



Cosmic Axion Background from the Primordial Bath

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DI PADOVA



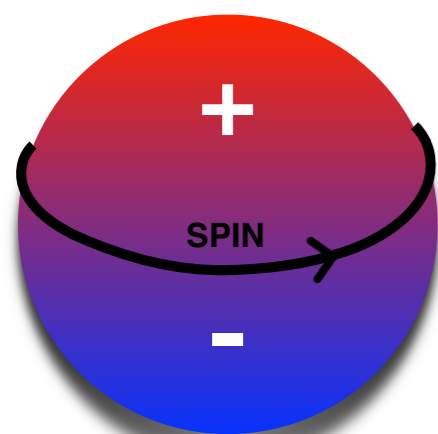
International Workshop on Baryon and Lepton Number Violation (BLV2024)

Karlsruhe Institute of Technology (KIT) — 10 October 2024

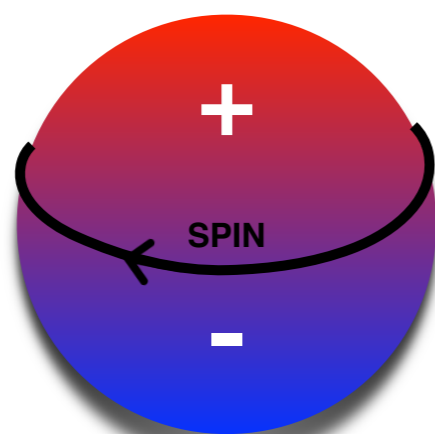
Virtues of the QCD Axion



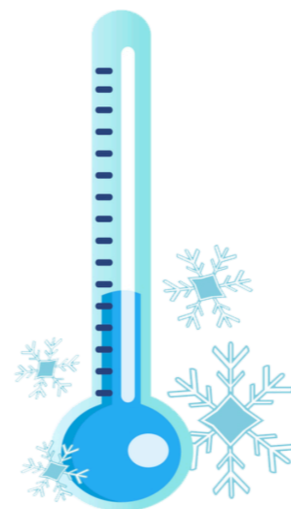
Strong CP



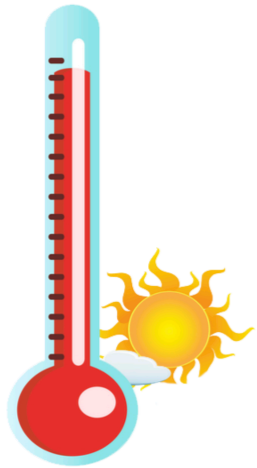
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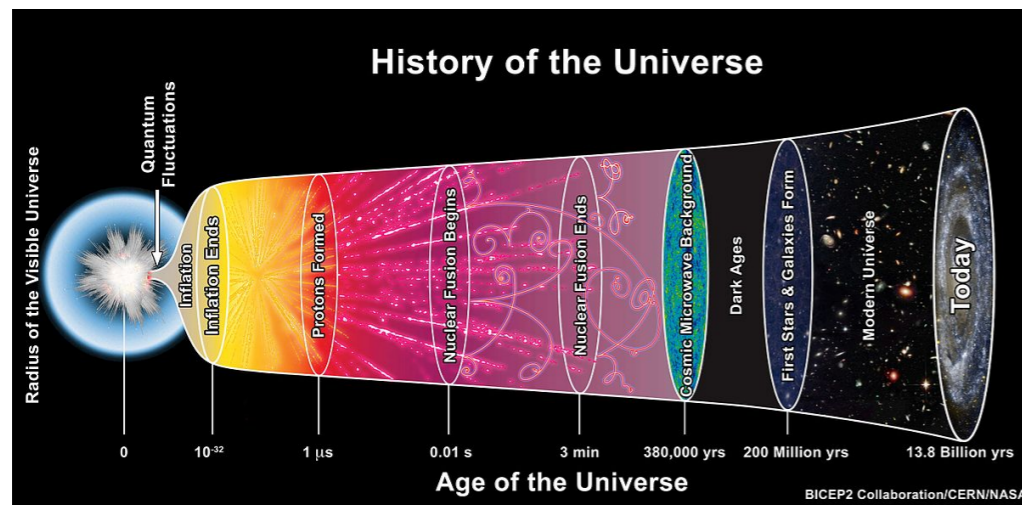
Cold Dark Matter



Plan for today: Hot Axions



Axions produced with kinetic energy much larger than their mass (i.e. “hot”)

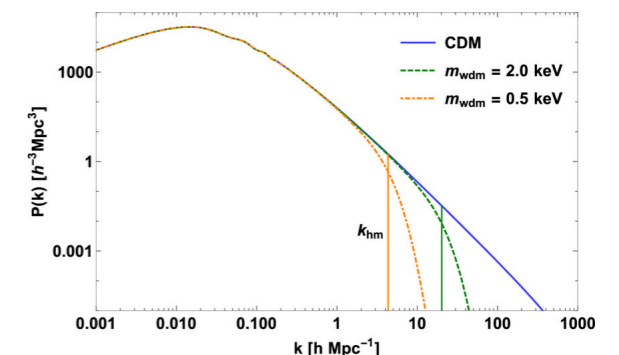
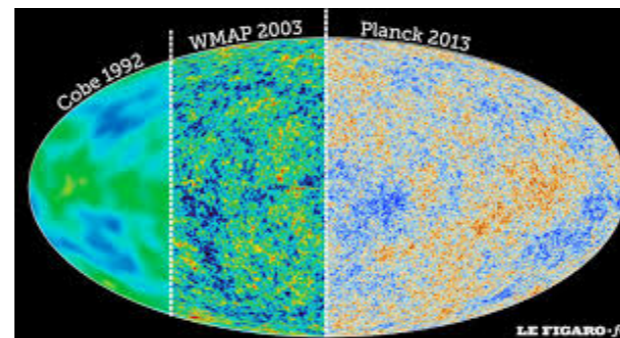


I. Production

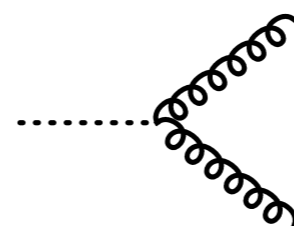
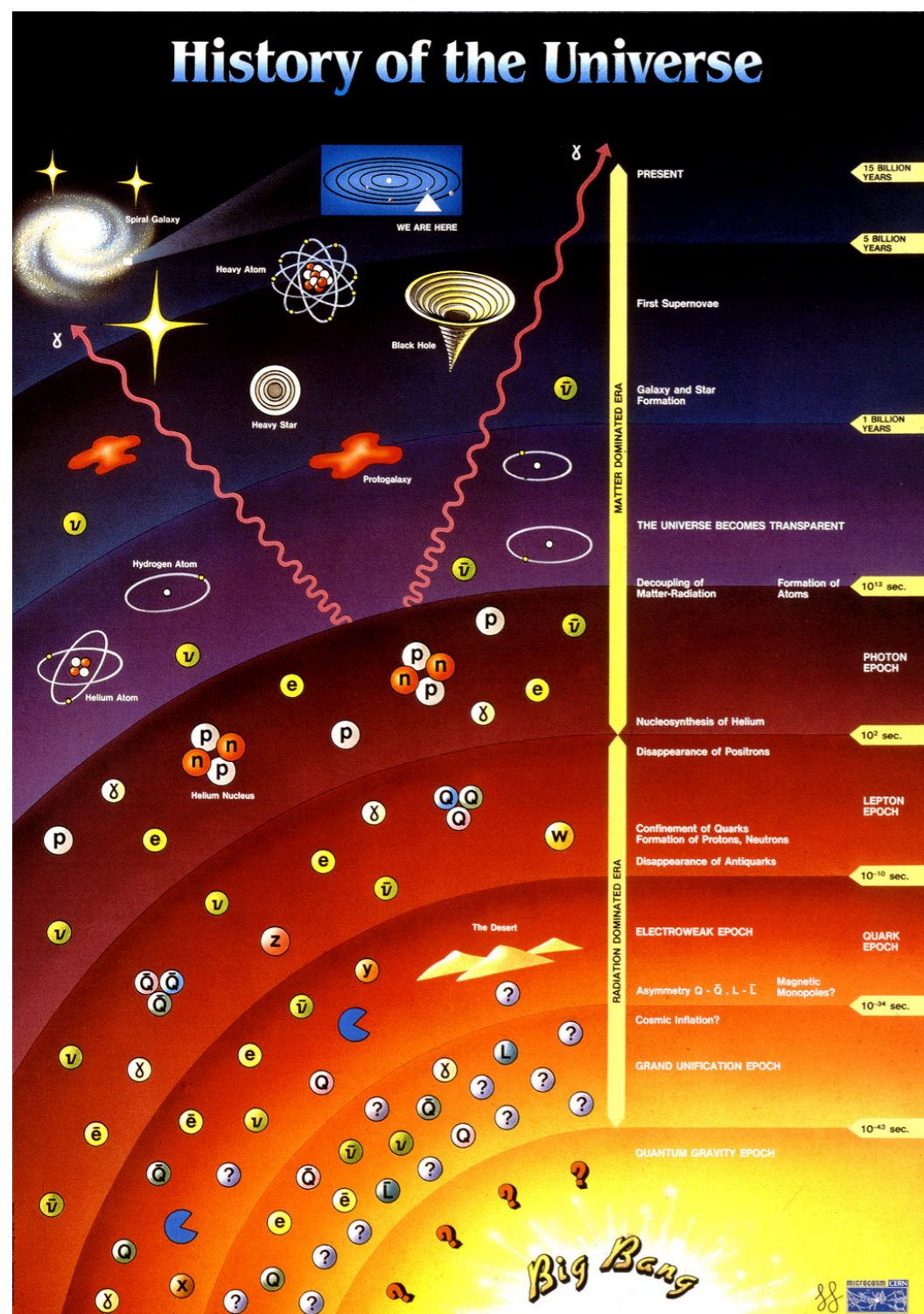
Processes with particles from the primordial thermal bath

2. Signals

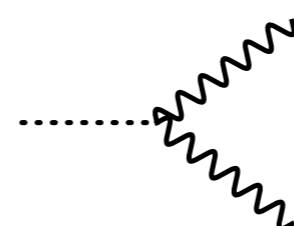
Dark radiation or warm dark matter



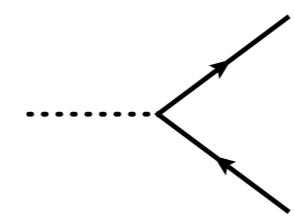
Unavoidable Thermal Production



$$\frac{\alpha_s}{8\pi} \frac{a}{f_a} G^{\mu\nu} \tilde{G}_{\mu\nu}$$



$$c_{\gamma\gamma} \frac{\alpha_{em}}{8\pi} \frac{a}{f_a} F^{\mu\nu} \tilde{F}_{\mu\nu}$$



$$c_{\psi} \frac{\partial_{\mu} a}{f_a} \bar{\psi} \gamma^{\mu} \gamma^5 \psi$$

Scatterings and/or decays of thermal bath particles (axion energy $\gg m_a$, i.e. “hot”)

Observable Effects

Dark Radiation

Additional radiation at:

- BBN ($m_a \lesssim \text{MeV}$)
- CMB formation ($m_a \lesssim 0.3 \text{ eV}$)

$$\rho_{\text{rad}} = \left[1 + \frac{7}{8} \left(\frac{T_\nu}{T_\gamma} \right)^4 N_{\text{eff}} \right] \rho_\gamma$$

$$\Delta N_{\text{eff}} = \frac{8}{7} \left(\frac{11}{4} \right)^{4/3} \frac{\rho_a}{\rho_\gamma}$$

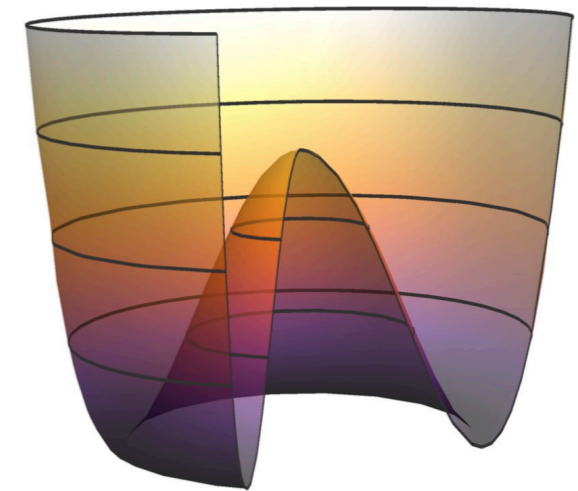
Warm Dark Matter

If $m_a \sim \text{eV}$ we have a warm dark matter component
(exactly as neutrinos in the standard model)

QCD Axion or ALPs?

Axion-Like-Particles (ALPs) are ubiquitous in extension of the standard model

- Pseudo-Nambu-Goldstone-bosons
- Axions in string theory



QCD Axion

$$m_a \simeq 5.7 \left(\frac{10^9 \text{ GeV}}{f_a} \right) \text{ meV}$$

ALPs

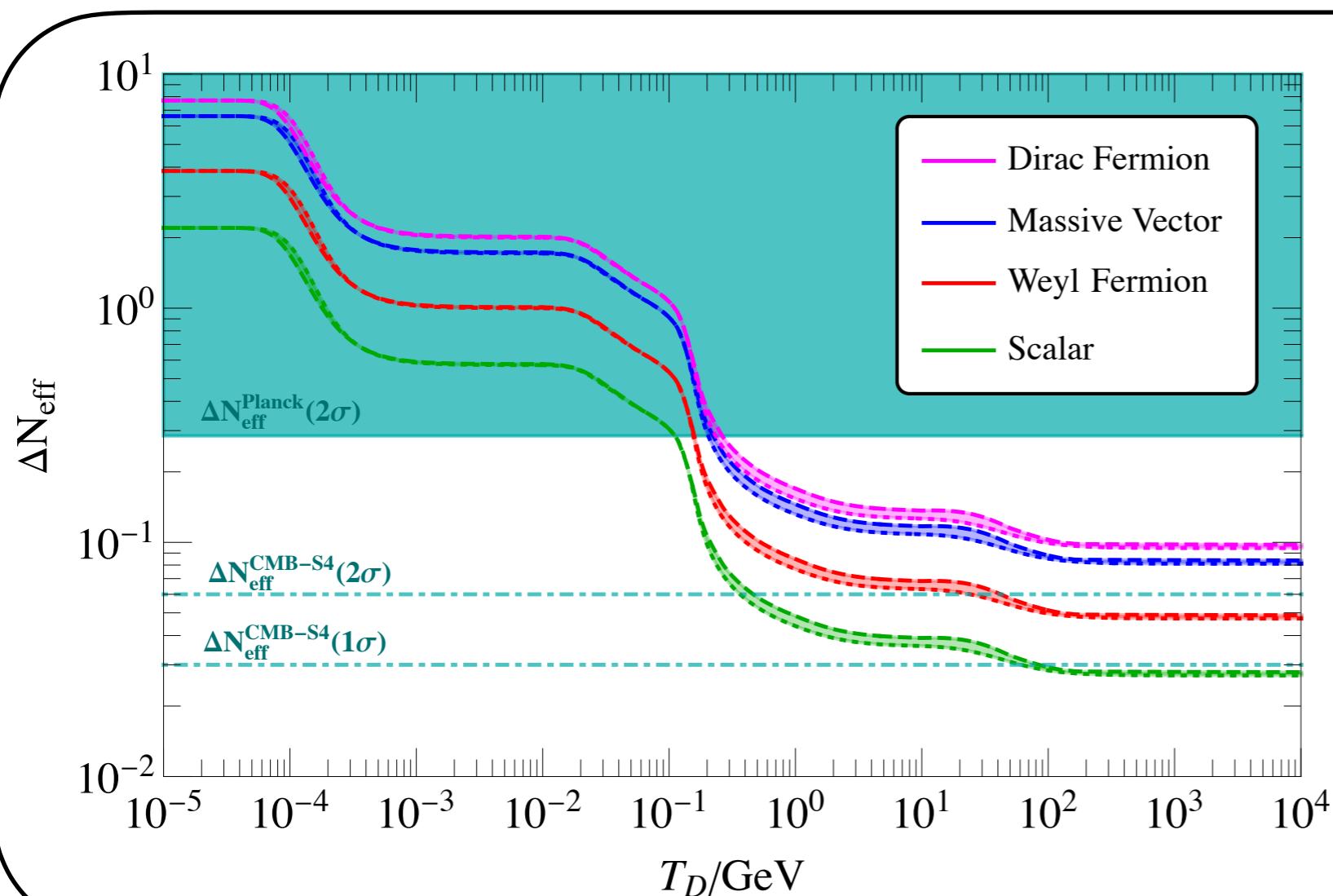
$$m_a \simeq \Lambda_X^2 / f_X$$

Results in this talk mostly about the QCD axion
(easily generalized when the mass is negligible)

How to Predict ΔN_{eff}

ΔN_{eff} - I: Instantaneous decoupling

- Assume they thermalize at early times
- Estimate the decoupling temperature from $\Gamma(T_D) = H(T_D)$



$$\Delta N_{\text{eff}} \simeq 0.027 \left(\frac{106.75}{g_{*s}(T_D)} \right)^{4/3}$$

How to Predict ΔN_{eff}

ΔN_{eff} - I: Instantaneous decoupling

- Assume they thermalize at early times
- Estimate the decoupling temperature from $\Gamma(T_D) = H(T_D)$

ΔN_{eff} - II: Boltzmann equation for n_a

- Track the number density of axions
- Convert the asymptotic result via the equilibrium distribution

$$\frac{dn_a}{dt} + 3Hn_a = \sum_{\alpha} \gamma_{\alpha}$$

$$\Delta N_{\text{eff}} \simeq 74.85 Y_a^{4/3}$$

$\alpha =$ Production processes

How to Predict ΔN_{eff}

ΔN_{eff} - I: Instantaneous decoupling

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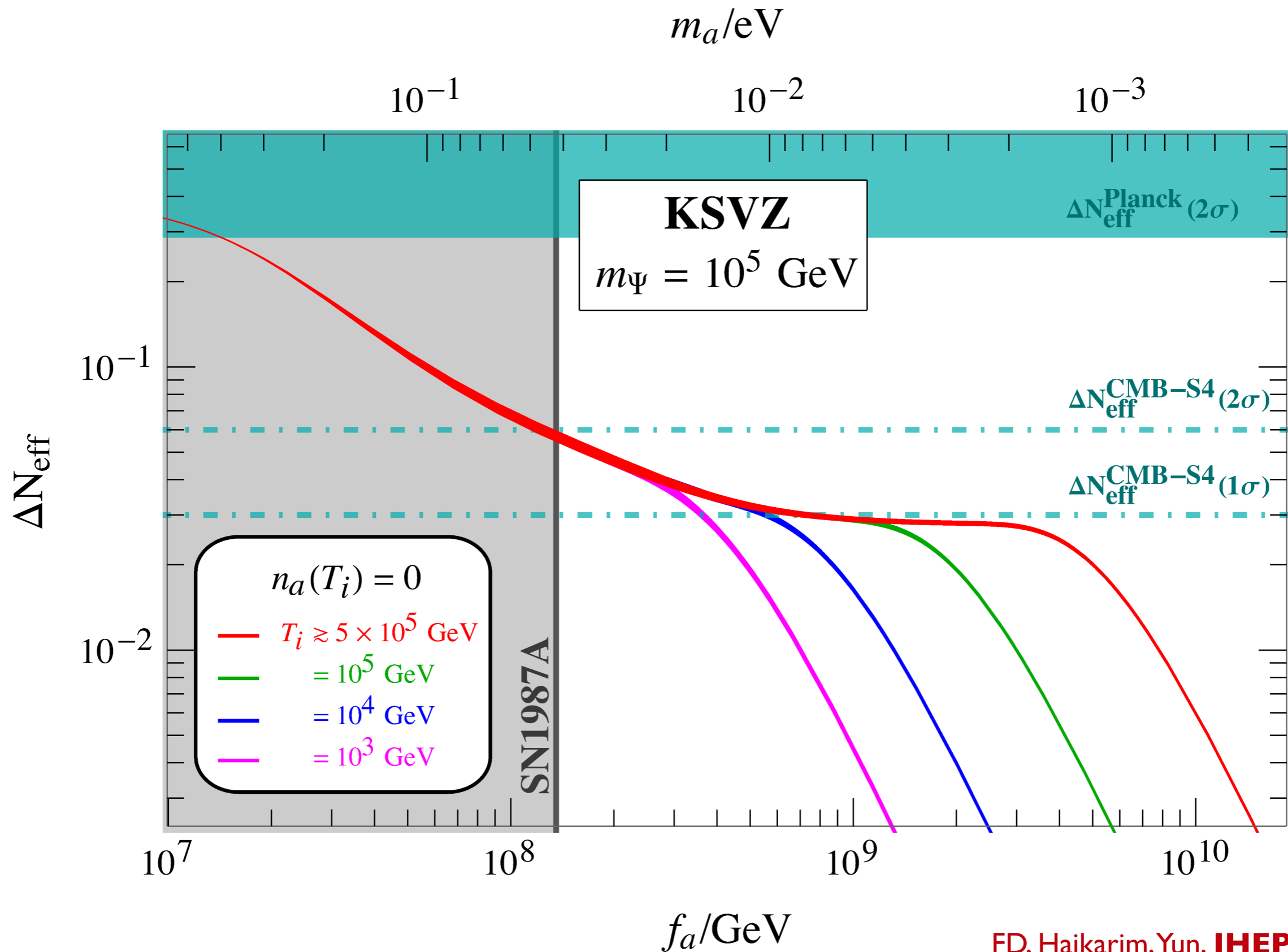
Equilibrium thermodynamics for the conversion to energy

Spectral distortions neglected

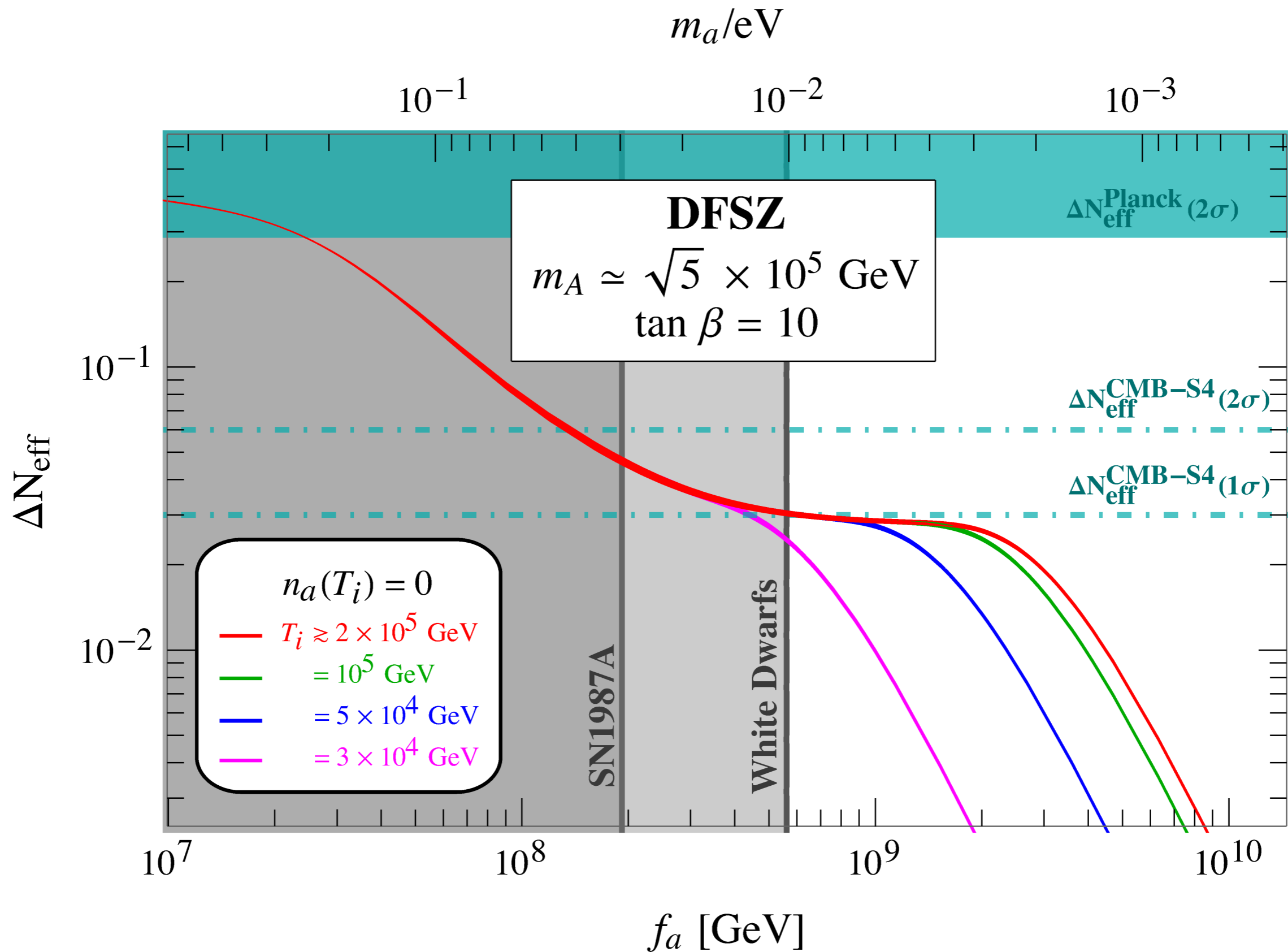
Maxwell-Boltzmann statistics (i.e., no quantum effects)

Static thermal bath (i.e., no energy exchanged)

KSVZ Axion



DFSZ Axion



Finite QCD Axion Mass Effects?

Planck: tension with astrophysics and axion mass non-negligible

Finite axion mass

- Pion scatterings

Ferreira et al., **Phys.Rev.D 103 (2021)**

Notari et al., **Phys.Rev.Lett. 131 (2023)**

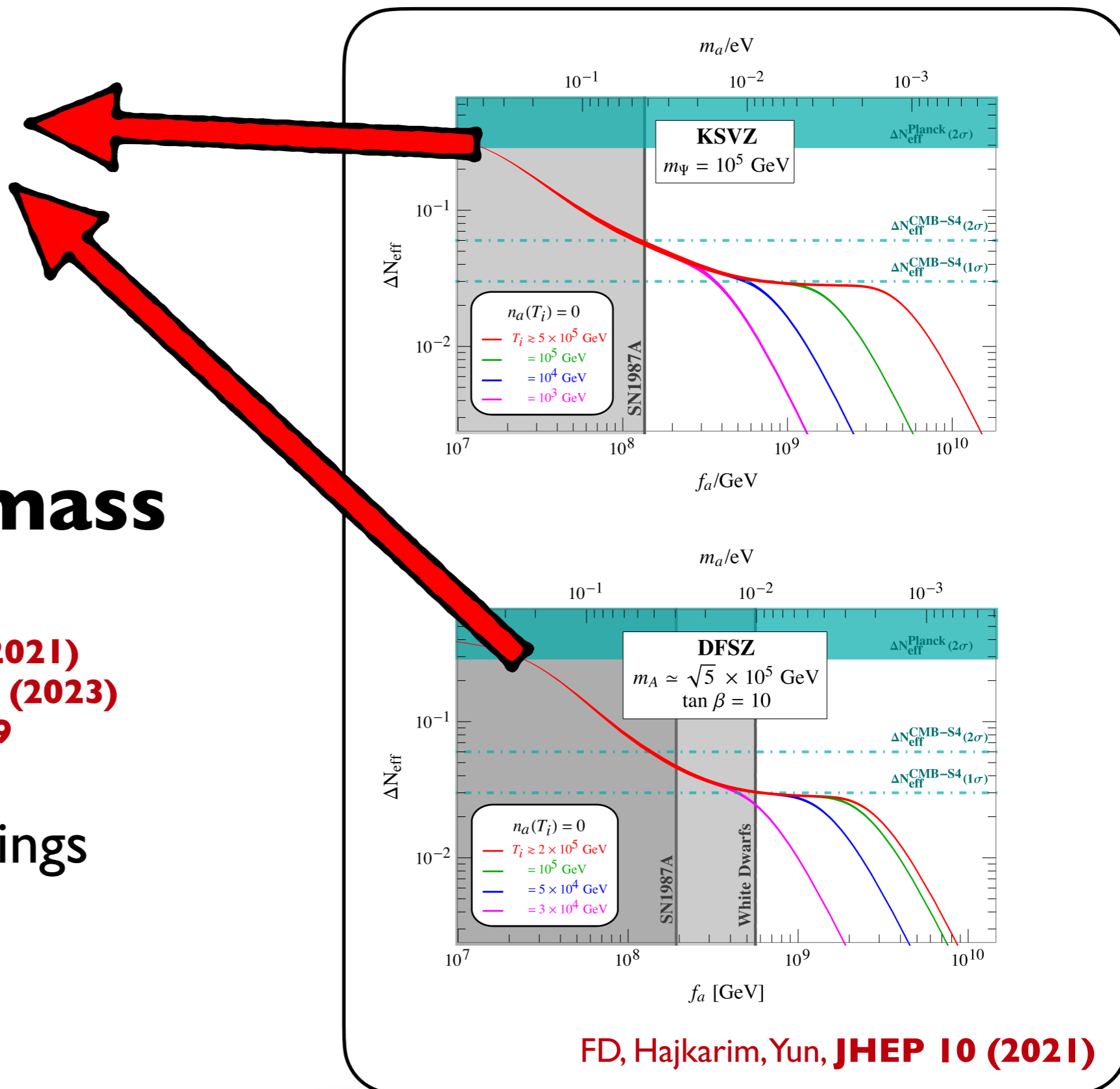
Bianchini et al., **arXiv:2310.08169**

- Gluon, photon couplings

Caloni et al., **JCAP 09 (2022)**

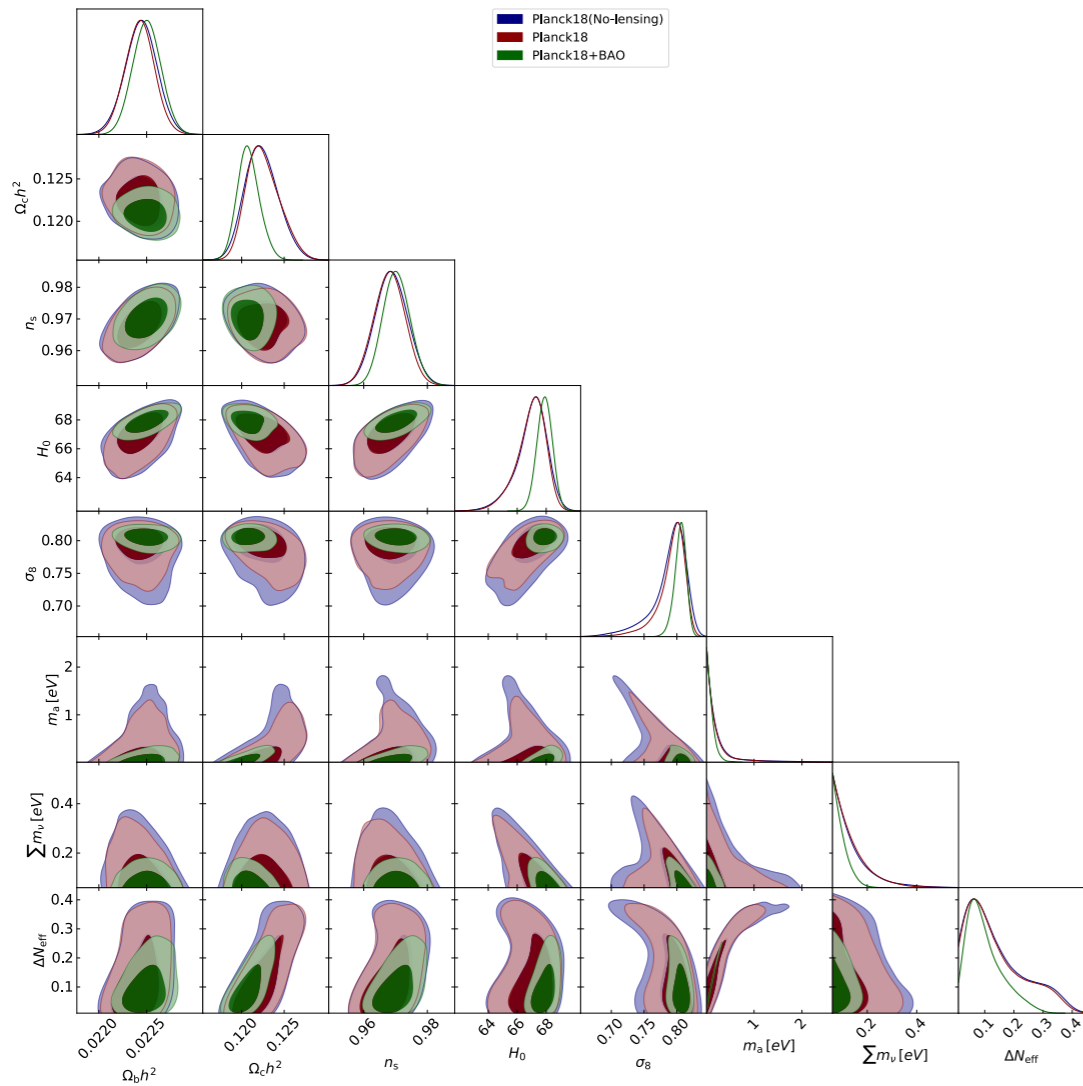
- KSVZ and DFSZ

FD et al., **JCAP 09 (2022)**



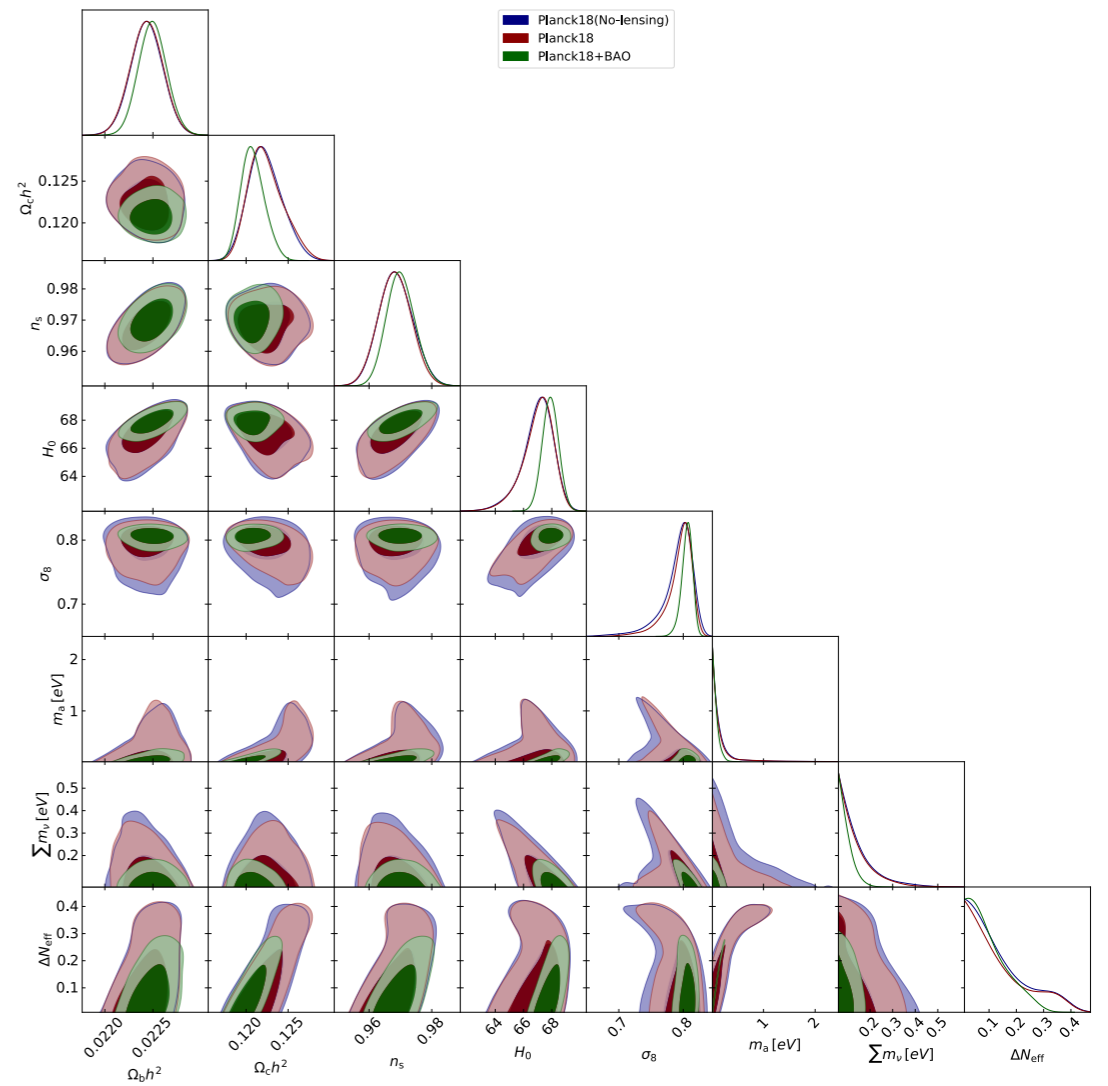
Axion Mass Bound

KSVZ



$$m_a \leq 0.282(0.420) \text{ eV}$$

DFSZ



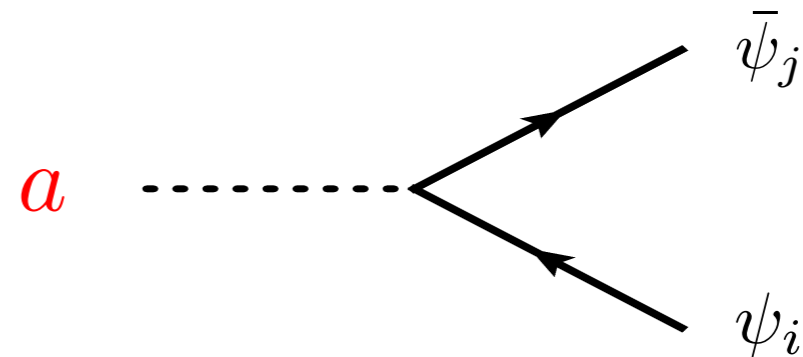
$$m_a \leq 0.209(0.293) \text{ eV}$$

A Minor Variation: FV Axions

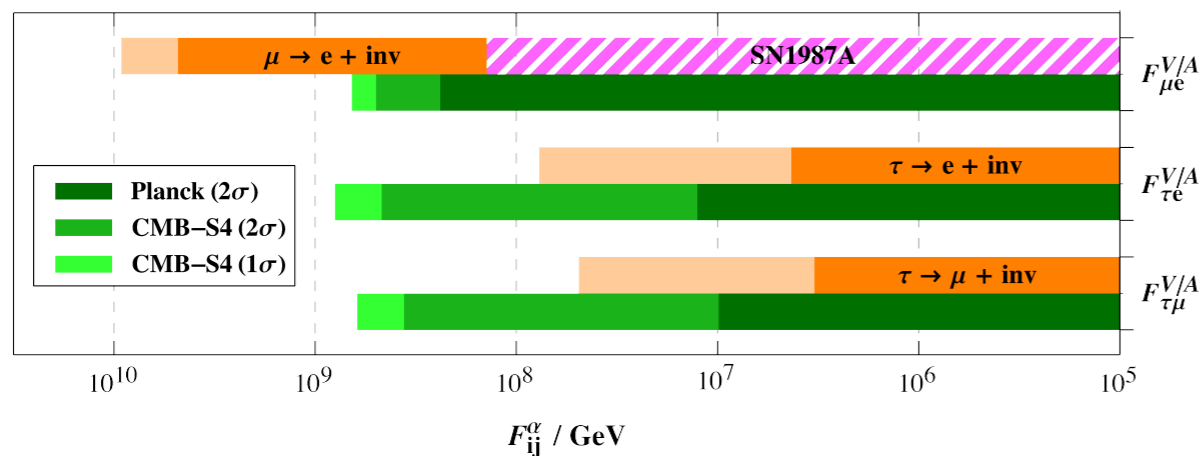
Target of several terrestrial experiments

What about their role in the early universe?

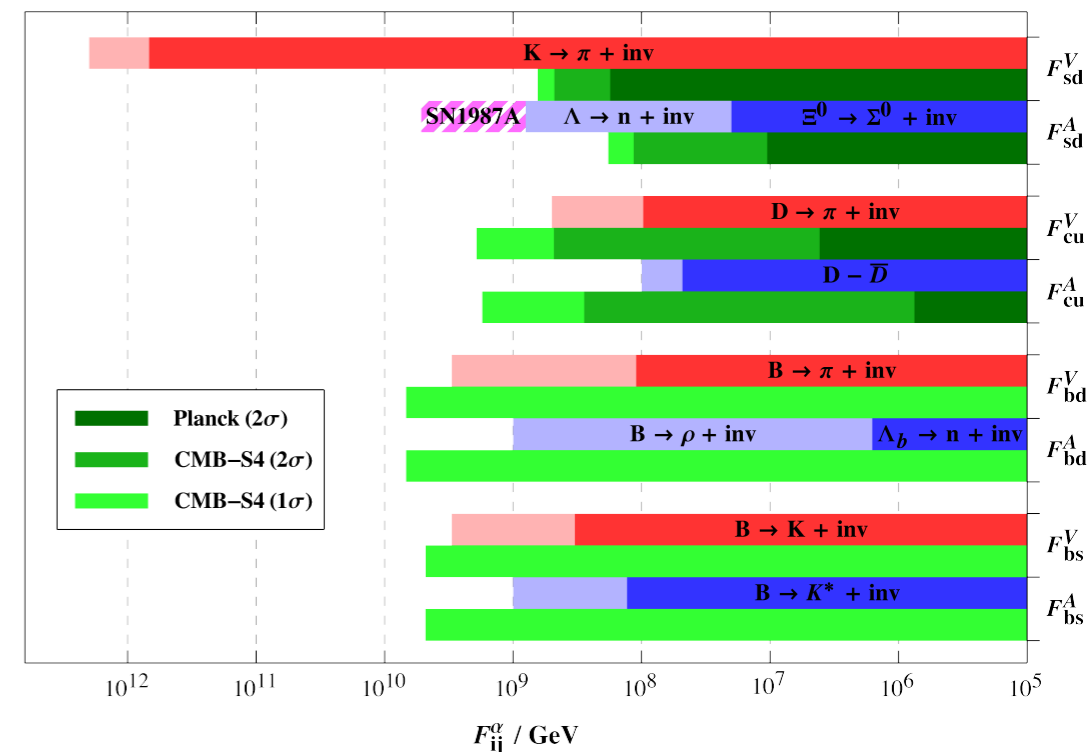
$$\mathcal{L}_{\text{FV}}^{(a)} = \frac{\partial_\mu a}{2f_a} \sum_{\psi_i \neq \psi_j} \bar{\psi}_i \gamma^\mu \left(c_{\psi_i \psi_j}^V + c_{\psi_i \psi_j}^A \gamma^5 \right) \psi_j$$



Leptonic FV



Hadronic FV



Current and future cosmological bounds competitive (or sometimes even better!) than terrestrial searches

Back to the Phase-Space

Model-independent analysis:
generic production of a light X $\mathcal{B}_1 \dots \mathcal{B}_n \rightarrow \mathcal{B}_{n+1} \dots \mathcal{B}_m X$

$$\frac{df_X(k, t)}{dt} = \left(1 - \frac{f_X(k, t)}{f_X^{\text{eq}}(k, t)} \right) C_{n \rightarrow mX}(k, t)$$

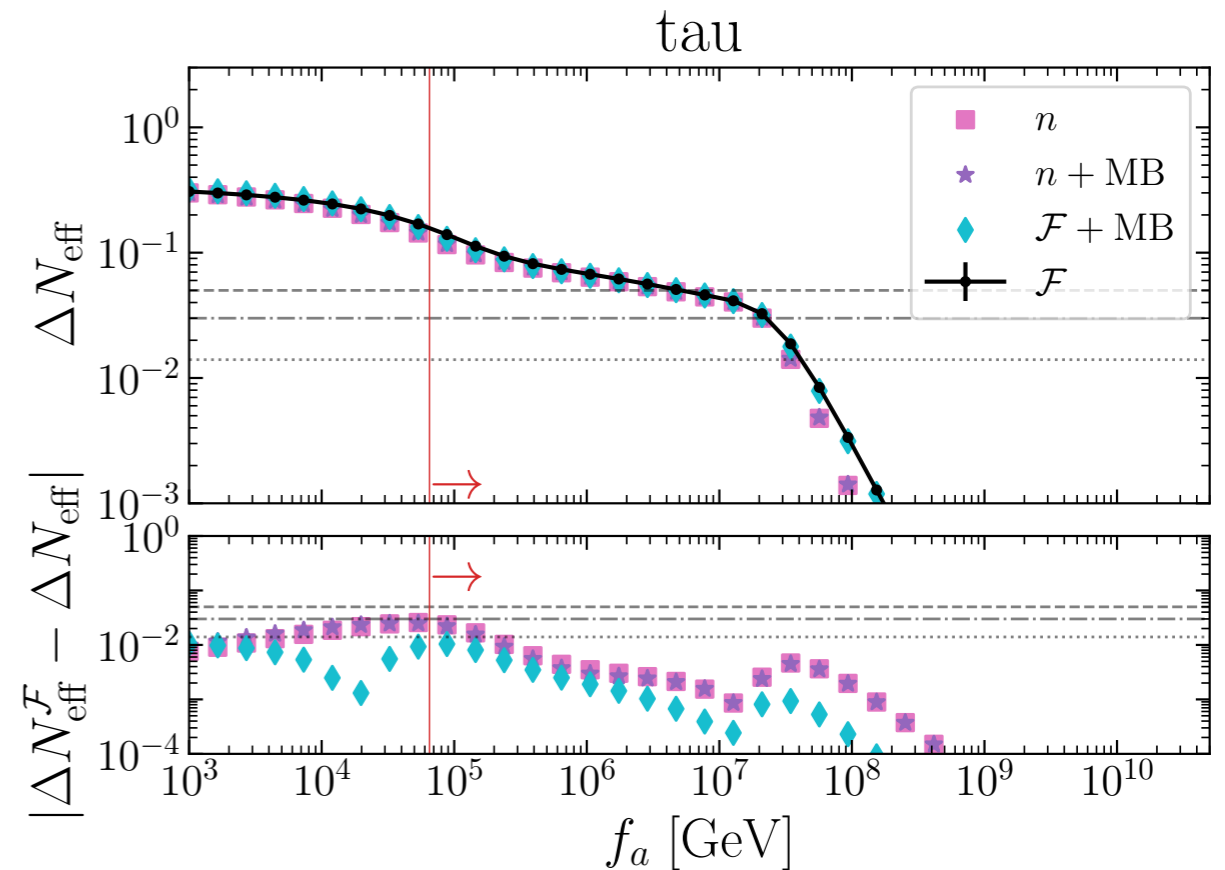
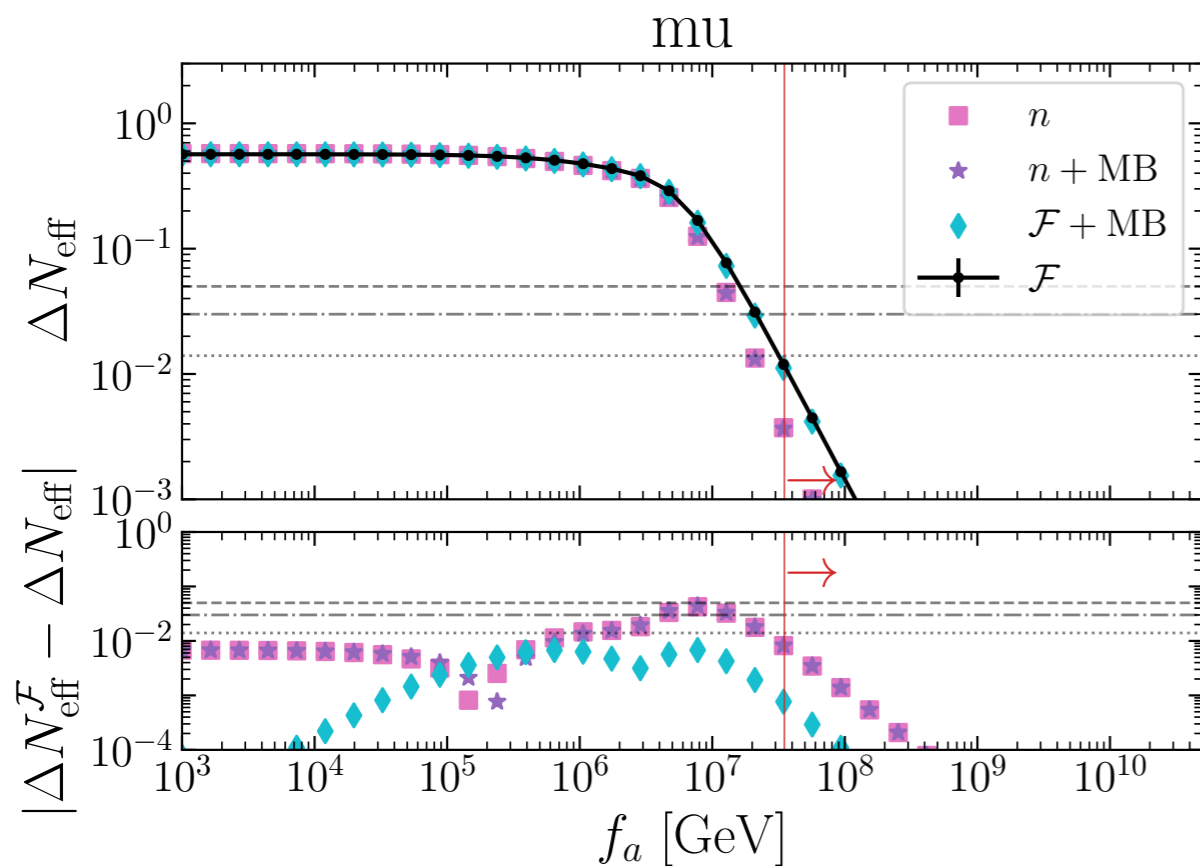
1. Keep track of phase-space and compute the energy density
2. Quantum statistical effects take into account
3. Energy exchanged with the thermal bath accounted for

Spectral distortions detectable in the future!

Axion-Fermion Interactions

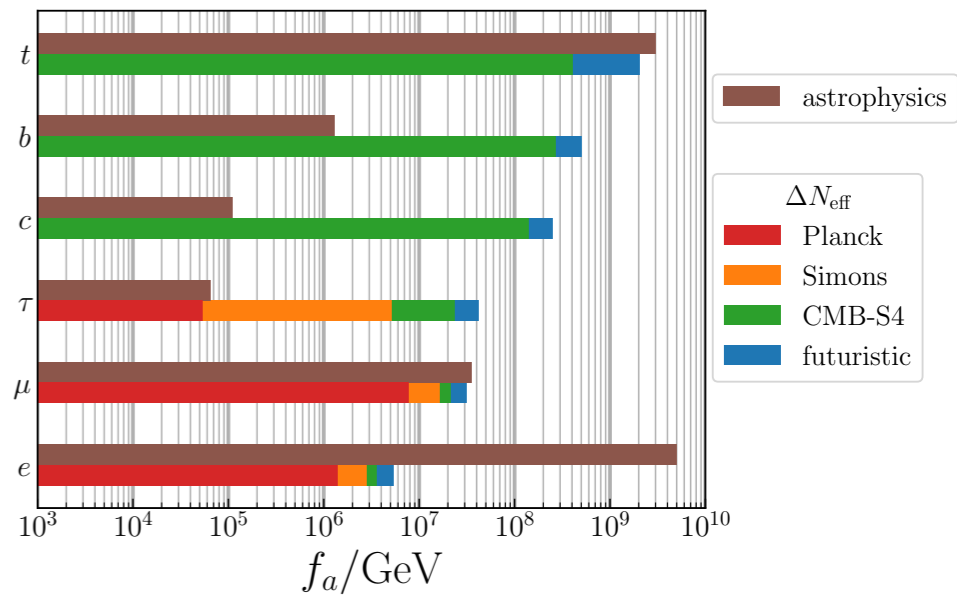
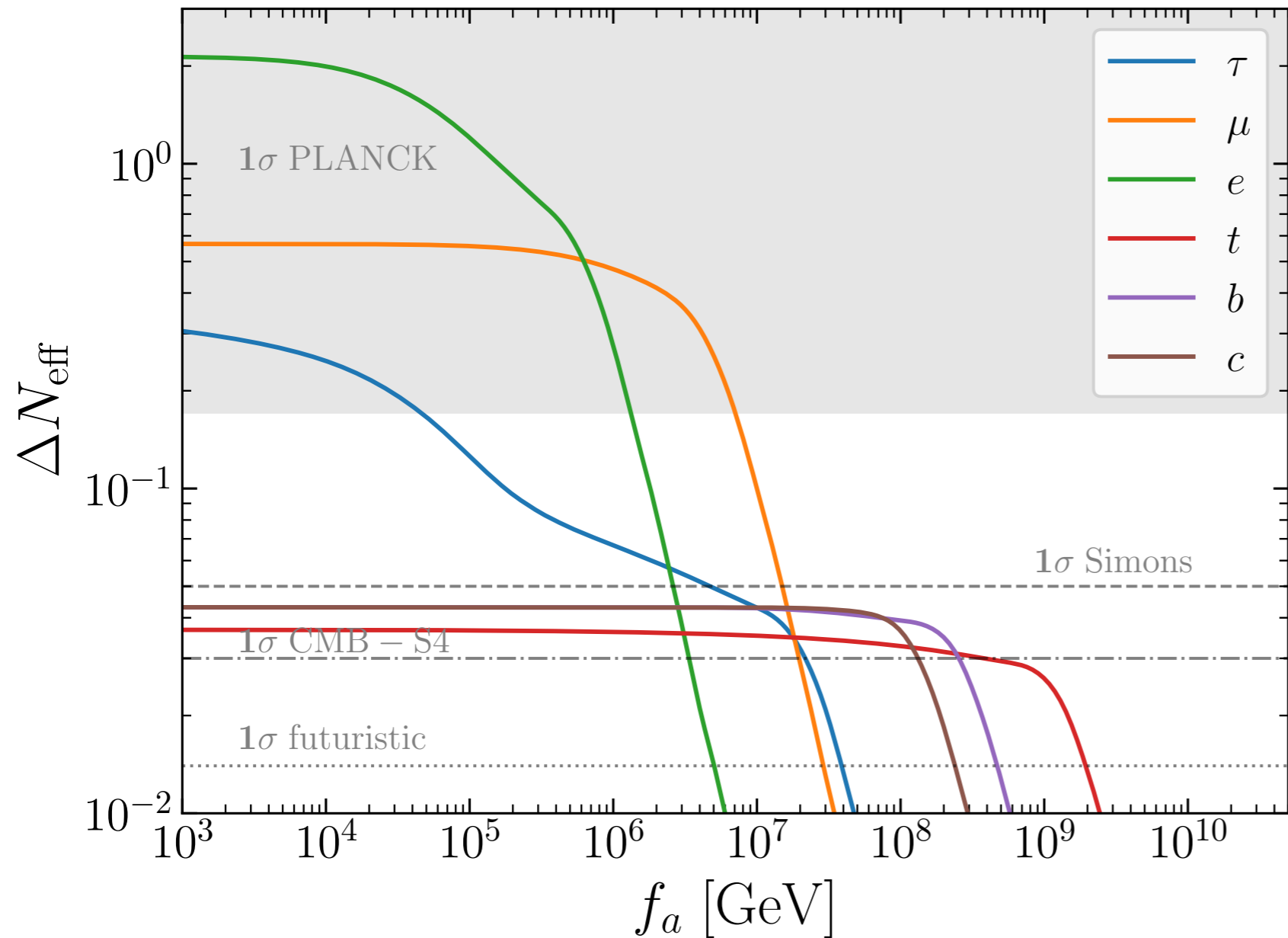
$$\mathcal{L}_{\text{int}} = \frac{\partial_\mu a}{2f_a} \sum_\psi c_\psi \bar{\psi} \gamma^\mu \gamma_5 \psi$$

PRELIMINARY



Difference detectable in the future!

Axion-Fermion Interactions



Outlook



Peccei-Quinn Mechanism and the QCD Axion

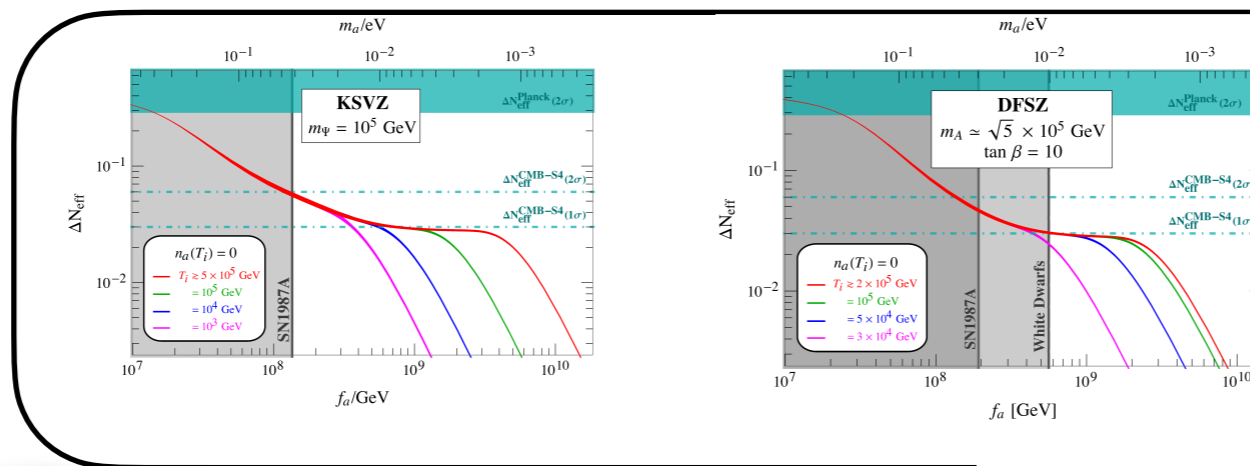
Motivated and testable scenario rich of cosmological consequences

Thermal Axions

Complementary to other probes of the PQ mechanism

Distinct signatures of ALPs coupled to standard model particles

Outlook



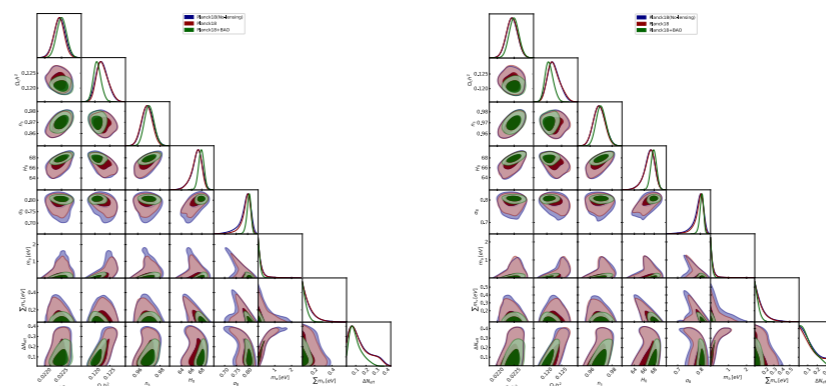
ΔN_{eff} tracking the number density

FD, Hajkarim, Yun, **JHEP 10 (2021)**

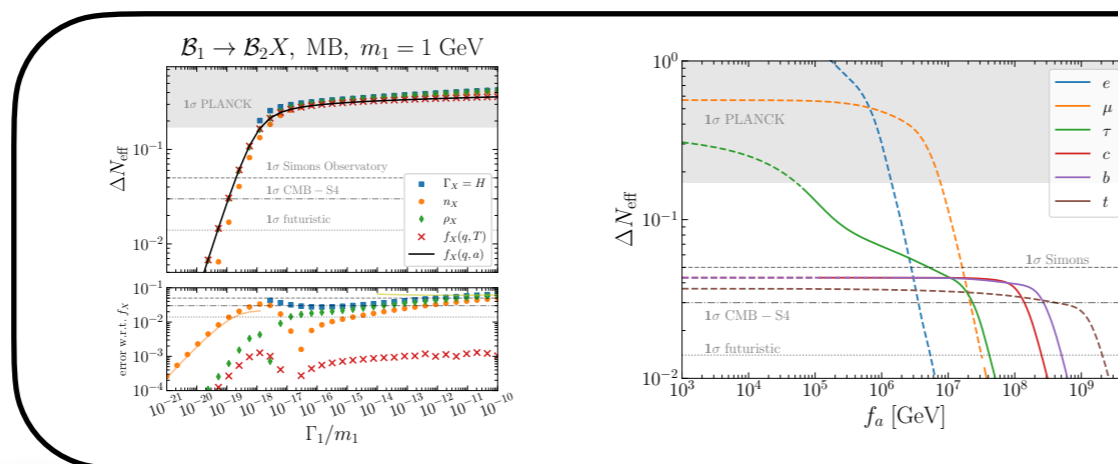
FD, Hajkarim, Yun, **Phys.Rev.Lett. 128 (2022)**

FD, Di Valentino, Giarè, Hajkarim, Melchiorri, Mena, Renzi, Yun, **JCAP 09 (2022)**

Axion cosmological mass bound



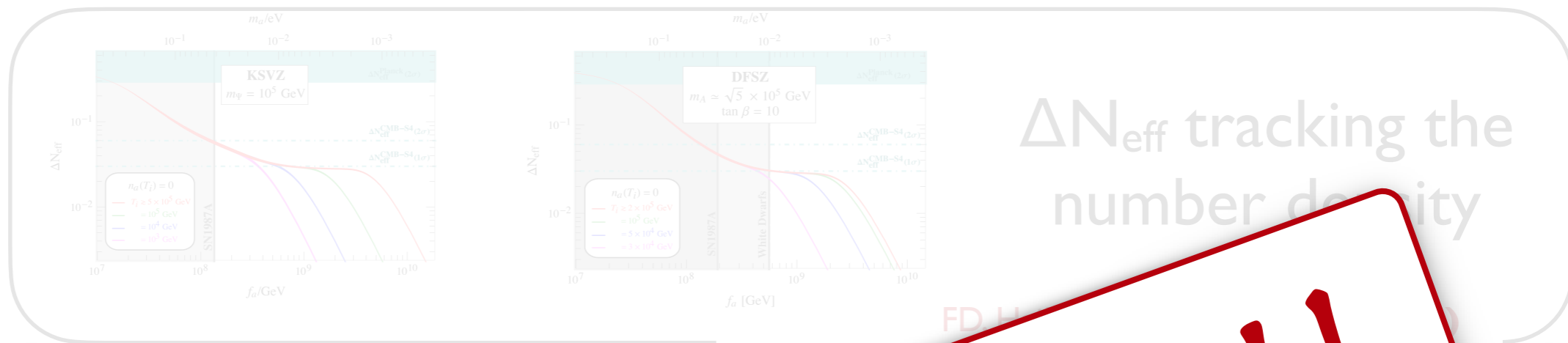
Importance of a phase space analysis



FD, Hajkarim, Lenoci, **JCAP 03 (2024)**

FD, Lenoci, **in preparation**

Outlook

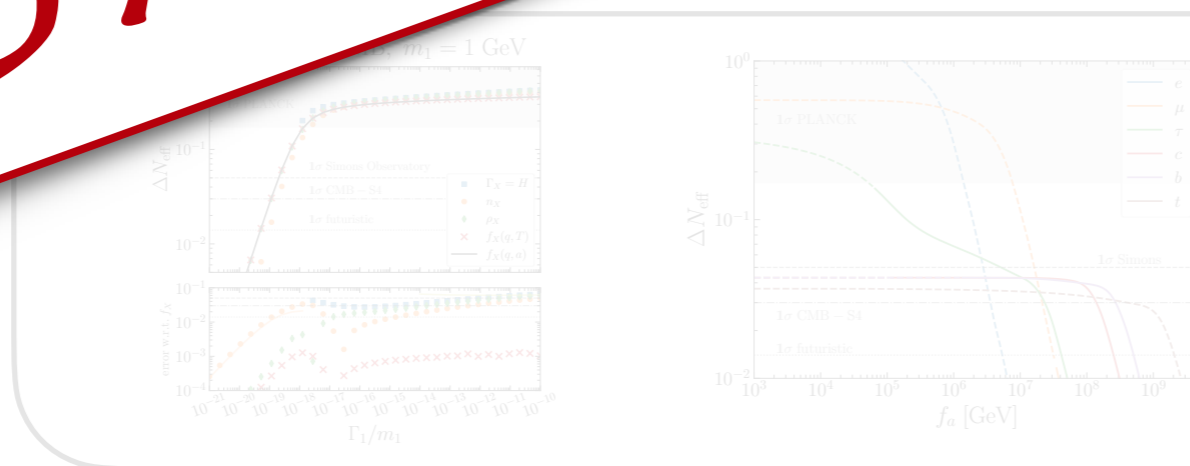


ΔN_{eff} tracking the number density

FD, Di Valentino, Giarè, Hajkarim, Melchiorri, Mena, Renzi, Yun, **JCAP 09 (2022)**

Axion cosmological mass bounds

DANKESCHÖN!



Importance of a phase space analysis

FD, Hajkarim, Lenoci, **JCAP 03 (2024)**
FD, Lenoci, in preparation