

Concept: ***normalizing flow networks***  
 Conserve probability

# Invertible Networks to map probability distributions

S. Radev, U. Mertens, A. Voss, L. Arduzone, U. Köthe, arxiv 2003.06281

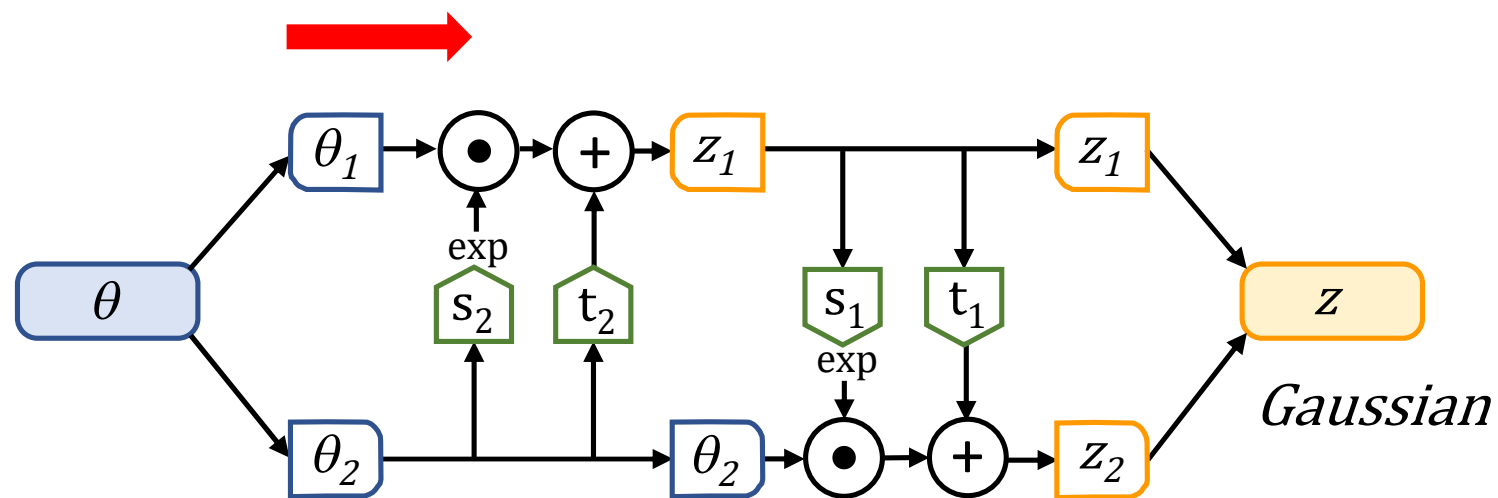
M. Bellagente, A. Butter, G. Kasieczka, T. Plehn, A. Rousselot, R. Winterhalder, L. Arduzone, U. Köthe, SciPost Phys. 9, 074 (2020)

T. Bister, M. Erdmann, U. Köthe, J. Schulte, The European Physical Journal C volume 82 (2022) 171, arXiv:2110.09493

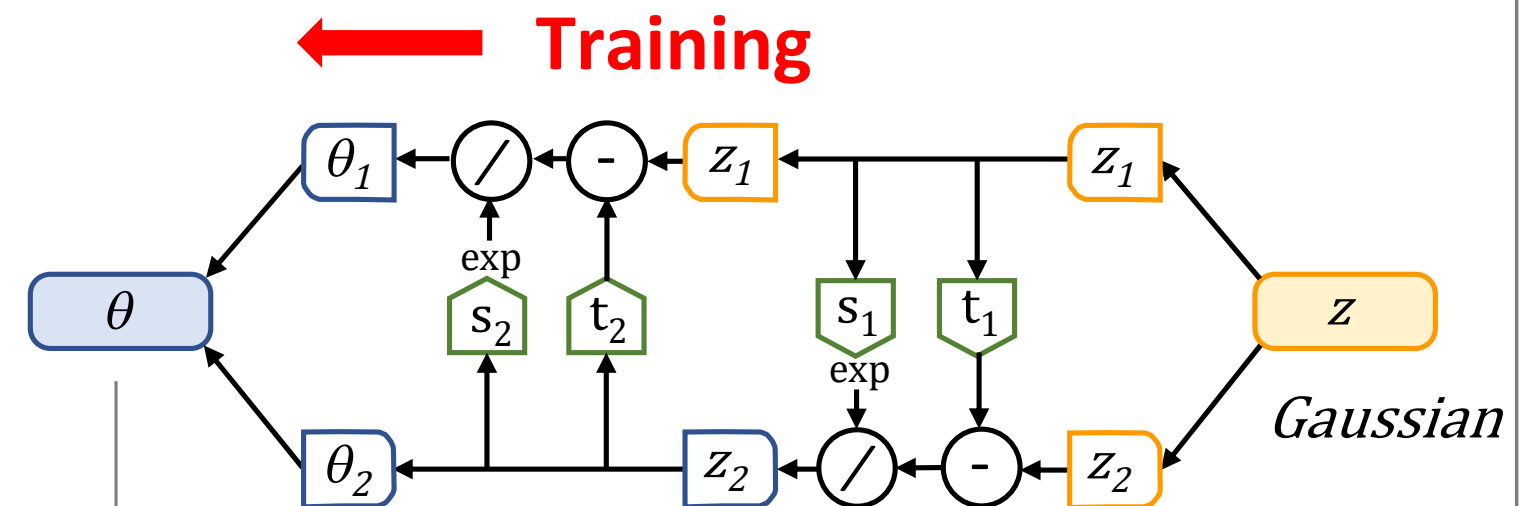
$$\theta = (\gamma, R_{\text{cut}}) @ \text{source}$$



$$J_{\text{inj}}(E) \propto E^{-\gamma} \cdot f_{\text{cut}}(E, Z \cdot R_{\text{cut}})$$



Probability conservation  $p_{\phi}(\theta) d\theta = p(z) dz$



$$\underset{\phi}{\operatorname{argmin}} \mathbb{E}_{p(\theta | \mathbf{x})} [\log p(\theta | \mathbf{x}) - \log p_{\phi}(\theta | \mathbf{x})]$$

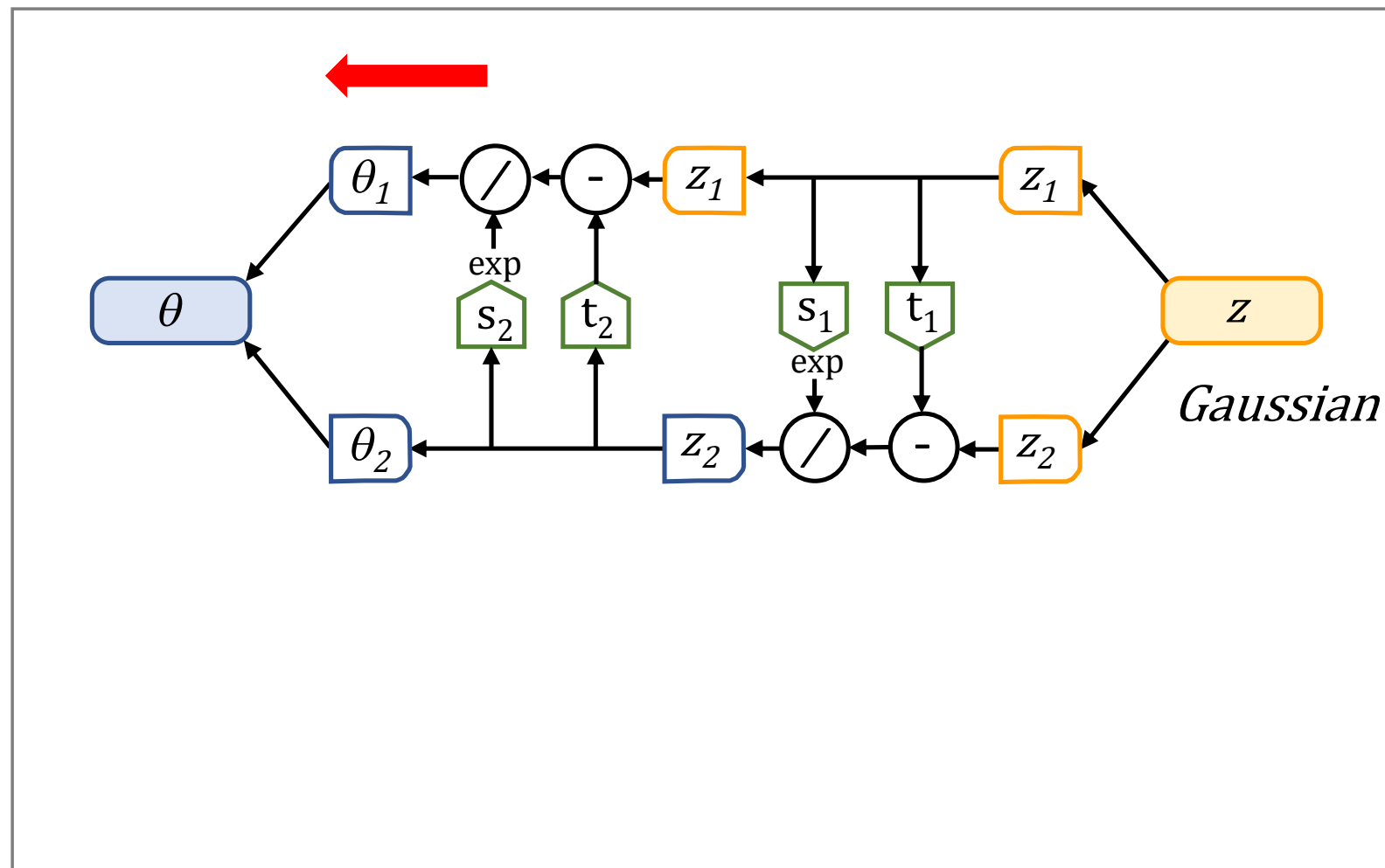
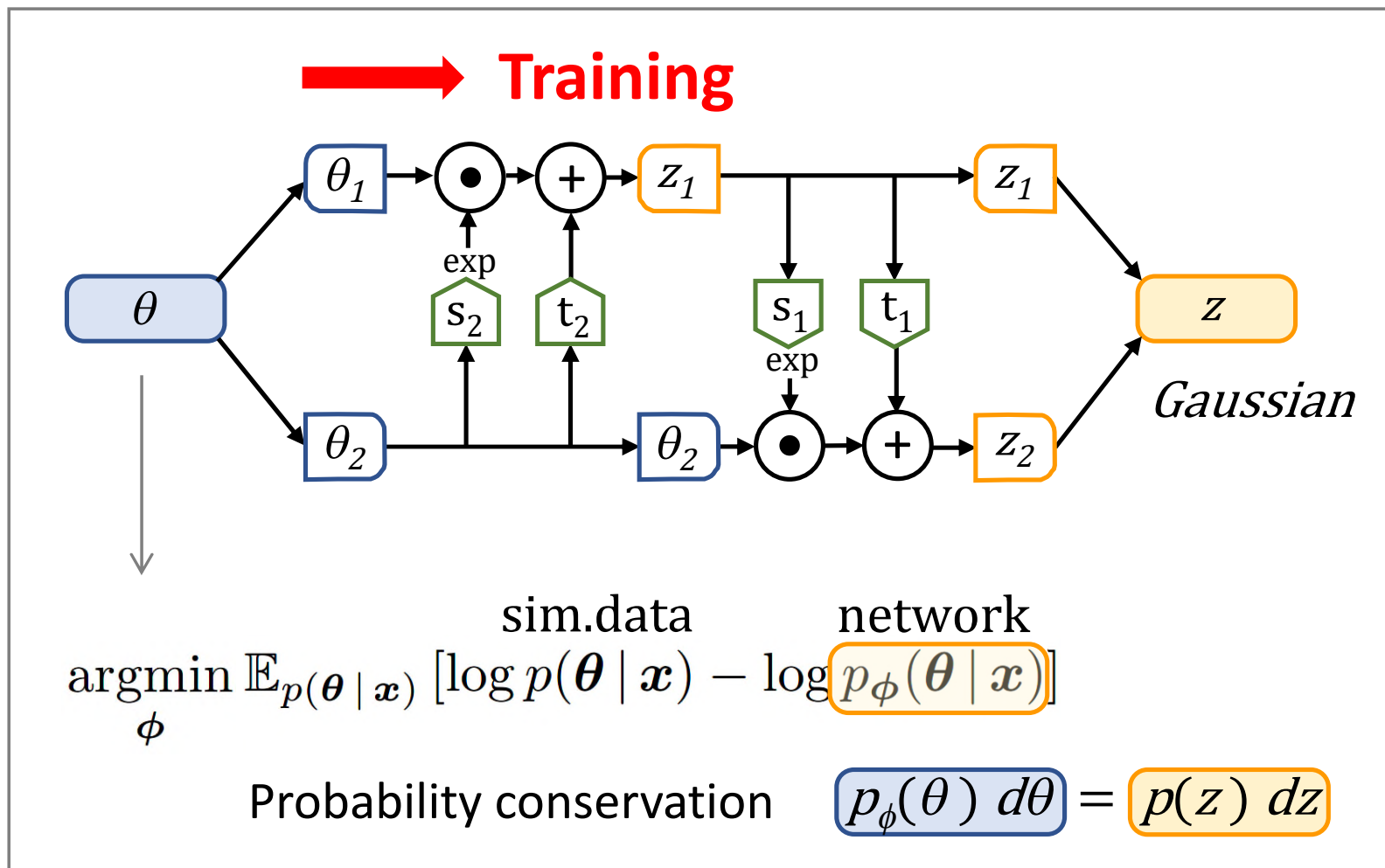
sim.data      network

# Invertible Networks to map probability distributions

$$\theta = (\gamma, R_{\text{cut}}) @ \text{source}$$



$$J_{\text{inj}}(E) \propto E^{-\gamma} \cdot f_{\text{cut}}(E, Z \cdot R_{\text{cut}})$$



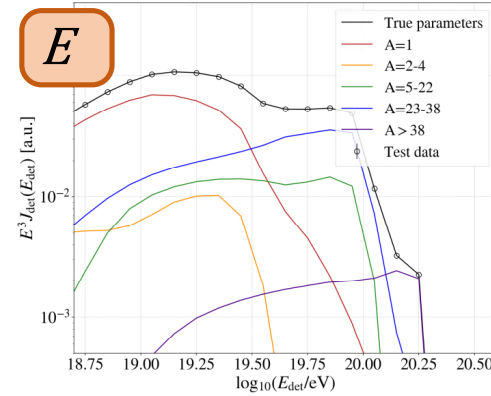
# Invertible Networks to unfold observed data

$$\theta = (\gamma, R_{\text{cut}}) @ \text{source}$$

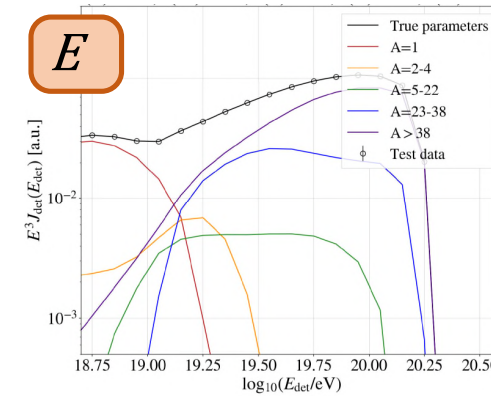


$$J_{\text{inj}}(E) \propto E^{-\gamma} \cdot f_{\text{cut}}(E, Z \cdot R_{\text{cut}})$$

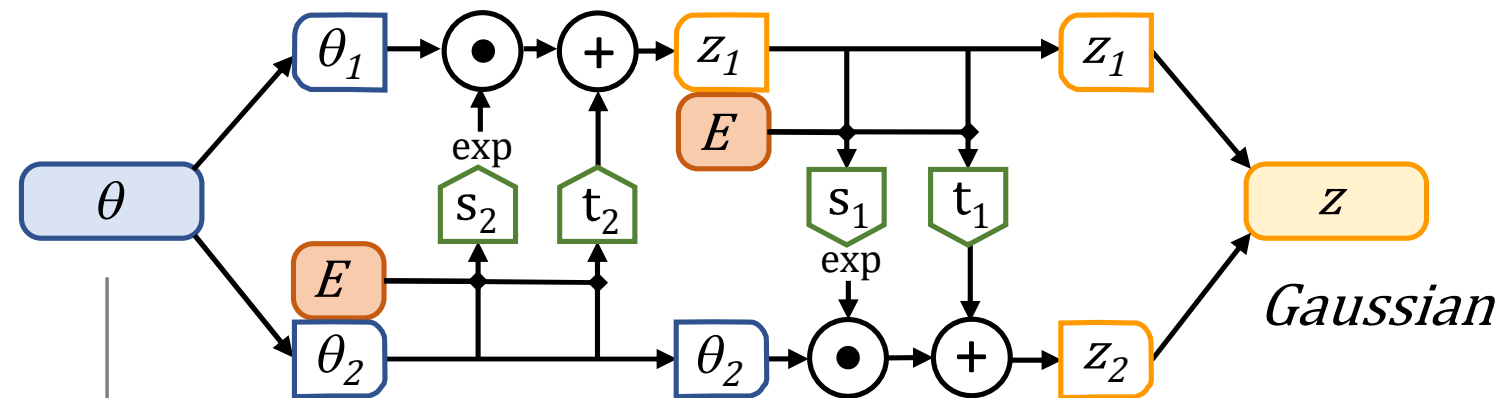
Energy  $E$  @ observation



'measurement'

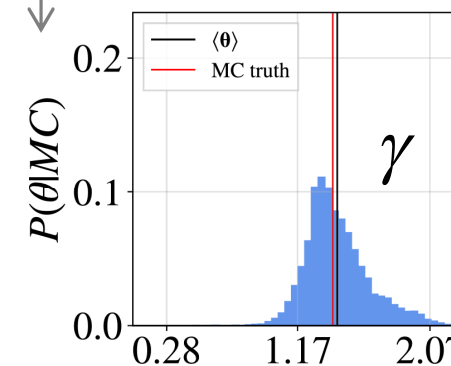
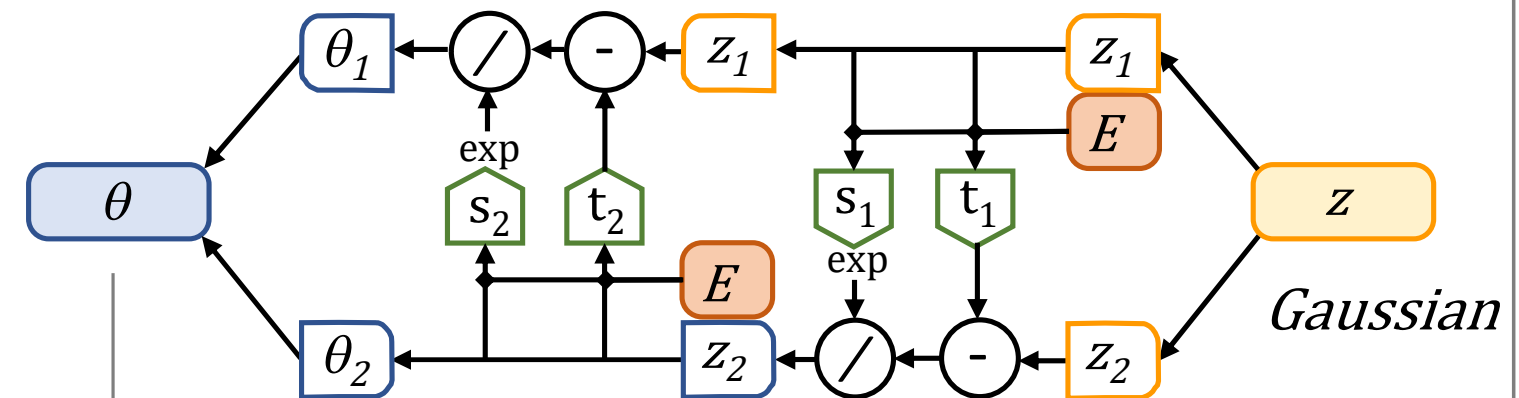


**Training**



$$\underset{\phi}{\operatorname{argmin}} \mathbb{E}_{p(\theta | \mathbf{x})} [\log p(\theta | \mathbf{x}) - \log p_{\phi}(\theta | \mathbf{x})]$$

**Evaluation**



Network learns to extract posterior distribution from given data