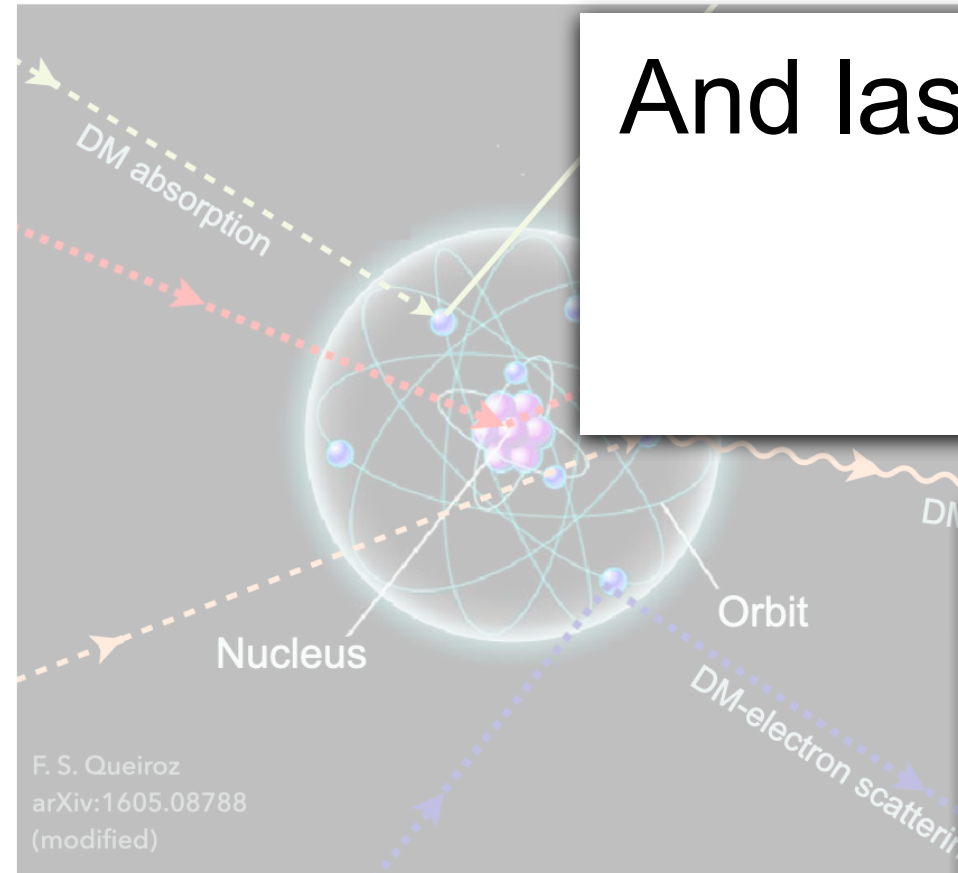
1. pick your interaction

2. pick your parameter space

3. pick your target material

And last but not least...

... pick your team - it's a team effort!



| | | | |
|----|----|---------|--|
| 18 | He | Helium | |
| | Ne | Neon | |
| | Ar | Argon | |
| | Kr | Krypton | |
| | Xe | Xenon | |

4. pick your underground

characterize your material

