

Testing the Standard Model with Most Accurate Muon $g-2$ Measurement

René Reimann for the Muon $g-2$ collaboration

Oct 8th, 2024

BLV2024, Karlsruhe



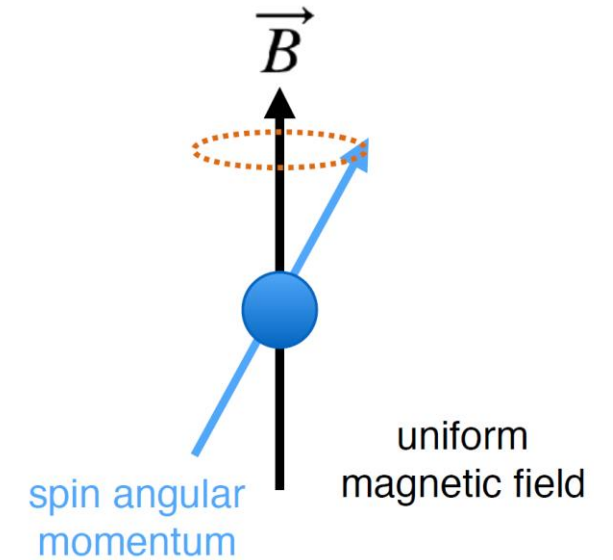
Outline

- **Why is Muon $g-2$ a good test of the SM?**
- How to measure the Muon $g-2$?
- Improvements in Run-2/3 results
- Outlook & Conclusions

Muon magnetic moment

$$\vec{\mu}_\mu = -g_\mu \frac{e}{2m_\mu} \vec{S}$$

magnetic moment proportionality constant spin



Potential energy

$$U = -\vec{\mu} \cdot \vec{B}$$

Torque → precession

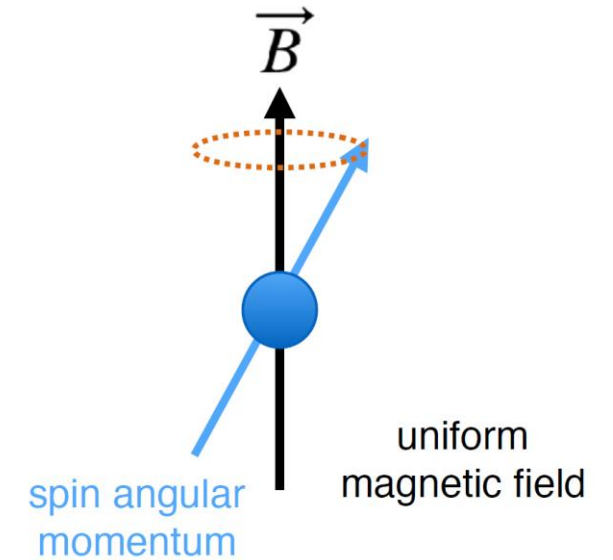
$$\vec{M} = \vec{\mu} \times \vec{B}$$



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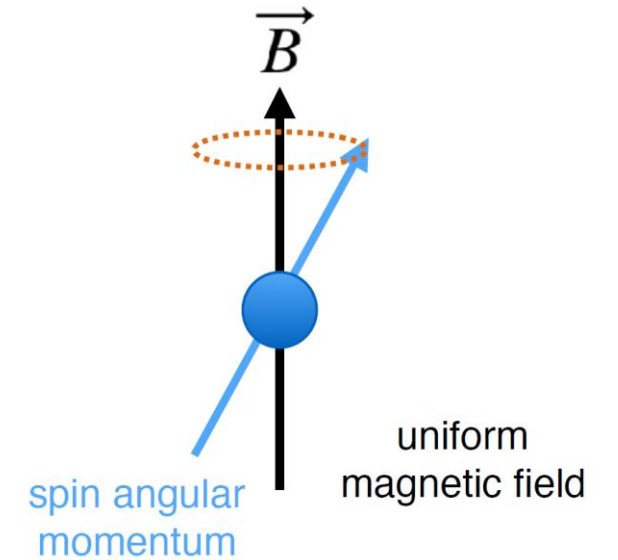
Dirac
(bare lepton)
 $g=2$

1928

Muon magnetic moment

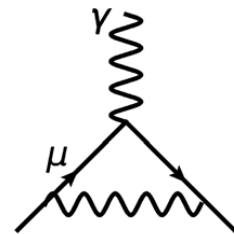
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Dirac
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 $g=2$

1928



Schwinger

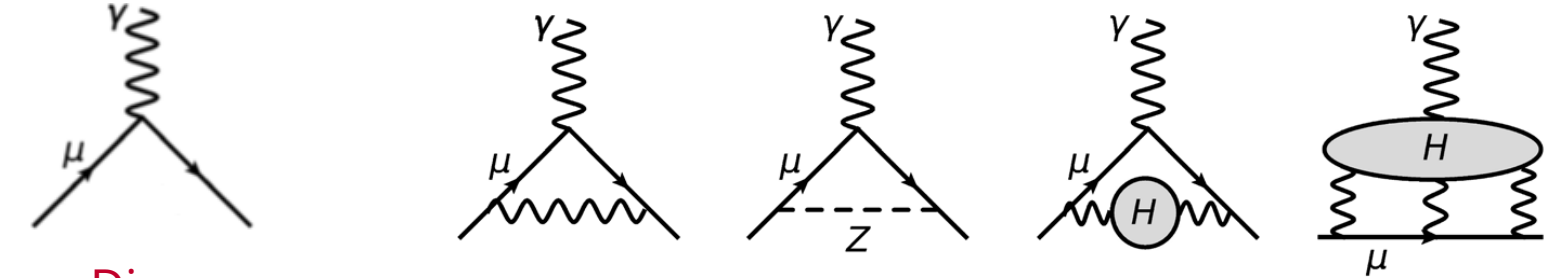
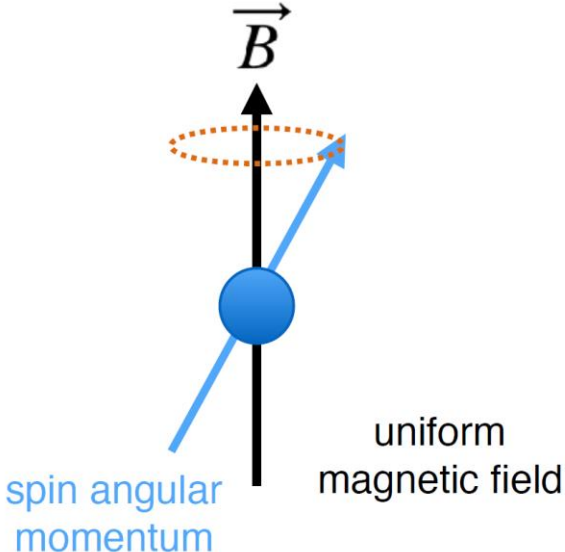
$\alpha/2\pi$

1947

Muon magnetic moment

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magnetic moment proportionality constant spin



Dirac
(bare lepton)
g=2

anomalous magnetic moment

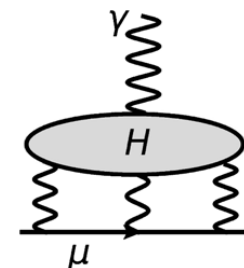
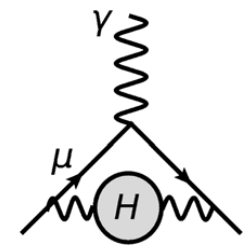
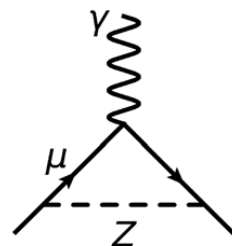
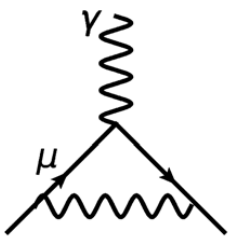
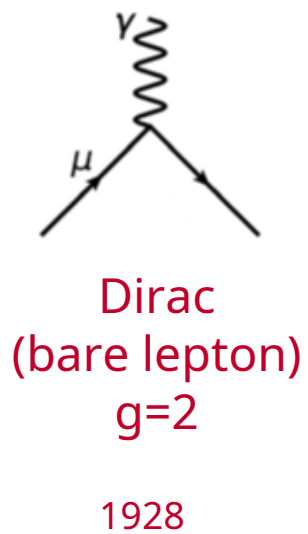
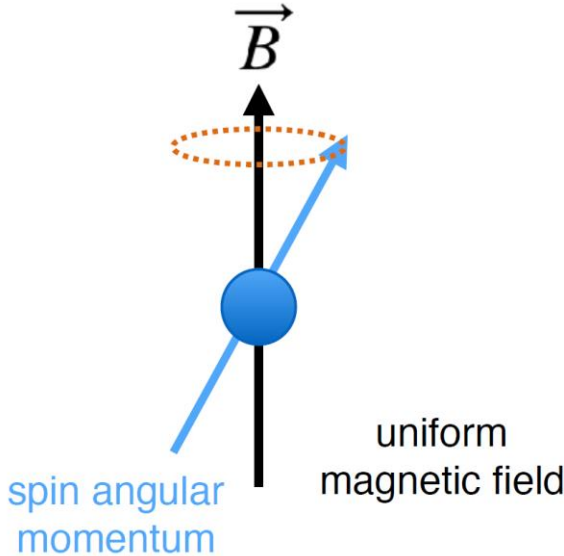
1928

today

Muon magnetic moment

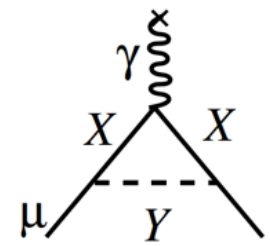
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magnetic moment proportionality constant spin



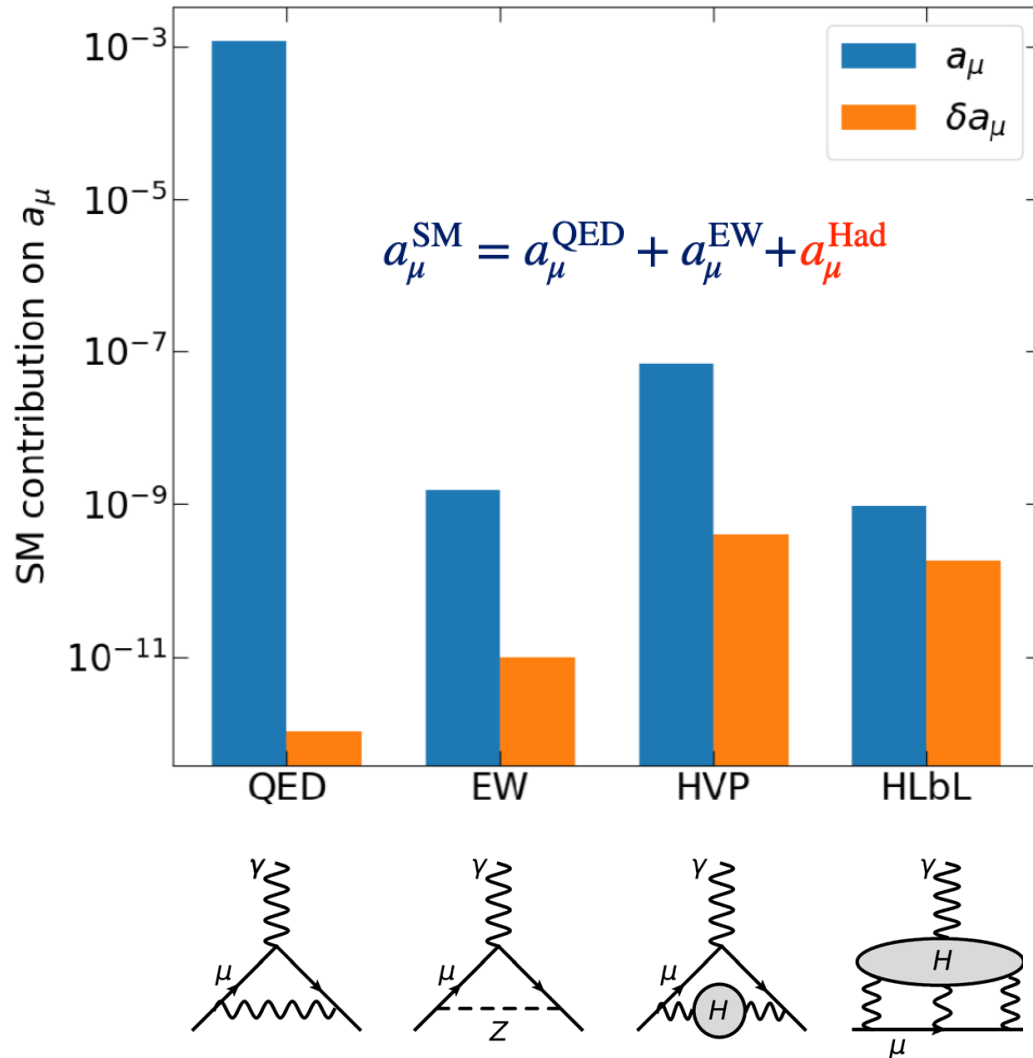
anomalous magnetic moment

today



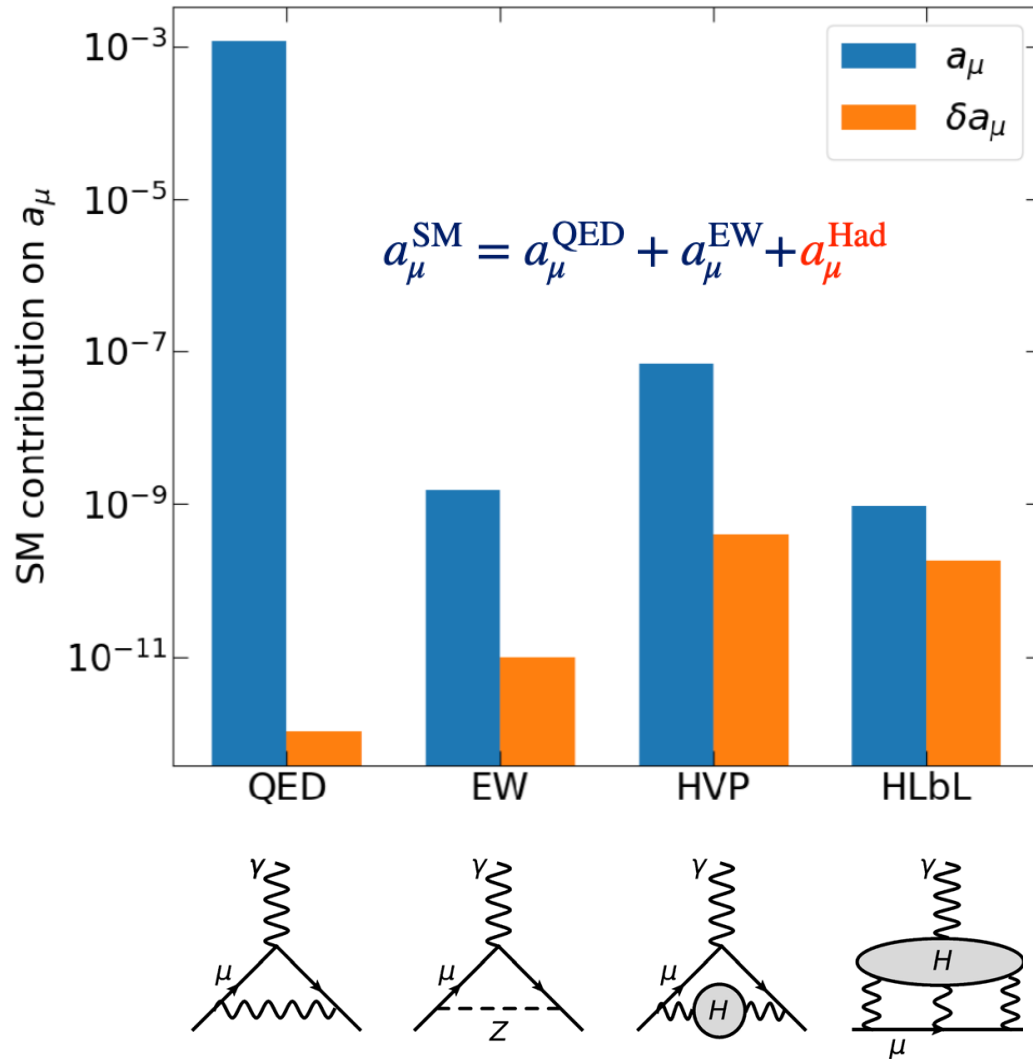
BSM physics

Standard Model Calculation



- QED: perturbative approach ($\alpha_{QED} \ll 1$) known to 5-loop level
- EW: perturbative approach ($\alpha_{EW} \ll 1$) known to 2-loop level
- Hadronic Vacuum Polarization (HVP)
 - no perturbative approach ($\alpha_{QCD} \sim 1$)
 - dispersive approach (data-driven)
 - lattice approach (first principle)
- Hadronic Light-by-light (HLbL)
 - no perturbative approach ($\alpha_{QCD} \sim 1$)
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Standard Model Calculation



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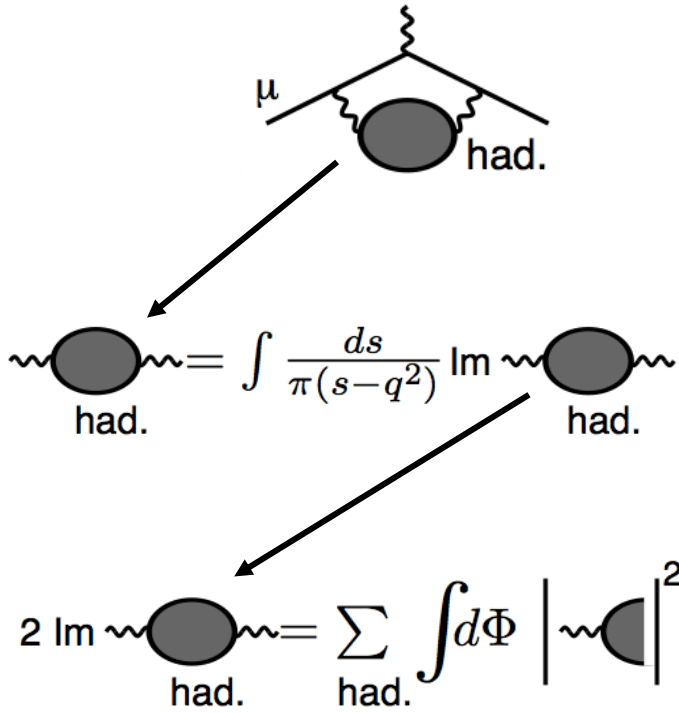
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tension

- Hadronic Light-by-light (HLbL)
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 - lattice approach (first principle)

agreement

Dispersive Approach

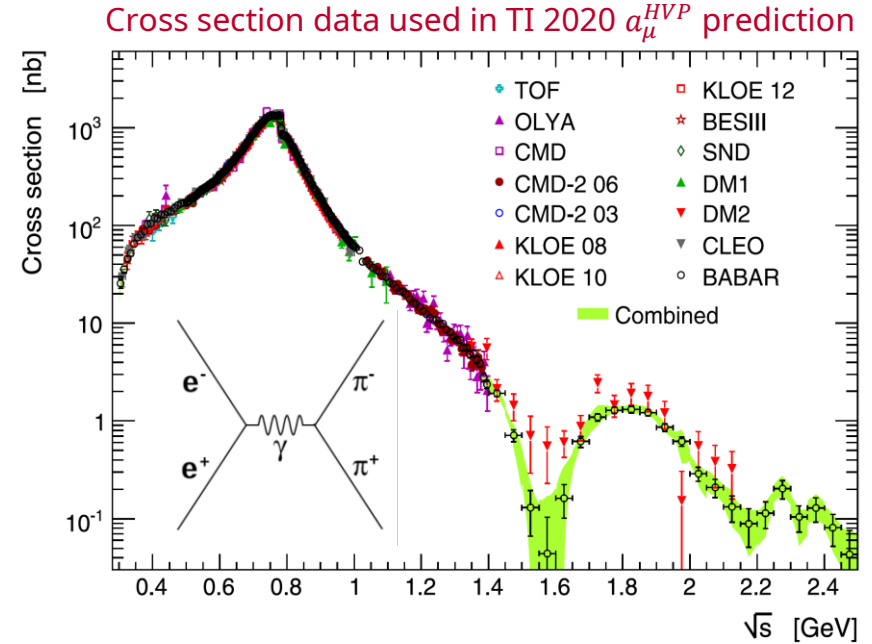


$$a_\mu^{\text{had,LO}}$$

Dispersion Relation
follows from causality

Optical Theorem
follows from unitarity
of scattering matrix

$$a_\mu^{\text{had,LO}} = \frac{m_\mu^2}{12\pi^3} \int_{s_{\text{th}}}^{\infty} ds \frac{1}{s} \hat{K}(s) \sigma_{\text{had}}(s)$$

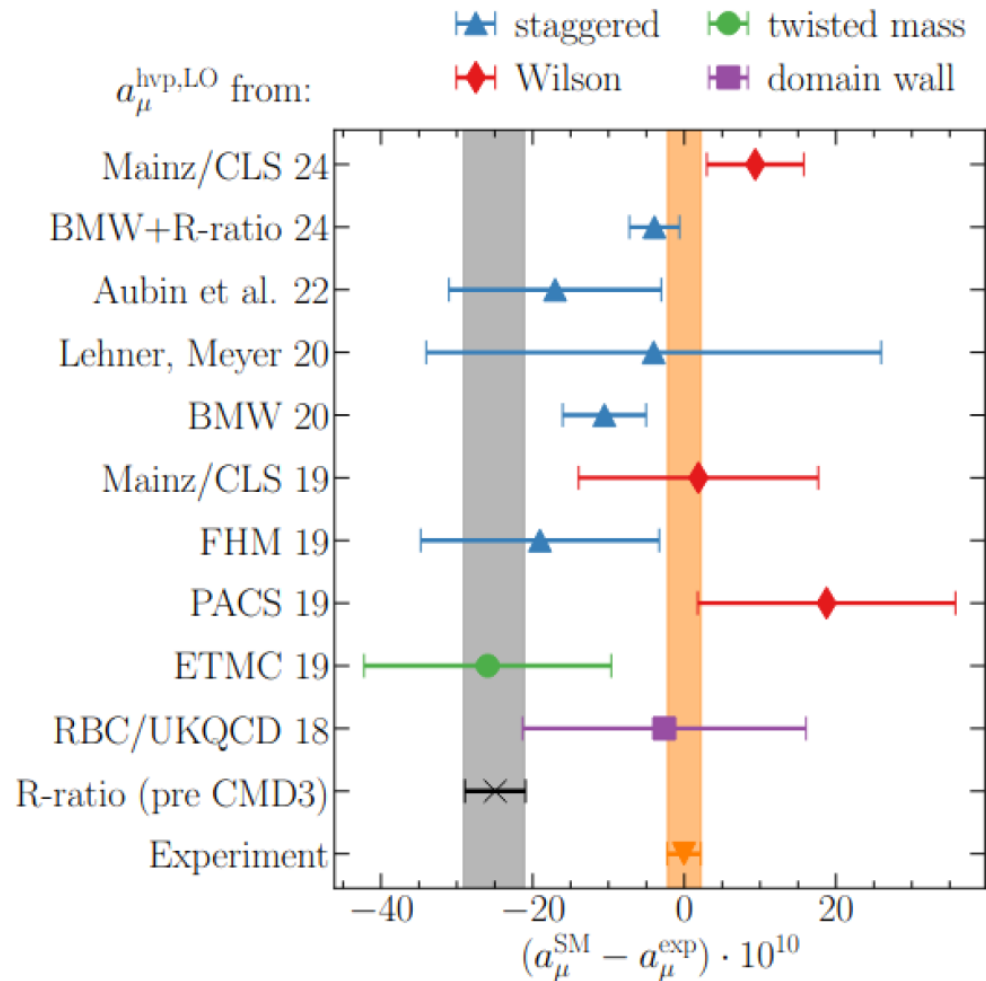
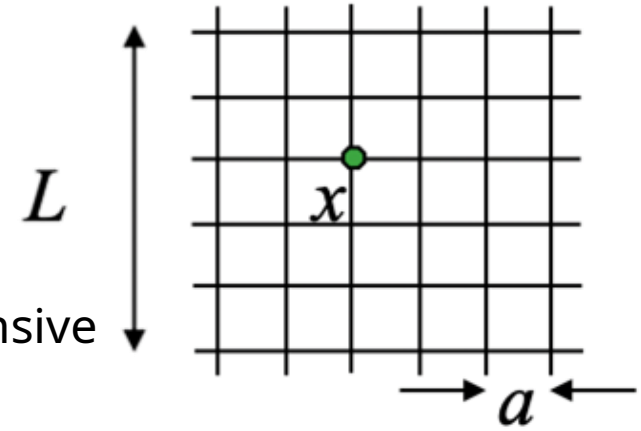


Davier et. al, Eur. Phys. J. C. 80 (2020)

- calculated from total hadronic cross-section $\sigma_{\text{had}}(s)$
- $1/s$ weight \rightarrow low energies most important
- $\pi^+ \pi^-$ contribute 73% to LO

Lattice QCD Approach

- First principle calculation to predict a_μ
- Numerical integration on finite space-time lattice \rightarrow very computing intensive



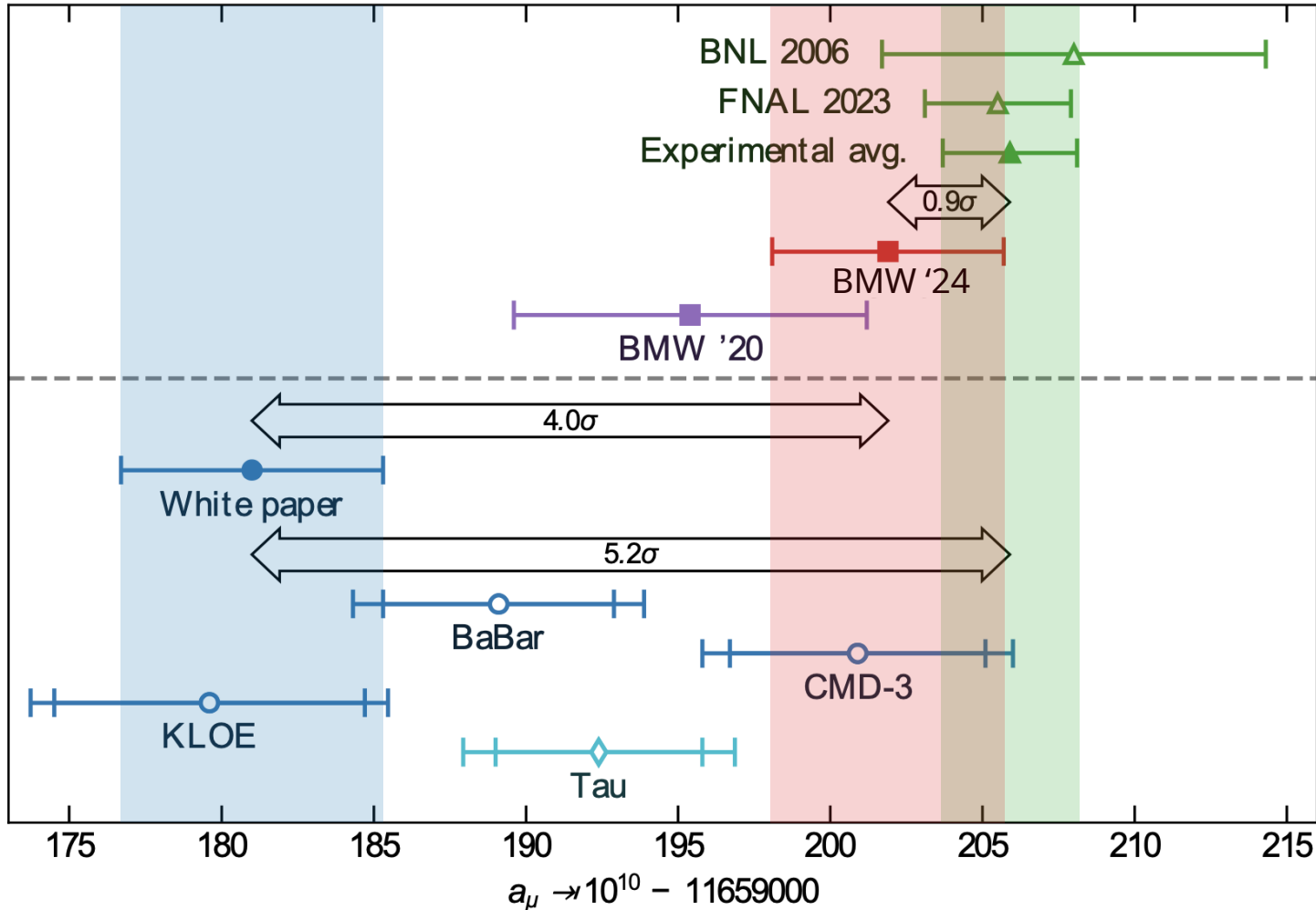
Preliminary: Consistency between different groups

First prediction with <1% uncertainty by BMW

Lattice results not included in TI white paper due to low precision

The Muon $g-2$ Puzzle

M. Hoferichter, Workshop of TI, Sep 2024 @KEK



Muon $g-2$ Puzzle
tension between theory (white paper)
and experiment

New muon $g-2$ Puzzle
Inconsistency between

- lattice and data-driven approach
- different e^+e^- experiments

Experiment
→ improve statistics & systematics
of measurement

Outline

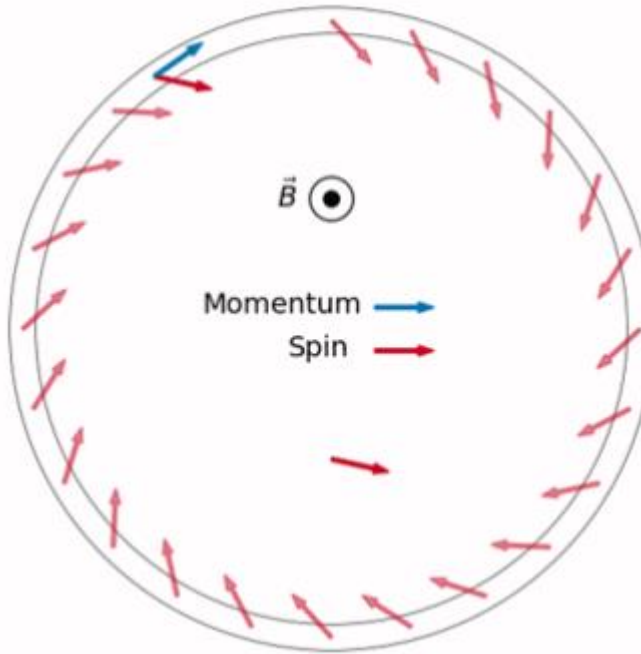
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Muon in homogeneous magnetic field

Cyclotron Motion

centrifugal force = Lorentz force

$$\vec{\omega}_C = -\frac{e}{m\gamma}\vec{B}$$



Spin Precession

magnetic moment and field couple

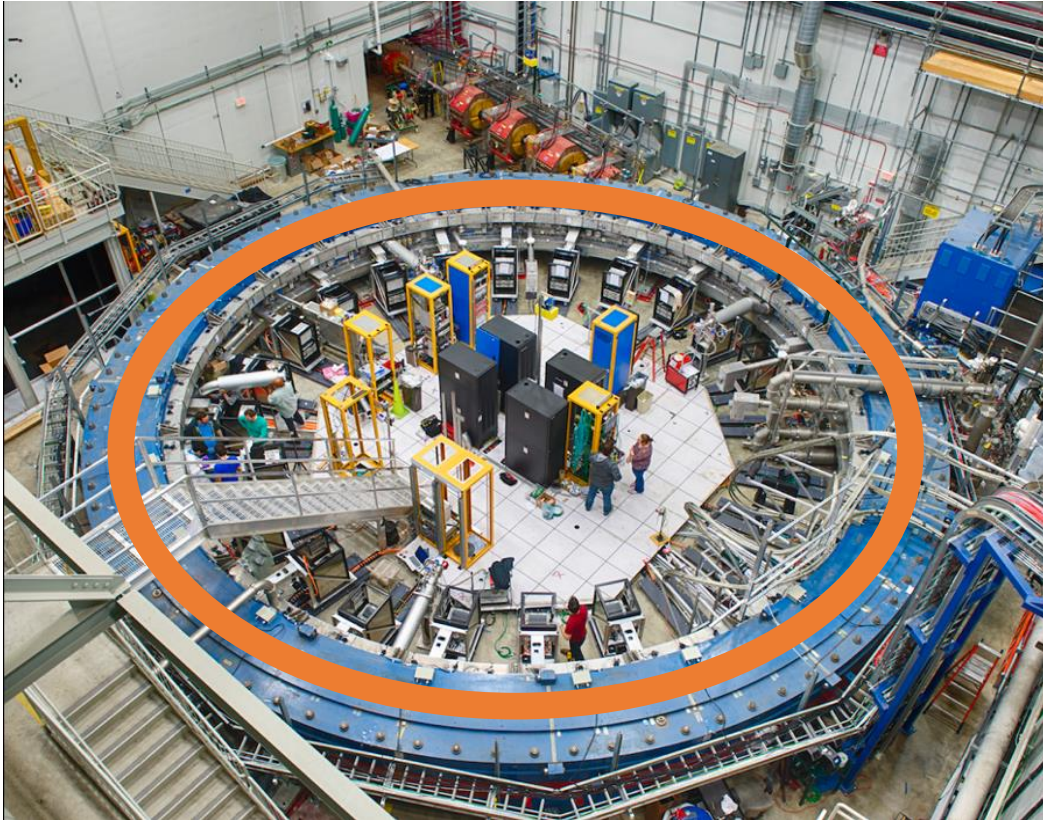
$$\vec{\omega}_S = -g\frac{e}{2m}\vec{B} - (1 - \gamma)\frac{e}{\gamma m}\vec{B}$$

$$\underbrace{\omega_S - \omega_C}_{\omega_a} = g_\mu \frac{e}{2m_\mu} B - \frac{e}{m} B = \underbrace{\frac{g_\mu - 2}{2}}_{a_\mu} \frac{e}{m_\mu} B$$

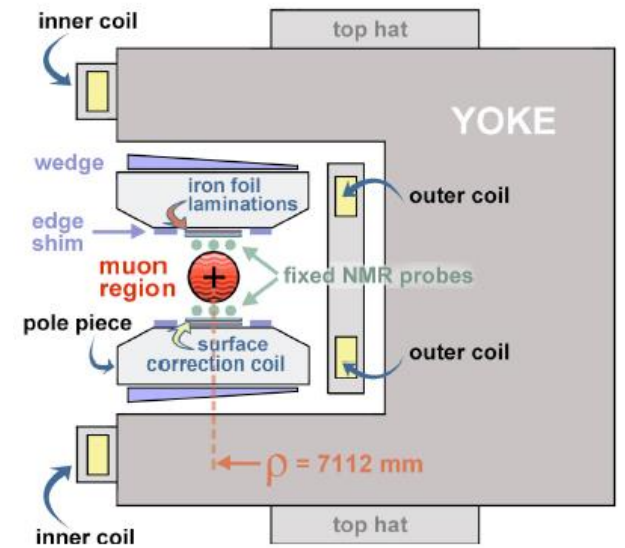
anomalous spin-precession
frequency

anomalous magnetic
moment

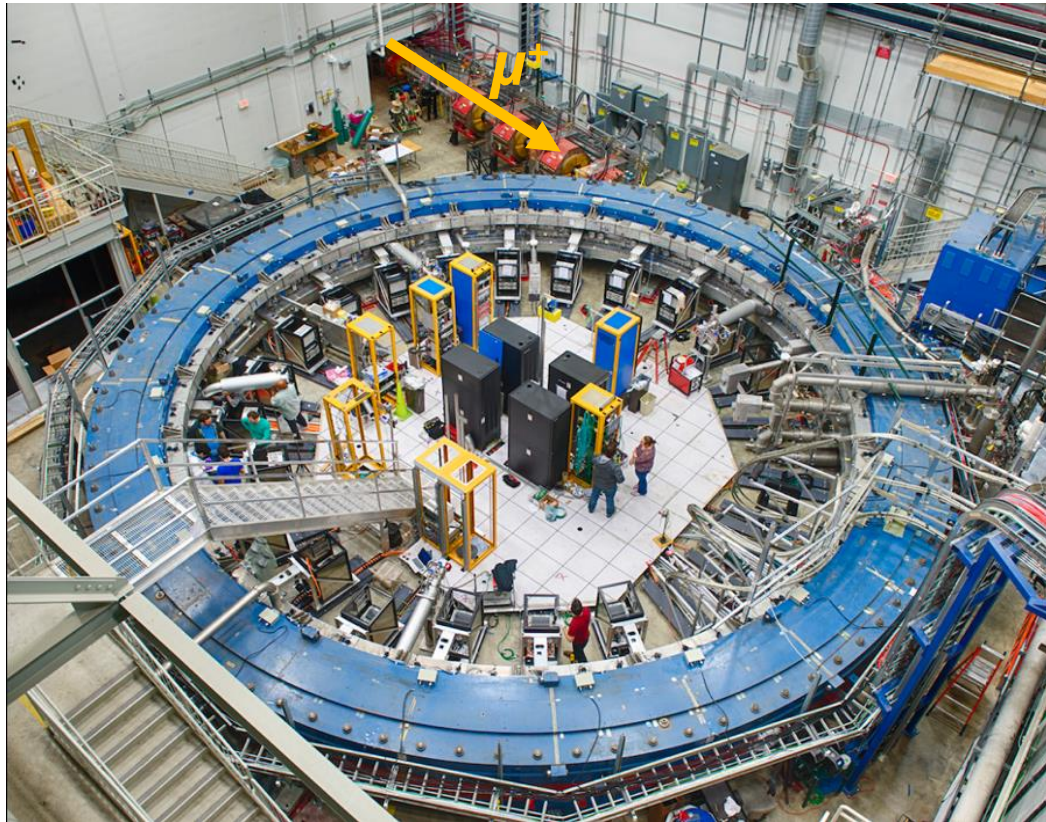
The Muon g-2 experiment at FNAL



- 1.45 T vertical magnetic field



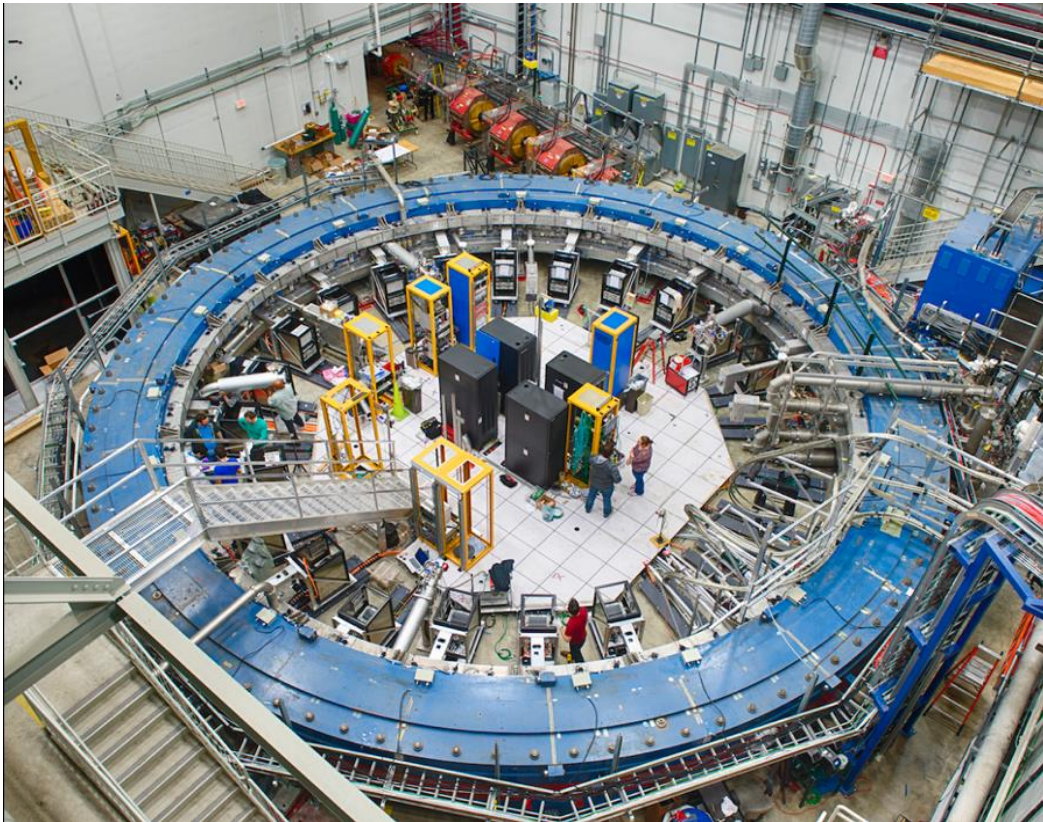
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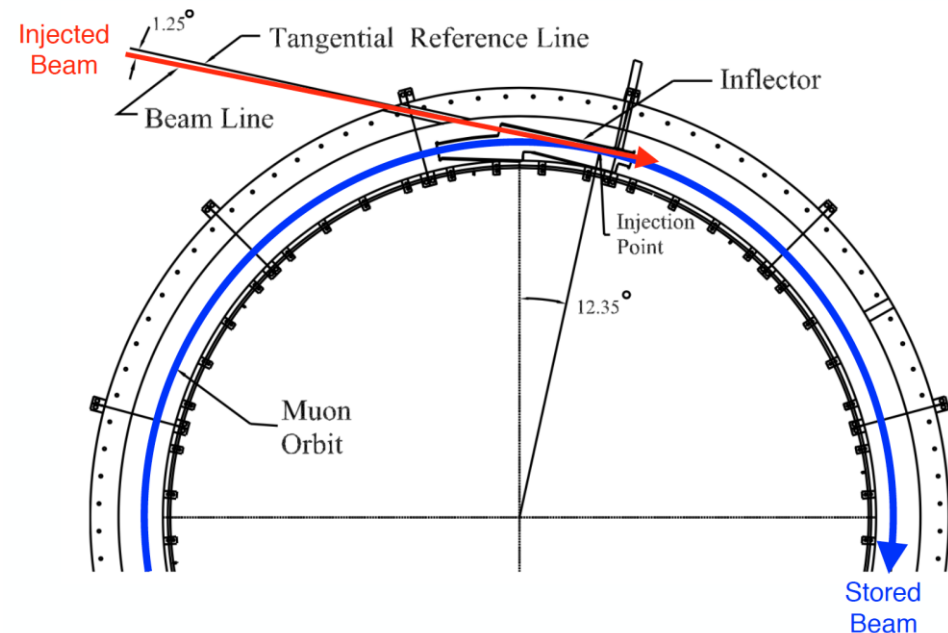
- 1.45 T vertical magnetic field
- highly polarized μ^+ provided by FNAL muon campus at

$$p_{\mu}^{magic} = 3.094 \frac{GeV}{c} \pm 0.5\%$$

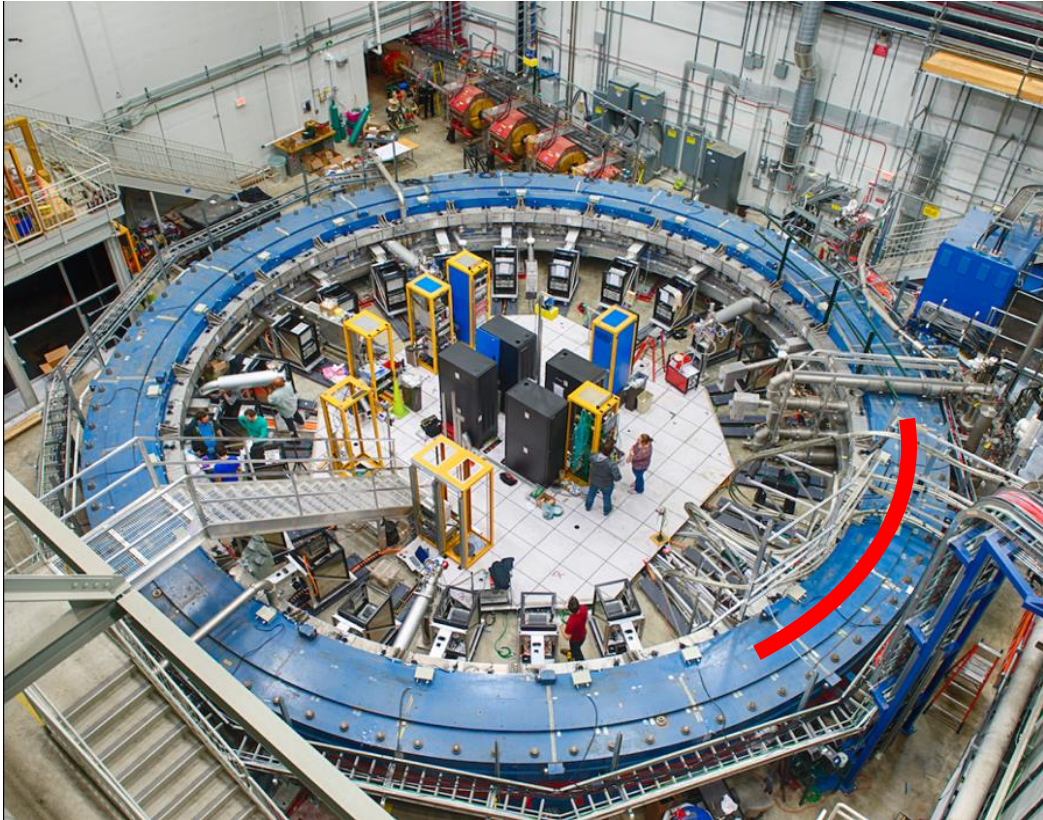
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- Superconducting inflector magnet in back of iron yoke

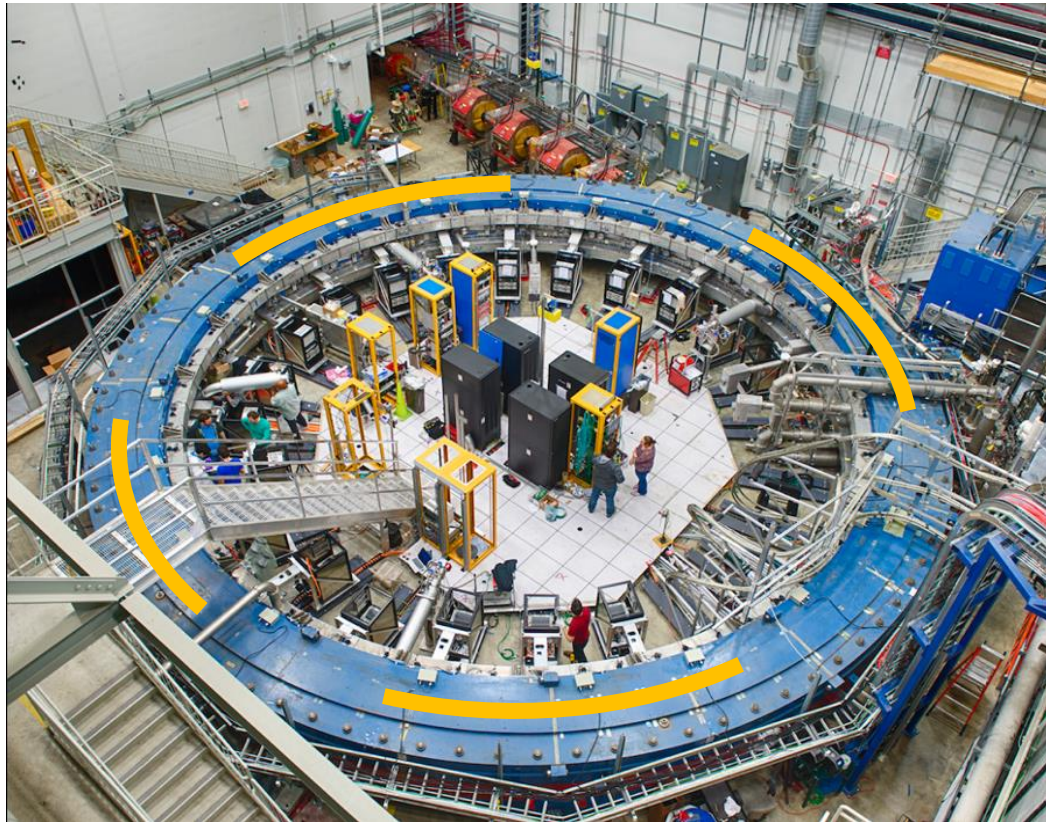


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- Three kicker plates change field locally by 2% within first cycle ($\sim 150ns$)

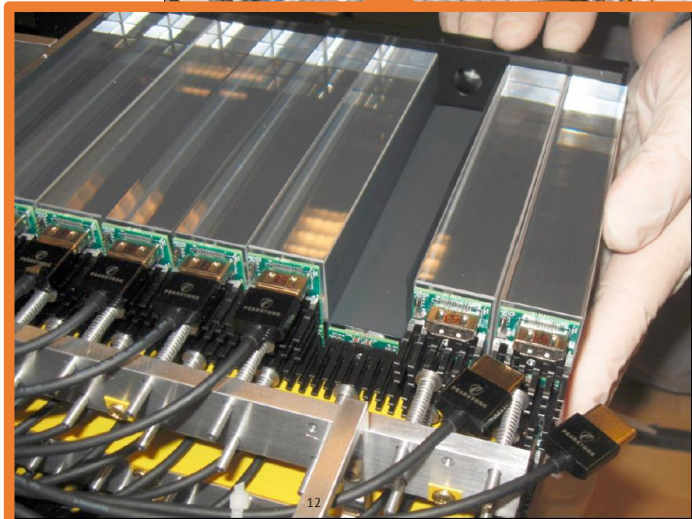
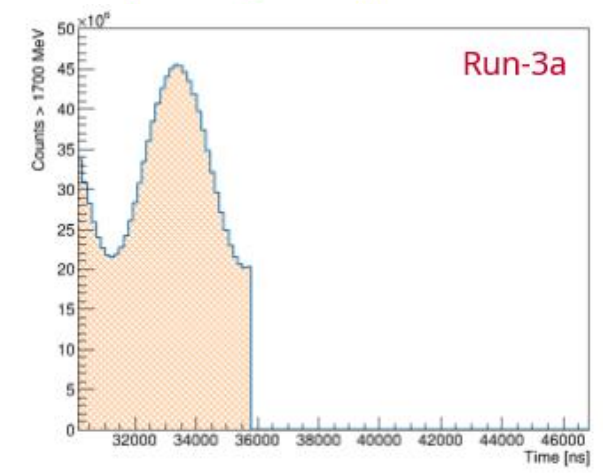
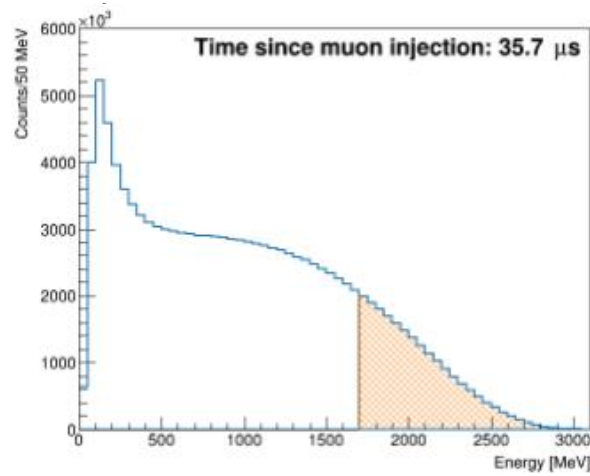
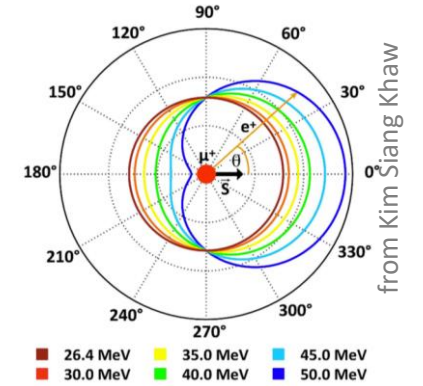
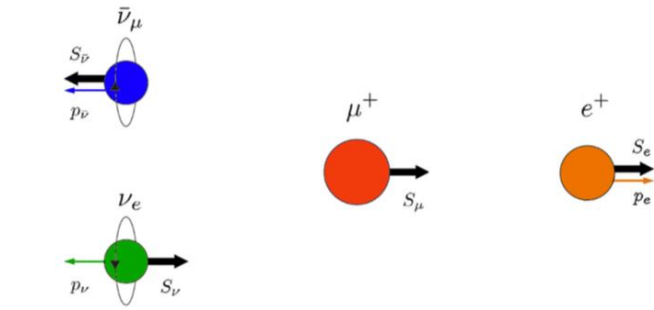
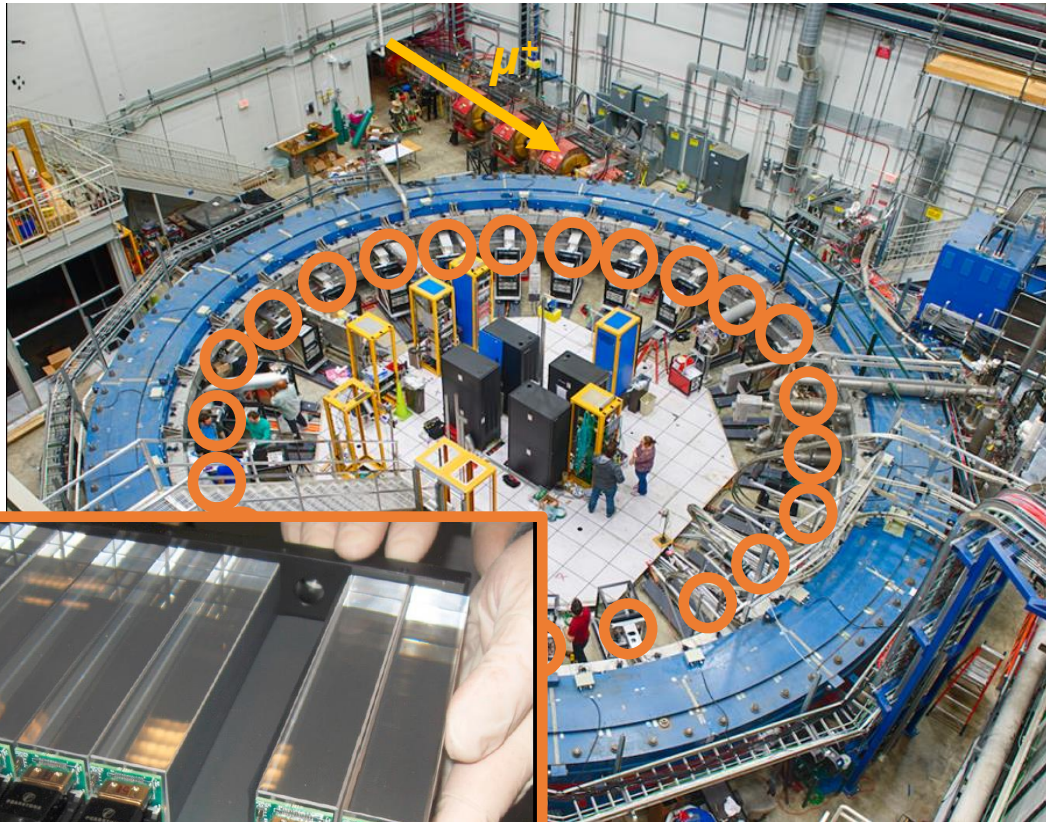
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- Superconducting inflector magnet in back of iron yoke
- Three kicker plates change field locally by 2% within first cycle ($\sim 150ns$)
- Four electro-static quadrupoles covering 43% of ring to focus beam

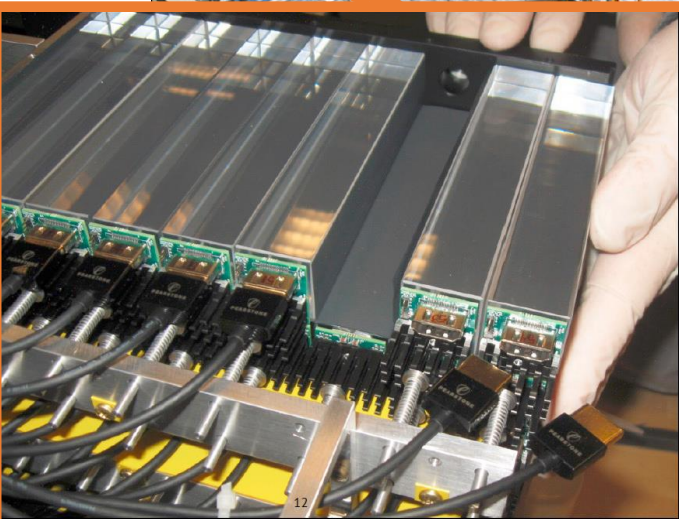
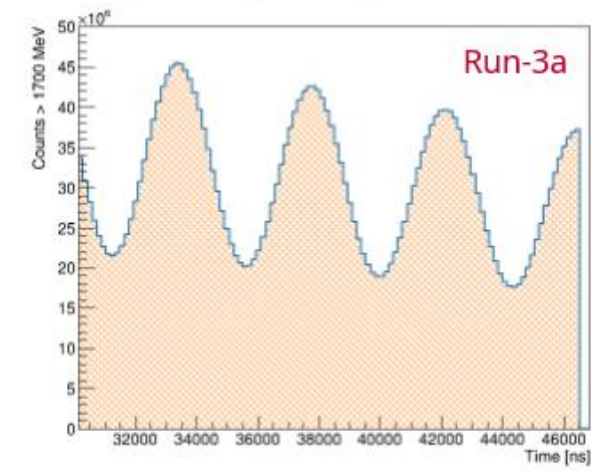
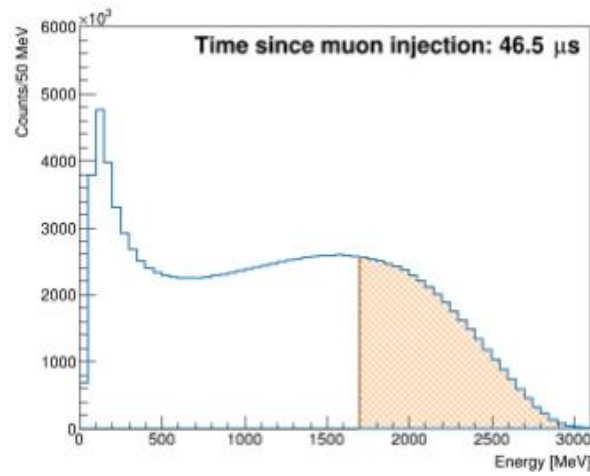
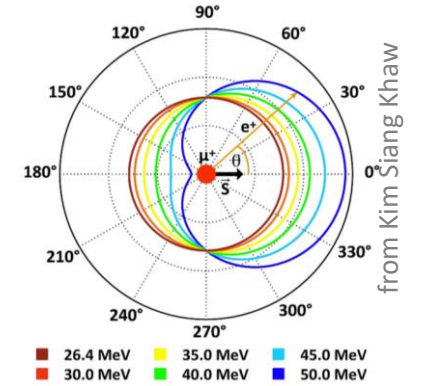
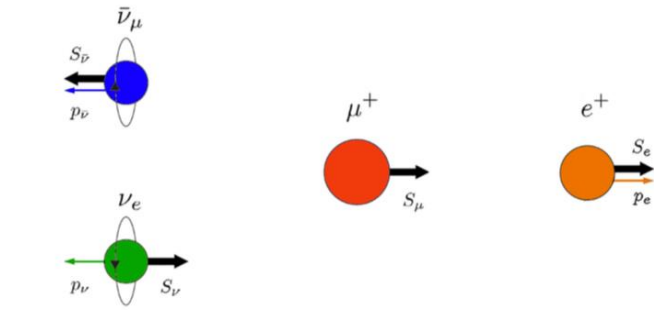
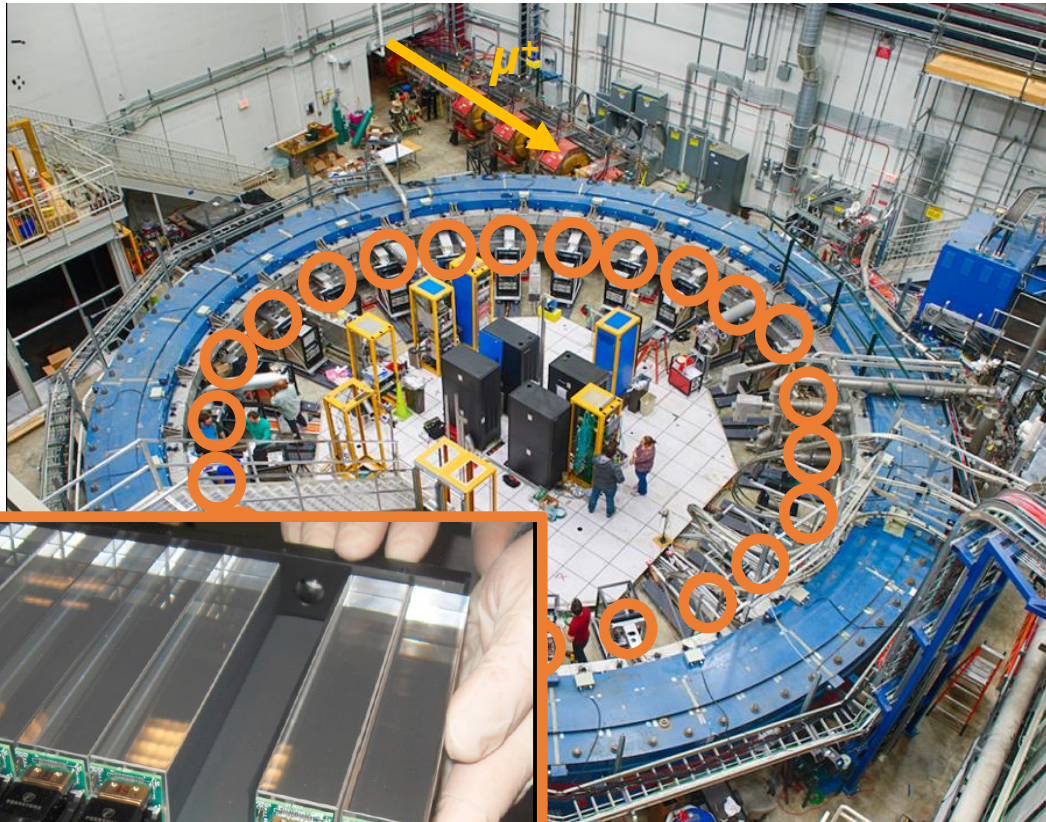
The Muon g-2 experiment at FNAL

- 24 PbF2 crystals calorimeters
- Detect in spiraling positrons from muon decay

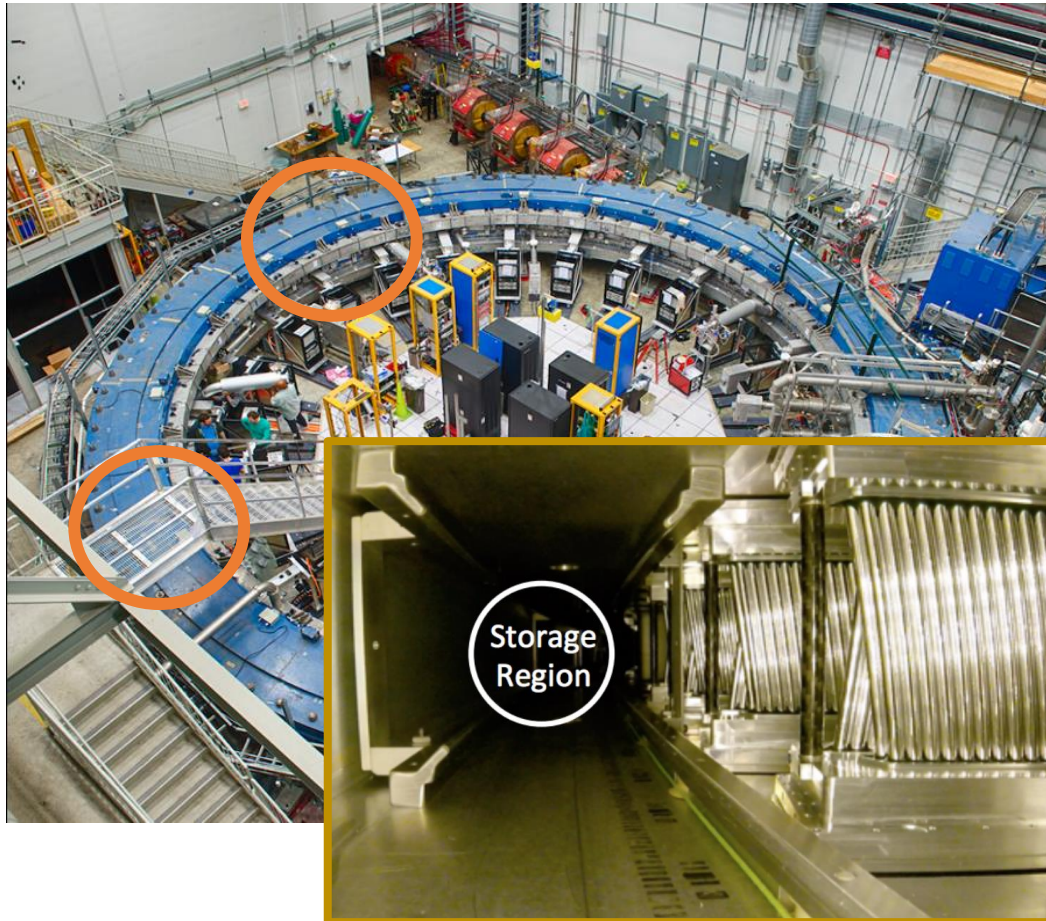


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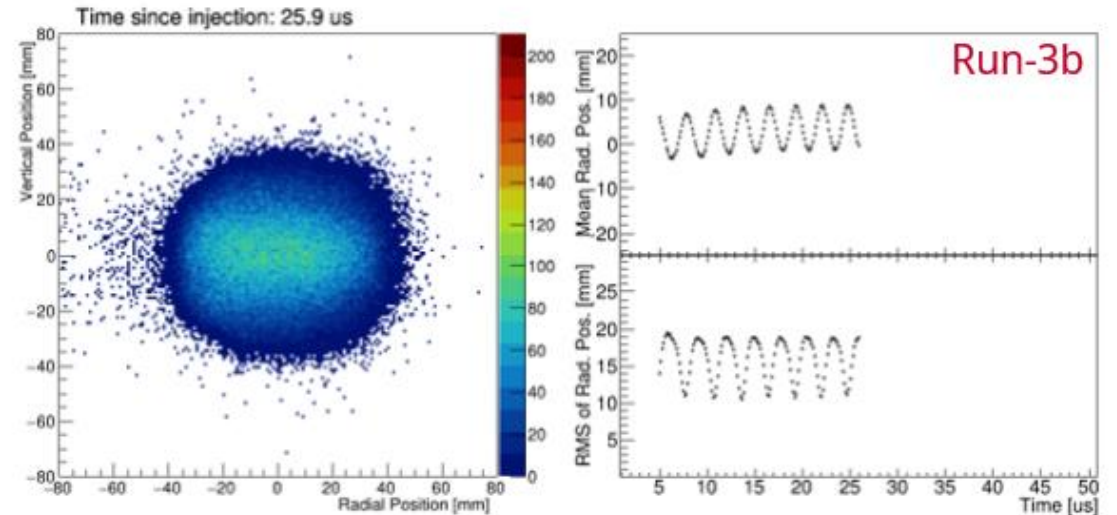
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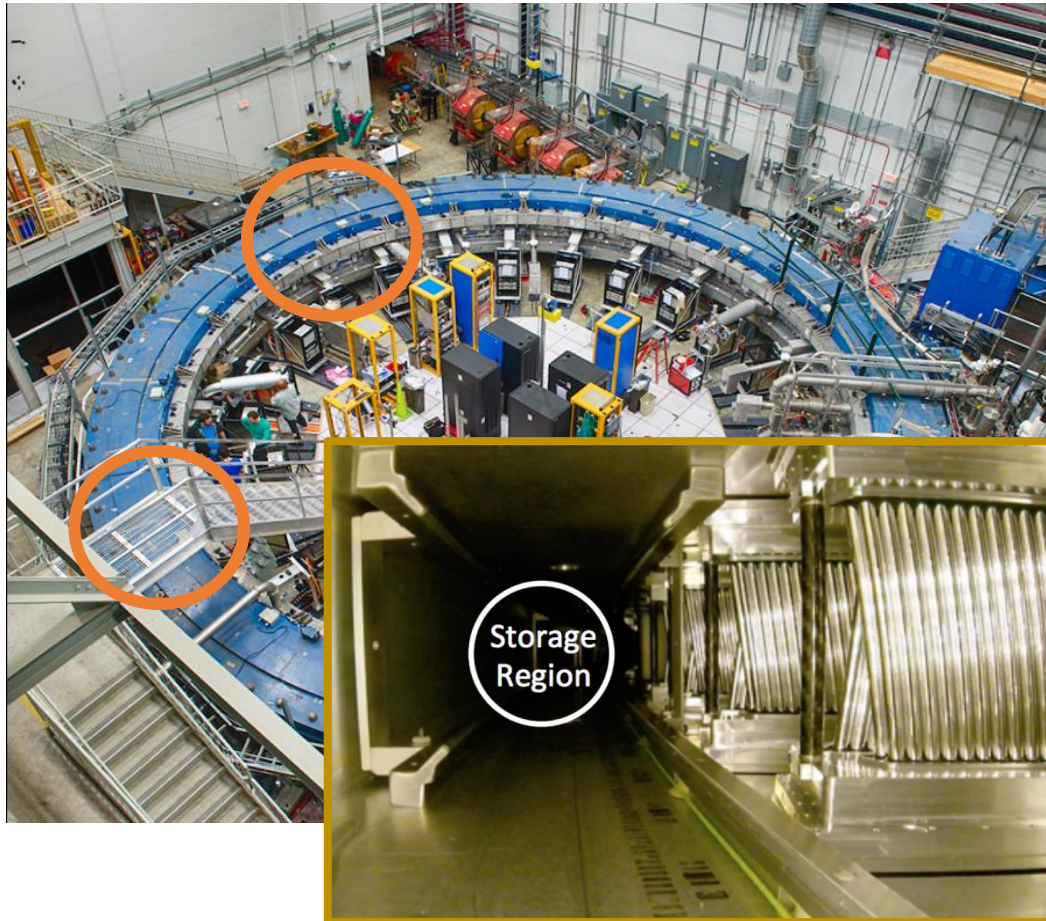
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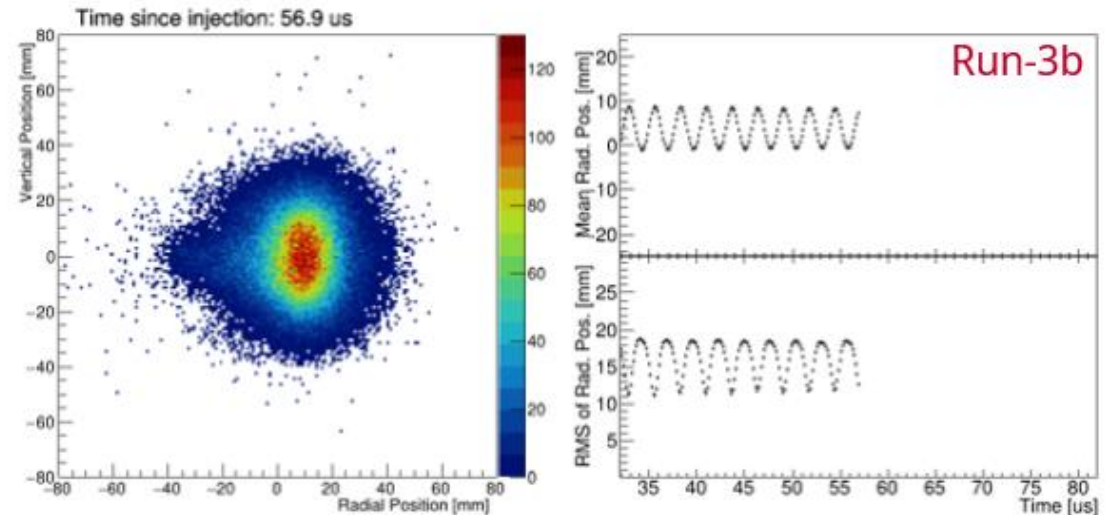
- Two tracking stations based on gas-filled straw tubes
- Determine e^+ trajectory to decay position and extrapolate to find muon beam distribution!



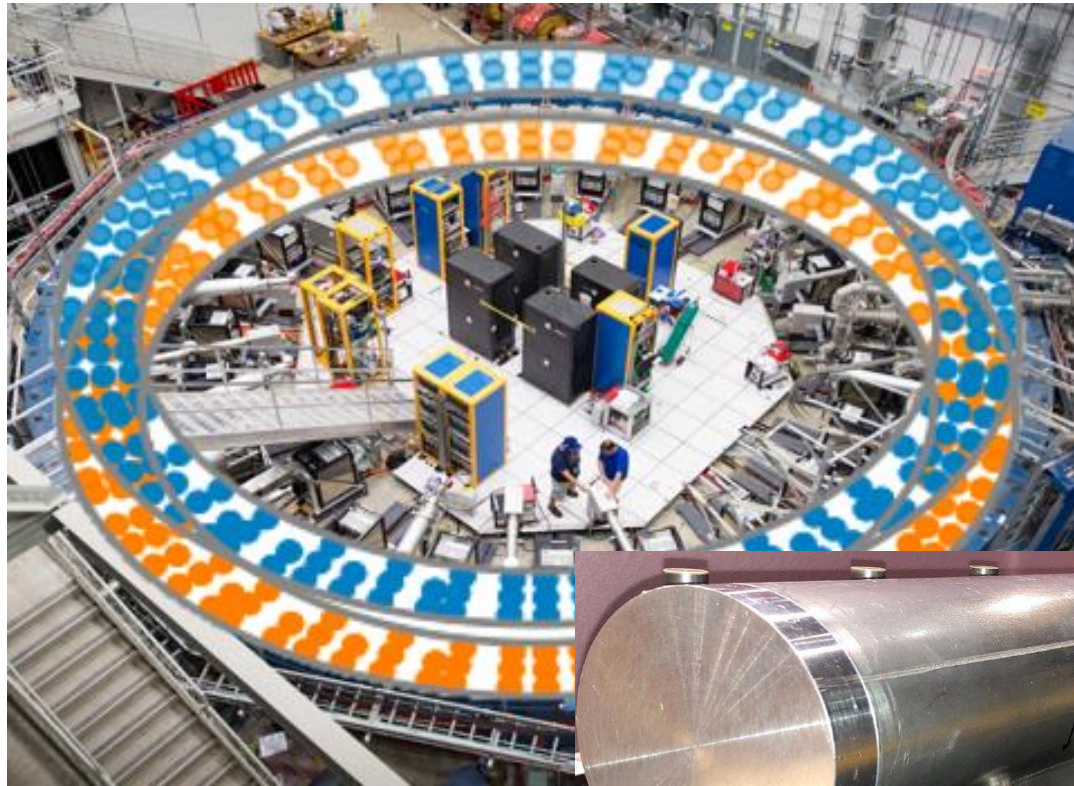
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The Muon g-2 experiment at FNAL



- 378 NMR probes in vacuum chamber walls to track magnetic field drift 24/7
- Movable device with 17 NMR probes measures spatial field distribution in muon storage region
- Externally calibrated absolute water NMR probe



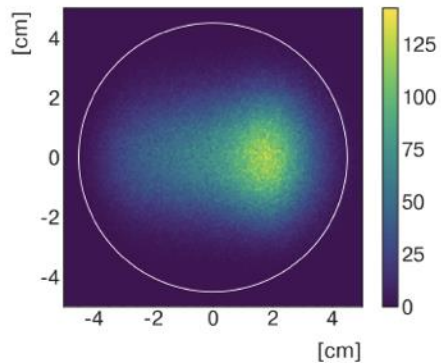
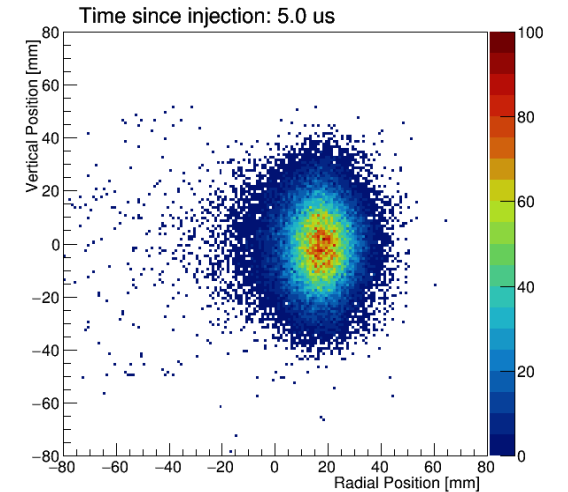
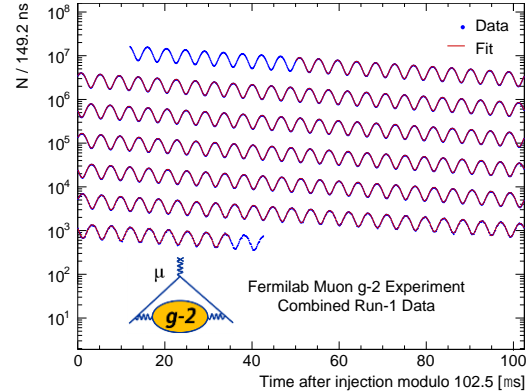
Extracting a_μ

Anomalous spin precession frequency

Muon beam dynamics corrections

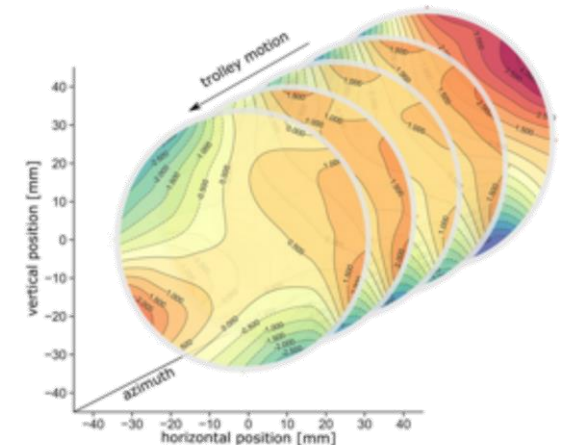
Clock blinding

$$\frac{\omega_a}{\tilde{\omega}'_p} = \frac{f_{\text{clock}} \omega_a^{\text{meas}} (1 + C_e + C_p + C_{ml} + C_{pa} + C_{dd})}{f_{\text{calib}} \langle M(x, y, \phi) \omega'_p(x, y, \phi) \rangle (1 + B_k + B_q)}$$



Spatial muon distribution

Magnetic field calibration
Spatial distribution of magnetic field
Transient magnetic fields



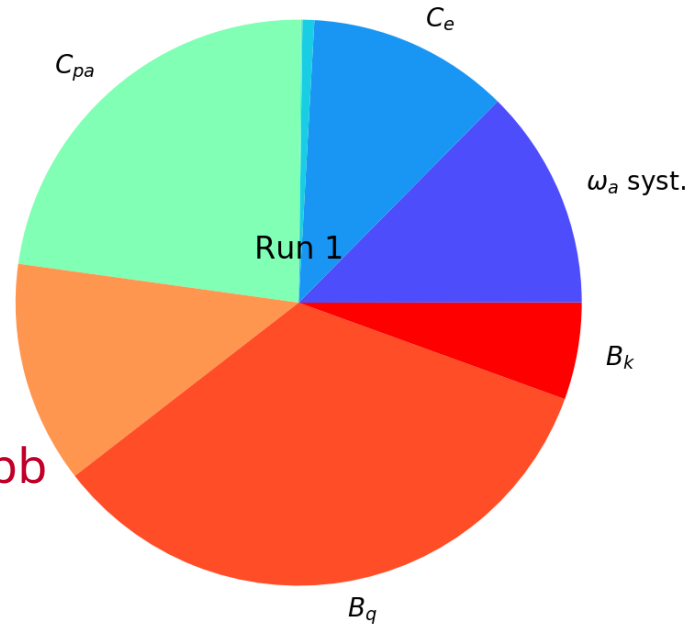
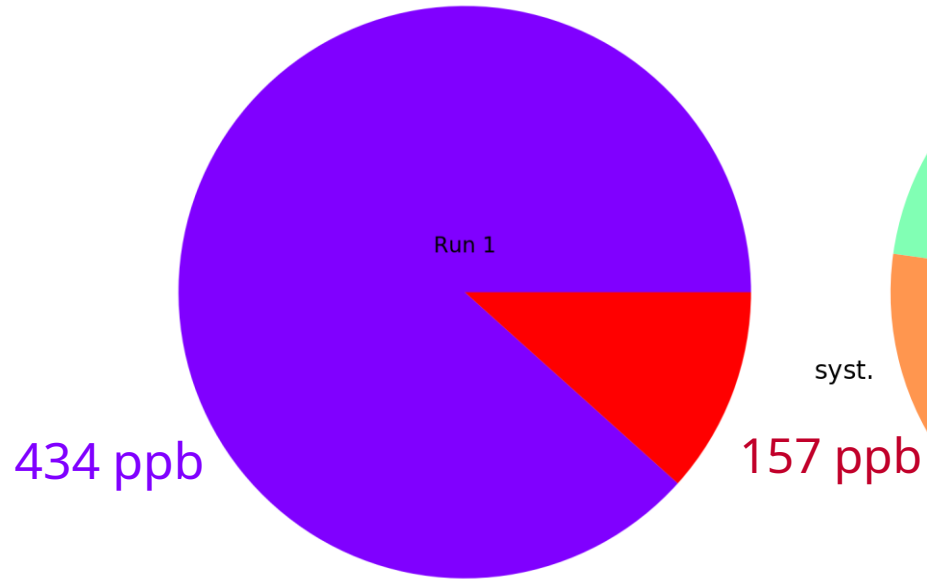
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Uncertainties Run1 vs Run2

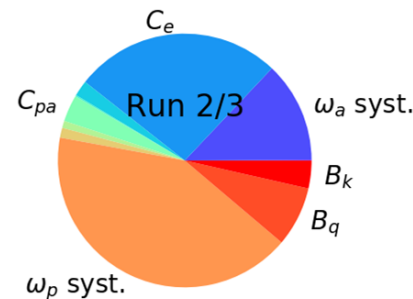
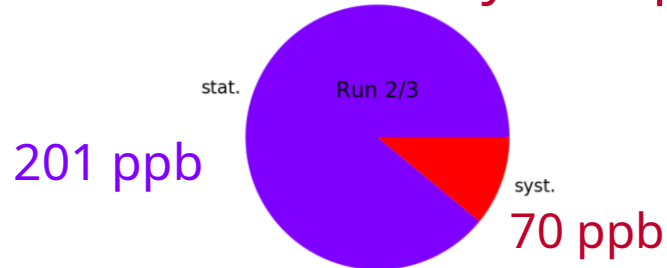
Run-1

Total uncertainty: 462 ppb



Run-2/3

Total uncertainty: 215 ppb

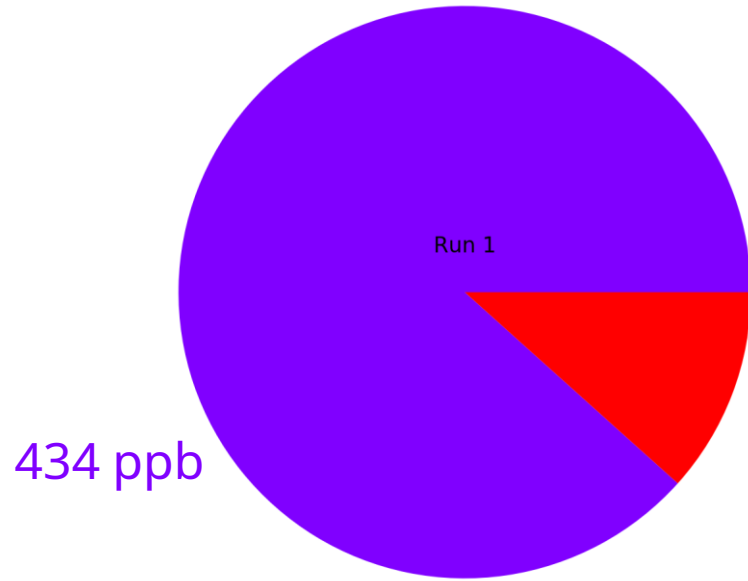


- Uncertainty reduced by factor >2
- Statistic and systematic uncertainty reduced by similar amount
- Systematic uncertainty below TRD goal
- Still statistics dominated

Radius: uncertainty
Area: variance

Improvements: Statistics

Run-1

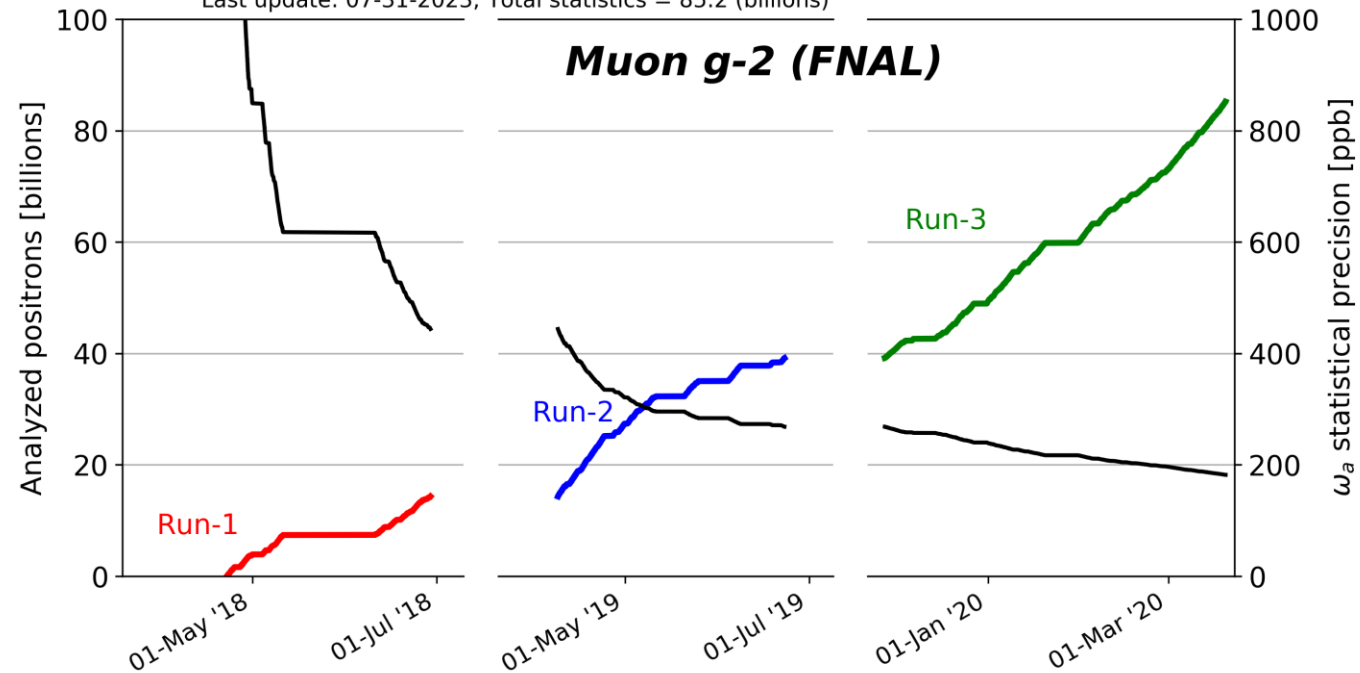


Run-2/3



Weighted e^+ in our final fit after quality control ($E > 1$ GeV, $t > 30$ us)

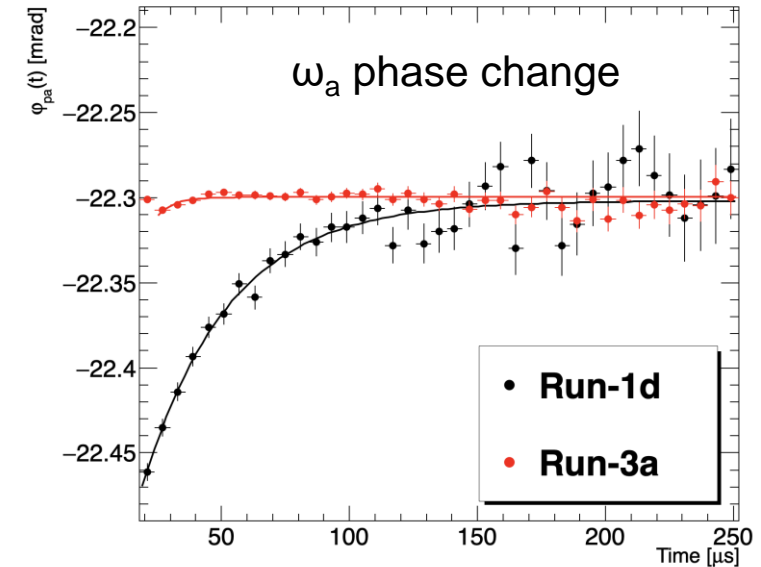
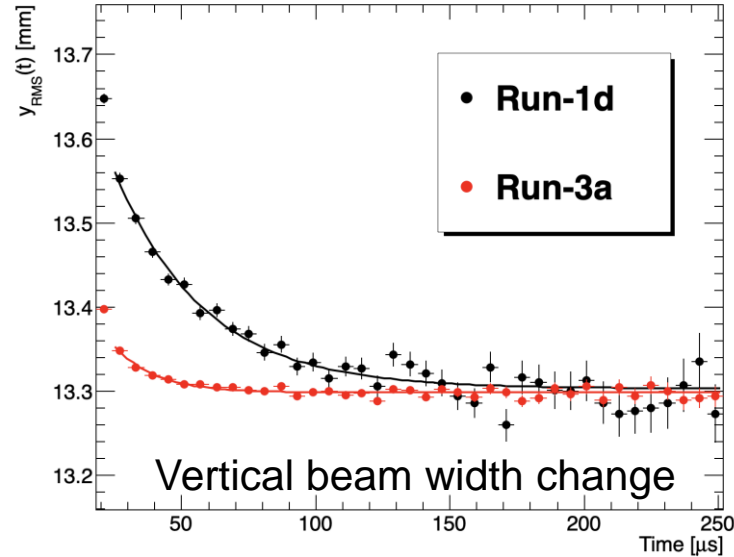
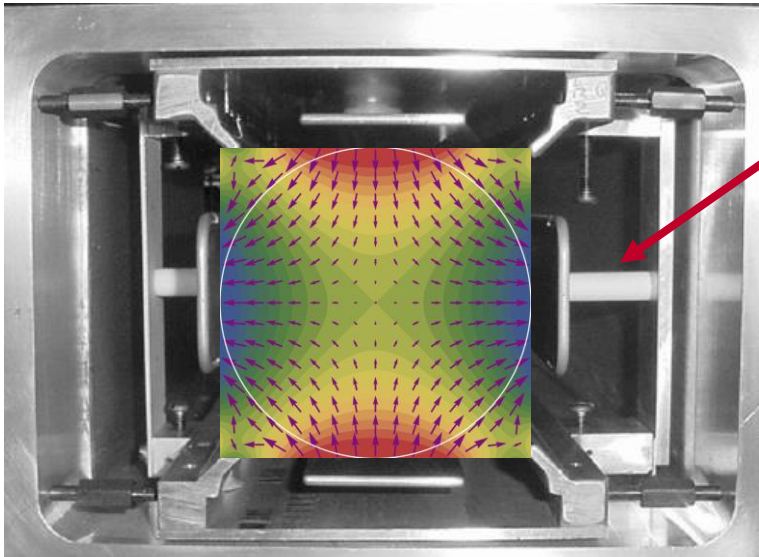
Last update: 07-31-2023; Total statistics = 85.2 (billions)



Radius: uncertainty
Area: variance

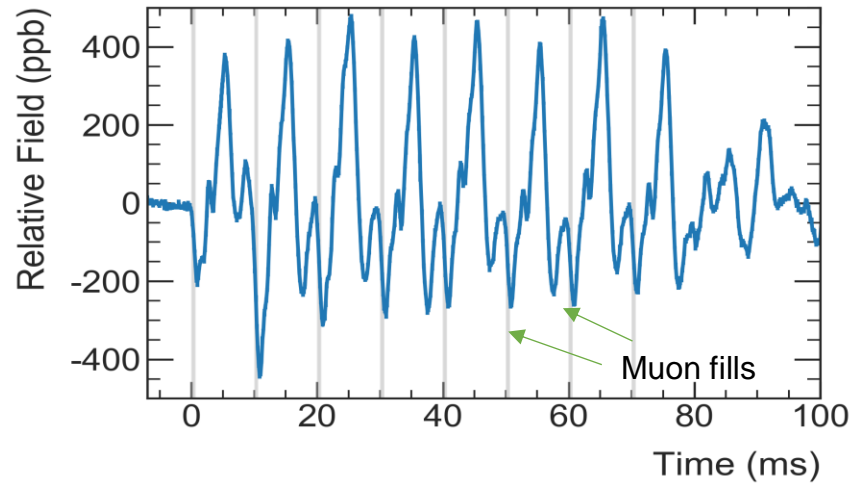
Improvements: Running Conditions

- Electro-static quadrupoles keep muon beam stable
- 2 out of 32 resistors damaged in quad plates → unstable beam storage
- Redesigned and replaced before Run-2



- Reduces phase acceptance uncertainties 75 ppb → 13 ppb
- Beam oscillation frequencies become also more stable

Improvements: Systematic Studies

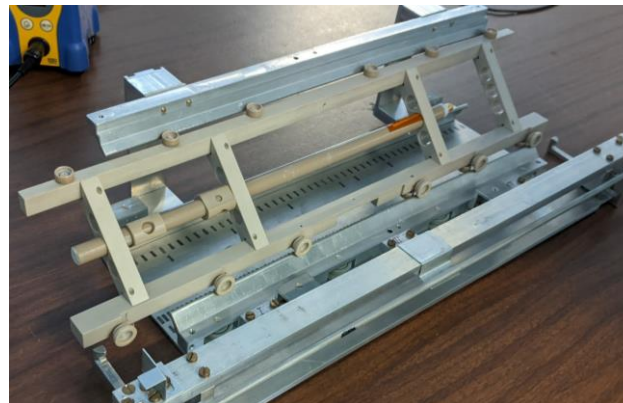
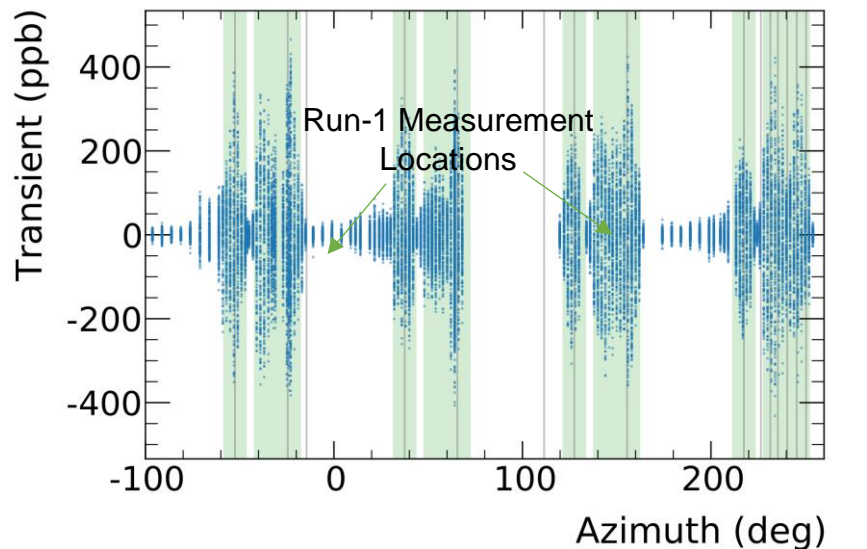


Pulsing electrostatic quadrupoles for beam confinement leads to magnetic field transient.



Run 1

- Limited measurement points
- Large uncertainty: 92 ppb



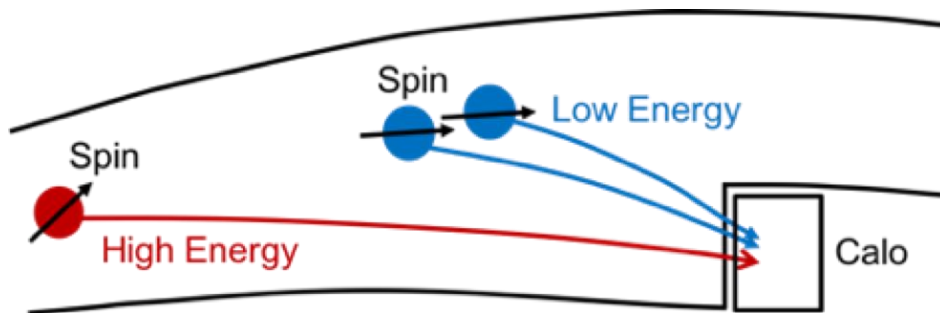
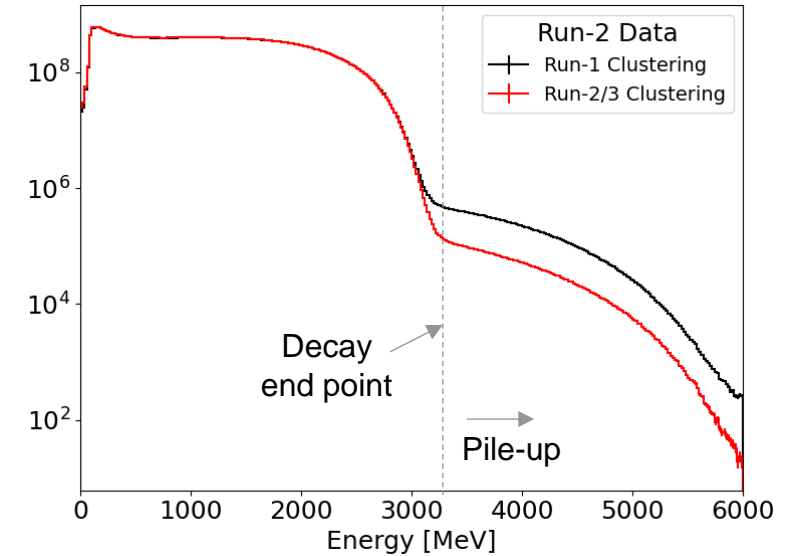
Run 2/3

- Probe movable on trolley rails
- Detailed measurement campaign over > 1 month
- Uncertainty reduced to 20 ppb

Improvements: Analysis

Pile-up correction

- 2 e^+ **arriving at same time** can be mistaken for 1
- Rate dependent \rightarrow can **bias ω_a**
- Reduced uncertainty by:
 - Improved **reconstruction**
 - Improved **correction algorithm**

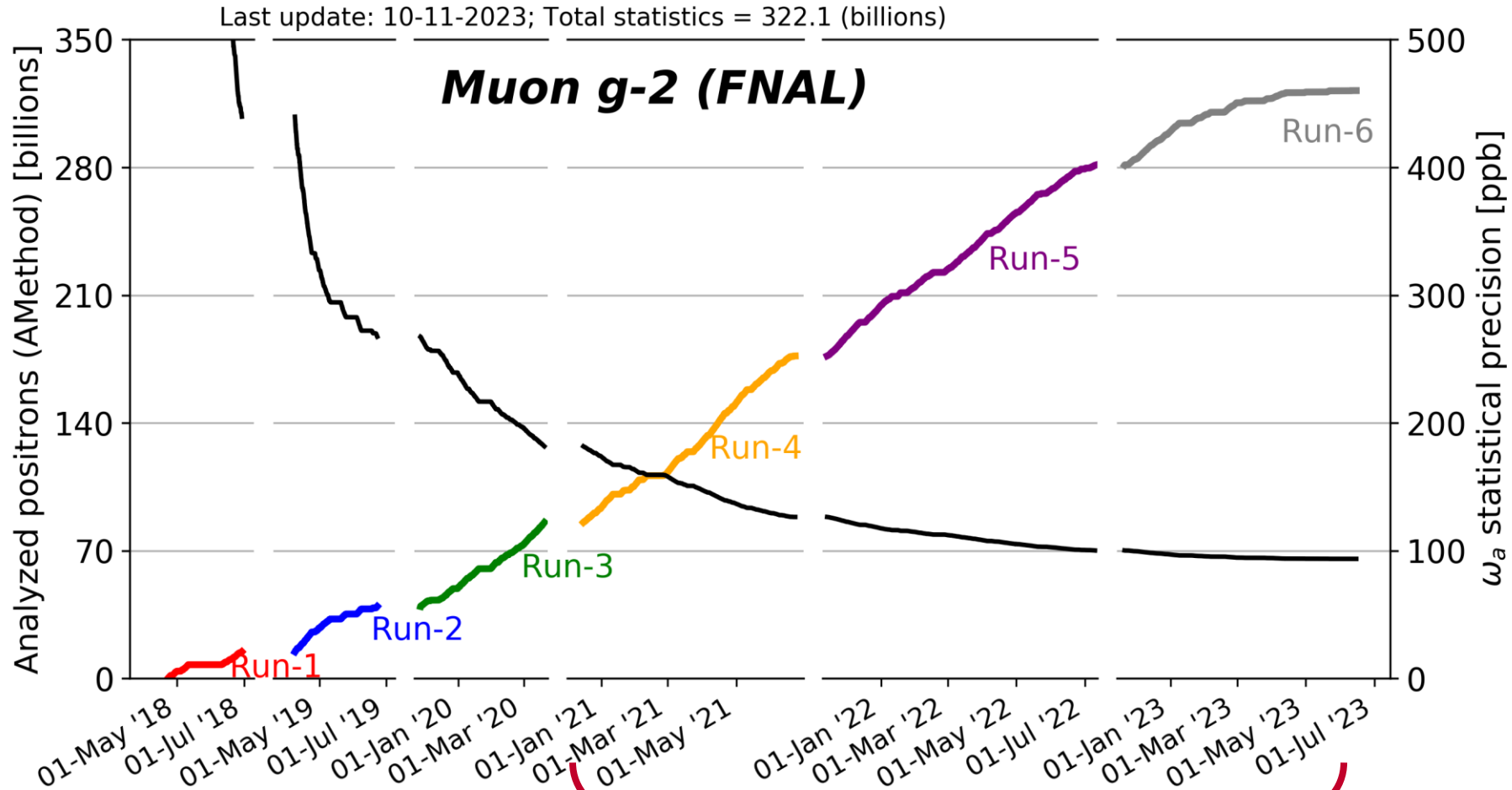


Phase of high-energy muon
 \neq
Phase of two low-energy muons

Outline

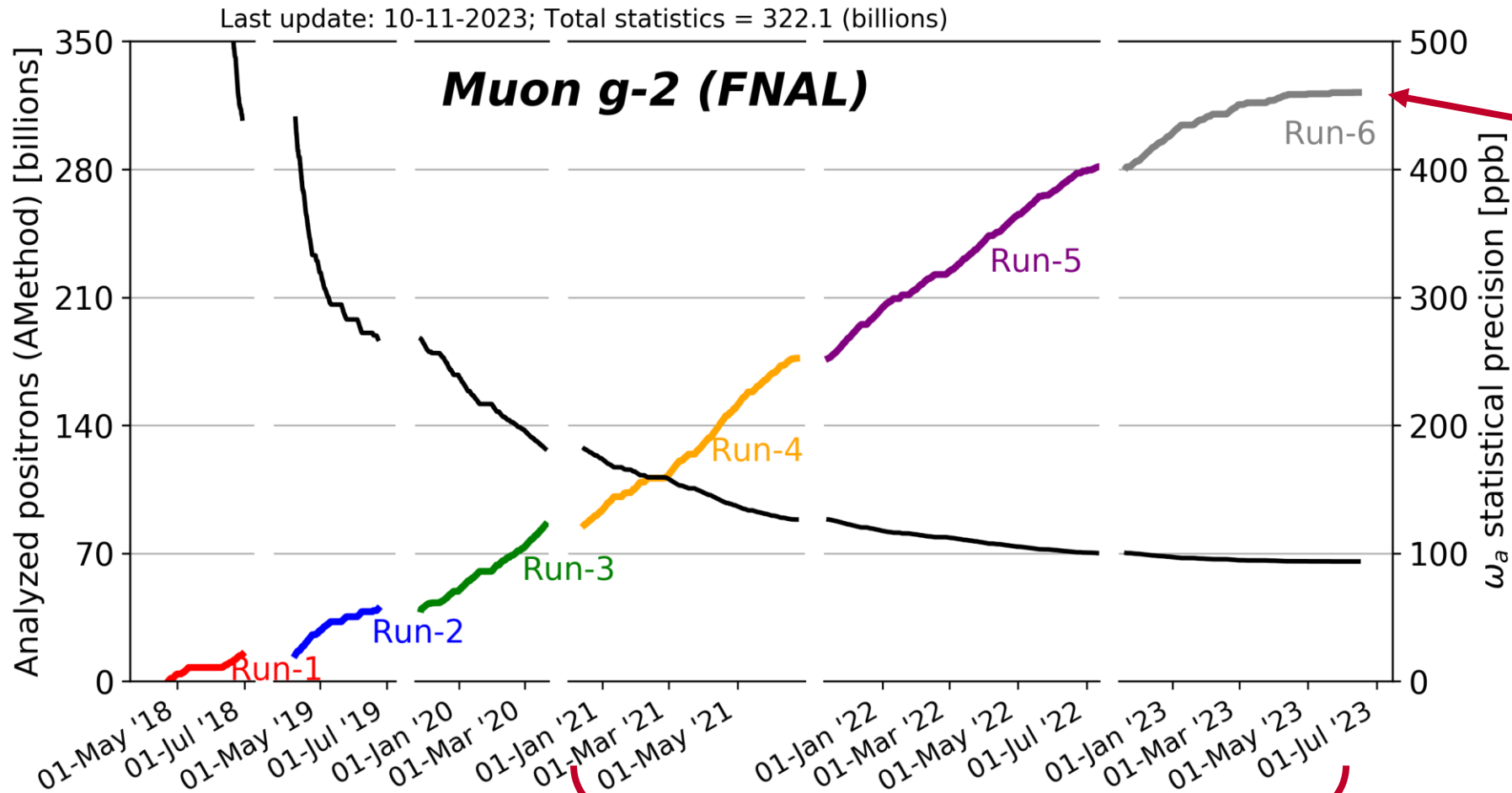
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Outlook



Much more statistics
Another factor of about 2 in statistic uncertainty

Outlook

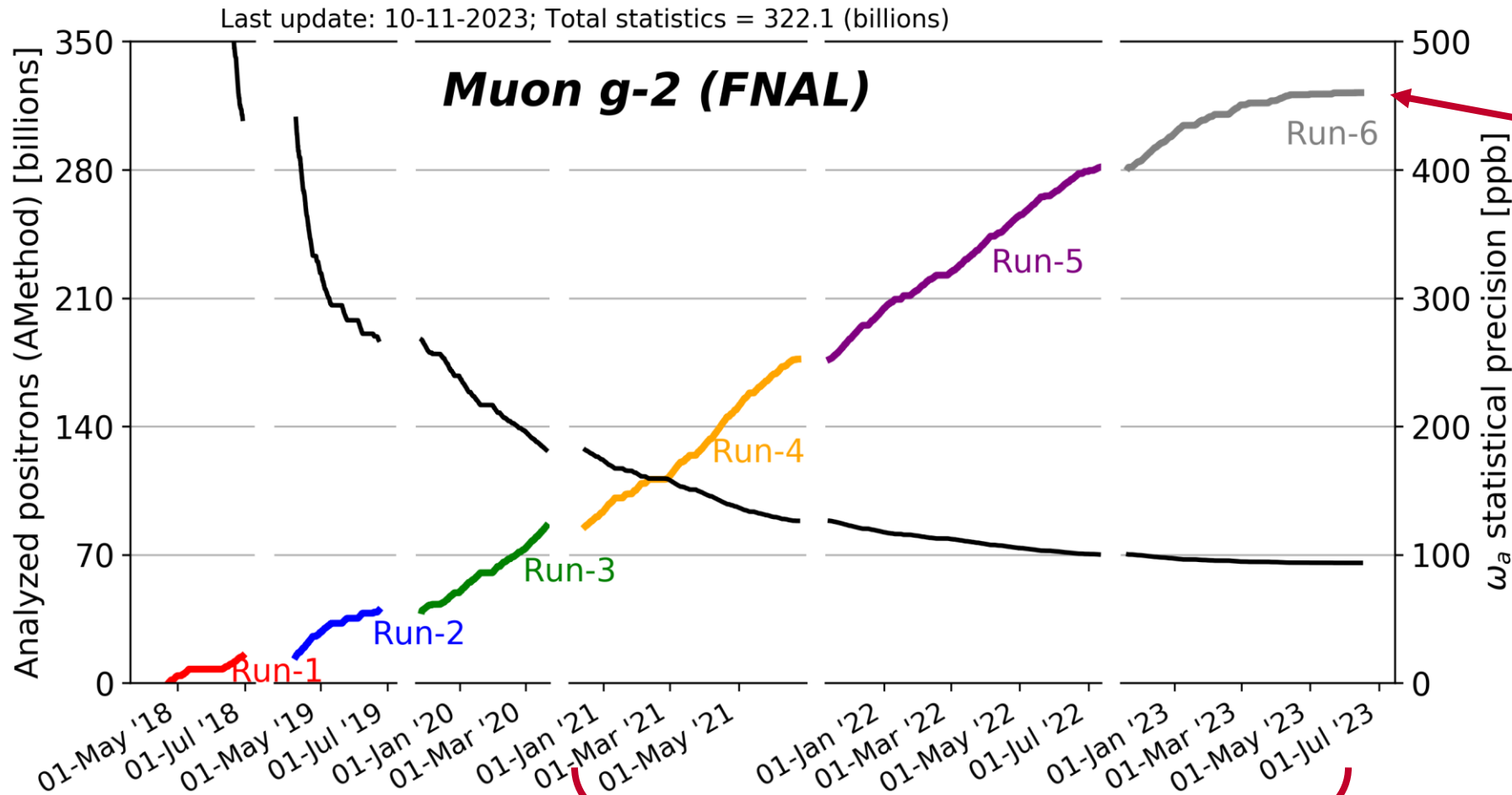


Exceeded TRD goal of 21 BNL statistics

Last part of run 6 dedicated to systematic studies

Much more statistics
Another factor of about 2 in statistic uncertainty

Outlook



Exceeded TRD goal of 21 BNL statistics

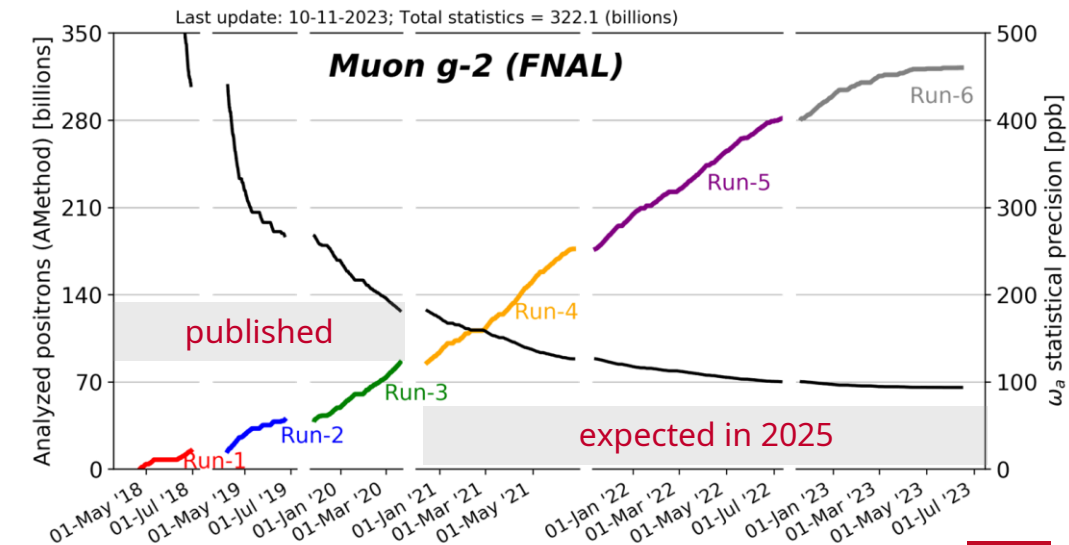
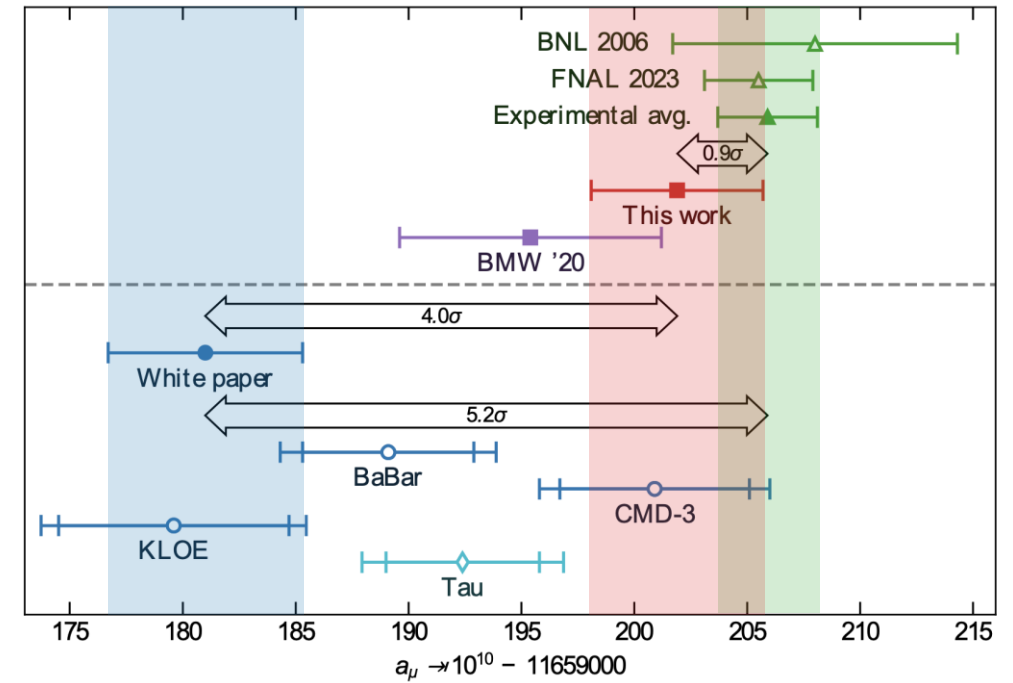
Last part of run 6 dedicated to systematic studies

Further systematic studies w/o beam concluded end Jan 2024

Much more statistics
Another factor of about 2 in statistic uncertainty

Conclusions

- High precision measurements of Muon $g-2$ stringent test on SM theory
- First time a three-way comparison of a_μ is possible
 - Dispersive-approach lattice approach, experiment
 - Very interesting
- Run-2/3 data consistent with Run-1 and BNL
- Improvement by factor >2 in statistical and systematic uncertainty
- Surpassed TRD goals in statistics and systematics
- Another reduction by factor of 2 in statistical uncertainty from Run-4/5/6
- Experimental result will be long standing reference for theory developments



Thank you for your attention



Summer Collaboration meeting at University of Liverpool July 24-28, 2023

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NEWS | 10 August 2023

Dreams of new physics fade with latest muon magnetism result

Precision test of particle's magnetism confirms earlier shocking findings – but theory might not need a rethink after all.

Backup

Beyond Standard Model Physics

- Extra contribution to anomalous magnetic moment

- Naïve scaling

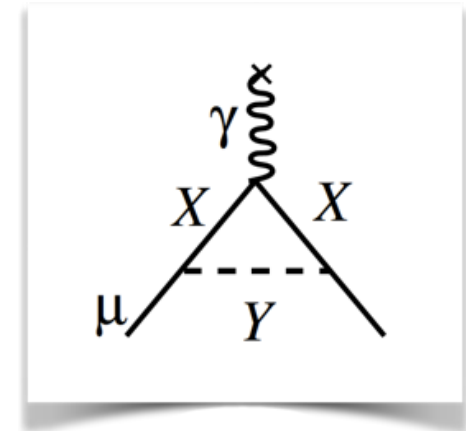
$$a_\mu = a_{\text{QED}} + a_{\text{weak}} + a_{\text{hadron}} + a_{\text{BSM}}$$

- Comparison with electron $g-2$

$$\Delta a_1^{\text{BSM}} \propto \frac{g_{\text{BSM}}}{16\pi^2} \frac{(\text{lepton mass})^2}{(\text{new particle mass})^2}$$

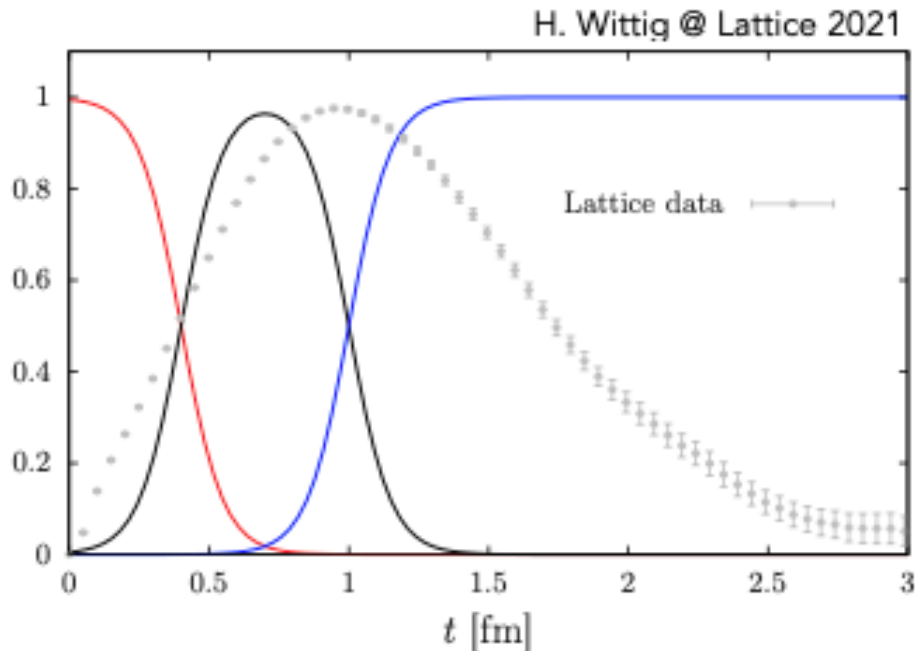
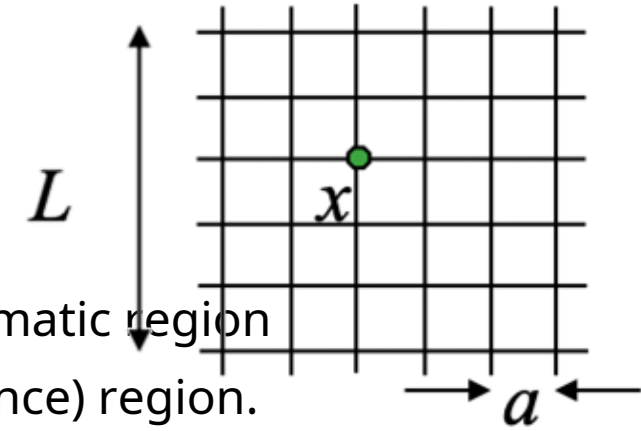
$$\left(\frac{m_\mu}{m_e}\right)^2 = \left(\frac{105 \text{ MeV}}{0.5 \text{ MeV}}\right)^2 \approx 43000$$

- Muon $g-2$ is ~43000 more sensitive to new physics compared to electron $g-2$

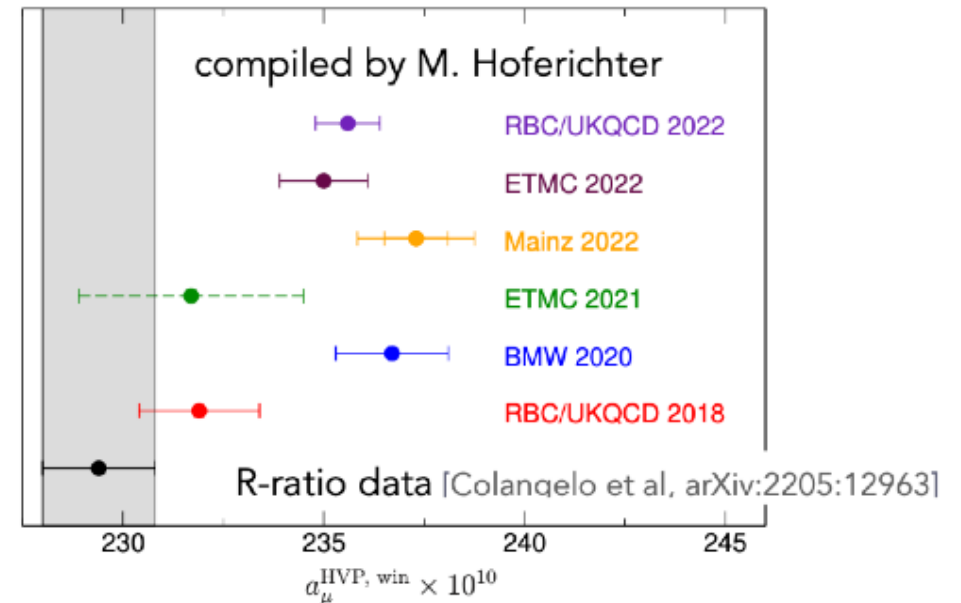


Lattice approach

- First principal calculation by discretizing Euclidian space-time
- BMW is presently the only sub 1% (HVP) lattice calculation in the full kinematic region
- Cross-checks performed by other groups but only **in limited** (30%) (distance) region.

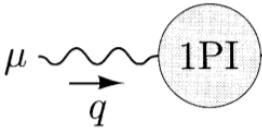


A. El-Khadra, P5 town hall, 21-24 Mar 2023

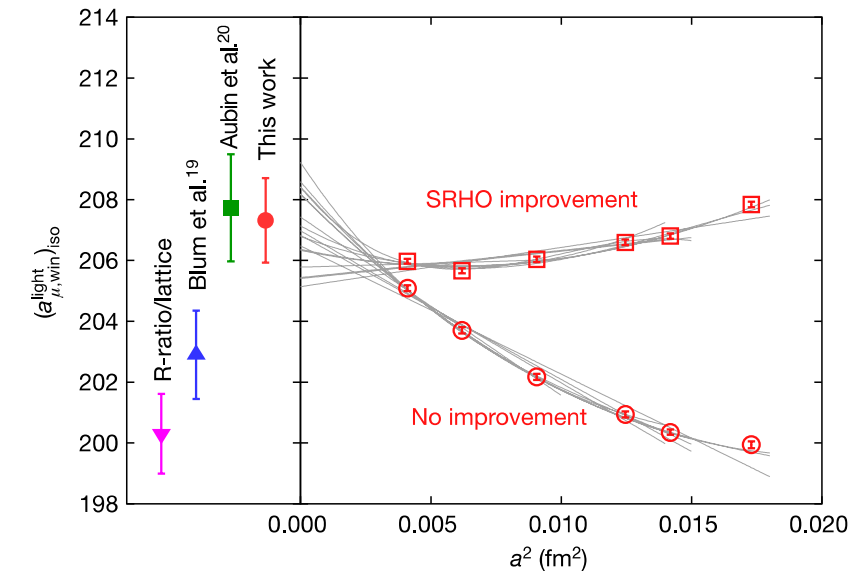
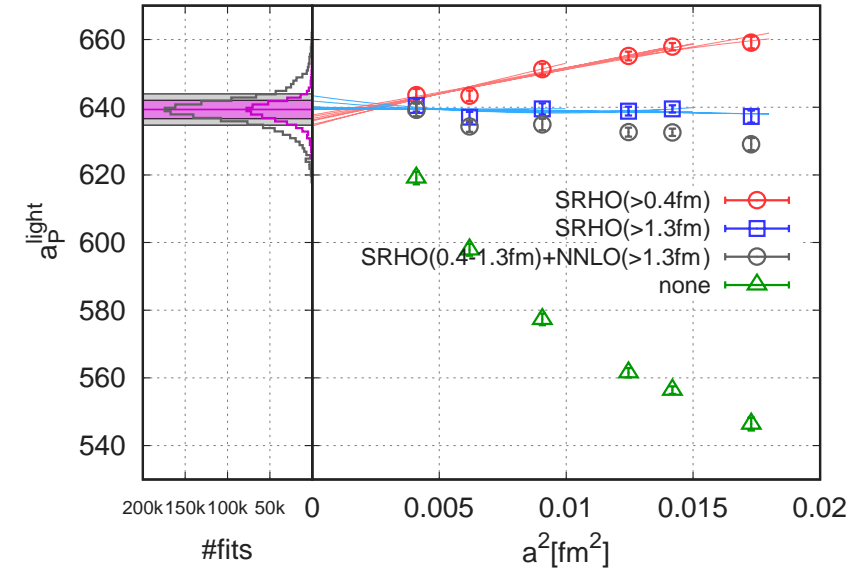


Lattice approach

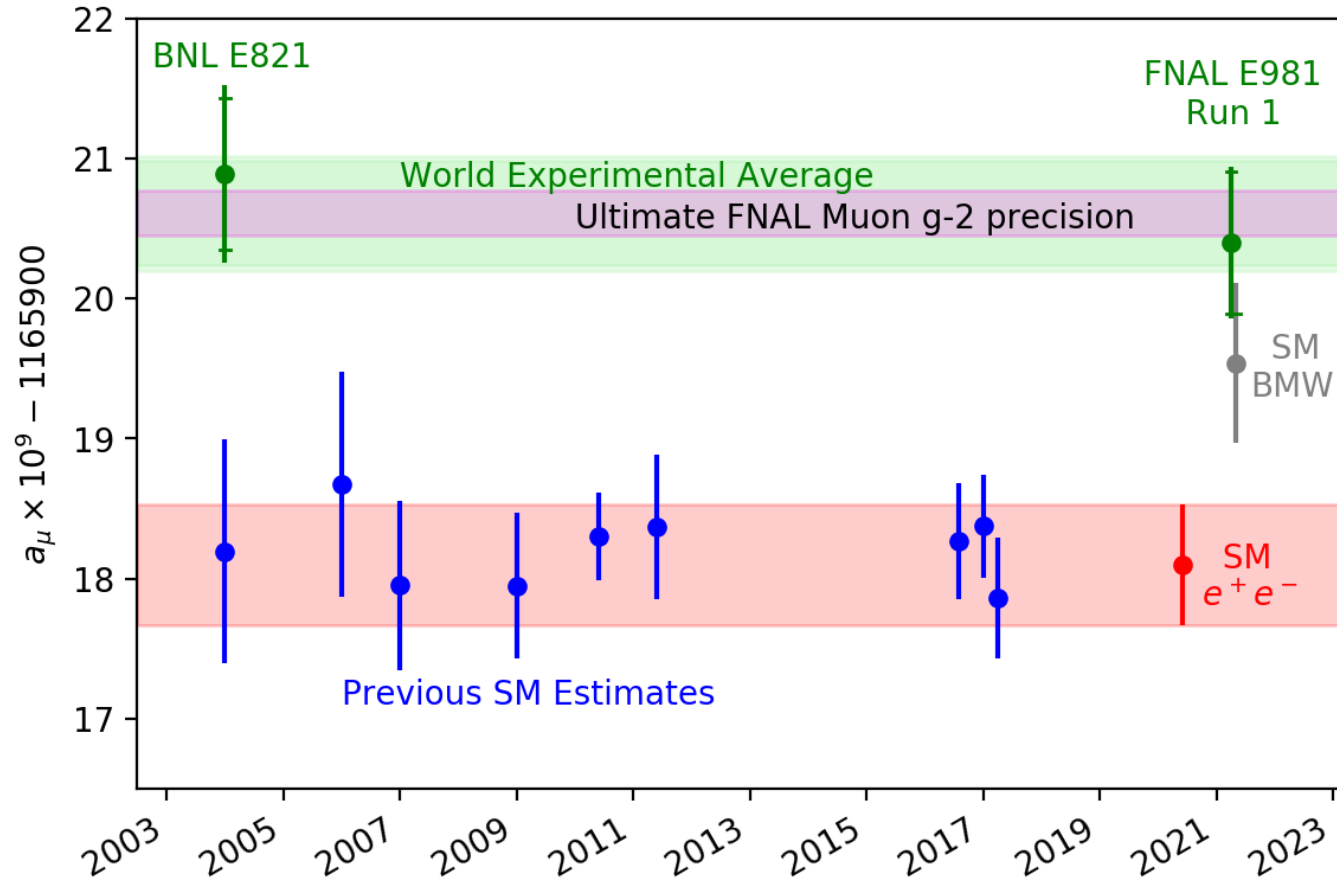
- BMW20: First sub% calculation of HVP contribution on lattice
- Calculation of “1 particle Irreducible diagrams”

- Large s  $\equiv i\Pi^{\mu\nu}(q)$, **1PI**

- upper right panel: limit and uncertainty estimation
- lower right panel: limit for central window compared to other lattice and data-driven results



The Muon g-2 Puzzle



- Long standing discrepancy between theory calculation and experimental result
- Uncertainty in theory calculation dominated by calculation of hadronic vacuum polarization

Extracting a_μ

Anchor B , e and m_μ to other high-precision measurements and calculations

$$a_\mu = \frac{\omega_a}{\tilde{B}} \frac{m_\mu}{e} = \frac{\omega_a}{\tilde{\omega}'_p(T_r)} \frac{\mu'_p(T_r)}{\mu_e(H)} \frac{\mu_e(H)}{\mu_e} \frac{m_\mu}{m_e} \frac{g_e}{2}$$

$$\tilde{B} = \frac{\hbar \tilde{\omega}'_p}{2\mu'_p}$$

Measure magnetic field with NMR
 → proton spin-precession

10.5 ppb uncertainty
 exact

22 ppb uncertainty
 0.13 ppt uncertainty

25 ppb total external uncertainty

Metrologia 13, 179 (1977)

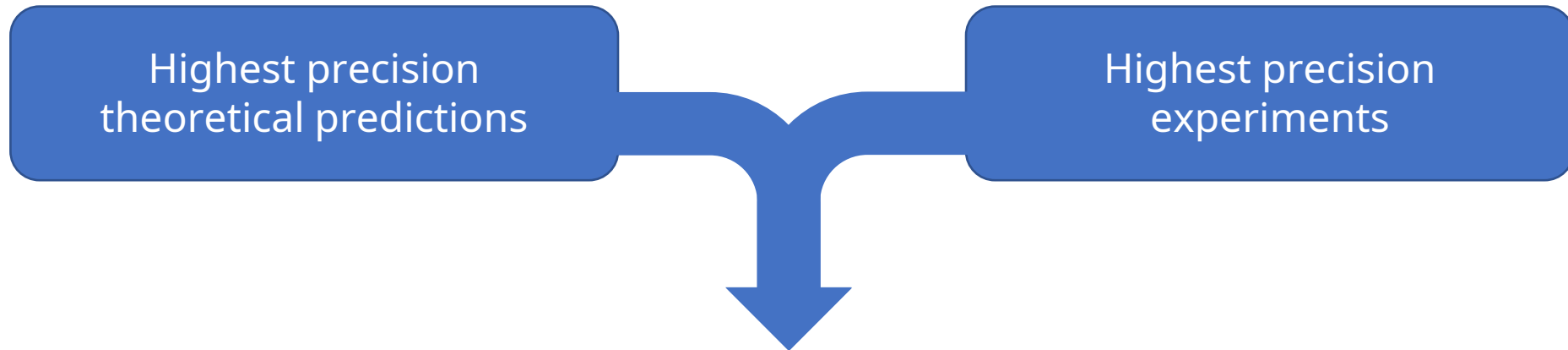
Rev. Mod. Phys. 88, 035009 (2016)

Phys. Rev. Lett. 82, 11 (1999)

Phys. Rev. Lett. 130, 071801 (2023) / CODATA

Why is Muon $g-2$ a good test of the SM?

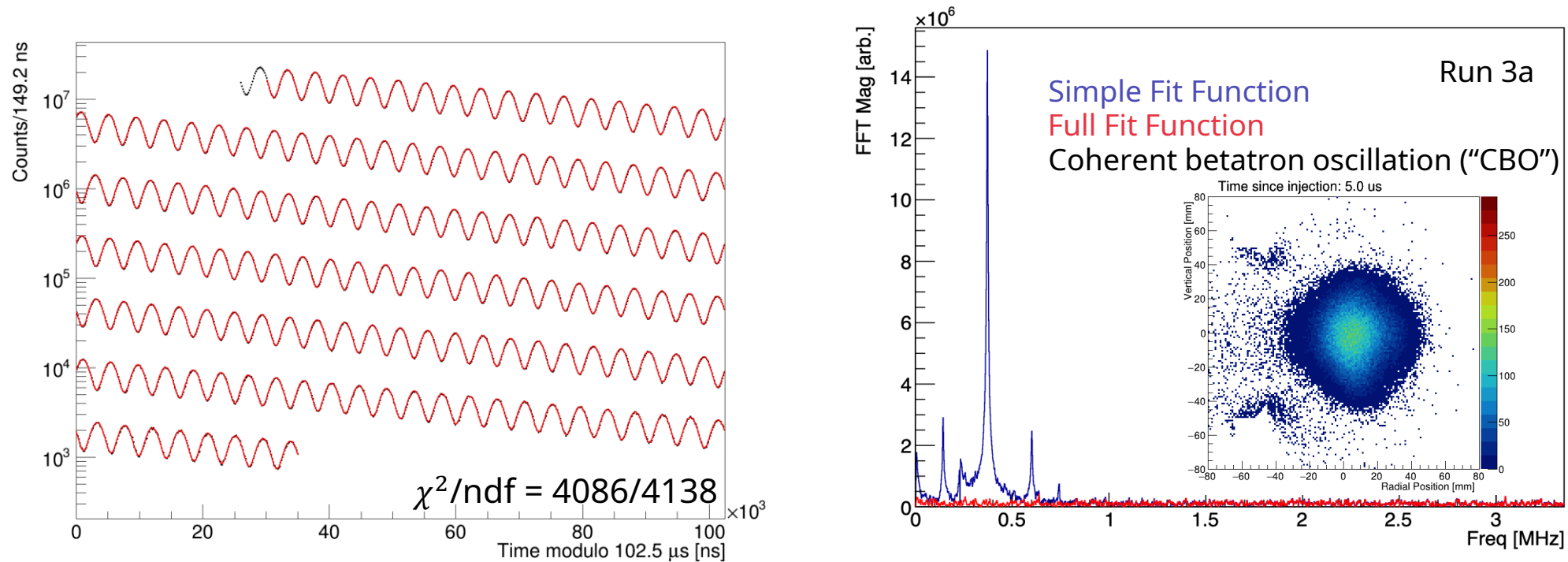
From a theoretician's point of view, the muon is a very clean system in which highest precision predictions are achievable!



“They allow for high-precision tests!”

Fitting the “wobble” plot

$$f(t) \propto \langle N \rangle_{\text{thresh}} e^{-\frac{t}{\gamma\tau}} [1 + \langle A \rangle_{\text{thres}} \cos(\omega_a t - \langle \phi \rangle_{\text{thres}})]$$

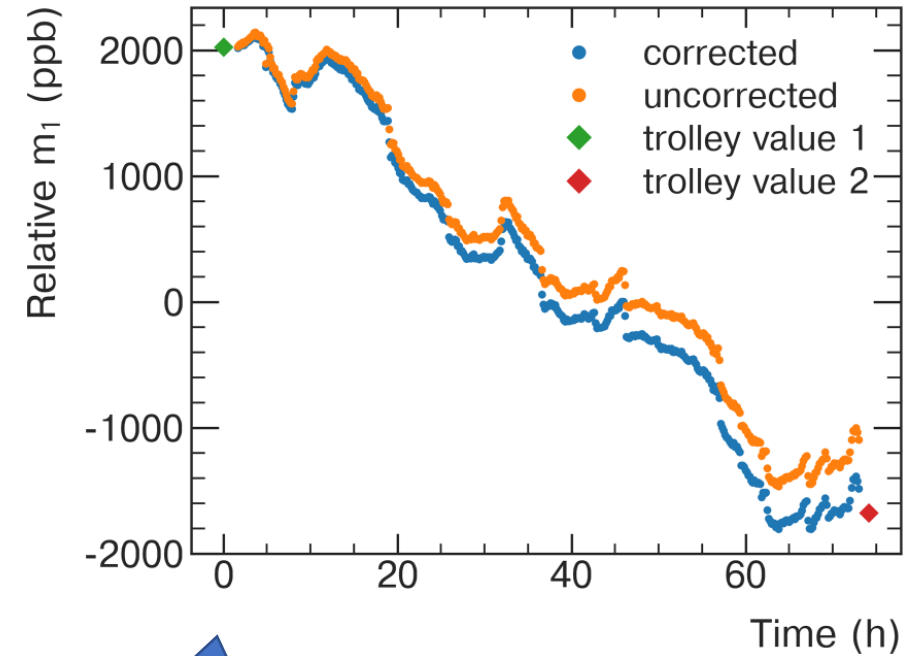
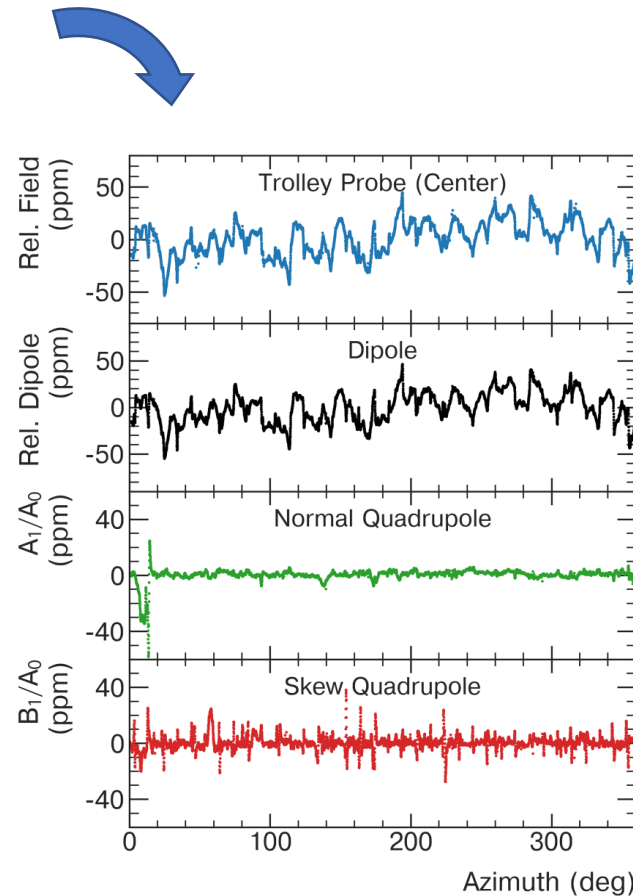
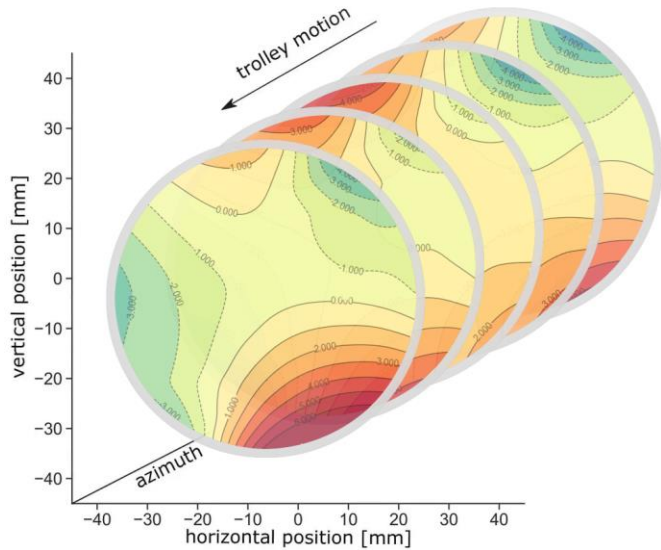


Any time dependent phase shift will bias the frequency

19 different analysis from 7 independent groups
 Account for complex beam dynamics ~27 free parameters in fit

Magnetic field tracking

Spatial distribution described by multipole expansion

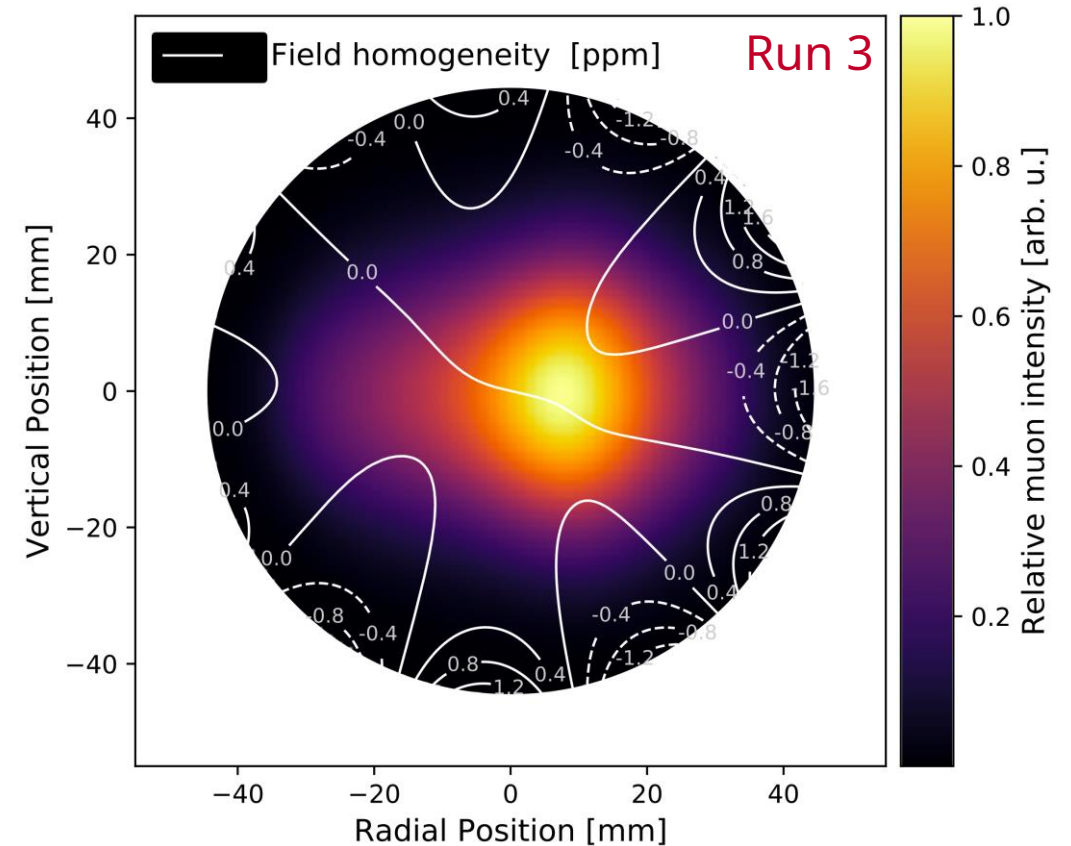


time interpolation
using fixed probe data

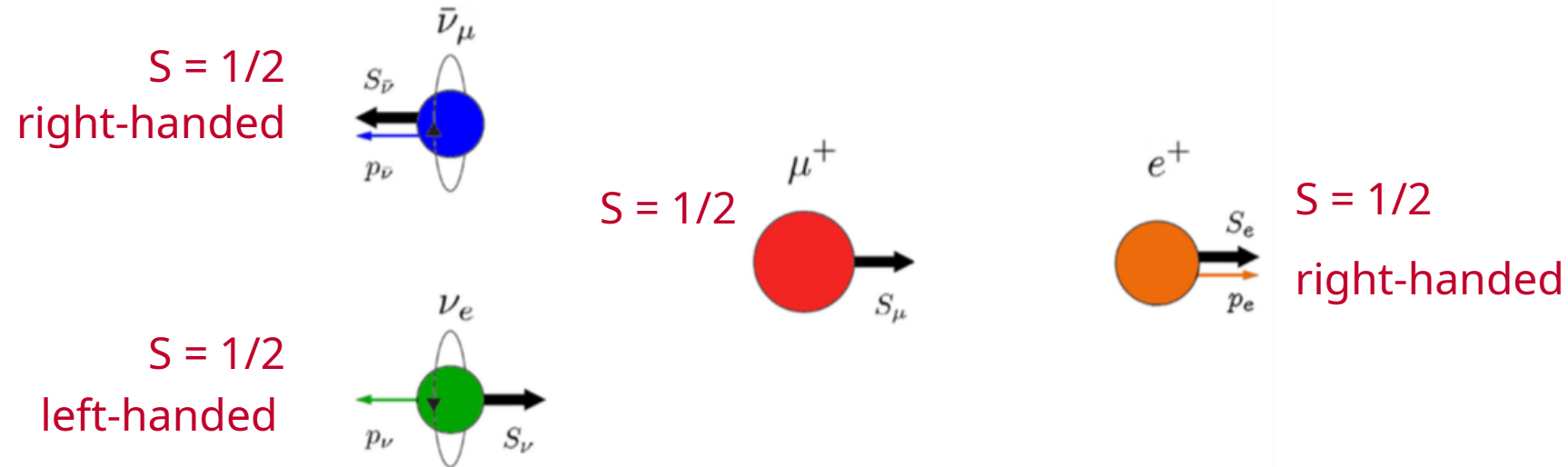
Muon weighted magnetic field

- We need the field seen by the muons
- Tracking magnetic field multipole moments
- Muon distribution given by tracker data and beam dynamics simulation

$$\frac{\omega_a}{\tilde{\omega}'_p} = \frac{f_{\text{clock}} \omega_a^{\text{meas}} (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{\text{calib}} \langle M(x, y, \phi) \omega'_p(x, y, \phi) \rangle (1 + B_k + B_q)}$$



Spin projection detection



Muon decay described by weak force \rightarrow parity violation

Maximum positron energy $\cong 52.8$ MeV

Positron emitted preferably in direction of muon spin!

Relativistic muon in magnetic & electric fields

$$\vec{\omega}_a = \vec{\omega}_s - \vec{\omega}_c = \frac{e}{m} \left[a_\mu \vec{B} - a_\mu \left(\frac{\gamma}{\gamma + 1} \right) (\vec{\beta} \cdot \vec{B}) \vec{\beta} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

non-relativistic limit

electron motion
non-perpendicular
to magnetic field

cyclotron motion assumed motion
perpendicular to magnetic field

pitch of electron

relativistically generated
motional magnetic field

proportional to electric field

$$a_\mu^{SM} = 116591810(43) \times 10^{-11}$$

disappears for $\gamma \approx 29.3$

magic momentum

$$p_\mu = 3.094 \text{ GeV}/c$$

Muon decay in rest frame

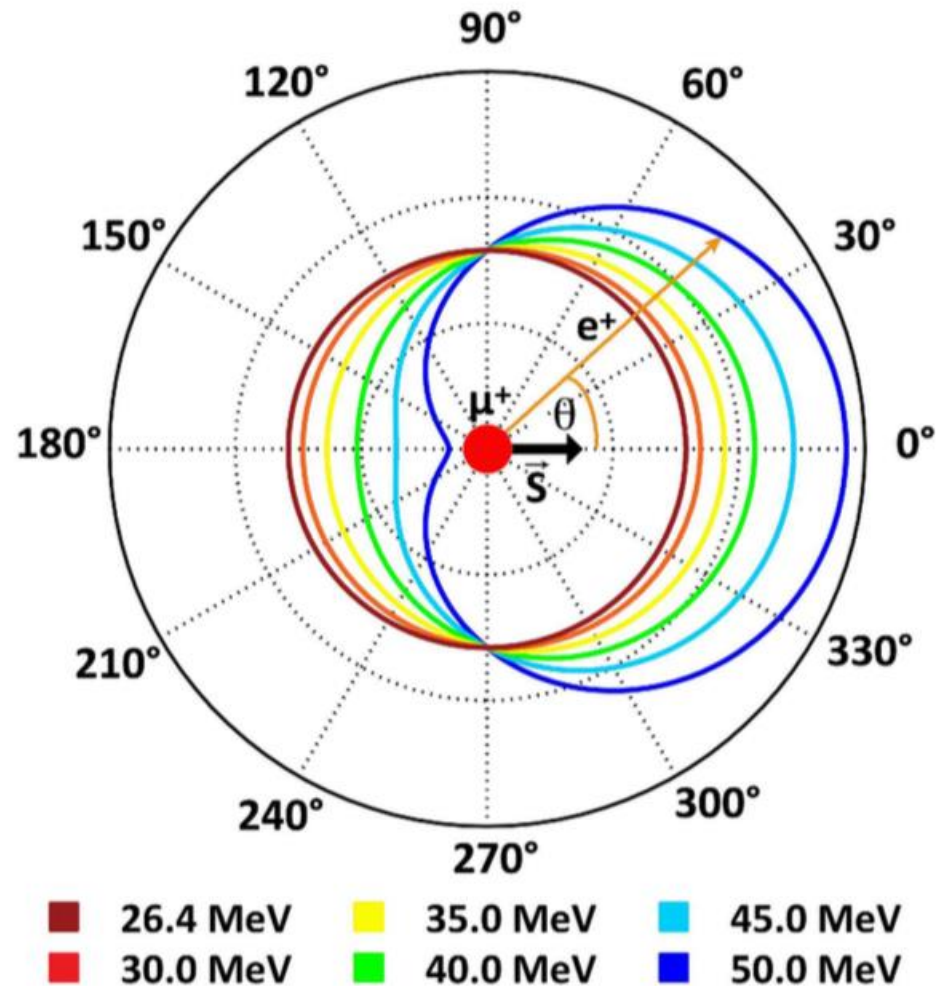


Figure credit: K.S. Khaw, PhD thesis, ETHZ, 2015

Angular differential decay distribution is energy dependent

$$N_e(\theta, E_e) \propto 1 - A(E_e) \cos \theta$$

$$A(E_e) = \frac{E_e^{\max} - 2E_e}{3E_e^{\max} - 2E_e}$$

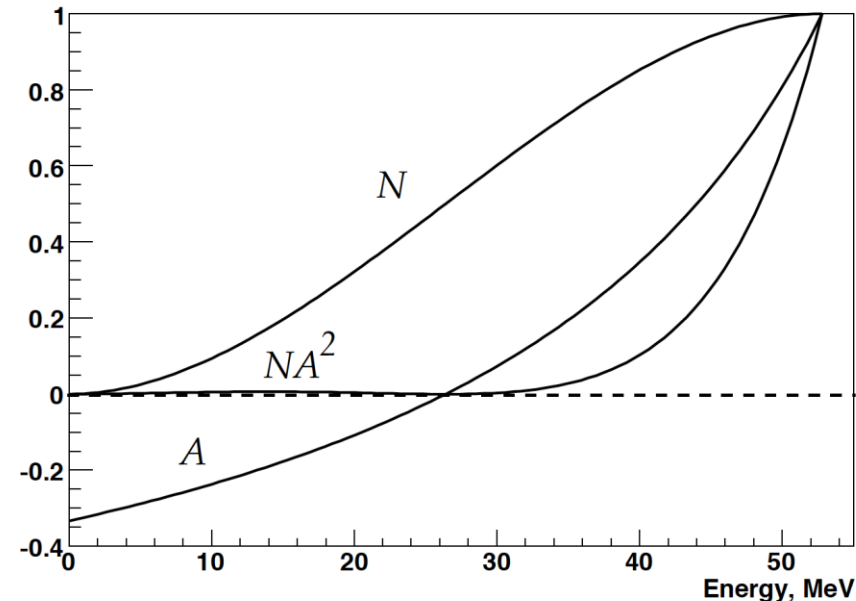


Figure: L. Roberts and W. Marciano, Lepton Dipole Moments

Magnetic field tracking

Trolley system

17 NMR probes

pulled through ring every ~3 days

measures spatial field dist. in storage region

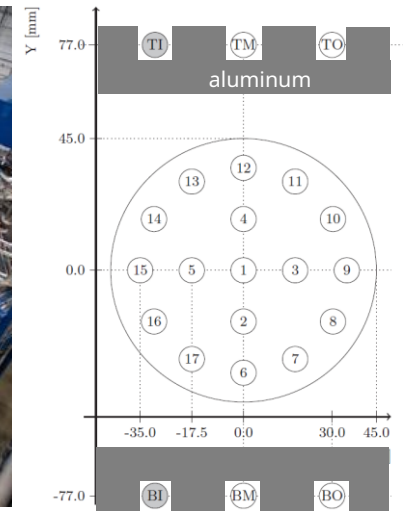


Fixed probe system

72 azimuthal location (stations)

tracks field drift 24/7

measures field differences (drift)



Muon Campus at Fermilab

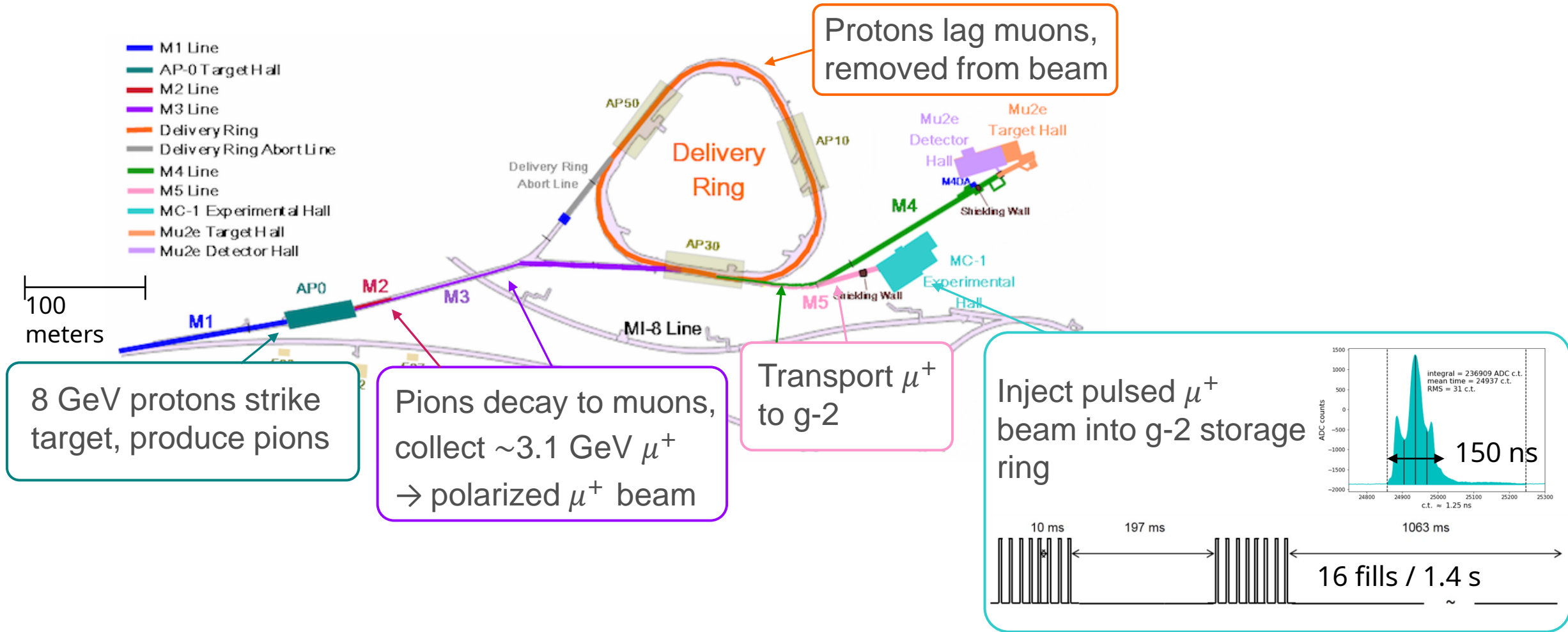


M. Fertl
R. Reimann

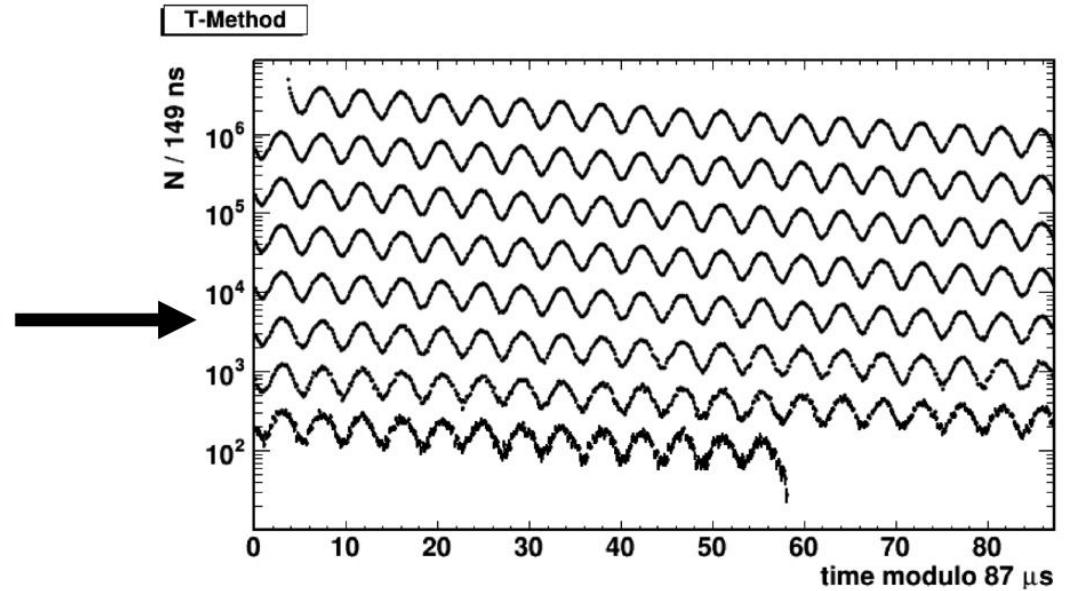
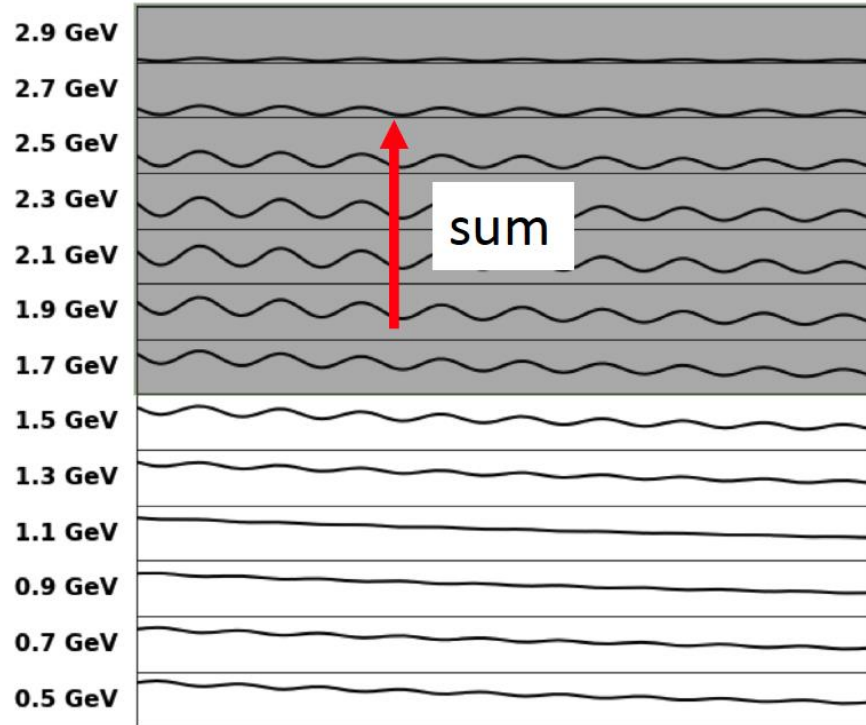
- Accelerating protons to 8 GeV
- Form 8 bunches
- Pion production in fixed target
- Pion decay to muons (95% polarization)
- Muons outrun protons
- Muon $g-2$ experimental hall

Producing the muon beam

~2.5 km beamline consisting of magnetic lenses and steering elements



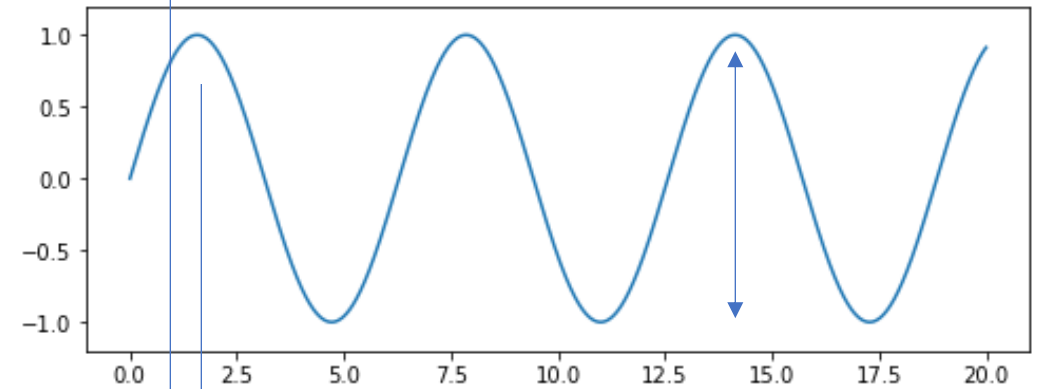
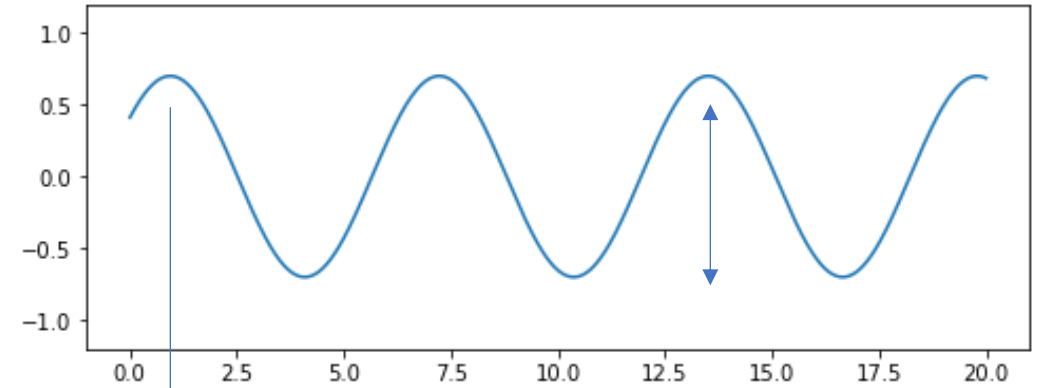
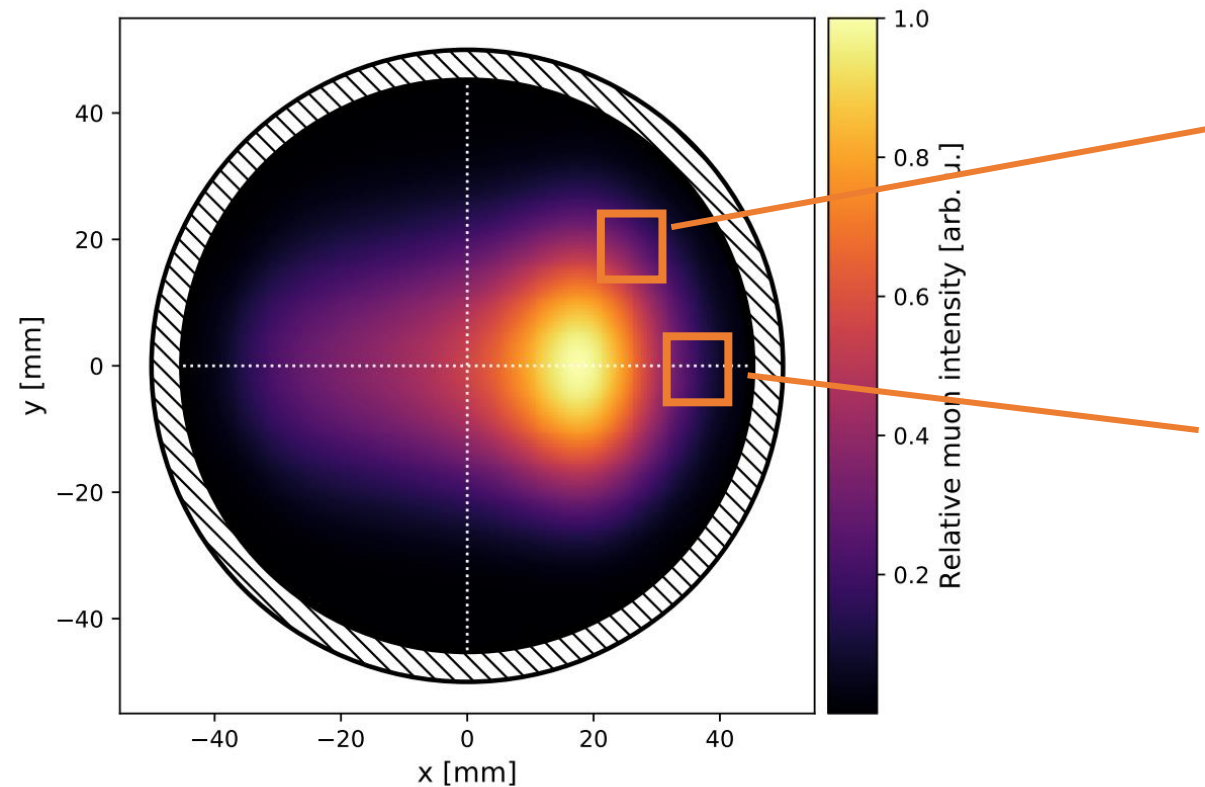
The “wiggle” plot



$$N(t) = N_0(E) e^{-\frac{t}{\gamma\tau}} [1 + A(E) \cos(\omega_a t - \phi(E))]$$

Exponential decay from muon lifetime modulated with $\omega_a = a_\mu \frac{e}{m_\mu} B$

Phase acceptance

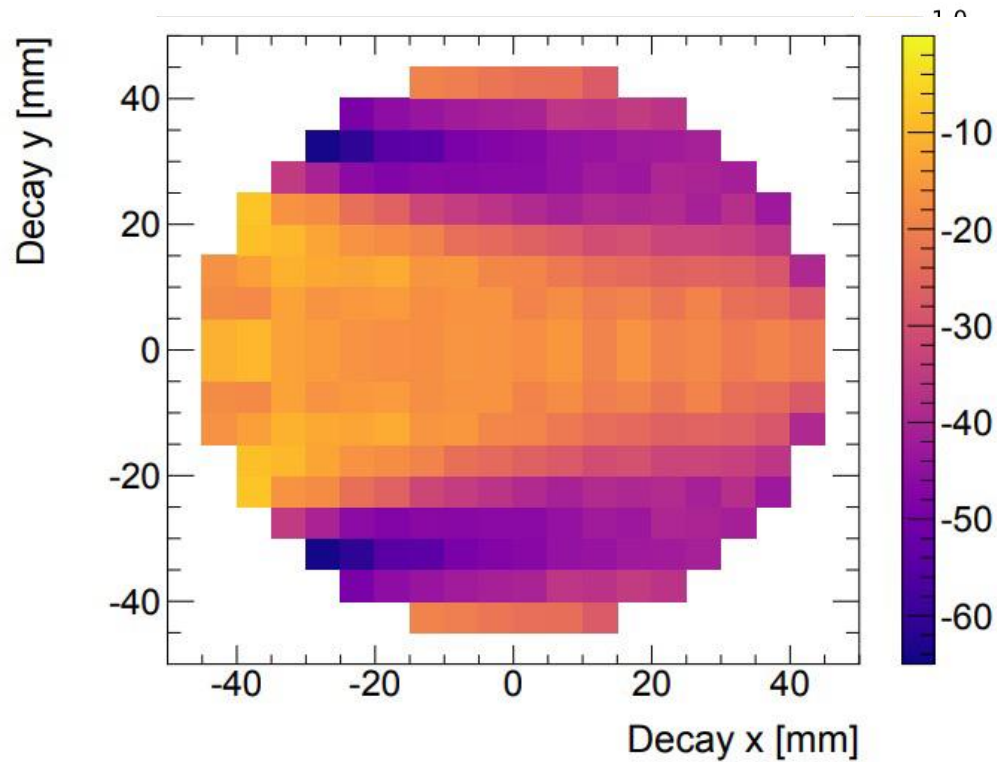


Phase shift

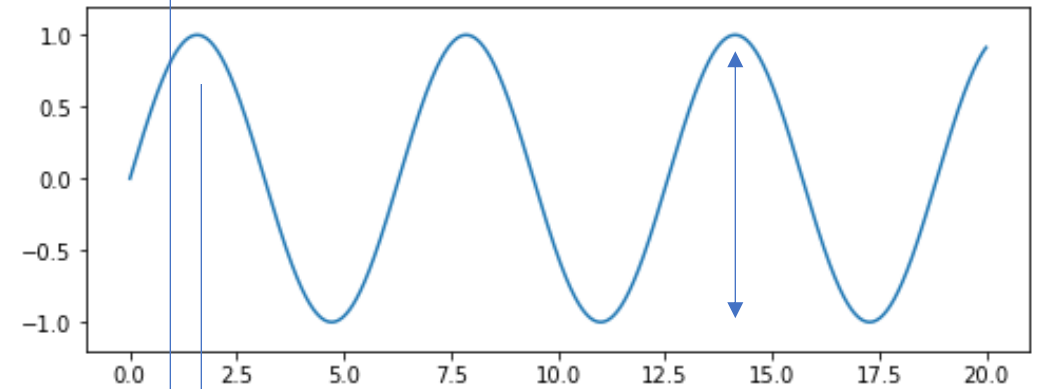
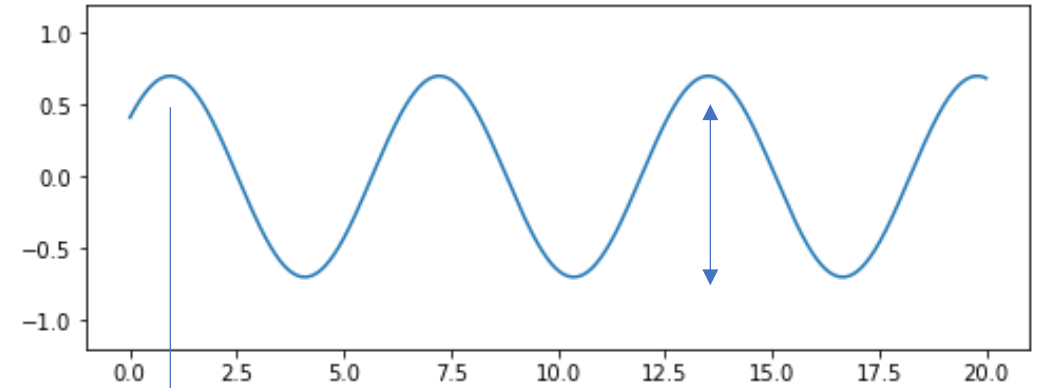
Asymmetry
difference

Depends on energy and time
Beam profile must be well-understood during measurement period

Phase acceptance



Detected Phase [mrad]



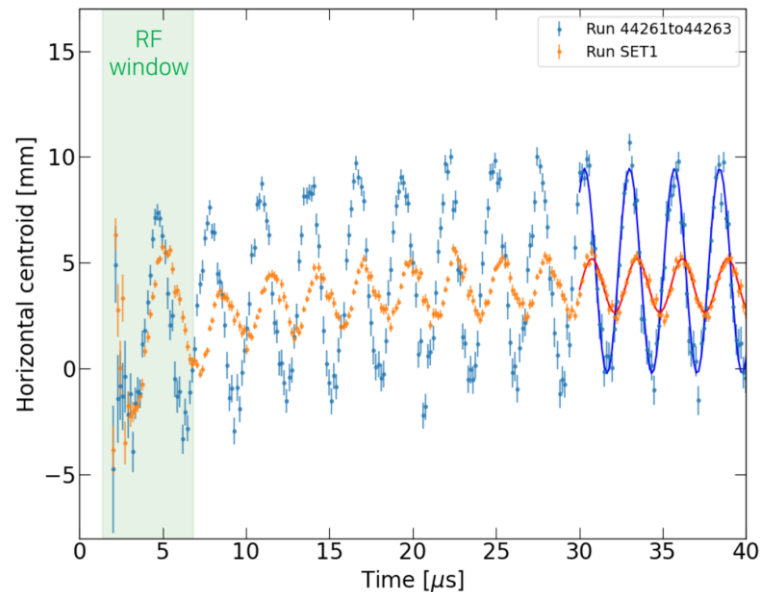
Phase shift

Asymmetry
difference

Depends on energy and time
Beam profile must be well-understood during measurement period

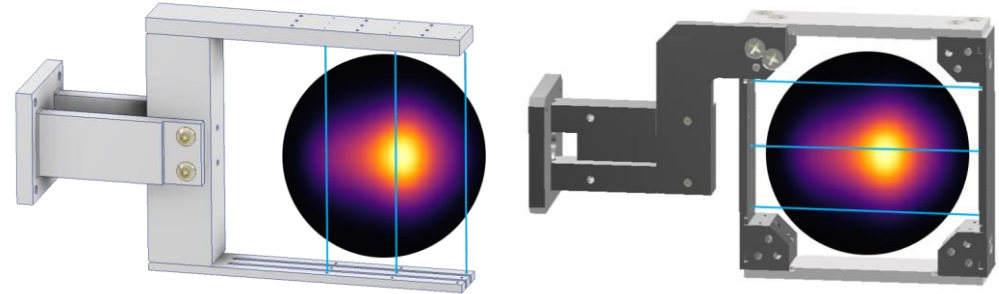
Further improvements

Improved Running Conditions



Quadrupole RF system (Run-5/6)
reduced horizontal beam oscillations

Systematic Measurements & Studies



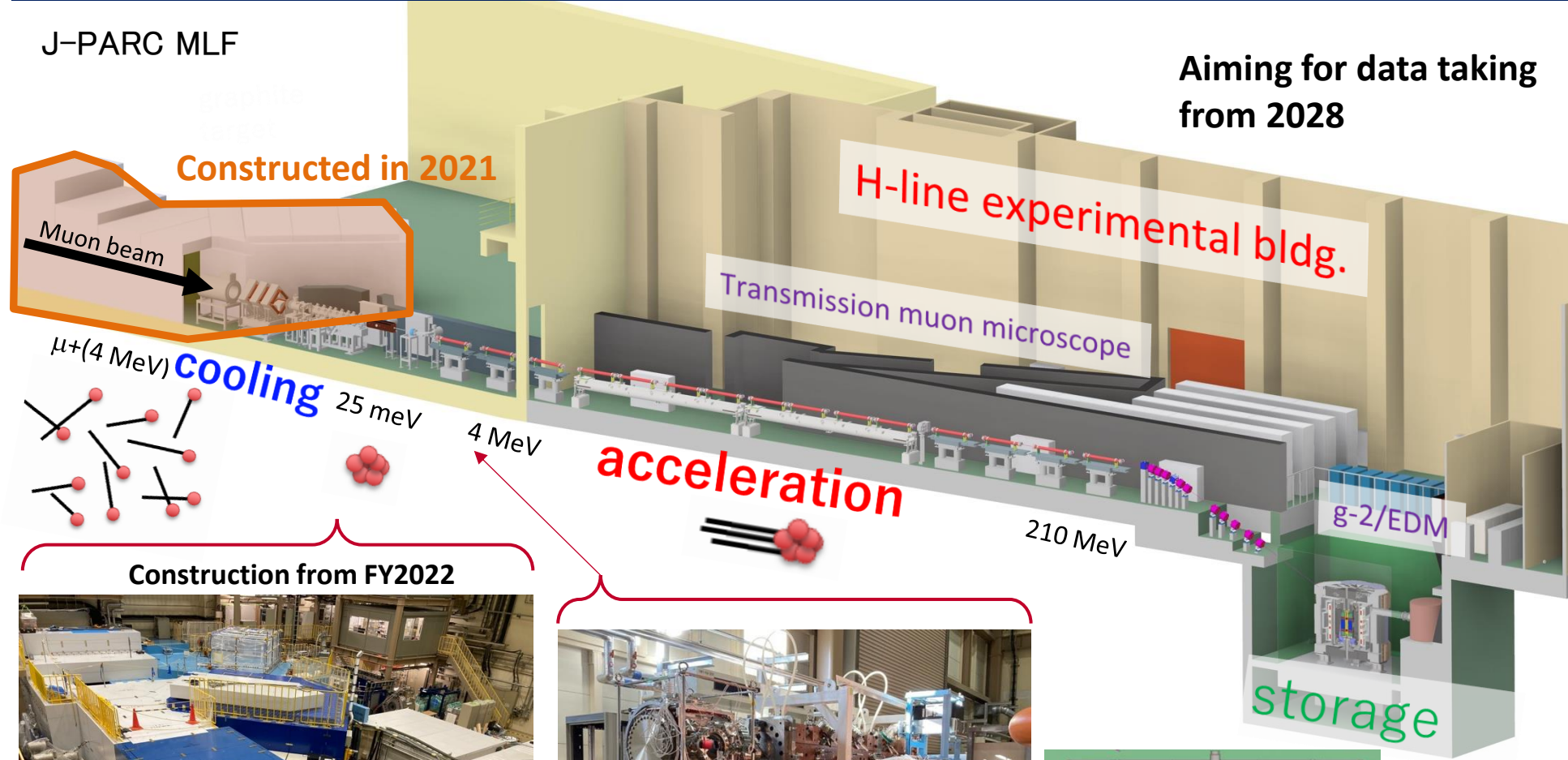
New detectors (scintillating fibers)
for direct beam measurements (Run-6)

Better understanding and modeling
of beam dynamics

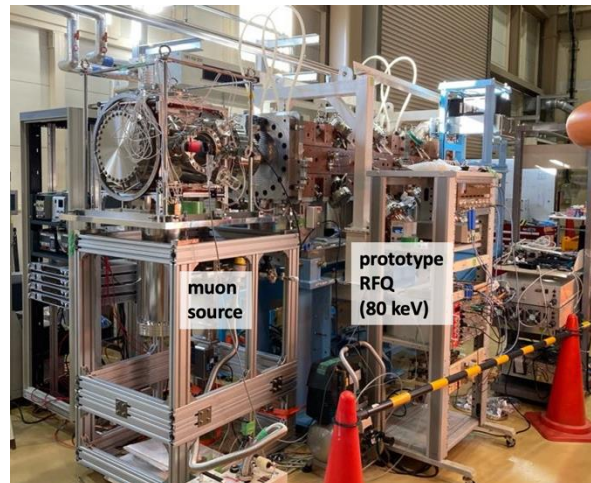
J-PARC muon g-2/EDM experiment

J-PARC MLF

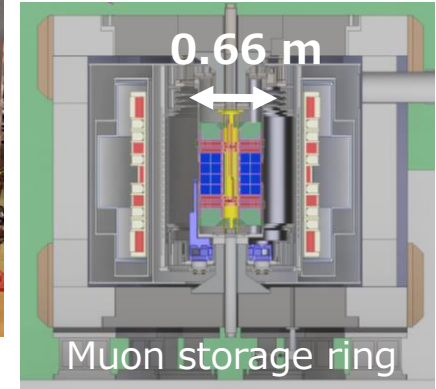
Aiming for data taking from 2028



Shields, area control (2022)



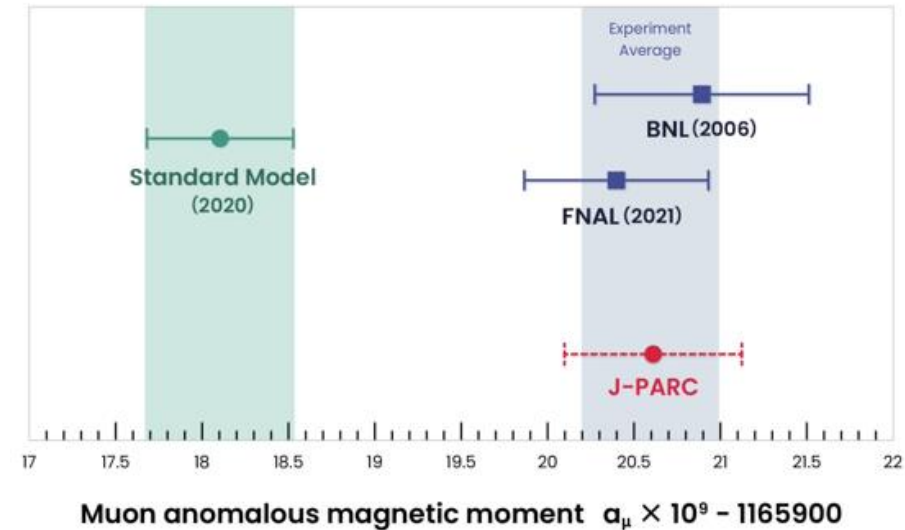
RF Acc. Test at S2 area (May 2023)



Muon storage ring

J-PARC Experiment

- Complementary technique
 - μ beam accelerated from rest
 - no E fields
 - smaller magnet
- Aiming for a result comparable to Run-1 result towards the end of the decade

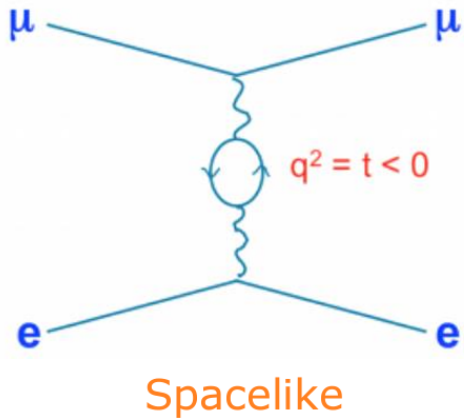


- Under construction aiming for data taking from 2028.
- Succeeded to deliver a surface muon beam to H-line.
- Constructed the experimental area for muon cooling and the first stage of the acceleration.
- Currently taking data to demonstrate the muon cooling by using the laser ionization of muonium, followed by RF acceleration tests.

New method to measure $\alpha_{\mu}^{HVP, LO}$



Muon-electron scattering $\mu e \rightarrow \mu e$



$$\frac{d\sigma}{dt} = \frac{d\sigma_0}{dt} \left| \frac{\alpha(t)}{\alpha(0)} \right|^2$$

Effective Born cross-section

VP effects in leading photon t-channel incorporated in the running of α

$$\alpha(t) = \frac{\alpha}{1 - \Delta\alpha(t)}$$

$$\Delta\alpha = \Delta\alpha_{lep} + \Delta\alpha_{had}$$

$$\alpha_{\mu}^{HLO} = \frac{\alpha_0}{\pi} \int_0^1 dx (1-x) \Delta\alpha_{had}[t(x)]$$

Leading-order hadronic contribution can be directly inferred by measuring the shape of the $\mu e \rightarrow \mu e$ cross-section

S. Charity

181 collaboration members worldwide



US Universities

- Boston
- Cornell
- UIUC
- James Madison
- Kentucky
- Massachusetts
- Michigan
- Michigan State
- Mississippi
- North Central College
- Regis
- Virginia
- Washington

US National Labs

- Argonne
- Brookhaven
- Fermilab



China

- Shanghai Jiao Tong



Germany

- Dresden
- Mainz



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- Frascati
- Molise
- Naples
- Pisa
- Roma Tor Vergata
- Trieste
- Udine



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