

# Neutrino Oscillation Anomalies and their Relation to Sterile Neutrinos

6th KSETA Plenary Workshop 2019, Durbach

Alvaro Hernandez-Cabezudo

Theoretical Astroparticle Physics, IKP

February 27, 2019

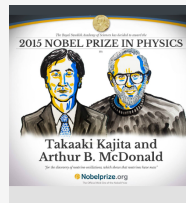


## Neutrino Oscillations

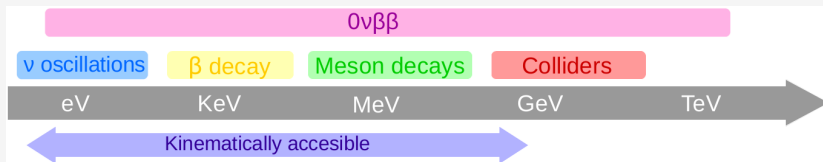
2015 Nobel Prize

Arthur B. McDonald, Takaaki Kajita

*For the discovery of neutrino oscillations, which shows that neutrinos have mass*



## New Physics and Sterile Neutrinos

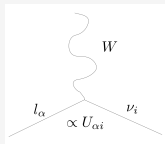


- $3\nu$  Oscillations and global analysis
- Short Baseline Anomalies and the status of their interpretation in terms of Sterile Neutrino Oscillations

## 3ν Standard Oscillations

After EWSB:  $\mathcal{L}_{CC} \propto U_{\alpha i} W_{\mu}^{-} \bar{\ell}_{\alpha} \gamma^{\mu} P_L \nu_i$

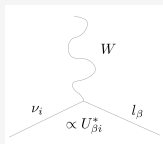
Lepton mixing matrix  $U$ , analogous to the CKM matrix.



$$|\nu_{\alpha}\rangle = U_{\alpha j} |\nu_j\rangle$$

Propagation

$$|\nu_{\alpha}(t)\rangle = U_{\alpha j} e^{-iE_j t} |\nu_j(t)\rangle = U_{\alpha j} e^{-iE_j t} U_{\gamma j}^* |\nu_{\gamma}\rangle$$

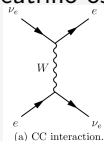


$$|\nu_j\rangle = U_{\beta j}^* |\nu_{\beta}\rangle$$

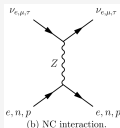
## Oscillation Probability (in Vacuum)

$$P_{\nu_{\alpha} \rightarrow \nu_{\beta}} = |\langle \nu_{\beta} | \nu_{\alpha}(t) \rangle|^2 = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re} (U_{\alpha j} U_{\beta j}^* U_{\alpha i}^* U_{\beta i}) \sin^2 \left( \frac{\Delta m_{ij}^2 L}{4E} \right) + 2 \sum_{i>j} \text{Im} (U_{\alpha j} U_{\beta j}^* U_{\alpha i}^* U_{\beta i}) \sin \left( \frac{\Delta m_{ij}^2 L}{2E} \right)$$

## Neutrino oscillations in matter



(a) CC interaction.



(b) NC interaction.

CC effective potential

- Oscillation probability enhancement, MSW effect.
- intrinsic CP violation.

NC effective potential do not have any effect

## PMNS Matrix Parametrization

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} ; \quad \Delta m_{\text{atm}}^2, \Delta m_{\text{sol}}^2 \quad \& \quad U_{\text{PMNS}} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix}$$

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{-i\alpha_1} & 0 \\ 0 & 0 & e^{-i\alpha_2} \end{pmatrix}$$

$$P_{\nu_\alpha \rightarrow \nu_\beta}^{(-)}(E, L, \theta) \quad \mathbf{6 \text{ Parameters: } } \theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP}, \Delta m_{\text{sol}}^2 \ll \Delta m_{\text{atm}}^2.$$

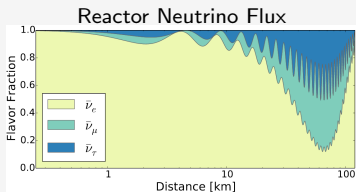
## Oscillation Regimes

$$\frac{\Delta m^2 E}{4L} \simeq 1.27 \Delta m_{ij}^2 (\text{eV}^2) \frac{L(\text{Km})}{E(\text{GeV})}$$

$$\Delta m_{\text{sol}}^2 \sim 10^{-4} \text{eV}^2 \Rightarrow L/E \sim 10^4 \text{Km/GeV}$$

Reactors:  $E \sim \text{MeV}$ ,  $L \sim 1\text{Km}$  Daya Bay

$L \sim 100\text{Km}$  KamLAND



P.Vogel et.al. [arXiv:1503.01059]

# Neutrino Oscillations, $3\nu$ NuFit combined analysis

NuFIT 4.0 (2018), [www.nu-fit.org](http://www.nu-fit.org) I. Esteban, C. Gonzalez-Garcia, A. Hernandez-Cabezudo, M. Maltoni, T. Schwetz

$$\chi^2(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP}, \Delta m_{\text{sol}}^2, \Delta m_{\text{atm}}^2) =$$

# Neutrino Oscillations, $3\nu$ NuFit combined analysis

NuFIT 4.0 (2018), [www.nu-fit.org](http://www.nu-fit.org) I. Esteban, C. Gonzalez-Garcia, A. Hernandez-Cabezudo, M. Maltoni, T. Schwetz

$$P_{\text{KLAND}} = \sin^4 \theta_{13} + \cos^4 \theta_{13} \left( 1 - \frac{1}{2} \sin^2(2\theta_{12}) \sin^2 \frac{\Delta_{\text{sol}} L}{4E} \right)$$

$$\chi^2(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP}, \Delta m_{\text{sol}}^2, \Delta m_{\text{atm}}^2) = \chi_{\text{sol+KLAND}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13})$$

# Neutrino Oscillations, $3\nu$ NuFit combined analysis

NuFIT 4.0 (2018), [www.nu-fit.org](http://www.nu-fit.org) I. Esteban, C. Gonzalez-Garcia, A. Hernandez-Cabezudo, M. Maltoni, T. Schwetz

$$P_{\text{KLAND}} = \sin^4 \theta_{13} + \cos^4 \theta_{13} \left( 1 - \frac{1}{2} \sin^2(2\theta_{12}) \sin^2 \frac{\Delta_{\text{sol}} L}{4E} \right)$$
$$P_{\text{reactor}} = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \frac{\Delta_{\text{sol}} L}{4E} - \sin^2 2\theta_{13} \left( \cos^2 \theta_{12} \sin^2 \frac{\Delta_{31} L}{4E} + \sin^2 \theta_{12} \sin^2 \frac{\Delta_{32} L}{4E} \right)$$

$$\chi^2(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP}, \Delta m_{\text{sol}}^2, \Delta m_{\text{atm}}^2) = \chi_{\text{sol+KLAND}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}) + \chi_{\text{reactor}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}, \Delta m_{\text{atm}}^2)$$

# Neutrino Oscillations, $3\nu$ NuFit combined analysis

NuFIT 4.0 (2018), [www.nu-fit.org](http://www.nu-fit.org) I. Esteban, C. Gonzalez-Garcia, A. Hernandez-Cabezudo, M. Maltoni, T. Schwetz

$$P_{\text{KLAND}} = \sin^4 \theta_{13} + \cos^4 \theta_{13} \left( 1 - \frac{1}{2} \sin^2(2\theta_{12}) \sin^2 \frac{\Delta_{\text{sol}} L}{4E} \right)$$
$$P_{\text{reactor}} = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \frac{\Delta_{\text{sol}} L}{4E} - \sin^2 2\theta_{13} \left( \cos^2 \theta_{12} \sin^2 \frac{\Delta_{31} L}{4E} + \sin^2 \theta_{12} \sin^2 \frac{\Delta_{32} L}{4E} \right)$$

$$\chi^2(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP}, \Delta m_{\text{sol}}^2, \Delta m_{\text{atm}}^2) =$$
$$\chi_{\text{sol+KLAND}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13})$$
$$+ \chi_{\text{reactor}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}, \Delta m_{\text{atm}}^2)$$
$$+ \chi_{\text{LBL}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}, \Delta m_{\text{atm}}^2, \theta_{23}, \delta_{CP})$$



# Neutrino Oscillations, $3\nu$ NuFit combined analysis

NuFIT 4.0 (2018), [www.nu-fit.org](http://www.nu-fit.org) I. Esteban, C. Gonzalez-Garcia, A. Hernandez-Cabezudo, M. Maltoni, T. Schwetz

$$P_{\text{KLAND}} = \sin^4 \theta_{13} + \cos^4 \theta_{13} \left( 1 - \frac{1}{2} \sin^2(2\theta_{12}) \sin^2 \frac{\Delta_{\text{sol}} L}{4E} \right)$$
$$P_{\text{reactor}} = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \frac{\Delta_{\text{sol}} L}{4E} - \sin^2 2\theta_{13} \left( \cos^2 \theta_{12} \sin^2 \frac{\Delta_{31} L}{4E} + \sin^2 \theta_{12} \sin^2 \frac{\Delta_{32} L}{4E} \right)$$

$$\chi^2(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP}, \Delta m_{\text{sol}}^2, \Delta m_{\text{atm}}^2) =$$
$$\chi_{\text{sol+KLAND}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13})$$
$$+ \chi_{\text{reactor}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}, \Delta m_{\text{atm}}^2)$$
$$+ \chi_{\text{LBL}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}, \Delta m_{\text{atm}}^2, \theta_{23}, \delta_{CP})$$
$$+ \chi_{\text{atm}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}, \Delta m_{\text{atm}}^2, \theta_{23}, \delta_{CP})$$

# Neutrino Oscillations, $3\nu$ NuFit combined analysis

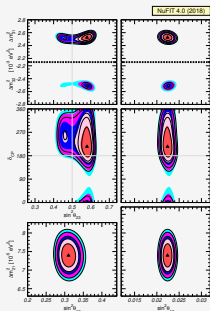
NuFIT 4.0 (2018), [www.nu-fit.org](http://www.nu-fit.org) I. Esteban, C. Gonzalez-Garcia, A. Hernandez-Cabezudo, M. Maltoni, T. Schwetz

$$P_{\text{KLAND}} = \sin^4 \theta_{13} + \cos^4 \theta_{13} \left( 1 - \frac{1}{2} \sin^2(2\theta_{12}) \sin^2 \frac{\Delta_{\text{sol}} L}{4E} \right)$$

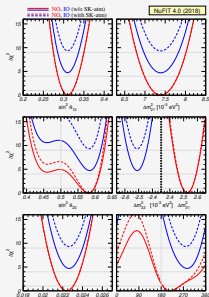
$$P_{\text{reactor}} = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \frac{\Delta_{\text{sol}} L}{4E} - \sin^2 2\theta_{13} \left( \cos^2 \theta_{12} \sin^2 \frac{\Delta_{31} L}{4E} + \sin^2 \theta_{12} \sin^2 \frac{\Delta_{32} L}{4E} \right)$$

## Combined analysis:

$$\begin{aligned} \chi^2(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP}, \Delta m_{\text{sol}}^2, \Delta m_{\text{atm}}^2) = & \\ \chi_{\text{sol+KLAND}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}) & \\ + \chi_{\text{reactor}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}, \Delta m_{\text{atm}}^2) & \\ + \chi_{\text{LBL}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}, \Delta m_{\text{atm}}^2, \theta_{23}, \delta_{CP}) & \\ + \chi_{\text{atm}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}, \Delta m_{\text{atm}}^2, \theta_{23}, \delta_{CP}) & \end{aligned}$$



I. Esteban et al. [arXiv:1811.05487]



I. Esteban et al. [arXiv:1811.05487]

# Neutrino Oscillations, $3\nu$ NuFit combined analysis

NuFIT 4.0 (2018), [www.nu-fit.org](http://www.nu-fit.org) I. Esteban, C. Gonzalez-Garcia, A. Hernandez-Cabezudo, M. Maltoni, T. Schwetz

$$P_{\text{KLAND}} = \sin^4 \theta_{13} + \cos^4 \theta_{13} \left( 1 - \frac{1}{2} \sin^2(2\theta_{12}) \sin^2 \frac{\Delta_{\text{sol}} L}{4E} \right)$$

$$P_{\text{reactor}} = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \frac{\Delta_{\text{sol}} L}{4E} - \sin^2 2\theta_{13} \left( \cos^2 \theta_{12} \sin^2 \frac{\Delta_{31} L}{4E} + \sin^2 \theta_{12} \sin^2 \frac{\Delta_{32} L}{4E} \right)$$

6 Parameters:  $\theta_{12}$ ,  $\theta_{23}$ ,  $\theta_{13}$  &  $\delta_{CP}$

$\Delta m_{\text{sol}}^2 \ll \Delta m_{\text{atm}}^2$  (Mass ordering)  
 $m1 < m2 < m3$   
 $m3 < m1 < m2$

[www.nu-fit.org](http://www.nu-fit.org)

Combined analysis:

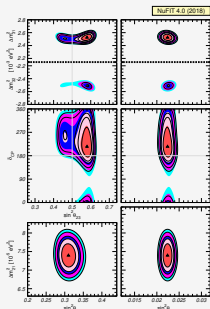
$$\chi^2(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP}, \Delta m_{\text{sol}}^2, \Delta m_{\text{atm}}^2) =$$

$$\chi_{\text{sol+KLAND}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13})$$

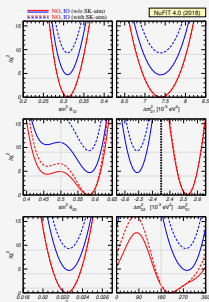
$$+ \chi_{\text{reactor}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}, \Delta m_{\text{atm}}^2)$$

$$+ \chi_{\text{LBL}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}, \Delta m_{\text{atm}}^2, \theta_{23}, \delta_{CP})$$

$$+ \chi_{\text{atm}}^2(\theta_{12}, \Delta m_{\text{sol}}^2, \theta_{13}, \Delta m_{\text{atm}}^2, \theta_{23}, \delta_{CP})$$



I. Esteban et al. [arXiv:1811.05487]



I. Esteban et al. [arXiv:1811.05487]

# Neutrino Oscillations, Reactor Neutrinos

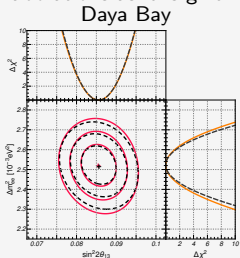
## Predictions

$$N_i^d = \mathcal{N} \sum_r \sum_{\text{iso}} \frac{\epsilon^d}{L_{rd}^2} \int_{E_i^{\text{rec}}}^{E_{i+1}^{\text{rec}}} dE^{\text{rec}} \int_0^\infty dE_\nu \sigma(E_\nu) f^{\text{iso}} \phi^{\text{iso}}(E_\nu) P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}^{rd}(E_\nu) R(E^{\text{rec}}, E_\nu)$$

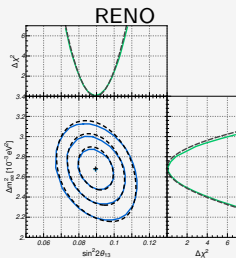
## Analysis, Pull approach

$$\chi^2(\theta, \eta) = \sum_{i,j} \frac{(\text{Obs}_i - \text{Pred}_i(\theta, \eta))^2}{(\sigma_i^{\text{stat}})^2} + \eta_k V_{kl}^{-1} \eta_l$$

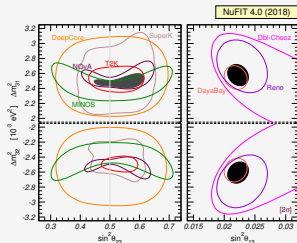
$\eta$ : pull parameters accounting for the **systematics**. We include as much information from the collaborations as it is given.



I.Esteban et al. [arXiv:1811.05487]



I.Esteban et al. [arXiv:1811.05487]



I.Esteban et al. [arXiv:1811.05487]

6 Parameters:  $\theta_{12}$ ,  $\theta_{23}$ ,  $\theta_{13}$  &  $\delta_{CP}$

$\Delta m_{sol}^2 \ll \Delta m_{atm}^2$  (Mass ordering)

$$m1 < m2 < m3$$

$$m3 < m1 < m2$$

**$3\nu$  Oscillation Framework** is very well tested

However there are experimental data that can not be accommodated in this framework

⇒ **Short Baseline Anomalies**

- Sterile Neutrino Oscillations
- Reactor Anti-neutrino Anomaly
- LSND and MiniBooNE Anomaly
- Appearance vs Disappearance Tension

**3 + 1  $\nu$  framework**

$$P_{\bar{\nu}_e \rightarrow \bar{\nu}_e} = 1 - 4 \sum_{i=1}^3 \sum_{j>i}^4 |U_{ei}|^2 |U_{ej}|^2 \sin^2 \left( \Delta m_{ij}^2 \frac{L}{4E} \right)$$

$$P_{\bar{\nu}_e \rightarrow \bar{\nu}_e} \underset{\text{SBL}}{\simeq} 1 - \sin^2 2\theta_{14} \sin^2 \left( \Delta m_{41}^2 \frac{L}{4E} \right)$$

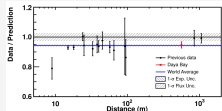
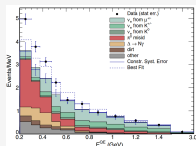
M.Dentler et.al. [arXiv:1803.10661]

M.Dentler, A.Hernandez-Cabezudo, J.Kopp, P.A.N.Machado, M.Maltoni, I.Martinez-Soler, T.Schwetz

# SBL Anomalies and Sterile Neutrino Oscillations

**Short Baseline (SBL) Experiments** measure in the  $L/E \sim 1\text{m}/\text{MeV}$  regime.  
They are not sensitive to the  $3\nu$  standard oscillations ( $\Delta m_{\text{atm}}^2$  and  $\Delta m_{\text{sol}}^2$ ).

- 1 LNSD & MiniBooNE  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$
- 2 Gallium  $\nu_e \rightarrow \nu_e$
- 3 Reactor  $\bar{\nu}_e \rightarrow \bar{\nu}_e$



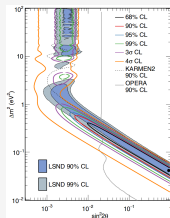
A.A. Aguilar-Arevalo et al. [arXiv:1805.12028]

F.P. An et al. [arXiv:1607.05378]

## eV Sterile Neutrino

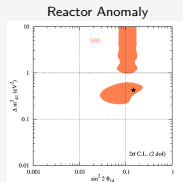
$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}; \quad \Delta m_{\text{new}}^2 \simeq 1\text{eV}^2$$

$$P_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta}^{\text{SBL}} = \left| \delta_{\alpha\beta} - \sin^2 2\theta_{\alpha\beta} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right) \right|$$



A.A. Aguilar-Arevalo et al.

[arXiv:1805.12028]



Total measured events vs predicted events

# Reactor Anti-neutrino Anomaly

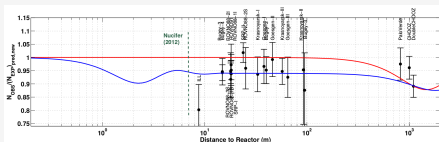
$$^{235}\text{U}, ^{239}\text{Pu}, ^{238}\text{U} \ \& \ ^{241}\text{Pu} \rightarrow \bar{\nu}_e \ (\sim \text{MeV}) \text{Flux.}$$

Reactor experiments measured a deficit  $\bar{\nu}_e$  events with respect to the theoretical predictions (Huber-Muller)

## Sterile Neutrino Oscillations

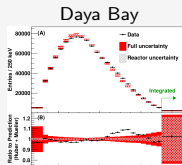
$$P_{\bar{\nu}_e \rightarrow \bar{\nu}_e} = 1 - \sin^2 2\theta_{14} \sin^2 \left( \frac{\Delta m_{\text{new}}^2 L}{4E} \right)$$

$$\text{averaged out : } P_{\bar{\nu}_e \rightarrow \bar{\nu}_e} = 1 - \frac{1}{2} \sin^2 2\theta_{14}$$

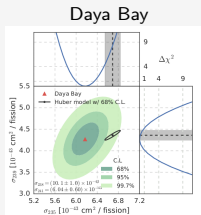


K. N. Abazajian et al. [arXiv:1204.5379]

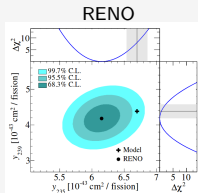
## Flux Mismodelling



F. P. An et al. [arXiv: 1607.05378]



F. P. An et al. [arXiv: 1704.01082]

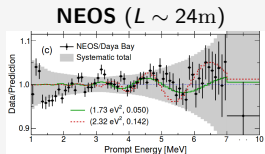


RENO cn. [arXiv: 1806.00574]

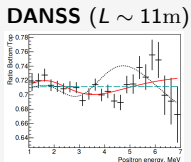
**Global fit** C.Giunti et al. [arXiv: 1901.01807] of the flux evolution and all-time integrated  $\bar{\nu}_e$  flux measurement do not favour the flux mismodelling hypothesis over the hybrid models.

# Reactor Anti-neutrino Anomaly

## Recent New Data Analysis independent of flux predictions



Y.J. Ko et al. [arXiv: 1610.05134]

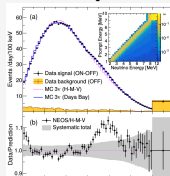


I Alekseev et al. [arXiv: 1804.04046]

**PROSPECT ( $L \sim 7 - 13\text{m}$ )**  
**STEREO ( $L \sim 10\text{m}$ )**  
**NEUTRINO 4\* ( $L \sim 6 - 12\text{m}$ )**

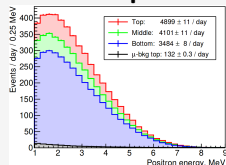
Based on ratios of measured spectra

### NEOS spectrum



Y.J. Ko et al. [arXiv: 1610.05134]

### DANSS spectrum



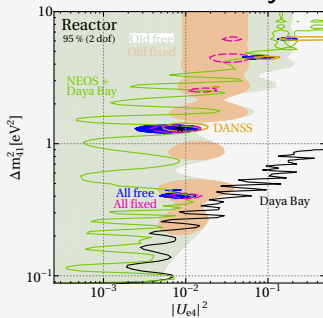
I.Alekseev et al. [arXiv: 1804.04046]

In our global analysis we perform a **Flux Free Analysis**, fitting the oscillation parameters as well as the normalizations of the flux predictions to the data.

M.Dentler et al. [arXiv:1803.10661]



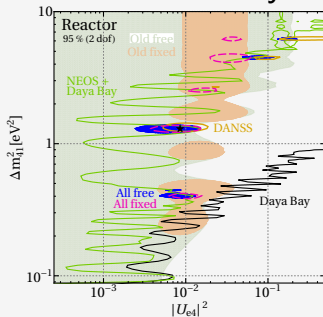
## Reactor Global Analysis



M.Dentler et.al. [arXiv:1803.10661]

# Reactor Anti-neutrino Anomaly

## Reactor Global Analysis

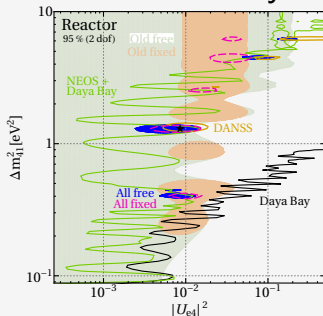


M.Dentler et.al. [arXiv:1803.10661]

Analysis	$\Delta m_{41}^2$ [eV <sup>2</sup> ]	$ U_{e4}^2 $	$\chi_{\min}^2/\text{dof}$	$\Delta\chi^2(\text{no-osc})$	significance
DANSS+NEOS	1.3	0.00964	74.4/(84 - 2)	13.6	3.3 $\sigma$
all reactor (flux-free)	1.3	0.00887	185.8/(233 - 5)	11.5	2.9 $\sigma$
all reactor (flux-fixed)	1.3	0.00964	196.0/(233 - 3)	15.5	3.5 $\sigma$

# Reactor Anti-neutrino Anomaly

## Reactor Global Analysis

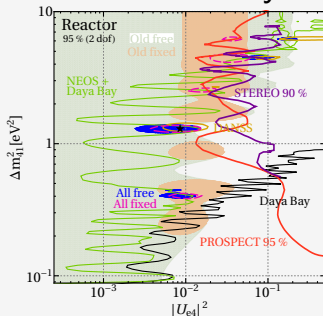


M.Dentler et.al. [arXiv:1803.10661]

Analysis	$\Delta m_{41}^2$ [eV <sup>2</sup> ]	$ U_{e4} ^2$	$\chi^2_{\min}/\text{dof}$	$\Delta\chi^2(\text{no-osc})$	significance
DANSS+NEOS	1.3	0.00964	74.4/(84 - 2)	13.6	3.3 $\sigma$
all reactor (flux-free)	1.3	0.00887	185.8/(233 - 5)	11.5	2.9 $\sigma$
all reactor (flux-fixed)	1.3	0.00964	196.0/(233 - 3)	15.5	3.5 $\sigma$

Reactor anomaly confirmed by ratios of measured spectra  
**independently** of flux predictions

## Reactor Global Analysis

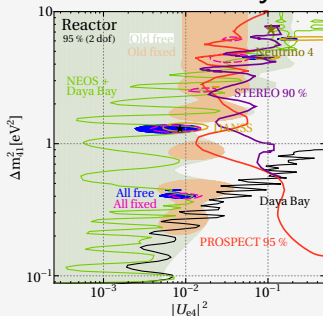


M.Dentler et.al. [arXiv:1803.10661]

Analysis	$\Delta m_{41}^2$ [eV <sup>2</sup> ]	$ U_{e4}^2 $	$\chi_{\min}^2/\text{dof}$	$\Delta\chi^2(\text{no-osc})$	significance
DANSS+NEOS	1.3	0.00964	74.4/(84 - 2)	13.6	3.3 $\sigma$
all reactor (flux-free)	1.3	0.00887	185.8/(233 - 5)	11.5	2.9 $\sigma$
all reactor (flux-fixed)	1.3	0.00964	196.0/(233 - 3)	15.5	3.5 $\sigma$

Reactor anomaly confirmed by ratios of measured spectra  
**independently** of flux predictions

## Reactor Global Analysis



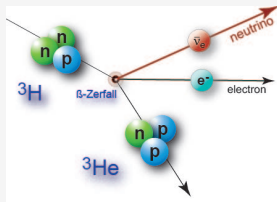
M.Dentler et.al. [arXiv:1803.10661]

Analysis	$\Delta m_{41}^2$ [eV <sup>2</sup> ]	$ U_{e4}^2 $	$\chi^2_{\min}/\text{dof}$	$\Delta\chi^2(\text{no-osc})$	significance
DANSS+NEOS	1.3	0.00964	74.4/(84 - 2)	13.6	3.3 $\sigma$
all reactor (flux-free)	1.3	0.00887	185.8/(233 - 5)	11.5	2.9 $\sigma$
all reactor (flux-fixed)	1.3	0.00964	196.0/(233 - 3)	15.5	3.5 $\sigma$

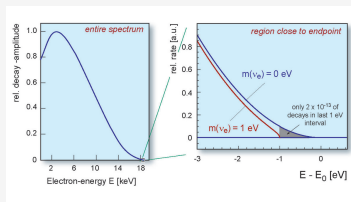
Reactor anomaly confirmed by ratios of measured spectra  
**independently** of flux predictions

# Ractor Anti-neutrino Anomaly and KATRIN

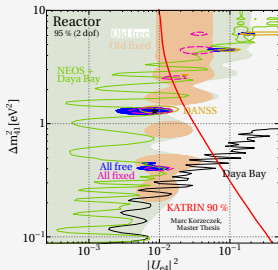
$$\frac{d\Gamma}{dE} = \Theta(E_0 - E - m_\beta) (1 - |U_{e4}|^2) \frac{d\Gamma}{dE}(m_\beta) + \Theta(E_0 - E - m_4) |U_{e4}|^2 \frac{d\Gamma}{dE}(m_4)$$



[www.katrin.kit.edu](http://www.katrin.kit.edu)

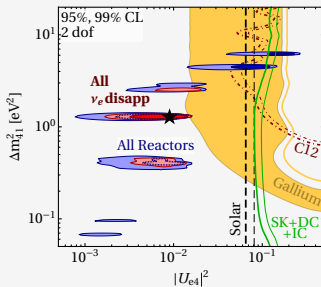


[www.katrin.kit.edu](http://www.katrin.kit.edu)



Marx Kroczek, Master Thesis: *eV- & KeV-sterile neutrino studies with KATRIN*

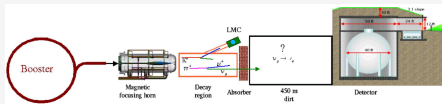
## Global $\bar{\nu}_e$ Disappearance Analysis



M.Dentler et.al. [arXiv:1803.10661]

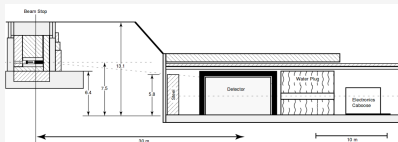
Analysis	$\Delta m_{41}^2$ [eV <sup>2</sup> ]	$ U_{e4} ^2$	$\chi_{\min}^2/\text{dof}$	$\Delta\chi^2(\text{no-osc})$	significance
$\bar{\nu}_e$ disap. (flux free)	1.3	0.00901	542.9/(594 - 8)	13.4	3.2 $\sigma$

# LSND and MiniBooNE Anomalies, $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$



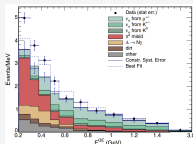
K. N. Abazajian et al. [arXiv:1204.5379]

Oscillation regime  $L/E \sim 0.15 - 2.3$  m/MeV



C. Athanassopoulos et al. [arXiv:nucl-es/9605002]

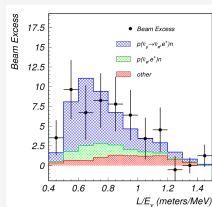
Oscillation regime  $L/E \sim 0.5 - 1.5$  m/MeV



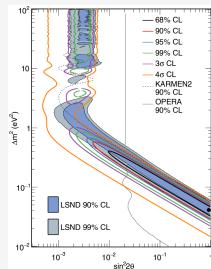
[arXiv:1805.12028]

A.A. Aguilar-Arevalo et al.

[arXiv:1805.12028]



[arXiv:1204.5379]

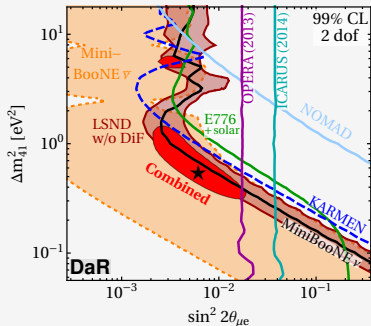




## LSND & MiniBooNE Anomalies

### Global $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ Analysis

(Updated data till Spring 2018)



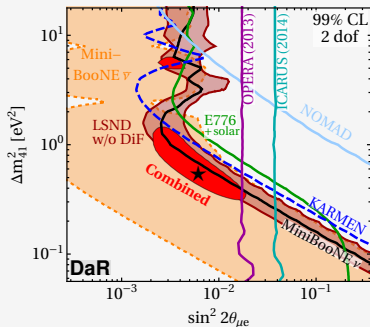
M.Dentler et.al. [arXiv:1803.10661]

$$\sin^2 2\theta_{\mu e} \propto |U_{\mu 4}|^2 |U_{e 4}|^2$$

## LSND & MiniBooNE Anomalies

### Global $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ Analysis

(Updated data till Spring 2018)



M. Dentler et al. [arXiv:1803.10661]

$$P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}^{(-)} = 1 - 4|U_{e4}|^2(1 - |U_{e4}|)^2 \sin^2 \left( \frac{\Delta m_{41}^2 E}{4L} \right)$$

$$P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu}^{(-)} = 1 - 4|U_{\mu 4}|^2(1 - |U_{\mu 4}|)^2 \sin^2 \left( \frac{\Delta m_{41}^2 E}{4L} \right)$$

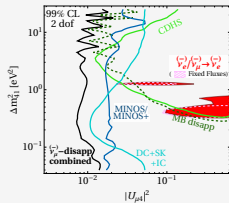
$$P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_e}^{(-)} = 4|U_{e4}|^2|U_{\mu 4}|^2 \sin^2 \left( \frac{\Delta m_{41}^2 E}{4L} \right)$$

$$\sin^2 2\theta_{e\mu} \simeq \frac{1}{4} \sin^2 2\theta_{ee} \sin^2 2\theta_{\mu\mu}$$

$$\sin^2 2\theta_{\mu e} \propto |U_{\mu 4}|^2 |U_{e4}|^2$$

# $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ Appearance vs $\bar{\nu}_\mu/\bar{\nu}_e$ Disappearance Tension

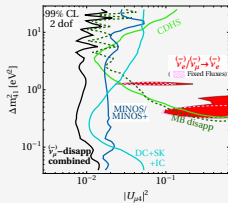
Global  $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$  Analysis  $\Rightarrow$



M.Dentler et.al. [arXiv:1803.10661]

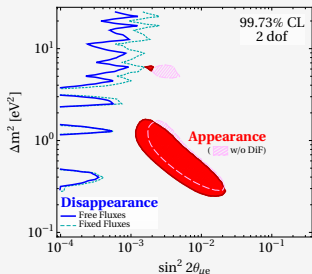
# $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ Appearance vs $\bar{\nu}_\mu/\bar{\nu}_e$ Disappearance Tension

Global  $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$  Analysis  $\Rightarrow$



M.Dentler et al. [arXiv:1803.10661]

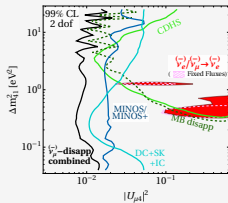
$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  vs  $\bar{\nu}_\mu/\bar{\nu}_e$  Tension



M.Dentler et al. [arXiv:1803.10661]

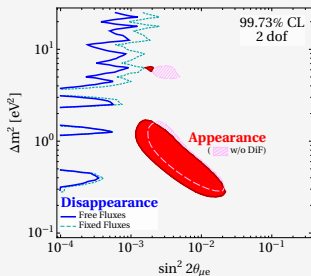
# $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ Appearance vs $\bar{\nu}_\mu/\bar{\nu}_e$ Disappearance Tension

Global  $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$  Analysis  $\Rightarrow$



M.Dentler et al. [arXiv:1803.10661]

$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  vs  $\bar{\nu}_\mu/\bar{\nu}_e$  Tension



M.Dentler et al. [arXiv:1803.10661]

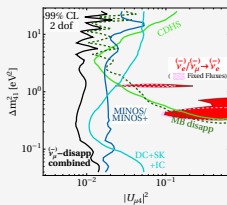
Parameter Goodness of Fit Test

Analysis	$\Delta\chi^2_{\text{app-disapp}}$	p-value	significance
Global	29.6	$3.7 \times 10^{-7}$	$5.1\sigma$
w/o Reactors	20.3	$3.9 \times 10^{-5}$	$4.1\sigma$

The tension is independent of the Reactor Anomaly

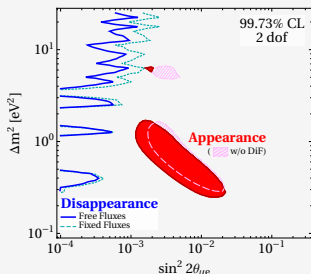
# $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ Appearance vs $\bar{\nu}_\mu/\bar{\nu}_e$ Disappearance Tension

Global  $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$  Analysis  $\Rightarrow$



M.Dentler et al. [arXiv:1803.10661]

$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  vs  $\bar{\nu}_\mu/\bar{\nu}_e$  Tension



M.Dentler et al. [arXiv:1803.10661]

Analysis	$\chi^2_{PG}/\text{dof}$	PG
Global	29.6/2	$3.71 \times 10^{-7}$
<b>Removing anomalous data sets</b>		
w/o LSND	12.9/2	$1.6 \times 10^{-3}$
w/o MiniBooNE	24.4/2	$5.2 \times 10^{-6}$
w/o reactors	20.3/2	$3.8 \times 10^{-5}$
w/o gallium	33.9/2	$4.4 \times 10^{-8}$
<b>Removing constraints</b>		
w/o IceCube	29.4/2	$4.2 \times 10^{-7}$
w/o MINOS(+)	24.5/2	$4.7 \times 10^{-6}$
w/o MB disapp	28.7/2	$6.0 \times 10^{-7}$
w/o CDHS	28.2/2	$7.5 \times 10^{-7}$

The tension is independent of any particular experiment

- $3\nu$  Oscillations unknown parameters:  $\delta_{CP}$ , mass ordering,  $\theta_{23}$  octant.
- $3\nu$  Oscillations are a very well tested framework. However there are some anomalies.
- Reactor Anti-neutrino anomaly is compatible with new data, independent of flux predictions, at the level of  $\sim 3\sigma$ :  $|U_{e4}|^2 \sim 0.01$  and  $\Delta m_{\text{new}}^2 \sim 1.3\text{eV}^2$ .
- $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  Appearance data (MiniBooNE and LSND) is in strong tension with the Disappearance data ( $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$  bounds), independently of the reactor data.
- MiniBooNE and LSND data should not be explained in terms of sterile neutrino oscillations.