

Testing Neutrino Mass Origins with Supernova Neutrinos

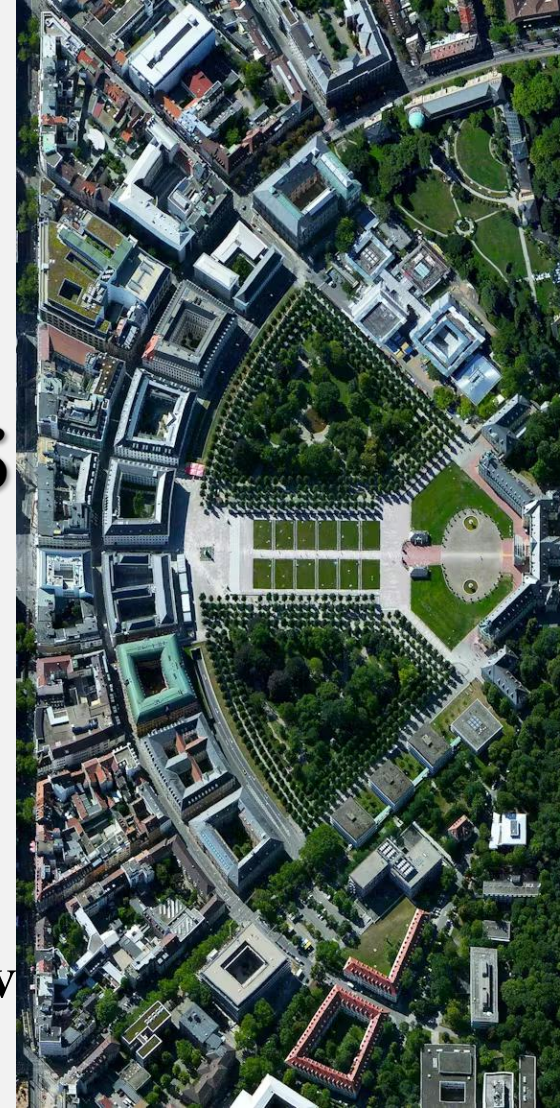
Chui-Fan Kong

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Tsung-Dao Lee Institute, Shanghai Jiao Tong University

arXiv:2404.17352 [hep-ph], PRL 133 (2024) 12, 121802

In collaboration with: Shao-Feng Ge & Alexei Y. Smirnov



李政道研究所
TSUNG-DAO LEE INSTITUTE

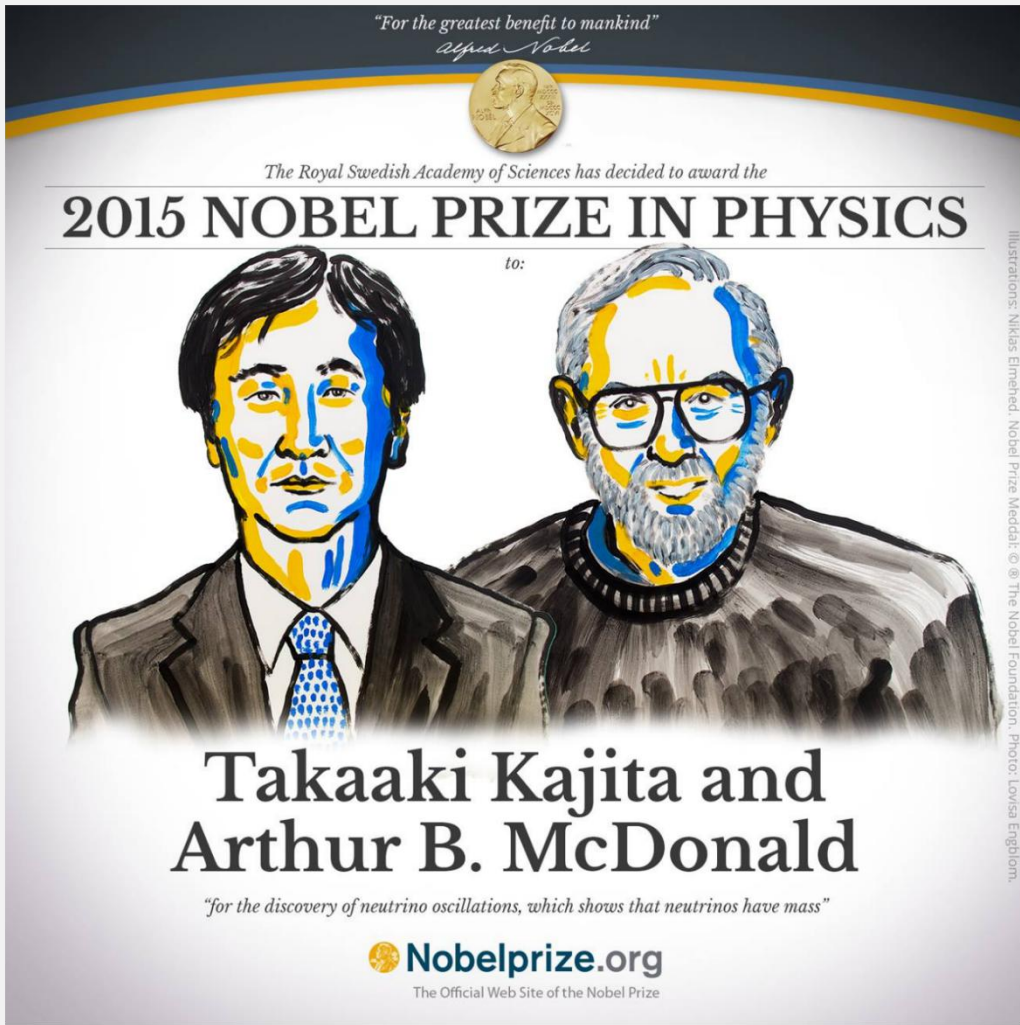


上海交通大學
SHANGHAI JIAO TONG UNIVERSITY



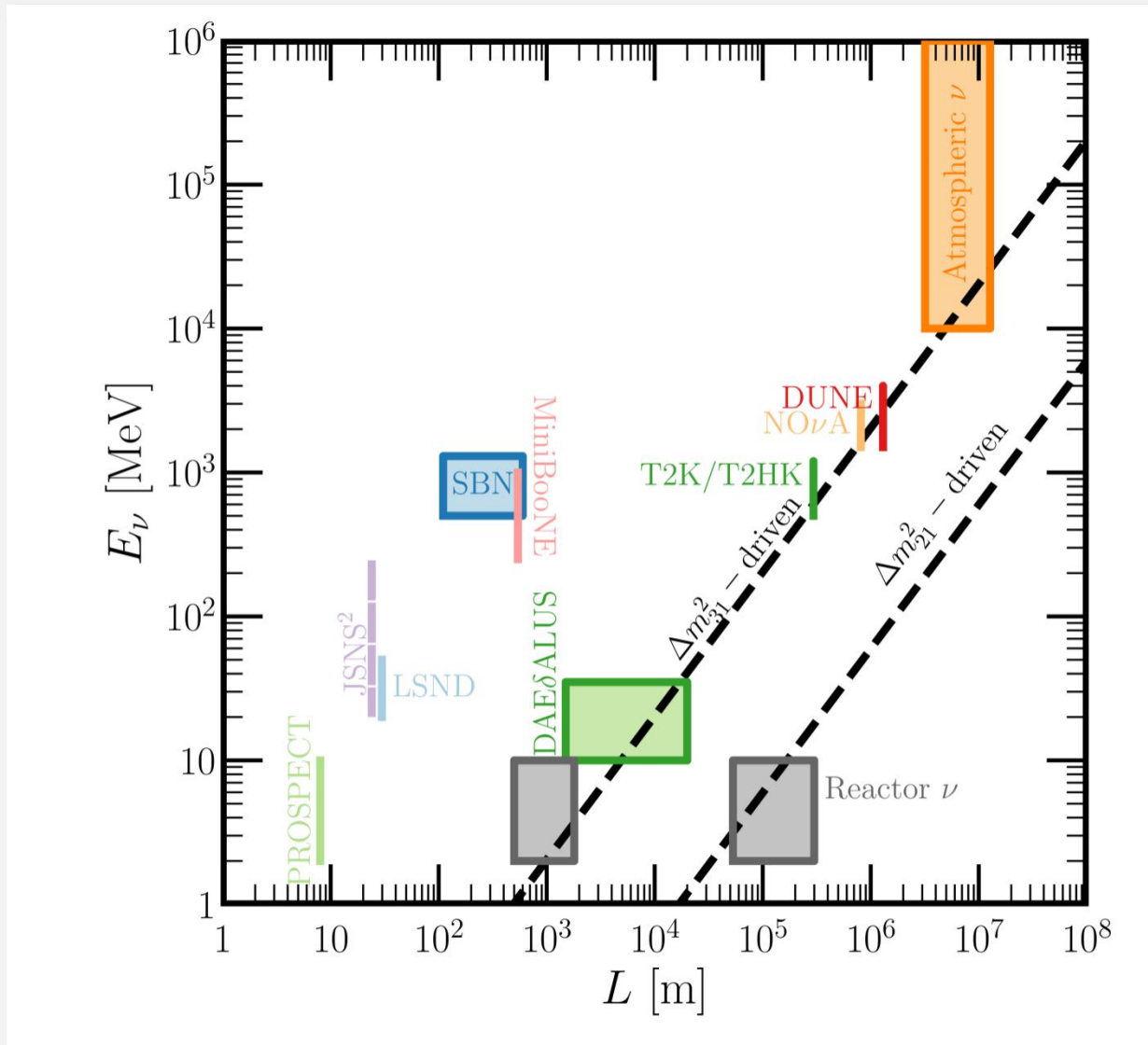
BLV @ KIT, Oct 8-11 2024

• Evidence of Neutrino Mass



“for the discovery of neutrino oscillations, which shows that neutrinos have mass”

• Evidence of Neutrino Mass

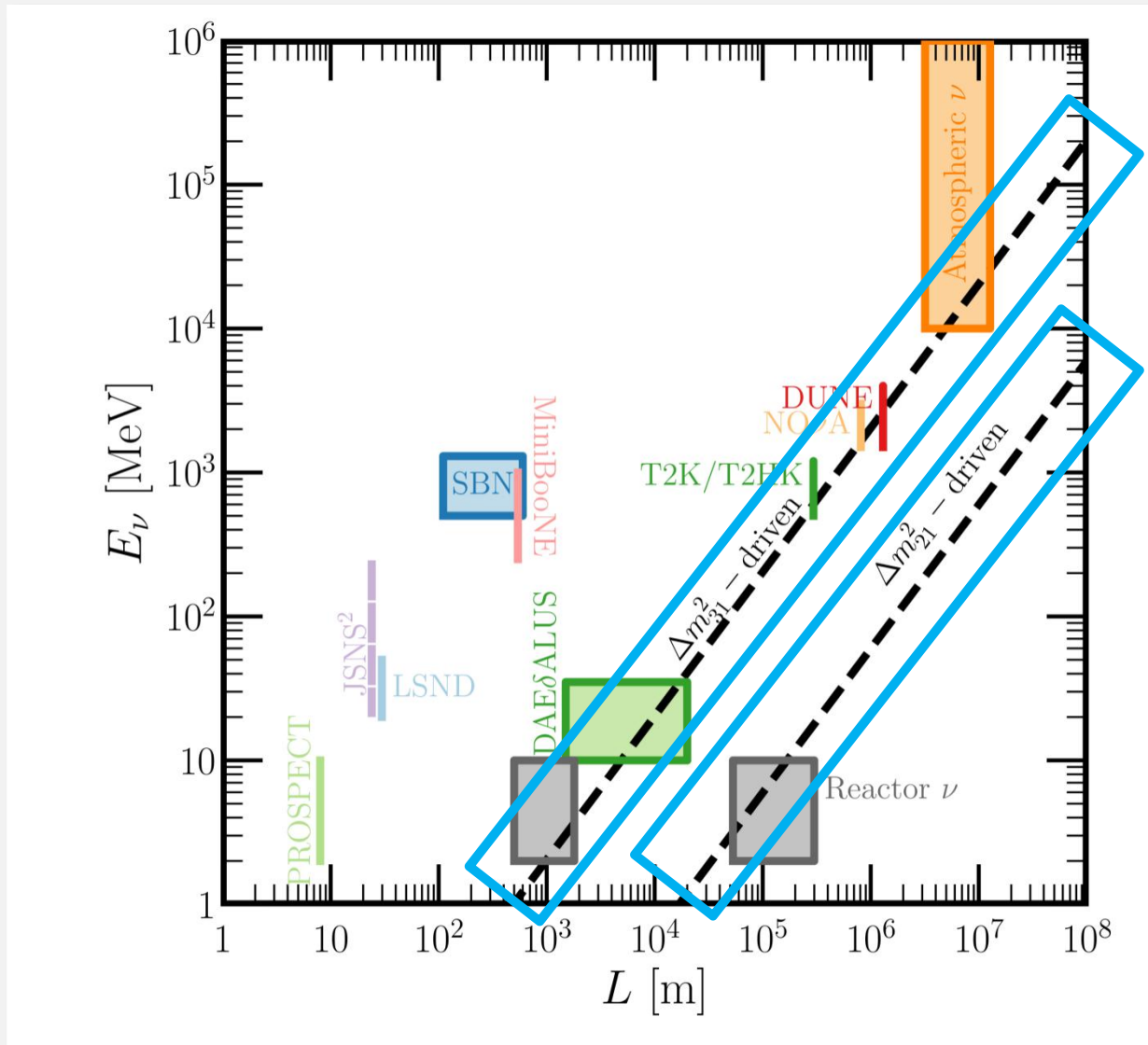


*R. Harnik, K. Kelly, P. Machado
arXiv: 1911.05088*

Evidence of Neutrino Mass

*[see talks by Michele Maltoni,
Renata Zukanovich Funchal,
Daniel Naredo]*

$$\text{oscillation phase} : \propto \frac{\Delta m_{ij}^2 L}{E_\nu}$$



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Evidence of Neutrino Mass

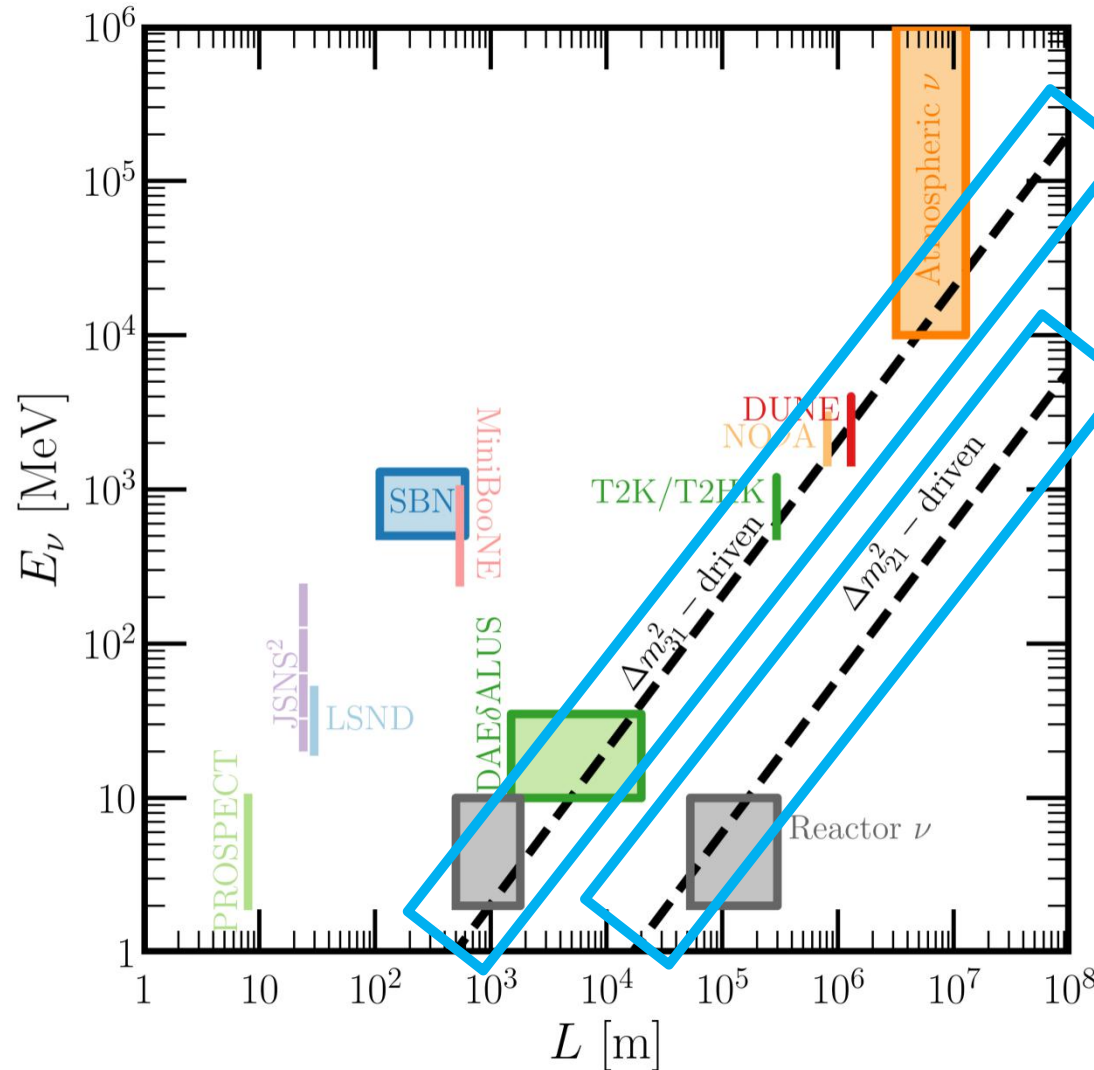
*[see talks by Michele Maltoni,
Renata Zukanovich Funchal,
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Q: What's the origin of
neutrino mass?

*R. Harnik, K. Kelly, P. Machado
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• Neutrino Mass Origin I: vacuum mass

*[see talks by Ana M. Teixeira,
Kevin Alberto Urquía-Calderón,
Stefan Antusch, Richard Ruiz,
Jonathan Kriewald]*

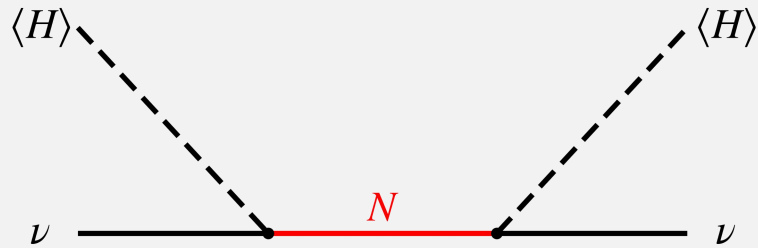
Vacuum Neutrino Mass

Type-I seesaw

Type-II seesaw

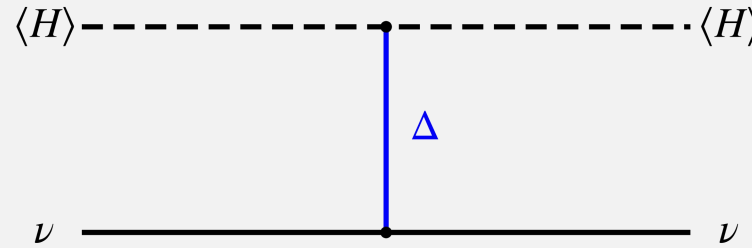
Type-III seesaw

...



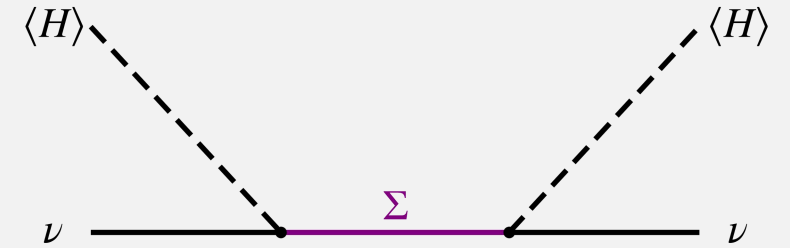
$$M_\nu = -\frac{1}{2} Y_\nu \frac{v^2}{M_R} Y_\nu^T$$

*P. Minkowski
T. Yanagida
M. Gell-Mann...*



$$M_\nu = \lambda_\Delta Y_\Delta \frac{v^2}{M_\Delta}$$

*M. Magg & C. Wetterich
G. Lazarides, Q. Shafi, & C. Wetterich
R. Mohapatra & G. Senjanovic...*



$$M_\nu = -\frac{1}{2} Y_\Sigma \frac{v^2}{M_\Sigma} Y_\Sigma^T$$

*R. Foot, H. Lew, X.-G. He, & G.C. Joshi
E. Ma...*

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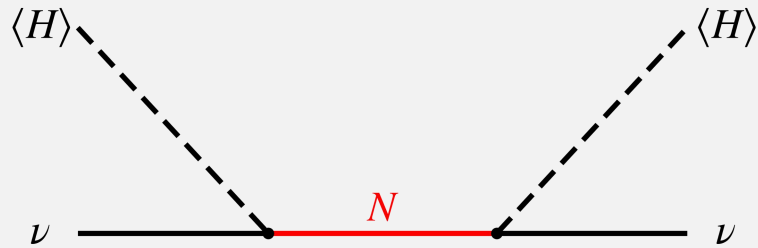
Vacuum Neutrino Mass

Type-I seesaw

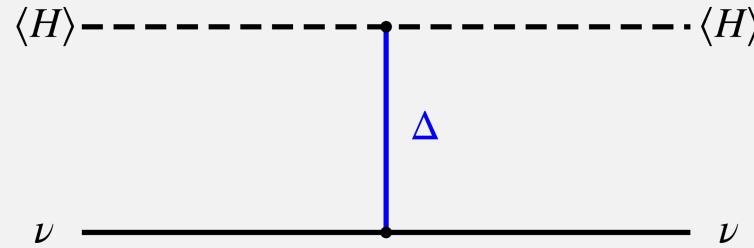
Type-II seesaw

Type-III seesaw

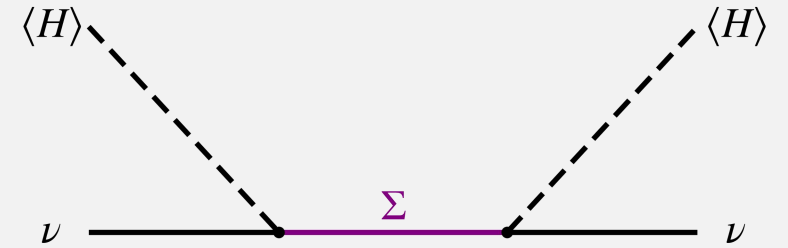
...



$$M_\nu = -\frac{1}{2} Y_\nu \frac{v^2}{M_R} Y_\nu^T$$



$$M_\nu = \lambda_\Delta Y_\Delta \frac{v^2}{M_\Delta}$$



$$M_\nu = -\frac{1}{2} Y_\Sigma \frac{v^2}{M_\Sigma} Y_\Sigma^T$$

$$m_{\text{vac}}^2 = A$$

• Neutrino Mass Origin II: dark mass

$$H \sim \sqrt{p^2 + |m|^2} \approx p + \frac{|m|^2}{2E}$$

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What if $m = 0$, but neutrino matter potential

$$H \approx p + V, \quad \text{with } V = \frac{\dots}{2E}$$

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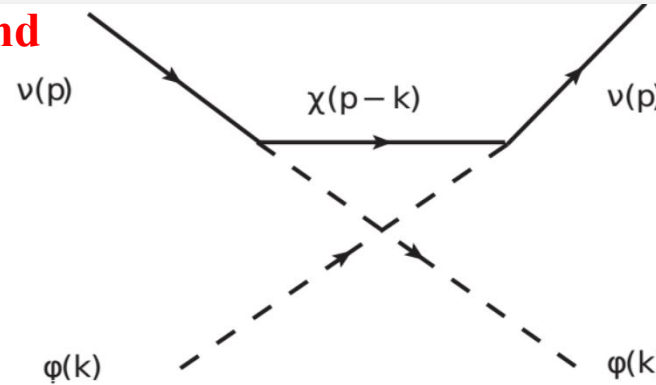
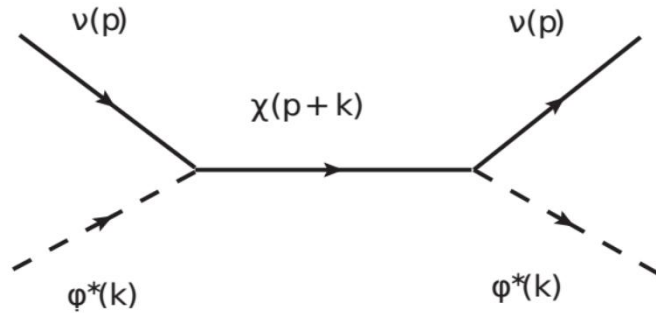
What if $m = 0$, but neutrino matter potential

$$H \approx p + V, \quad \text{with } V = \frac{\boxed{\dots}}{2E} \rightarrow \text{interpreted as effective mass or dark mass}$$

• Neutrino Mass Origin II: dark mass

Dark Neutrino Mass

Forward scattering with DM background



Introduce the effective or refractive mass squared as

$$V = m_{\text{ref}}^2 / 2E$$

$$m_{\text{ref}}^2 = 2EV$$

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$$m_{\text{ref}}^2 = m_{\text{as}}^2 \frac{y(y - \varepsilon)}{y^2 - 1}$$

$$m_{\text{as}}^2 = \sum_k g_{\alpha k} g_{\beta k}^* \frac{\rho_\phi}{m_\phi^2}$$

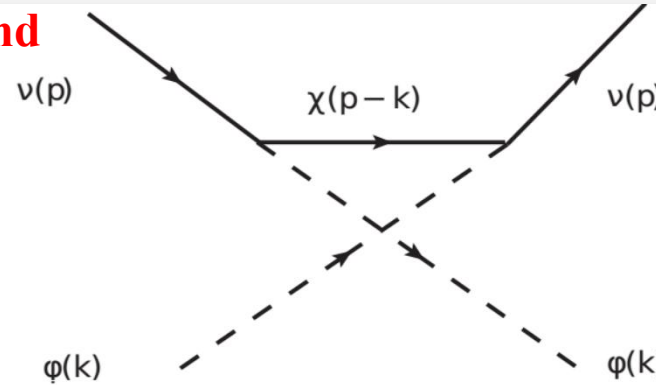
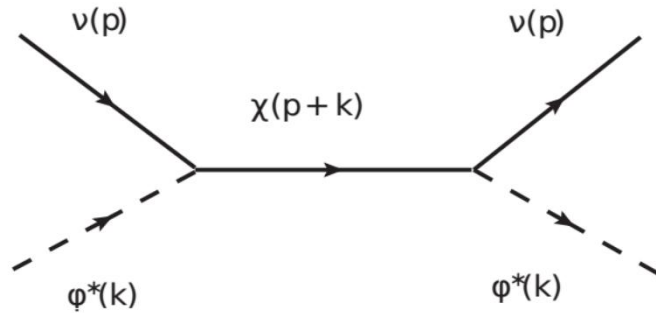
A. Y. Smirnov, talks@MAYORANA Workshop

[H. Davoudiasl, G. Mohlabeng, & M. Sullivan, arXiv:1803.00012; S.-F. Ge & H. Murayama, arXiv:1904.02518; K. Y. Choi, E. J. Chun & J. Kim, arXiv:1909.10478, 2012.09474; M. Sen and A. Y. Smirnov, arXiv:2306.15718]

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A. Y. Smirnov, talks@MAYORANA Workshop

$$m_{\text{dark}}^2(x) \propto \rho_\phi$$

• Neutrino Mass Origins Comparison

Vacuum Neutrino Mass: $m_{\text{vac}}^2 = A$

vs.

Dark Neutrino Mass: $m_{\text{dark}}^2(x) \propto \rho_\phi$

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Vacuum Neutrino Mass: $m_{\text{vac}}^2 = A$

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Can we distinguish these two origins ?

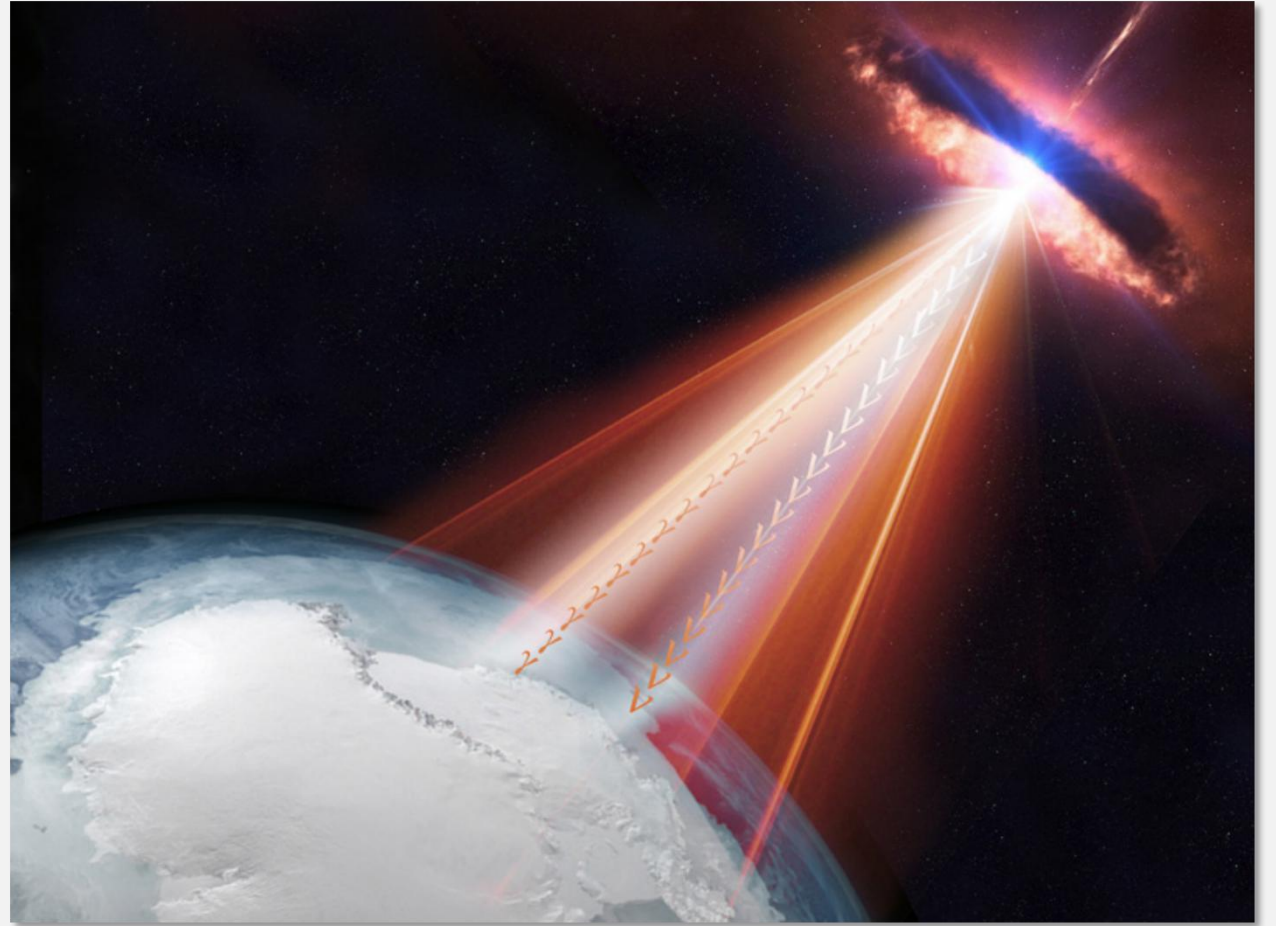
• Large Scales

Yes! Look into larger scales!

$$m_{\text{vac}}^2 = A$$

vs.

$$m_{\text{dark}}^2(x) \propto \rho_\phi$$



Credit: IceCube

• Supernova Neutrino Time Delay

Galactic supernovae are ideal neutrino sources!

POSSIBILITY OF DETERMINING THE UPPER LIMIT OF THE NEUTRINO MASS FROM THE TIME OF FLIGHT

G. I. Zatsepin

P. N. Lebedev Physics Institute, USSR Academy of Sciences

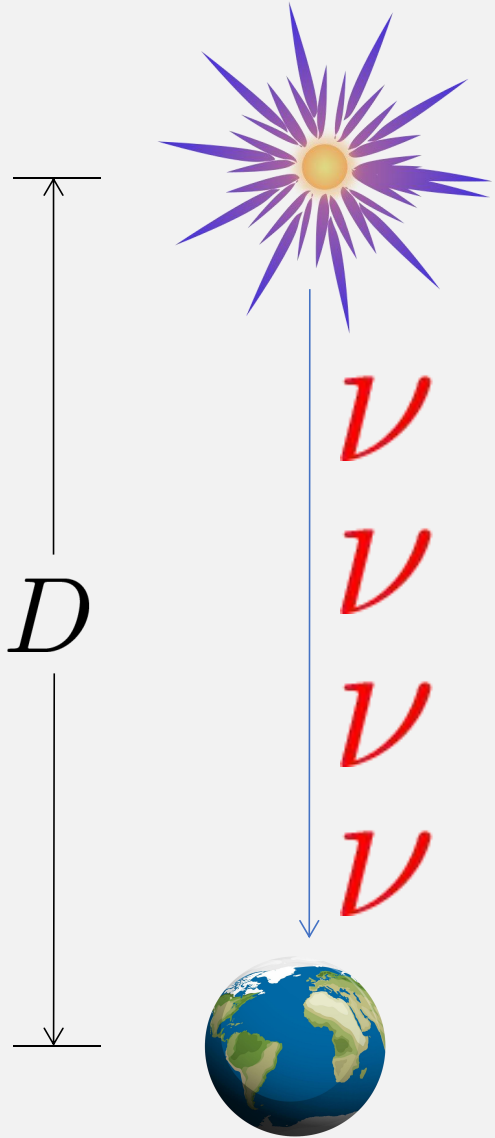
Submitted 20 July 1968

ZhETF Pis. Red. 8, No. 6, 333-334 (20 September 1968)

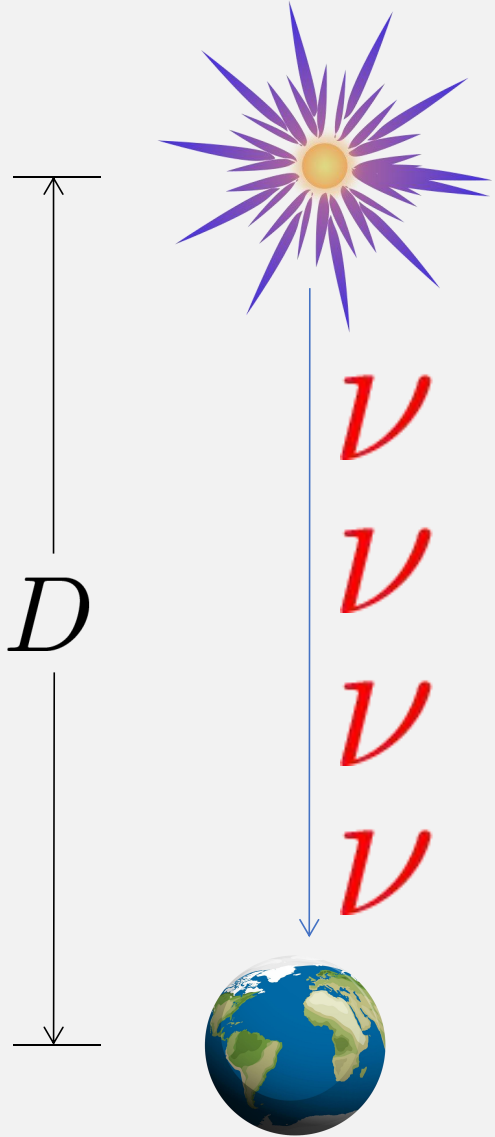
56 years ago!

[T. J. Loredo and D. Q. Lamb, *astro-ph/0107260*; E. Nardi and J. I. Zuluaga, *astro-ph/0306384*, *hep-ph/0412104*; G. Pagliaroli, F. Rossi-Torres and F. Vissani 1002.3349; J. S. Lu, J. Cao, Y. F. Li and S. Zhou, 1412.7418; R. S. L. Hansen, M. Lindner and O. Scholer, 1904.11461; F. Pompa, F. Capozzi, O. Mena and M. Sorel, 2203.00024; F. Pompa and O. Mena, 2310.05474; G. Parker and M. Wurm, 2311.10682 ...]

• Supernova Neutrino Time Delay



• Supernova Neutrino Time Delay (vacuum neutrino mass)

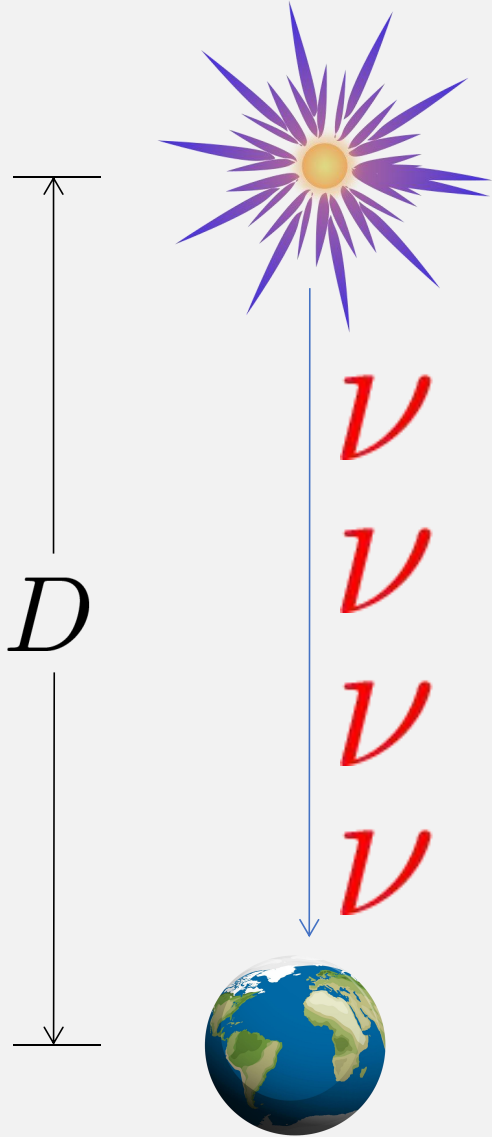


$$\downarrow E_\nu = \sqrt{p_\nu^2 + m^2}, \quad v = \frac{dE_\nu}{dp_\nu}$$

group velocity:

$$v = \frac{p}{E} = \sqrt{1 - \frac{m_{\text{vac}}^2}{E^2}} \approx 1 - \frac{m_{\text{vac}}^2}{2E^2}$$

• Supernova Neutrino Time Delay (vacuum neutrino mass)



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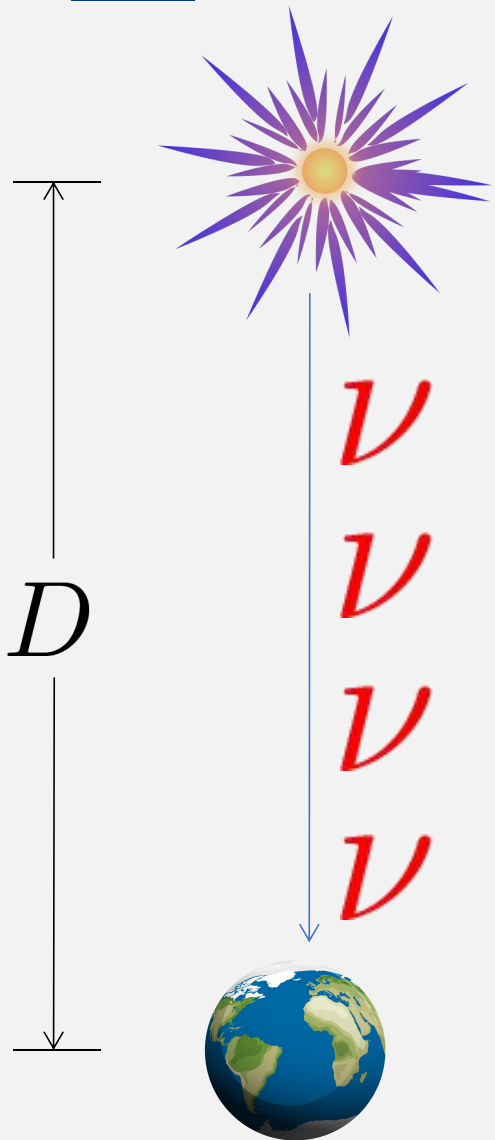
$$v = \frac{p}{E} = \sqrt{1 - \frac{m_{\text{vac}}^2}{E^2}} \approx 1 - \frac{m_{\text{vac}}^2}{2E^2}$$

smaller than speed of light!

&

space-time independent

• Supernova Neutrino Time Delay (vacuum neutrino mass)



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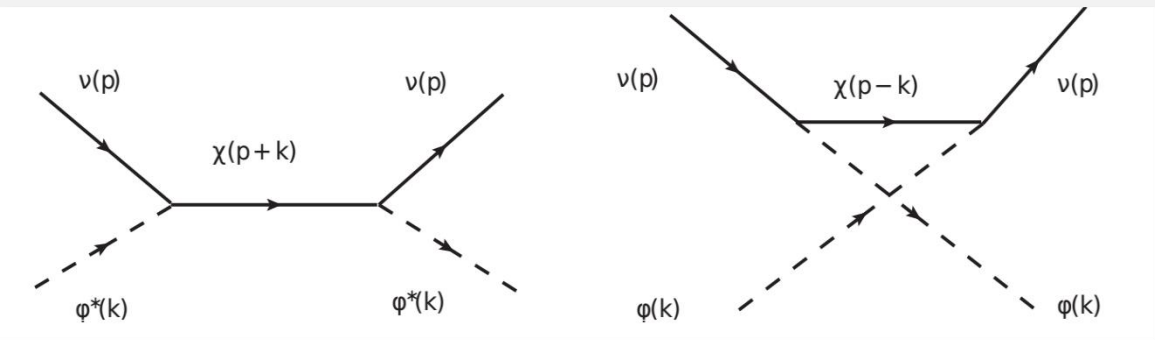
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time delay:

$$\Delta t_{\text{vac}} \equiv \frac{D}{v} - \frac{D}{c(\equiv 1)} = \frac{m_{\text{vac}}^2}{2E^2} D \approx 5.14 \text{ ms} \left(\frac{m_{\text{vac}}}{\text{eV}} \right)^2 \left(\frac{10 \text{ MeV}}{E} \right)^2 \frac{D}{10 \text{ kpc}}$$

Supernova Neutrino Time Delay (dark neutrino mass)

Recall



Introduce the effective or refractive mass squared as

$$V = m_{\text{ref}}^2 / 2E$$

$$m_{\text{ref}}^2 = 2EV$$



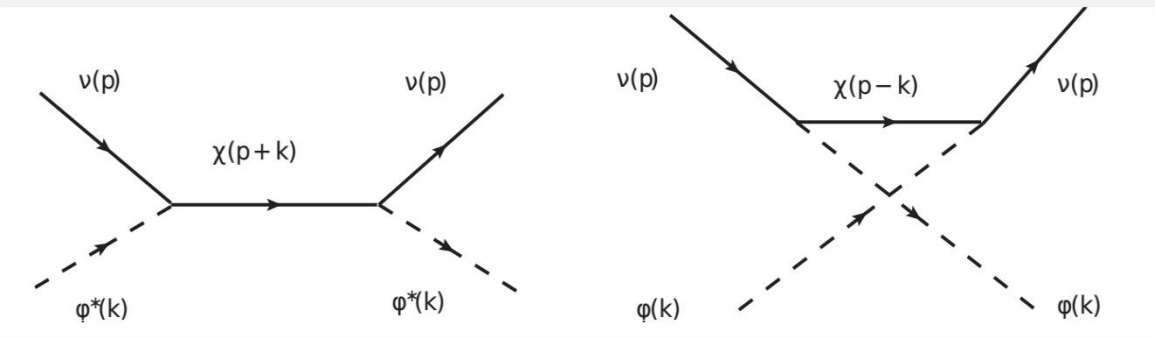
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$$1 - v(\mathbf{x}) = \frac{m_{\text{dark}}^2(\mathbf{x}, p_\nu)}{2p_\nu^2} - \frac{1}{2p_\nu} \frac{dm_{\text{dark}}^2(\mathbf{x}, p_\nu)}{dp_\nu}$$

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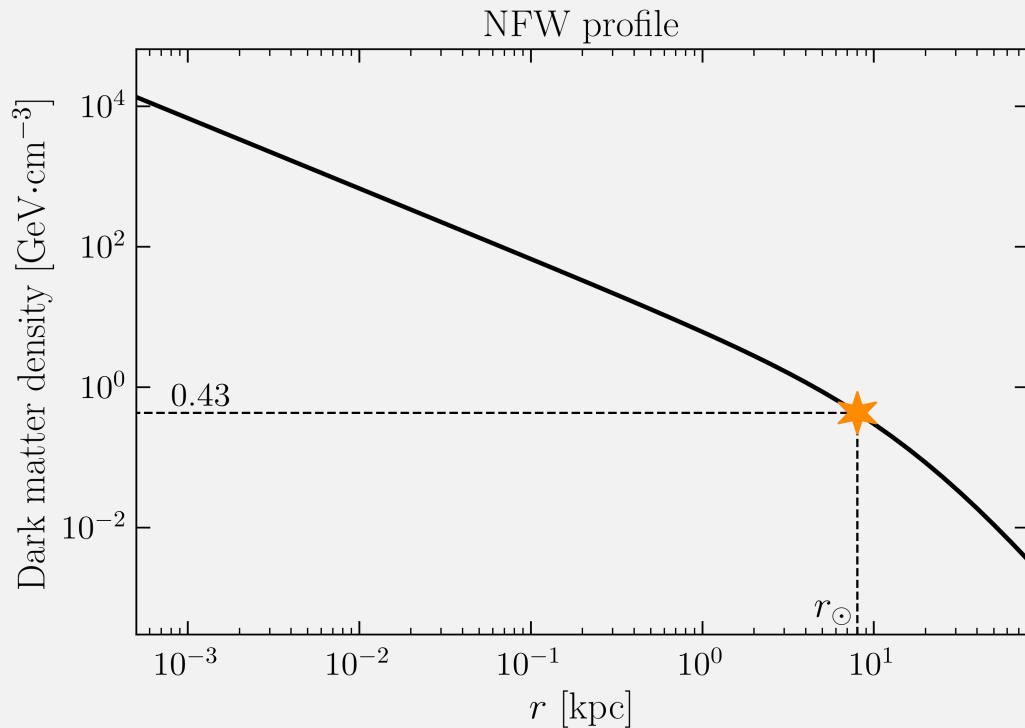
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$$1 - v(\mathbf{x}) = \frac{m_{\text{dark}}^2(\mathbf{x}_\odot)}{2E^2} \frac{\rho_\phi(\mathbf{x})}{\rho_\phi(\mathbf{x}_\odot)}$$

space-time dependent!

[\mathbf{x}_\odot : solar system position]

Supernova Neutrino Time Delay (dark neutrino mass)



Navarro-Frenk-White profile

$$E_{\nu} = p_{\nu} + V, \quad v = \frac{dE_{\nu}}{dp_{\nu}}$$

group velocity:

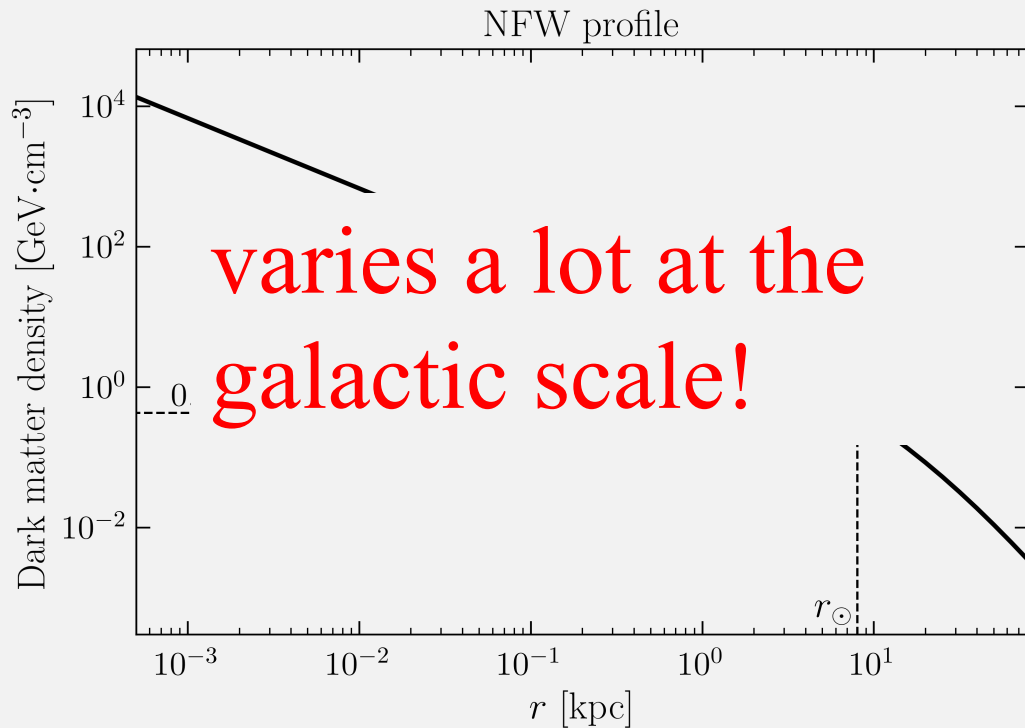
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$$\Delta t_{\text{dark}} \equiv \int_{\mathbf{x}_{*}}^{\mathbf{x}_{\odot}} \left(\frac{1}{v(\mathbf{x})} - 1 \right) |d\mathbf{x}| \approx \int_{\mathbf{x}_{*}}^{\mathbf{x}_{\odot}} (1 - v(\mathbf{x})) |d\mathbf{x}|$$

just an integration over neutrino trajectory

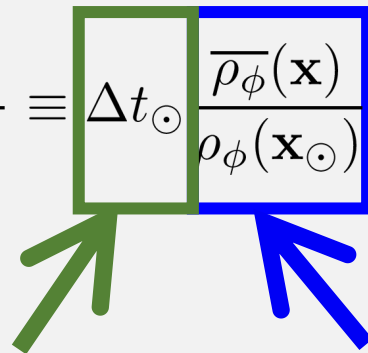
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vacuum neutrino mass

differed by this factor!

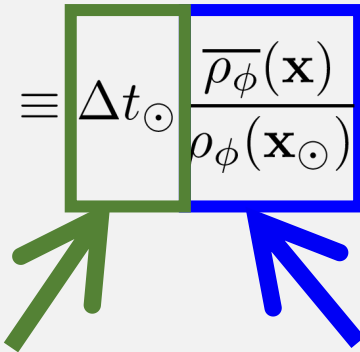
Supernova Neutrino Time Delay (dark neutrino mass)

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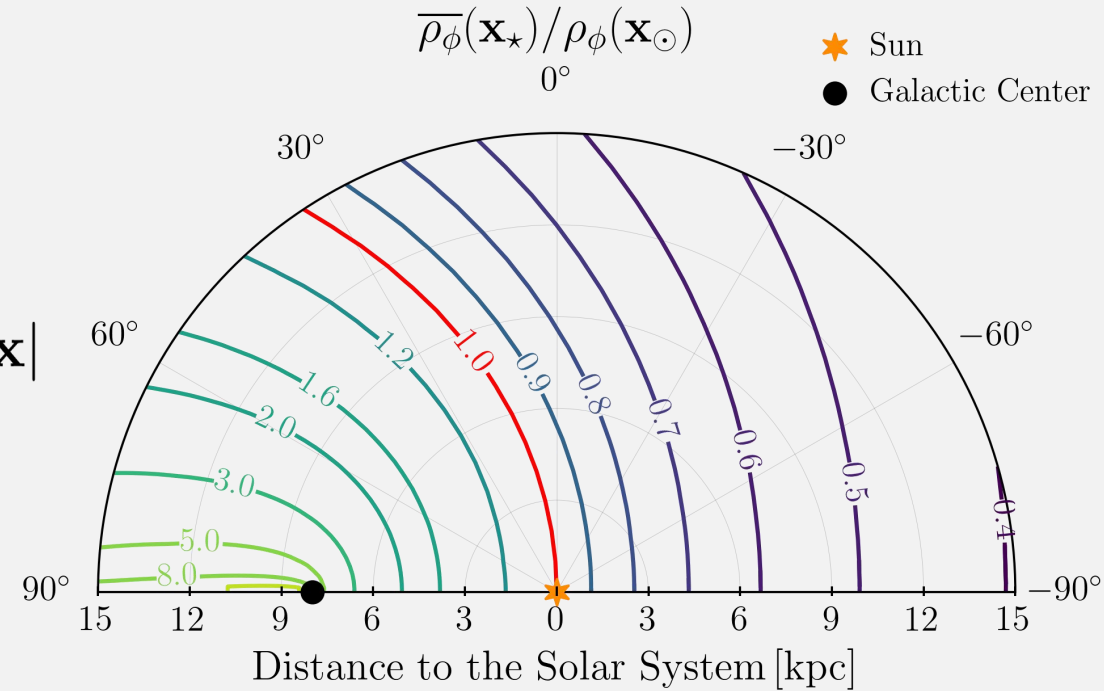
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Ge, CFK, Smirnov
arXiv: 2404.17352



Simulation

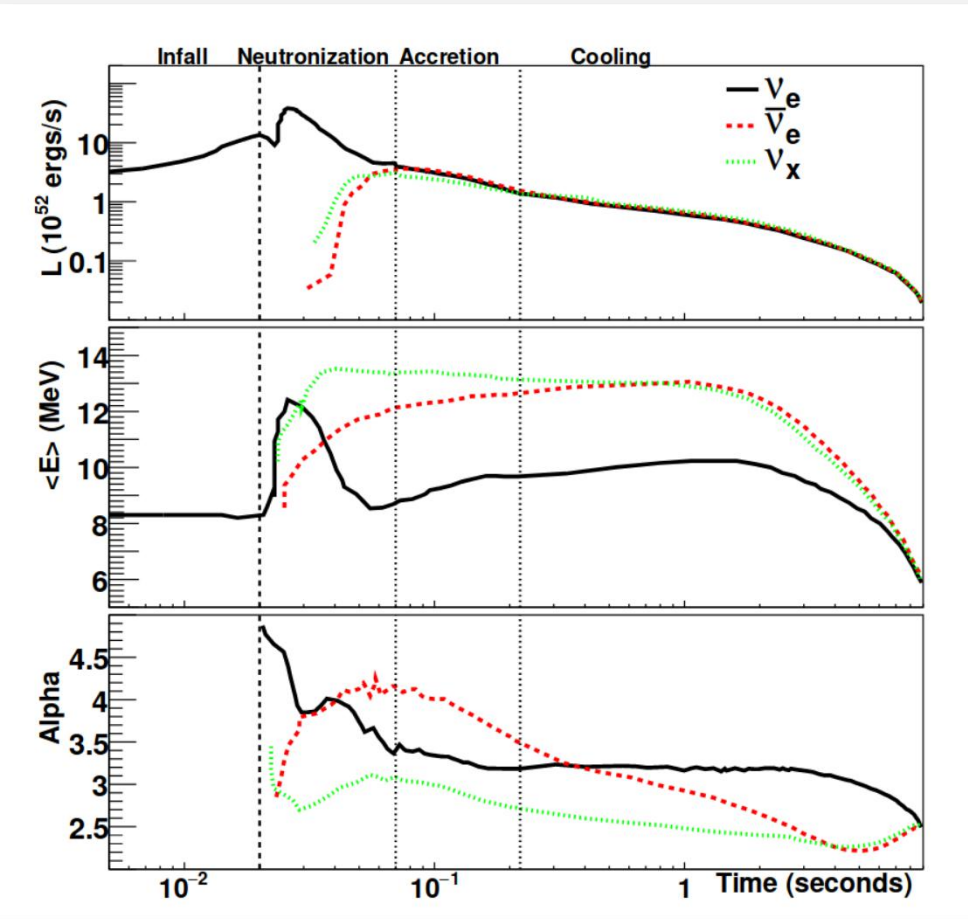
• Supernova Neutrino Production

❖ ν_e SN burst production (Garching model):

$$\Phi_{\nu\beta}^0(t_e, E_\nu) = \frac{L_{\nu\beta}(t_e)}{\langle E_{\nu\beta}(t_e) \rangle} \varphi_{\nu\beta}(t_e, E_\nu)$$

$$\varphi_{\nu\beta}(t_e, E_\nu) \equiv \xi_\beta(t_e) \left(\frac{E_\nu}{\langle E_{\nu\beta}(t_e) \rangle} \right)^{\alpha_\beta(t_e)} e^{-\frac{(\alpha_\beta(t_e)+1)E_\nu}{\langle E_{\nu\beta}(t_e) \rangle}}$$

Supernova Neutrino Production



DUNE Collaboration
arXiv: 2008.06647

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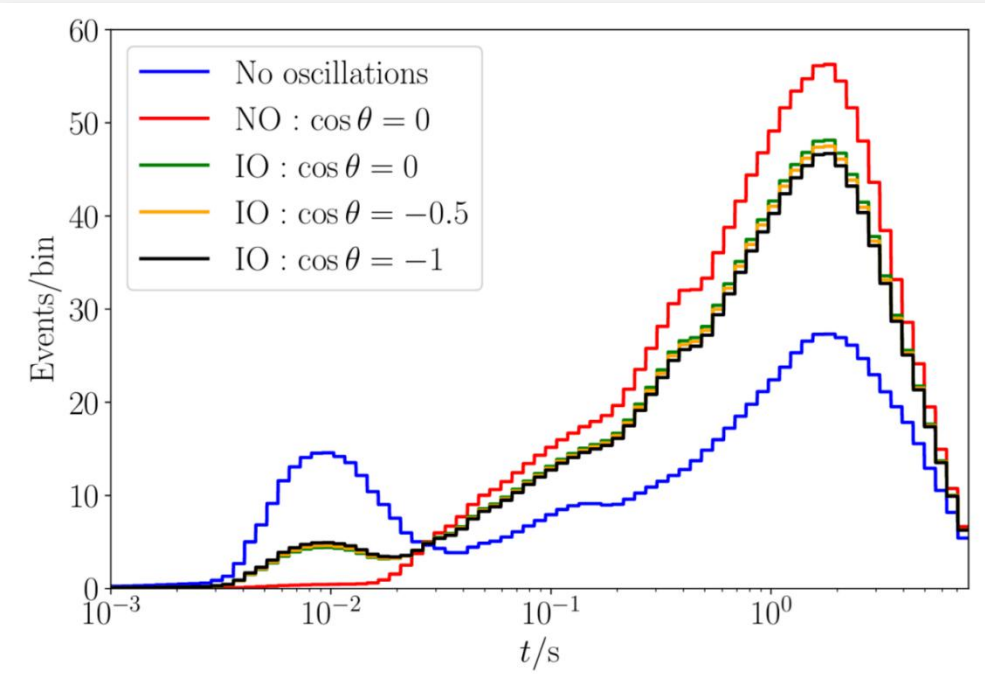
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Supernova Neutrino Production

NO: normal ordering

IO: inverted ordering



F. Pompa, F. Capozzi, O. Mena, & M. Sorel

arXiv:2203.00024

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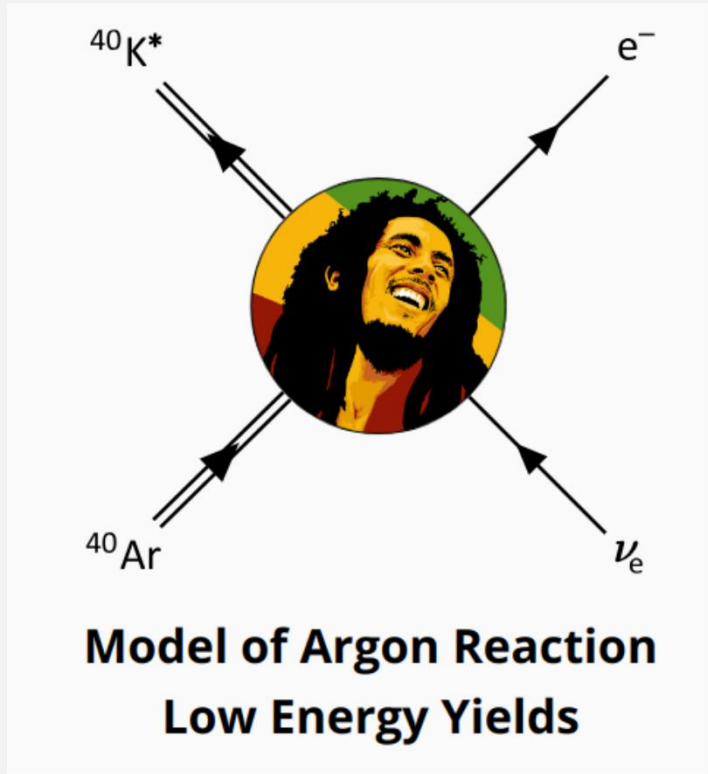
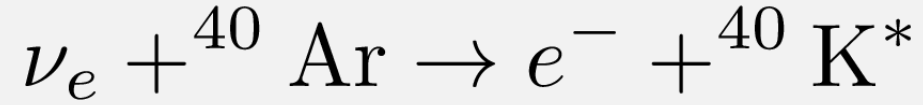
❖ MSW matter effect (from core to surface):

$$\Phi_{\nu_e} = p\Phi_{\nu_e}^0 + (1-p)\Phi_{\nu_x}^0$$

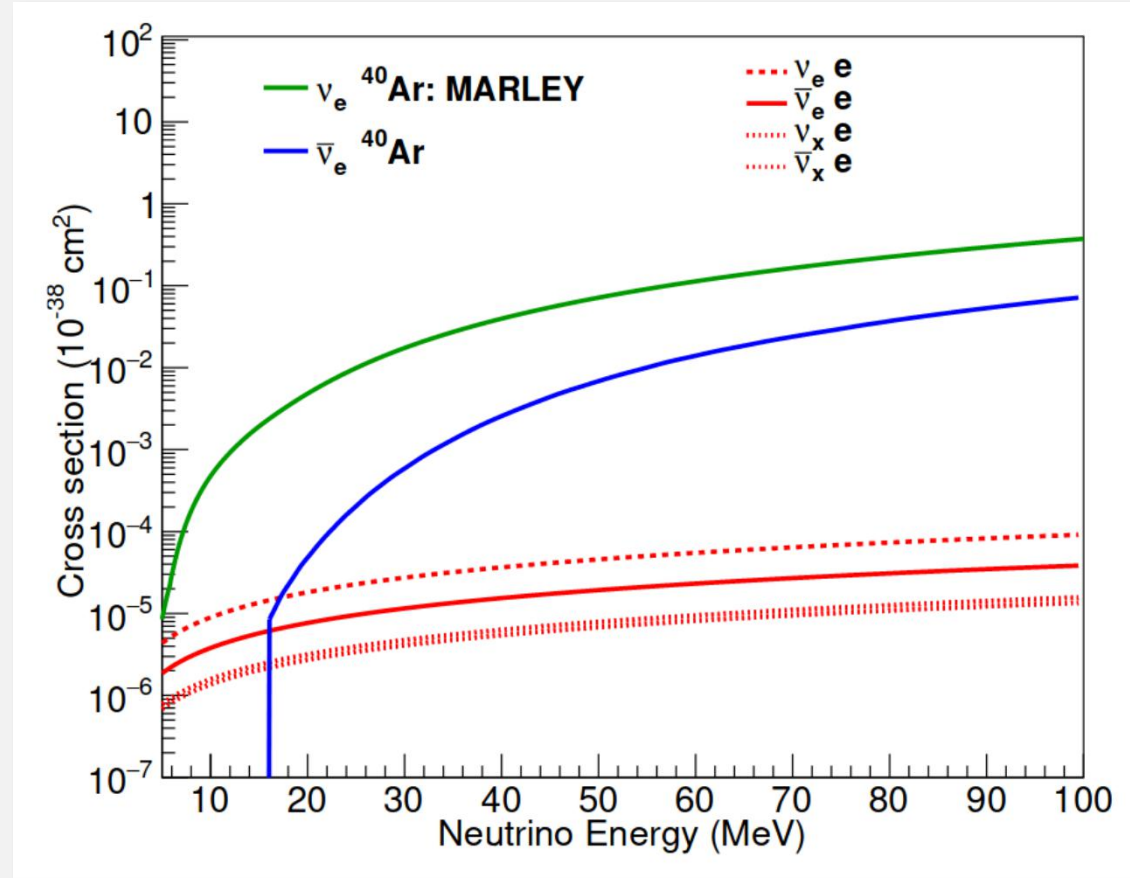
$$p = |U_{e3}|^2 \approx \sin^2 \theta_{13}, \text{ NO}$$

$$p \approx |U_{e2}|^2 \approx \sin^2 \theta_{12}, \text{ IO}$$

Supernova Neutrino Detection @ DUNE



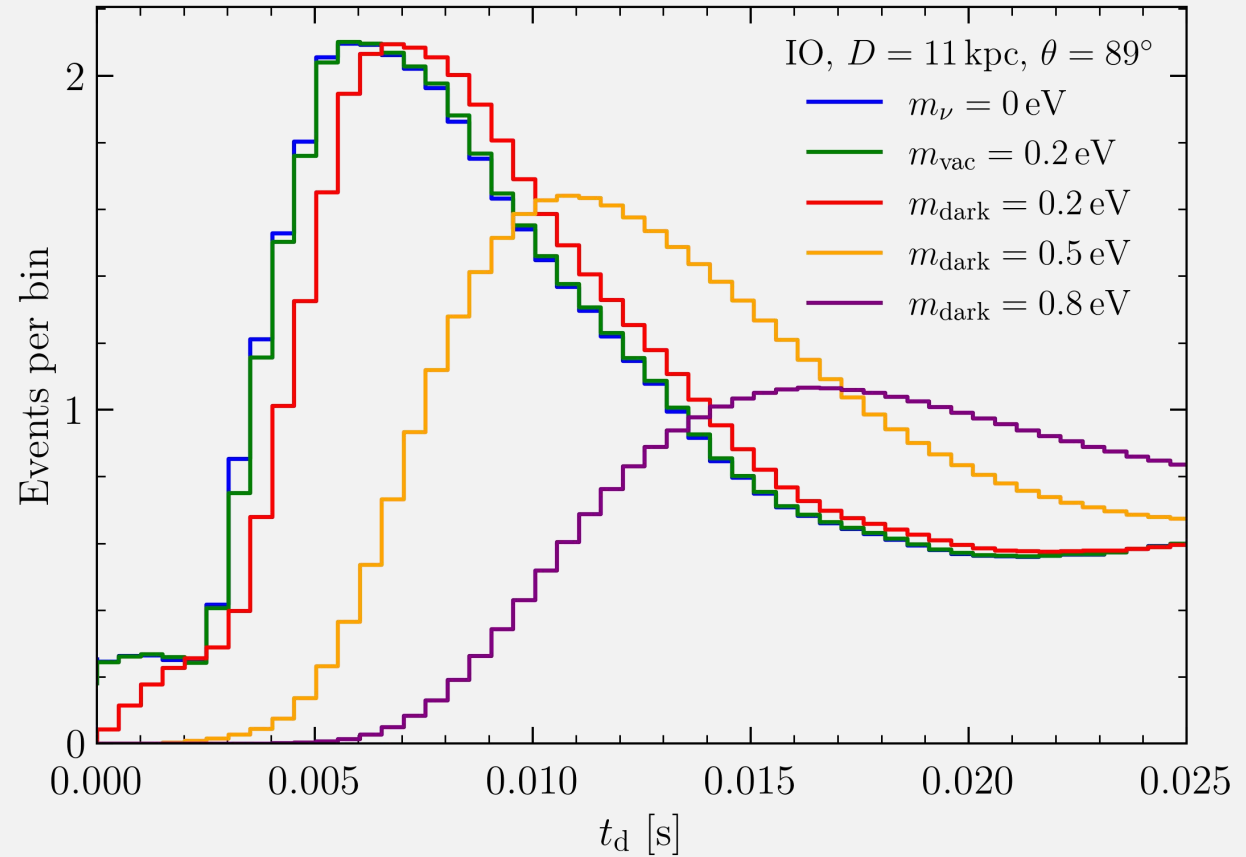
*S. Gardiner, 2010.02393
& 2101.11867*



*DUNE Collaboration
arXiv: 2008.06647*

• Time Distribution

The time distribution becomes wider as the neutrino mass increases

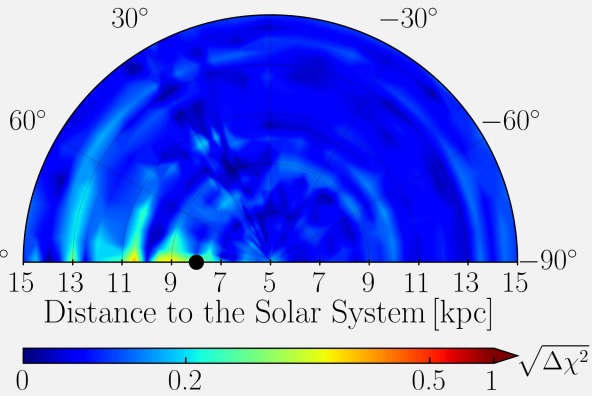


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Sensitivities

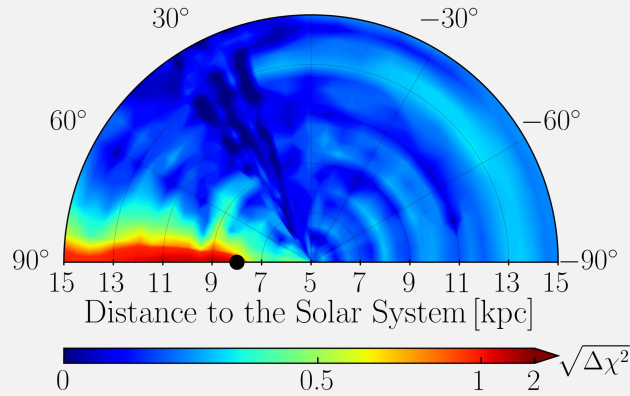
NO ($m_{\text{vac}}^{\text{fit}} = m_{\text{dark}}^{\text{fit}} = 0.2 \text{ eV}$)

0° ● Galactic Center



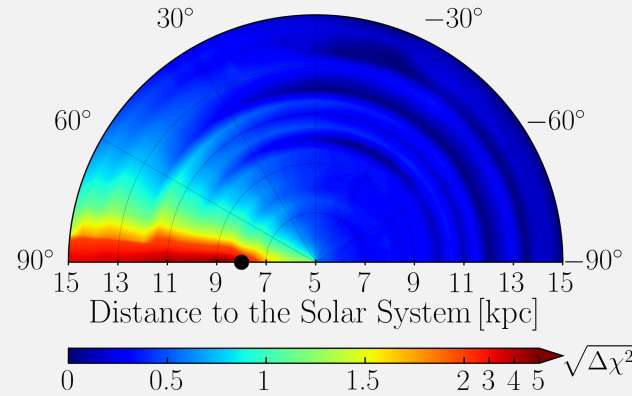
IO ($m_{\text{vac}}^{\text{fit}} = m_{\text{dark}}^{\text{fit}} = 0.2 \text{ eV}$)

0° ● Galactic Center



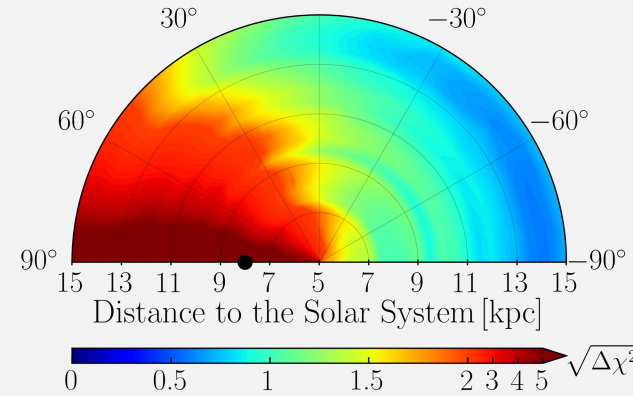
NO ($m_{\text{vac}}^{\text{fit}} = 0.2 \text{ eV}, m_{\text{dark}}^{\text{fit}} = 0.8 \text{ eV}$)

0° ● Galactic Center



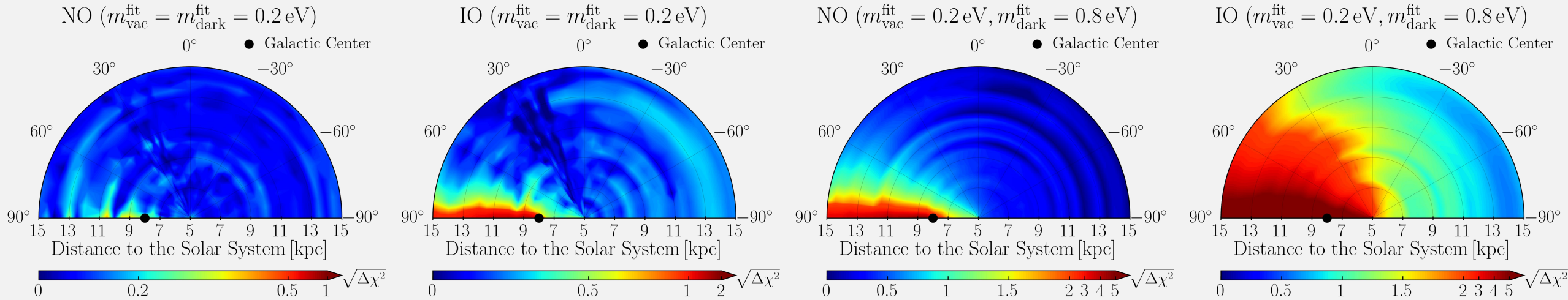
IO ($m_{\text{vac}}^{\text{fit}} = 0.2 \text{ eV}, m_{\text{dark}}^{\text{fit}} = 0.8 \text{ eV}$)

0° ● Galactic Center



Ge, CFK, Smirnov
arXiv: 2404.17352

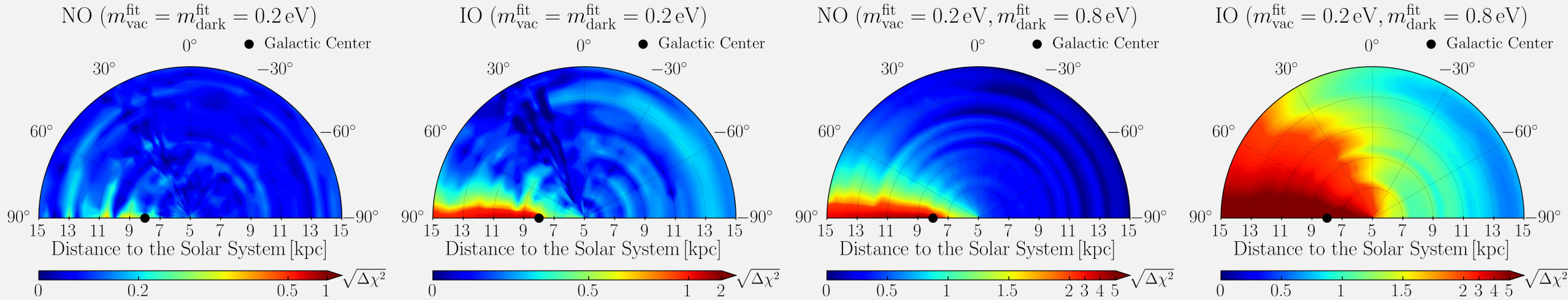
Sensitivities



❖ The sensitivity is enlarged by measuring supernova neutrinos around the galaxy center

*Ge, CFK, Smirnov
arXiv: 2404.17352*

Sensitivities



- ❖ The sensitivity is enlarged by measuring supernova neutrinos around the galaxy center
- ❖ Sensitivity for normal ordering (NO) is reduced by MSW matter effect

*Ge, CFK, Smirnov
arXiv: 2404.17352*

• Summary

- The dark neutrino mass is **space-time dependent** due to the DM distribution
- The supernova neutrino time delay can be **much enhanced** around galaxy center
- The neutrino mass origins (vacuum or dark mass) can be tested by measuring supernova neutrinos
- Better test can be done by measuring neutrinos from supernovae at different locations

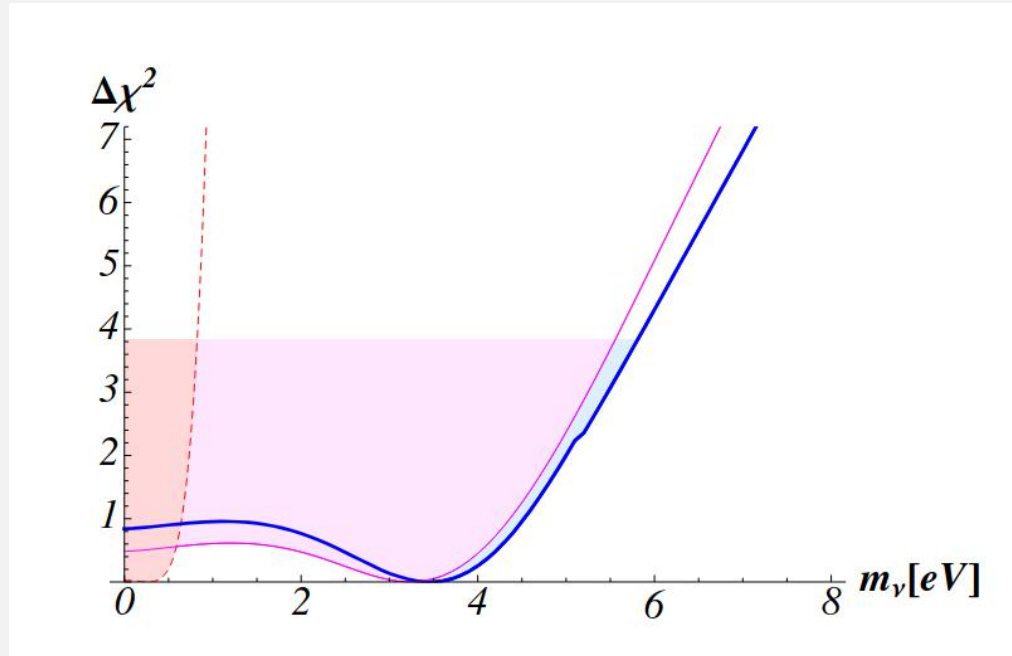
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Thank you for your attention!

• Backup

SN1987A



The minimum is located at ~ 3.5 eV, although not statistically significant

G. Pagliaroli, F. Rossi-Torres, & F. Vissani
arXiv:1002.3349

• Backup

parameter space

(i) $m_\phi \sim 10^{-10}$ eV, $g \sim 10^{-10}$, $m_\chi \sim 10^{-4}$ eV, and (ii)
 $m_\phi \sim 10^{-22}$ eV, $g \sim 10^{-21}$, $m_\chi \sim 10^{-10}$ eV.

M. Sen and A. Y. Smirnov, arXiv:2306.15718, 2407.02462

• Backup

matter potential

$$V_{\alpha\beta} = \sum_k g_{\alpha k} g_{\beta k}^* \left[\frac{\bar{n}_\phi (2Em_\phi - m_{\chi k}^2)}{(2Em_\phi - m_{\chi k}^2)^2 + (m_\chi \Gamma_{\chi k})^2} + \frac{n_\phi}{2Em_\phi + m_{\chi k}^2} \right],$$

M. Sen and A. Y. Smirnov, arXiv:2306.15718