# *Some novel searches for neutrino dipole moments*

#### Michele Frigerio

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*\* Muon collider probes of Majorana neutrino dipole moments and masses* with **Natascia Vignaroli ,** arXiv:2409.02721

*\* Testing the dipole moment of GeV-scale sterile neutrinos* with **Enrico Bertuzzo**, arXiv:241x.xxxxx

#### **Baryon & Lepton Number Violation 2024** KIT Karlsruhe - 8 / 11 October

#### Searching for new physics ...

**THE ROAD Corman McCarthy, 2006 Joe Penhall, 2009**

#### Neutrinos: masses vs dipoles

Two Weyl spinors :  $\nu = \begin{pmatrix} \nu e \\ \end{pmatrix}$  Flavour symmetry

 $\mathcal{L} \supset \nu_{\alpha}^{\dagger} i \bar{\sigma}^{\mu} \partial_{\mu} \delta_{\alpha \beta} \nu_{\beta}$ 

**Kinetic operator:** marginal (dim = 4),  $\Delta$  L = 0, preserves SU(2)<sub>F</sub>

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$$
\n
$$
m_{\alpha\beta} = m_{\beta\alpha}
$$
\n
$$
m \equiv m_A (\epsilon \sigma_A)
$$
\nMass operator: relevant (dim = 3),  $\Delta L = 2$ , breaks SU(2)<sub>F</sub>

\n
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m_A \text{ real preserves } U(1)_F : \text{ one Dirac fermion}
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m_A \text{ complex breaks } U(1)_F : \text{two Majorana fermions}
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m_A \sim 3_F
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$$
\mathcal{L} \supset \frac{1}{2} \nu_\alpha \, \sigma^{\mu\nu} \, \lambda_{\alpha\beta} \, \nu_\beta \, F_{\mu\nu} + h.c. \qquad \lambda_{\alpha\beta} = -\lambda_{\beta\alpha}
$$

**Dipole operator:** irrelevant (dim = 5),  $\Delta L = 2$ , preserves SU(2)<sub>F</sub>

 $\Rightarrow$  small mass and large dipole is technically natural !

 $\lambda \sim 1_F$ 

#### ν dipole from SM EFT operators

Δ L = 2 operators in the SM effective field theory :

 $m_{\alpha\beta}=C_{\alpha\beta}^5v^2$ dimension-5  $\mathcal{L}_5 = C^5 \mathcal{O}_5$  $(\mathcal{O}_5)_{\alpha\beta} = (\overline{\ell_{L\alpha}^c} \epsilon H)(H^T \epsilon l_{L\beta})$  $\frac{\nu_{\alpha}}{\gamma}$   $\frac{\nu_{\beta}}{\gamma}$ 

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#### Some current bounds on ν dipole

\* Solar neutrino elastic scattering on nuclei (photon exchange)

$$
\lambda_{\nu} \simeq \left(\sum_{k} |U_{ek}|^2 \sum_{j} |\lambda_{jk}|^2\right)^{1/2} < 0.6 \cdot 10^{-11} \mu_B \ (90\% \, C.L.)
$$

**Giunti Studenikin 1403.6344 XENON 2207.11330, LZ 2207.03764**

\* Stellar energy loss (red giant branch of globular clusters)

 $\lambda_{\nu} \leq 0.1 \cdot 10^{-11} \mu_B (95\% C.L.)$ 

**Capozzi Raffelt 2007.03694**

 $\mu_B \equiv \frac{e}{2m_e}$ 

- indirect (neutrinos not observed)

- effective combination of flavours
- insensitive to lepton number
- large systematic uncertainties ?

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\* Neutrino-to-antineutrino conversion in solar magnetic field

$$
\lambda_{\nu} \lesssim 500 \cdot 10^{-11} \mu_B \left[ \frac{kG}{B} \right] \ (90\% \, C.L.)
$$

**KamLAND 2108.08527 Akhmedov Martínez-Miravé 2207.04516**  $\mu_B \equiv \frac{e}{2m_e}$ 

- indirect (neutrinos not observed)

- effective combination of flavours
- insensitive to lepton number
- large systematic uncertainties ?

- sensitive to lepton number violation

- large uncertainty on value of solar magnetic field

#### ν dipole @ future hadron colliders



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**Recasting** an LHC analysis for the same final state. After selection cuts: **signal** efficiency ~ 0.5 and **background** (mostly from  $V$  V  $i$   $i$ ) ~ 10 fb [reducible]

**ATLAS 2403.15016**

 $HL - LHC$  {3 ab<sup>-1</sup>}  $|\lambda_{e\mu}|/\mu_B < 2.2 \cdot 10^{-7}$  [3.8  $\cdot 10^{-8}$ ]  $@2\sigma$  $\text{FCC} - \text{hh} \ \{30 \text{ ab}^{-1}\}\$  $|\lambda_{e\mu}|/\mu_B < 3.8 \cdot 10^{-8}$  [2.0  $\cdot 10^{-9}$ ]  $\omega$   $2\sigma$ 

#### Sensitivity about **2-3 orders of magnitude weaker than current bounds**

### ν dipole @ future muon collider (I)



Illustrative for  $\sim$  100 diagrams

2 leptons (**same-sign different-flavour)** + 2 fat jets (**W into hadrons**)

Clean, unambiguous signal of lepton number and flavour violation

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Including acceptance cuts & reconstruction efficiency

Achievable integrated luminosity for 5-years data taking :

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 $\mu^-$ 







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Signal **simulation & reconstruction** (Madgraph, Pythia8, FastJet, ...) Same for background (mostly from **W W µ<sup>+</sup> µ** & **W W W W**) ~ 1 ab [reducible]

## ν dipole @ future muon collider (II)

Improving discrimination by **kinematic variables**

Signal events have **higher**  $p_T \&$ are **more central**

With tailored cuts, **background down to**  $\sim$  **0.1 ab** transverse





## ν dipole @ future muon collider (II)



further background rejection,

improved lepton identification

#### ν mass @ future muon collider

 $\mu^-$ 

 $e^{-}$ 

 $W^+$ 

 $W^+$ 



$$
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0 $\nu$ 2 $\beta$  - decay :  $m_{ee} \lesssim 0.1 \text{ eV}$   
LHC (FCC - hh) :  $m_{e\mu,\mu\mu} \lesssim 10 \text{ (1) GeV}$ 

**ATLAS 2305.14931 Fuks Neundorf Peters Ruiz Saimpert 2012.09882**

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#### **Improvement up to 5 orders of magnitude !**

Still far above the neutrino mass scale ...

#### A dipole for sterile neutrinos

Effective Field Theory for **SM + 2 sterile neutrinos N**<sub>1,2</sub>

$$
N = \begin{pmatrix} N_1 \\ N_2 \end{pmatrix} \qquad \begin{array}{c} \mathcal{L}_N = i N_i^{\dagger} \bar{\sigma}^{\mu} \partial_{\mu} \delta_{ij} N_j \\ \frac{1}{2} N_i \mathcal{M}_{ij} N_j - \tilde{H}^{\dagger} \ell_{\alpha} Y_{\alpha i} N_i + h.c. \end{array} \qquad \begin{array}{c} \\ \\ \\ \\ \end{array} + \qquad \frac{1}{2} \left( d N_i \sigma^{\mu \nu} \epsilon_{ij} N_j B_{\mu \nu} + h.c. \right) + \dots \end{array}
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**How large can this dipole be ?**

$$
d \simeq \frac{g'}{16\pi^2} \frac{g_\star^2}{m_\star} \simeq \frac{1}{3\text{TeV}} \left(\frac{g_\star}{4\pi}\right)^2 \left(\frac{\text{TeV}}{m_\star}\right)
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**U(1)<sub>L</sub>** conserving limits a)  $L(N_{1,2}) = 0$  : zero Yukawas, no active-sterile mixing,  $M_{1,2}$  arbitrary **Barducci Bertuzzo Taoso Toni 2022**

b) 
$$
L(N_1) = -L(N_2) = 1
$$
:  
\n
$$
M_{\nu} = \begin{pmatrix} 0 & 0 & m \\ 0 & 0 & M \\ m & M & 0 \end{pmatrix} \qquad m_{\alpha} \equiv Y_{2\alpha} \frac{v}{\sqrt{2}} \qquad s_{\alpha} \simeq \frac{m_{\alpha}}{M} \qquad M_i \simeq M
$$

#### Bounds on active-sterile mixing

**In the U(1)**<sup>L</sup> limit m<sub>ν</sub> = 0, still mixing is constrained by a variety of lepton precision measurements

\* **Indirect bounds** (on sterile neutrinos heavier than charged leptons) :

$$
s_e^2 \lesssim 10^{-3}, \qquad s_\mu^2 \lesssim 10^{-3}, \qquad s_\tau^2 \lesssim 3 \cdot 10^{-3}
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if  $s_e \simeq s_\mu$ , then  $s_{e,\mu}^2 \lesssim 10^{-5} [10^{-7}]$ 

**Coy Frigerio 2019,2022**

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\* **Direct searches** for sterile neutrinos :

 $\begin{array}{ll} \mbox{for}\ \ 2\ \mbox{GeV}\lesssim M_D\lesssim 80\ \mbox{GeV}\,,\quad s_{e,\mu}^2\lesssim 10^{-5}\,,\quad s_\tau^2\lesssim 10^{-5}\,,\\ \mbox{for}\ \ 0.5\ \mbox{GeV}\lesssim M_D\lesssim 2\ \mbox{GeV}\,,\quad s_{e,\mu}^2\lesssim 10^{-7}\,,\quad s_\tau^2\lesssim 10^{-6}\,,\\ \mbox{for}\ \ 0.2\ \mbox{GeV}\lesssim M_D\lesssim 0.5\ \mbox{GeV}\,,\, s_{e,\mu}^2\lesssim 10^{-9}\,,$ 

**Snowmass Review 2203.08039**

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#### **Snowmass Review 2203.08039**

**Departing from the U(1)L limit** , assuming oscillation data are reproduced by **N1,2 seesaw** :

normal ordering  $(m_1 < m_2 < m_3):$   $\hat{s}_e^2 \leq 0.1$ ,  $0.25 \leq \hat{s}_u^2 \leq 0.85$ ,  $\hat{s}_\tau^2 \simeq 1 - \hat{s}_u^2$ , inverted ordering  $(m_3 < m_1 < m_2)$ :  $0.05 \lesssim \hat{s}_{e}^2 \lesssim 0.95$ ,  $\hat{s}_{\mu}^2 \simeq \hat{s}_{\tau}^2 \simeq 0.5(1 - \hat{s}_{e}^2)$ ,

**Blennow Fernández-Martínez Hernández-García Lopéz-Pavón Marcano Naredo-Tuero et al. 2306.01040**

 $\hat{s}_{\alpha}^2 \equiv \frac{s_{\alpha}^2}{\sum_{\beta} s_{\beta}^2}$ 

#### Sterile production & decay

**Beam-dump** experiments (SHiP, NA62, CHARM, …): mesons from protons on target

**Barducci Bertuzzo Taoso Toni Ternes 2024**



Photons with  $E > 1$  GeV can be seen in the detector calorimeter

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**Production** both from dipole & active-sterile mixing Photon signal from **decays** via dipole only

Photons with  $E > 1$  GeV can be seen in the detector calorimeter  $N_2$  at SHiP – mixing with  $\tau$  flavor ( $\delta$  = 0)  $10^{-3}$  $m<sub>1</sub> = 400$  GeV,  $q<sub>2</sub> = 4\pi$  $s_r^2 = 10^{-6}$  $10^{-4}$  $m<sub>z</sub> = 400$  GeV,  $q<sub>z</sub> = 1$  $10^{-5}$ d [GeV<sup>-1</sup>]  $10^{-6}$  $M_1 = 3$  GeV  $M_1 = 1$  GeV  $N_{pot}$  = 6  $\cdot$  10<sup>20</sup>  $10^{-7}$  $M_1 = 0.3$  GeV  $E_{pot} \doteq 400 \text{GeV}$  $N_{\text{dipole}} > N_{\text{mixing}}$  $L_{initial} = 33$ m  $\Gamma_{\text{dipole}} > \Gamma_{\text{mixing}}$  $L_{final} = 85$ m  $10^{-8}$  $10^{-4}$  $10^{-6}$  $10^{-5}$  $10^{-3}$  $10^{-7}$  $10^{-2}$  $|\theta_{\tau}|$ 

#### Future experimental sensitivity (I)



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#### Future experimental sensitivity (II)

$$
\delta \equiv \frac{M_2 - M_1}{M_2 + M_1}
$$



#### Future experimental sensitivity (II)

**with E.Bertuzzo**



**with E.Bertuzzo**

#### Future experimental sensitivity (III)



**Mixing with τ flavour** 

$$
N_D\to\nu_\tau\gamma
$$

Future experimental sensitivity (III)



**with E.Bertuzzo**

#### … waiting for some ν light

**LE RAYON VERT Jules Verne, 1882**

**Eric Rohmer, 1986**