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Lepton number violation and neutrino masses in *N*_RSMEFT

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- → What type of UV models give rise to LNV interactions in NRSMEFT?
- → What is the connection between LNV operators and Majorana masses for active neutrinos?
- → Can we derive any constraints on the operators from neutrino masses?

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Opening up *N*_R**SMEFT**

N_R**SMEFT**

SMEFT extended with invariant operators containing RH neutrinos:

• Following a diagrammatic procedure

NRSMEFT operators

d=6

	$\psi^2 H^3$ (+h.c.)		$(\overline{R}R)(\overline{R}R)$	$(\overline{L}L)(\overline{R}R)$		
\mathcal{O}_{LNH^3}	$(\overline{L}N_R)\tilde{H}(H^{\dagger}H)$	$\mathcal{O}_{NN} (\overline{N_R}\gamma^\mu N_R)(\overline{N_R}\gamma_\mu N_R)$		\mathcal{O}_{LN}	$(\overline{L}\gamma^{\mu}L)(\overline{N_R}\gamma_{\mu}N_R)$	
1	$\psi^2 H^2 D$ (+h.c.)	\mathcal{O}_{eN}	$(\overline{e}_R \gamma^\mu e_R) (\overline{N_R} \gamma_\mu N_R)$	\mathcal{O}_{QN}	$(\overline{Q}\gamma^{\mu}Q)(\overline{N_R}\gamma_{\mu}N_R)$	
\mathcal{O}_{NH^2D}	$(\overline{N_R}\gamma^\mu N_R)(H^\dagger i\overleftrightarrow{D_\mu}H)$	\mathcal{O}_{uN}	$(\overline{u}_R \gamma^\mu u_R)(\overline{N_R} \gamma_\mu N_R)$	(\overline{L})	$R)(\overline{L}R)$ (+h.c.)	
\mathcal{O}_{NeH^2D}	$(\overline{N_R}\gamma^\mu e_R)(\tilde{H}^\dagger i D_\mu H)$	\mathcal{O}_{dN}	$(\overline{d}_R \gamma^\mu d_R) (\overline{N_R} \gamma_\mu N_R)$	\mathcal{O}_{LNLe}	$(\overline{L}N_R)\epsilon(\overline{L}e_R)$	
(7	$(\overline{L}R)(\overline{R}L) $ (+h.c.)	\mathcal{O}_{duNe}	$(\overline{d}_R\gamma^\mu u_R)(\overline{N_R}\gamma_\mu e_R)$	$(\overline{d}_R \gamma^\mu u_R) (\overline{N_R} \gamma_\mu e_R) O_{LNQd} (\overline{L}N_R)$		
\mathcal{O}_{QuNL}	$(\overline{Q}u_R)(\overline{N_R}L)$	\mathcal{O}_{NNNN}	$(\overline{N_R^c}N_R)(\overline{N_R^c}N_R)$	\mathcal{O}_{LdQN}	$(\overline{L}d_R)\epsilon(\overline{Q}N_R)$	

Generated @ loop level:

neutrino magnetic moment operators [2405.08877] RB, Bolton, Deppisch, Hati, Hirsch

$\psi^2 HX(+h.c.)$						
\mathcal{O}_{NB}	$g_1(\overline{L}\sigma_{\mu\nu}N)\tilde{H}B^{\mu\nu}$					
${\cal O}_{NW}$	$g_2(\overline{L}\sigma_{\mu\nu}N)\tau^I\tilde{H}W^{I\mu\nu}$					

NRSMEFT operators

d=7, $\Delta L = 2$

 $L(N_R) = 1$

$\psi^2 H^3 D$			$\psi^4 H$	$\psi^4 H$		
0	$\epsilon_{ij}(\overline{N_R^c}\gamma_\mu L^i)(iD^\mu H^j)(H^\dagger H)$	\mathcal{O}_{LNLH}	$\epsilon_{ij}(\overline{L}\gamma_{\mu}L)(\overline{N_{R}^{c}}\gamma^{\mu}L^{i})H^{j}$	\mathcal{O}_{LNeH}	$(\overline{L}N_R)(\overline{N_R^c}e_R)H$	
O_{NLH^3D}	$\epsilon_{ij}(\overline{N_R^c}\gamma_{\mu}L^i)H^j(H^{\dagger}i\overleftrightarrow{D^{\mu}}H)$	Oonuu	$\epsilon_{ij}(\overline{Q}\gamma_{\mu}Q)(\overline{N_{R}^{c}}\gamma^{\mu}L^{i})H^{j}$	\mathcal{O}_{eLNH}	$H^{\dagger}(\overline{e_R}L)(\overline{N_R^c}N_R)$	
$\psi^2 H^2 D^2$		UQNLH	$\epsilon_{ij}(\overline{Q}\gamma_{\mu}Q^{i})(\overline{N_{R}^{c}}\gamma^{\mu}L^{j})H$	\mathcal{O}_{QNdH}	$(\overline{Q}N_R)(\overline{N_R^c}d_R)H$	
$\mathcal{O}_{NeH^2D^2}$	$\epsilon_{ij}(\overrightarrow{N_R^c} \overset{\longleftrightarrow}{D_\mu} e_R)(H^i D^\mu H^j)$	\mathcal{O}_{eNLH}	$\epsilon_{ij}(\overline{e_R}\gamma_\mu e_R)(\overline{N_R^c}\gamma^\mu L^i)H^j$	\mathcal{O}_{dQNH}	$H^{\dagger}(\overline{d_R}Q)(\overline{N_R^c}N_R)$	
Ouropa	$(\overrightarrow{N_R^c}\overleftrightarrow{\partial_\mu}N_R)(H^\dagger\overleftrightarrow{D^\mu}H)$	\mathcal{O}_{dNLH}	$\epsilon_{ij}(\overline{d_R}\gamma_\mu d_R)(\overline{N_R^c}\gamma^\mu L^i)H^j$	\mathcal{O}_{QNuH}	$(\overline{Q}N_R)(\overline{N_R^c}u_R)\tilde{H}$	
$\mathcal{O}_{NH^2D^2}$	$(\overline{N_R^c}N_R)(D_\mu H)^\dagger D^\mu H$	\mathcal{O}_{uNLH}	$\epsilon_{ij}(\overline{u_R}\gamma_\mu u_R)(\overline{N_R^c}\gamma^\mu L^i)H^j$	\mathcal{O}_{uQNH}	$\tilde{H}^{\dagger}(\overline{u_R}Q)(\overline{N_R^c}N_R)$	
$\psi^2 H^2 X$		\mathcal{O}_{duNLH}	$\epsilon_{ij}(\overline{d_R}\gamma_\mu u_R)(\overline{N_R^c}\gamma^\mu L^i)\tilde{H}^j$	\mathcal{O}_{LNNH}	$(\overline{L}N_R)(\overline{N_R^c}N_R)\tilde{H}$	
\mathcal{O}_{NeH^2W}	$(\epsilon \tau^{I})_{ij} (\overline{N_{R}^{c}} \sigma^{\mu\nu} e_{R}) (H^{i} H^{j}) W^{I}_{\mu\nu}$	\mathcal{O}_{dQNeH}	$\epsilon_{ij}(\overline{d_R}Q^i)(\overline{N_R^c}e_R)H^j$	\mathcal{O}_{NLNH}	$\tilde{H}^{\dagger}(\overline{N_R}L)(\overline{N_R^c}N_R)$	
\mathcal{O}_{NH^2B}	$(\overline{N_R^c}\sigma^{\mu\nu}N_R)(H^{\dagger}H)B_{\mu\nu}$	(Do y y	$(\overline{Q}u_R)(\overline{N_R^c}e_R)H$		$\psi^2 H^4$	
\mathcal{O}_{NH^2W}	$(\overline{N_R^c}\sigma^{\mu\nu}N_R)(H^\dagger\tau^I H)W^I_{\mu\nu}$	♥QuNeH	$(\overline{Q}\sigma_{\mu\nu}u_R)(\overline{N_R^c}\sigma^{\mu\nu}e_R)H$	\mathcal{O}_{NH^4}	$(\overline{N_R^c}N_R)(H^{\dagger}H)^2$	

Missing those generated @ loop level

Diagrammatic method



Diagrammatic method



[1204.5862] Bonnet, Hirsch, Ota, Winter [2009.13537] Gargalionis, Volkas [2207.13714] Cepedello, Esser, Hirsch, Sanz

Particle dictionary

	Sca	ılars										
Na	me	S	\mathcal{S}_1	φ	Ξ	Ξ_1	ω_1	ω_2	2 П]	Π_7	ζ
Irre	ер (1	1, 1, 0)	(1, 1, 1)	$\left(1,2,\frac{1}{2}\right)$	(1,3,0)	(1,3,1)	$(3, 1, -\frac{1}{3})$	$\left(\frac{1}{3}\right)$ $\left(3,1\right)$	$,\frac{2}{3})$ (3, 2	$\left(\frac{1}{6}\right)$ $\left(3, \frac{1}{6}\right)$	$2, \frac{7}{6}$) (3	$,3,-rac{1}{3}ig)$
			Fermi	ons								
		Na	ime J	V	E	Δ_1	Δ_3	Σ	Σ_1			
		Irr	ep $(1,$	(1,0) (1,1)	(1, -1) (1	$(2, -\frac{1}{2})$	$\left(1,2,-\frac{3}{2}\right)$	(1, 3, 0)	(1, 3, -	1)		
		Na	ime l	J	D	Q_1	Q_5	Q_7	T_1	T_2	2	
		Irr	ep (3, 2)	$\left(1,\frac{2}{3}\right)$ $\left(3,1\right)$	$(,-\frac{1}{3})$ ($3, 2, \frac{1}{6}$	$\left(3,2,-\frac{5}{6}\right)$	$(3, 2, \frac{7}{6})$) (3, 3, -	$\frac{1}{3}$) (3, 3	$,\frac{2}{3})$	
	Vec	tors:										
Name	${\mathcal B}$	Ľ	\mathcal{S}_1	W W	\mathcal{V}_1 \mathcal{L}	1	\mathcal{L}_3	\mathcal{U}_1	\mathcal{U}_2	\mathcal{Q}_1	\mathcal{Q}_5	\mathcal{X}
Irrep	(1, 1, 0)	(1, 1)	(1, 1) (1,	(1, 3, 0) (1, 3)	3,1) (1,2	$(1, \frac{1}{2})$	$(3, -\frac{3}{2})$	$(1, -\frac{1}{3})$	$\left(3,1,\frac{2}{3}\right)$	$\left(3, 2, \frac{1}{6}\right)$	$(3, 2, -\frac{5}{6})$	$(3, 3, \frac{2}{3})$

[1711.10391] de Blas, Criado, Pérez-Victoria, Santiago "Granada Dictionary"

Dictionary for d=6

Оре	rator classes	$\square \rangle$	Diagrams		Mode	els
	$^{2/24}$.				Models	Operators
	T		\setminus /		S	$\mathcal{O}_{NN}, \mathcal{O}_{NNNN}$
				/	\mathcal{S}_1	$\mathcal{O}_{LNLe},\mathcal{O}_{eN}$
	$\psi^2 H^2 D$:	>	$\langle \rangle$	\prec	φ	$\mathcal{O}_{QuNL},\mathcal{O}_{LNLe},\mathcal{O}_{LNQd},\mathcal{O}_{LN},\mathcal{O}_{LNH^3}$
		/	·. /	Ň	ω_1	$\mathcal{O}_{LNQd},\mathcal{O}_{dN},\mathcal{O}_{duNe}$
	$\psi^2 H^3$:	>			ω_2	\mathcal{O}_{uN}
	φ ·				Π_1	$\mathcal{O}_{LNQd},\mathcal{O}_{QN}$
					Δ_1	$\mathcal{O}_{NH^2D},\mathcal{O}_{NeH^2D}$
			\prec \rightarrow		B	$\mathcal{O}_{NH^2D}, \mathcal{O}_{NN}, \mathcal{O}_{eN}, \mathcal{O}_{uN}, \mathcal{O}_{dN}, \mathcal{O}_{LN}, \mathcal{O}_{QN}$
		1	\setminus /		\mathcal{B}_1	$\mathcal{O}_{NeH^2D},\mathcal{O}_{eN},\mathcal{O}_{duNe}$
$\psi^2 H^3$	Two-particle mod	lels			\mathcal{L}_1	\mathcal{O}_{LN}
	$SS: (\mathcal{S}, \varphi), (\Xi_1$	$, \varphi), (\Xi, \varphi)$			\mathcal{U}_1	\mathcal{O}_{dN}
\mathcal{O}_{LNH^3}	$FF: (\Delta_1, \mathcal{N}), (\Delta_1, \mathcal{N})$	$\Delta_1, \Sigma_1), (\Delta$	$_{1},\Sigma)$		\mathcal{U}_2	$\mathcal{O}_{QuNL}, \mathcal{O}_{uN}, \mathcal{O}_{duNe}$
	$FS: (\mathcal{N}, \mathcal{S}), (\Delta$	$(\Delta_1, \mathcal{S}), \ (\Delta_1, \Xi)$	Ξ_1), (Σ_1, Ξ_1), (Δ_1	$, \Xi), (\Sigma, \Xi)$	\mathcal{Q}_1	$\mathcal{O}_{QuNL}, \mathcal{O}_{QN}$



Operator classes

Diagrams

Models



Explicit example: \mathcal{O}_{LNLH}

$$\mathcal{O}_{LNLH} \quad \epsilon_{ij}(\overline{L}\gamma_{\mu}L)(\overline{N_R^c}\gamma^{\mu}L^i)H^j \quad \mathbf{rec} \qquad 16 \text{ models } (SS, FS, FV)$$

$\psi^4 H$	Models
	SS : $(\mathcal{S}_1, arphi) \; (arphi, \Xi_1)$
${\cal O}_{LNLH}$	$FS : (E, \mathcal{S}_1) (\Sigma_1, \Xi_1) (\Delta_1, \mathcal{S}_1) (\Delta_1, \Xi_1) (\mathcal{N}, \varphi) (\Sigma, \varphi)$
	$FV : (\mathcal{N}, \mathcal{B}) (\Sigma, \mathcal{W}) (\mathcal{N}, \mathcal{L}_1) (\Sigma, \mathcal{L}_1) (\Delta_1, \mathcal{B}) (\Delta_1, \mathcal{W}) (E, \mathcal{L}_1) (\Sigma_1, \mathcal{L}_1)$

$$\psi^4 H$$
 :

Models for the rest of the operators + Lagrangian terms listed in [2306.12578] RB, Cepedello, Hirsch

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A black box for NRSMEFT

Extended black box:* Observation of LNV @ LHC guarantees the existence of Majorana masses for the active neutrinos.

We want to prove it in **NRSMEFT**, where $\Delta(L) = 2$ processes are generated by either:

A) two LNC operators and a Majorana propagator



B) one LNC and one **LNV operator**, along with a LNC propagator (no mass flip).



LNV from Majorana propagator

 $\mathcal{O}_{duNe} \ (\overline{d_R}\gamma^\mu u_R)(\overline{N_R}\gamma_\mu e_R)$ (d=6 LNC) Majorana mass M_N A) +Majorana neutrino mass: LNV process @LHC: 4-loop realisation of Weinberg operator $pp \rightarrow e^+ e^+ j j$ $\overline{d_R}$ Q e_R u_R UR $\overline{N_R}$, $\overline{N_R}$ e_R UR u_R Both observables are present or none of them is, as in the black box theorem for $0\nu\beta\beta$ decay

LNV from d=7 operator

B) \mathcal{O}_{LdQN} $(\overline{L^{i}}d_{R})\epsilon_{ij}(\overline{Q^{j}}N_{R})$ (d=6 LNC) + \mathcal{O}_{dNLH} $\epsilon_{ij}(\overline{d_{R}}\gamma^{\mu}d_{R})(\overline{N_{R}^{c}}\gamma_{\mu}L^{i})H^{j}$ (d=7 LNV)

2-loop realisation of Weinberg operator:



LNV processes @LHC:

 $pp \to e^+ e^+ j j W$



LNV from d=7 operator

B) \mathcal{O}_{LdQN} $(\overline{L^{i}}d_{R})\epsilon_{ij}(\overline{Q^{j}}N_{R})$ (d=6 LNC) + \mathcal{O}_{dNLH} $\epsilon_{ij}(\overline{d_{R}}\gamma^{\mu}d_{R})(\overline{N_{R}^{c}}\gamma_{\mu}L^{i})H^{j}$ (d=7 LNV)



Note. Divergent loop integral, it should be cancelled with a lower order diagram. For the leading contribution **one needs to know the underlying UV model.**

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Neutrino masses in d=7 models

Neutrino masses:

- tree level

 φ^{\dagger} Ξ_1^{\dagger} $arphi^\dagger$ \mathcal{N} H' N_R N_R H \mathcal{S}_1^\dagger \mathcal{S}_1 φ^{\dagger} E N_R LН N_R

- loop level

Neutrino masses:

tree level
 type I seesaw



- loop level

Neutrino masses:

tree level

type I seesaw type II seesaw

- loop level



Neutrino masses:

tree level
 type I seesaw

type II seesaw

- loop level Zee model



Neutrino masses:

tree level
 type I seesaw
 type II seesaw

- loop level Zee model 2-loop



 $\#1(\mathcal{N}, arphi)$ Lagrangian of the model

$$\mathcal{L} \propto y_{NL}^{\varphi} \left(\overline{N_R} L \right) \varphi + y_{\mathcal{N}L}^{\varphi} \left(\overline{\mathcal{N}} L \right) \varphi + y_{\mathcal{N}L} \left(\overline{\mathcal{N}} L \right) H + \frac{1}{2} M_{\mathcal{N}} \overline{\mathcal{N}^c} \mathcal{N} + \text{h.c.}$$

Leading neutrino mass contribution

$$m_{\nu} \propto y_{\mathcal{N}L}^2 \frac{v^2}{M_{\mathcal{N}}}$$

Matching to the operator WC

$$c_{LNLH} = -\frac{1}{4} \frac{y_{NL}^{\varphi} y_{\mathcal{N}L}^{\varphi} y_{\mathcal{N}L}}{M_{\mathcal{N}} m_{\varphi}^2}$$

 $M_{\mathcal{N}} \simeq m_{\varphi} \simeq \Lambda$

 $\#1(\mathcal{N}, arphi)$ Lagrangian of the model

$$\mathcal{L} \propto y_{NL}^{\varphi} \left(\overline{N_R} L \right) \varphi + y_{\mathcal{N}L}^{\varphi} \left(\overline{\mathcal{N}} L \right) \varphi + y_{\mathcal{N}L} \left(\overline{\mathcal{N}} L \right) H + \frac{1}{2} M_{\mathcal{N}} \overline{\mathcal{N}^c} \mathcal{N} + \text{h.c.}$$

Leading neutrino mass contribution

 $m_{\nu} \propto y_{\mathcal{N}L}^2 \frac{v^2}{M_{\mathcal{N}}}$

Matching to the operator WC

$$c_{LNLH} = -\frac{1}{4} \frac{y_{NL}^{\varphi} y_{\mathcal{N}L}^{\varphi} y_{\mathcal{N}L}}{M_{\mathcal{N}} m_{\varphi}^2}$$

We can derive an upper limit on the WC:

$$c_{LNLH} \lesssim 10^{-6} \frac{y_{NL}^{\varphi} y_{NL}^{\varphi}}{\Lambda^3} \left(\frac{\Lambda}{v}\right)^{1/2} \left(\frac{m_{\nu}}{0.1 \,\mathrm{eV}}\right)$$

Negligible observable processes

 $M_{\mathcal{N}} \simeq m_{\varphi} \simeq \Lambda$

 $\#3(\mathcal{S}_1, arphi)$ Lagrangian of the model

$$\mathcal{L} \propto y_L^{\mathcal{S}_1} \left(\overline{L^c} L \right) \mathcal{S}_1 + y_{Ne}^{\mathcal{S}_1} \left(\overline{N_R^c} e_R \right) \mathcal{S}_1 + y_{eL}^{\varphi} \left(\overline{e_R} L \right) \varphi^{\dagger} + \kappa_{\mathcal{S}_1 \varphi} \mathcal{S}_1^{\dagger} H \varphi + \text{h.c.} + \dots$$





 $#3(\mathcal{S}_1, \varphi)$ Lagrangian of the model

 $\mathcal{L} \propto y_L^{\mathcal{S}_1} \left(\overline{L^c} L \right) \mathcal{S}_1 + y_{Ne}^{\mathcal{S}_1} \left(\overline{N_R^c} e_R \right) \mathcal{S}_1 + y_{eL}^{\varphi} \left(\overline{e_R} L \right) \varphi^{\dagger} + \kappa_{\mathcal{S}_1 \varphi} \mathcal{S}_1^{\dagger} H \varphi + \text{h.c.} + \dots$





Observability depends on which are the suppressed couplinas:

$$y_L^{\mathcal{S}_1} \sim y_{eL}^{\varphi} \sim (\kappa_{\mathcal{S}_1 \varphi} / \Lambda) \sim \epsilon$$
 or

 $y_L^{\mathcal{S}_1} \sim \epsilon^3$ or $y_{\epsilon T}^{\varphi} \sim \epsilon^3$ 18



★ We provide the first systematic decomposition of d=6 and d=7 operators in N_R SMEFT at tree level.

★ Models for LNV d=7 operators will always lead to Majorana active neutrino masses at tree-, 1- or 2-loop level.

Neutrino masses put tight constraints on the Wilson coefficients*
 *Except for decompositions leading to radiative neutrino masses, where some operators might lead to observable effects.





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Lepton number violation and neutrino masses in *N*_RSMEFT

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Backup: BNV models

	$\psi^4 (d = 6)$	Models			
Occur	$\varepsilon = \left(\overline{O^{c}}O_{c}\right)\left(\overline{d^{c}}N_{B}\right)$	S :	ω_1		
	$c_{ij}(a_ia_j)(a_{R^{IVR}})$	V :	\mathcal{Q}_1		
\mathcal{O}_{uddN}	$\left(\overline{u_R^c}d_R ight)\left(\overline{d_R^c}N_R ight)$	S :	ω_1, ω_2		
	$\psi^4 H (d=7)$		Models		
		SS :	(ω_2,Π_1)		
\mathcal{O}_{QNddH}	$\varepsilon_{ij}\left(\overline{Q_i}N_R\right)\left(\overline{d_R}d_R^c\right)\tilde{H}_j$	FS :	(U,ω_2) (Δ_1,ω_2) (Q_1,Π_1)		
		FV :	$(Q_1, \mathcal{Q}_1) (Q_1, \mathcal{U}_1) (\Delta_1, \mathcal{Q}_1) (U, \mathcal{U}_1)$		
		SS :	(ω_1,Π_1) (Π_1,ζ)		
\mathcal{O}_{QNQH}	$\varepsilon_{ij}\left(\overline{Q_i}N_R\right)\left(\overline{Q_j}Q^c\right)H$	FS :	(D,ω_1) (Δ_1,ω_1) (T_1,ζ) (Δ_1,ζ)		
			$(D,\Pi_1) \ (T_1,\Pi_1)$		
		SS :	(ω_1,Π_1)		
\mathcal{O}_{QNudH}	$\left(\overline{Q}N_R\right)\left(\overline{u_R}d_R^c\right)H$	FS :	(D,ω_1) (Δ_1,ω_1) (Q_5,Π_1) (Q_1,Π_1)		
		FV :	$(Q_1, \mathcal{Q}_1) (Q_1, \mathcal{U}_1) (Q_5, \mathcal{Q}_5) (Q_5, \mathcal{U}_2)$		
			$(\Delta_1, \mathcal{Q}_1) (D, \mathcal{U}_1) (\Delta_1, \mathcal{Q}_5) (D, \mathcal{U}_2)$		

Table 10. Baryon number violating operators of d = 6 and d = 7 in N_R SMEFT and their tree-level decompositions. Models are classified in terms of the Lorentz nature of the fields.

Backup: All d=7 operators

	$N\psi H^3D$		$N\psi^3D$	$N^2\psi^2H$		
\mathcal{O}_{NL1}	$\epsilon_{ij}(\overline{N^C}\gamma_{\mu}L^i)(iD^{\mu}H^j)(H^{\dagger}H)$	\mathcal{O}_{eNLLD}	$\epsilon_{ij}(\overline{e}\gamma_{\mu}N)(\overline{L^{i,C}}i\overleftrightarrow{D}^{\mu}L^{j})$	\mathcal{O}_{LNeH}	$(\overline{L}N)(\overline{N^C}e)H$	
\mathcal{O}_{NL2}	$\epsilon_{ij}(\overline{N^C}\gamma_{\mu}L^i)H^j(H^{\dagger}i\overleftrightarrow{D^{\mu}}H)$	\mathcal{O}_{duNeD}	$(\overline{d}\gamma_{\mu}u)(\overline{N^{C}}i\overleftrightarrow{D}^{\mu}e)$	\mathcal{O}_{eLNH}	$H^{\dagger}(\overline{e}L)(\overline{N^{C}}N)$	
	$N\psi H^2 D^2$	O_{QuNLD}	$(\overline{Q}i\overleftrightarrow{D}_{\mu}u)(\overline{N^C}\gamma^{\mu}L)$	\mathcal{O}_{QNdH}	$(\overline{Q}N)(\overline{N^C}d)H$	
\mathcal{O}_{NeD}	$\epsilon_{ij}(\overrightarrow{N^C}\overrightarrow{D}^{\mu}e)(H^iD^{\mu}H^j)$	\mathcal{O}_{dQNLD}	$\epsilon_{ij}(\overline{d}i\overleftrightarrow{D}_{\mu}Q^{i})(\overline{N^{C}}\gamma^{\mu}L^{j})$	\mathcal{O}_{dQNH}	$H^{\dagger}(\overline{d}Q)(\overline{N^C}N)$	
	$N\psi H^2 X$		$N^2 \psi^2 D$	\mathcal{O}_{QNuH}	$(\overline{Q}N)(\overline{N^C}u) ilde{H}$	
\mathcal{O}_{NeW}	$g_2(\epsilon \tau^I)_{ij}(\overline{N^C}\sigma^{\mu\nu}e)(H^iH^j)W^I_{\mu\nu}$	\mathcal{O}_{LND}	$(\overline{L}\gamma_{\mu}L)(\overline{N^{C}}i\overleftrightarrow{\partial}^{\mu}N)$	O_{uQNH}	$\tilde{H}^{\dagger}(\overline{u}Q)(\overline{N^{C}}N)$	
	$N\psi HDX$	\mathcal{O}_{QND}	$(\overline{Q}\gamma_{\mu}Q)(\overline{N^{C}}i\overleftrightarrow{\partial}^{\mu}N)$		$N^3\psi H$	
\mathcal{O}_{NLB1}	$g_1\epsilon_{ij}(\overline{N^C}\gamma^{\mu}L^i)(D^{\nu}H^j)B_{\mu\nu}$	\mathcal{O}_{eND}	$(\overline{e}\gamma_{\mu}e)(\overline{N^{C}}i\overleftrightarrow{\partial}^{\mu}N)$	\mathcal{O}_{LNNH}	$(\overline{L}N)(\overline{N^C}N)\tilde{H}$	
\mathcal{O}_{NLB2}	$g_1 \epsilon_{ij} (\overline{N^C} \gamma^\mu L^i) (D^\nu H^j) \tilde{B}_{\mu\nu}$	\mathcal{O}_{uND}	$(\overline{u}\gamma_{\mu}u)(\overline{N^{C}}i\overleftrightarrow{\partial}^{\mu}N)$	\mathcal{O}_{NLNH}	$\tilde{H}^{\dagger}(\overline{N}L)(\overline{N^{C}}N)$	
\mathcal{O}_{NLW1}	$g_2(\epsilon\tau^I)_{ij}(\overline{N^C}\gamma^{\mu}L^i)(D^{\nu}H^j)W^I_{\mu\nu}$	\mathcal{O}_{dND}	$(\overline{d}\gamma_{\mu}d)(\overline{N^{C}}i\overleftrightarrow{\partial}^{\mu}N)$		$B: N\psi^3 D \& N\psi^3 H$	
\mathcal{O}_{NLW2}	$g_2(\epsilon\tau^I)_{ij}(\overline{N^C}\gamma^{\mu}L^i)(D^{\nu}H^j)\tilde{W}^I_{\mu\nu}$		N^4D	\mathcal{O}_{uNdD}	$\epsilon_{\alpha\beta\sigma}(\overline{u}_{\alpha}\gamma_{\mu}N)(\overline{d}_{\beta}i\overleftarrow{D}^{\mu}d_{\sigma}^{C})$	
	N^2H^4	\mathcal{O}_{NND}	$(\overline{N}\gamma_{\mu}N)(\overline{N^{C}}i\overleftrightarrow{\partial}^{\mu}N)$	\mathcal{O}_{dNQD}	$\epsilon_{ij}\epsilon_{\alpha\beta\sigma}(\overline{d}_{\alpha}\gamma_{\mu}N)(\overline{Q}_{i\beta}i\overleftrightarrow{D}^{\mu}Q_{j\sigma}^{C})$	
\mathcal{O}_{NH}	$(\overline{N^C}N)(H^{\dagger}H)^2$		$N\psi^3H$	\mathcal{O}_{QNdH}	$\epsilon_{ij}\epsilon_{\alpha\beta\sigma}(\overline{Q}_{i\alpha}N)(\overline{d}_{\beta}d_{\sigma}^{C})\tilde{H}^{j}$	
	$N^2H^2D^2$	\mathcal{O}_{LNLH}	$\epsilon_{ij}(\overline{L}\gamma_{\mu}L)(\overline{N^C}\gamma^{\mu}L^i)H^j$	\mathcal{O}_{QNQH}	$\epsilon_{ij}\epsilon_{\alpha\beta\sigma}(\overline{Q}_{i\alpha}N)(\overline{Q}_{j\beta}Q^C_{\sigma})H$	
\mathcal{O}_{NHD1}	$(\overrightarrow{N^C}\overleftrightarrow{\partial}_{\mu}N)(H^{\dagger}\overrightarrow{D^{\mu}}H)$	\mathcal{O}_{QNLH1}	$\epsilon_{ij}(\overline{Q}\gamma_{\mu}Q)(\overline{N^C}\gamma^{\mu}L^i)H^j$	\mathcal{O}_{QNudH}	$\epsilon_{\alpha\beta\sigma}(\overline{Q}_{\alpha}N)(\overline{u}_{\beta}d_{\sigma}^C)H$	
\mathcal{O}_{NHD2}	$(\overline{N^C}N)(D_{\mu}H)^{\dagger}D^{\mu}H$	\mathcal{O}_{QNLH2}	$\epsilon_{ij}(\overline{Q}\gamma_{\mu}Q^{i})(\overline{N^{C}}\gamma^{\mu}L^{j})H$		$N^2 X^2$	
	$N^2 H^2 X$	\mathcal{O}_{eNLH}	$\epsilon_{ij}(\overline{e}\gamma_{\mu}e)(\overline{N^C}\gamma^{\mu}L^i)H^j$	\mathcal{O}_{NB1}	$\alpha_1(\overline{N^C}N)B_{\mu u}B^{\mu u}$	
\mathcal{O}_{NHB}	$g_1(\overline{N^C}\sigma_{\mu\nu}N)(H^{\dagger}H)B^{\mu\nu}$	\mathcal{O}_{dNLH}	$\epsilon_{ij}(\overline{d}\gamma_{\mu}d)(\overline{N^C}\gamma^{\mu}L^i)H^j$	\mathcal{O}_{NB2}	$\alpha_1(\overline{N^C}N)B_{\mu\nu}\tilde{B}^{\mu\nu}$	
\mathcal{O}_{NHW}	$g_2(\overline{N^C}\sigma_{\mu\nu}N)(H^{\dagger}\tau^I H)W^{I\mu\nu}$	\mathcal{O}_{uNLH}	$\epsilon_{ij}(\overline{u}\gamma_{\mu}u)(\overline{N^C}\gamma^{\mu}L^i)H^j$	\mathcal{O}_{NW1}	$\alpha_2(\overline{N^C}N)W^I_{\mu\nu}W^{I\mu\nu}$	
		\mathcal{O}_{duNLH}	$\epsilon_{ij}(\overline{d}\gamma_{\mu}u)(\overline{N^C}\gamma^{\mu}L^i)\tilde{H}^j$	\mathcal{O}_{NW2}	$\alpha_2(\overline{N^C}N)W^I_{\mu\nu}\tilde{W}^{I\mu\nu}$	
		\mathcal{O}_{dQNeH}	$\epsilon_{ij}(\overline{d}Q^i)(\overline{N^C}e)H^j$	\mathcal{O}_{NG1}	$\alpha_3(\overline{N^C}N)G^A_{\mu u}G^{A\mu u}$	
		\mathcal{O}_{QuNeH1}	$(\overline{Q}u)(\overline{N^C}e)H$	\mathcal{O}_{NG2}	$lpha_3(\overline{N^C}N)G^A_{\mu u} ilde{G}^{A\mu u}$	
		\mathcal{O}_{QuNeH2}	$(\overline{Q}\sigma_{\mu\nu}u)(\overline{N^C}\sigma^{\mu\nu}e)H$			

Backup: Black box theorem of $0\nu\beta\beta$

 $\mathbf{0}\mathbf{\nu}\mathbf{\beta}\mathbf{\beta}$ decay guarantees a radiative contribution to the Majorana neutrino mass of a SM neutrino



Cutting at the thinner lines gives a contribution to ${\cal O}_{u \bar d e}^9 \propto u_R^2 \overline{d_R}^2 e_R^2$