

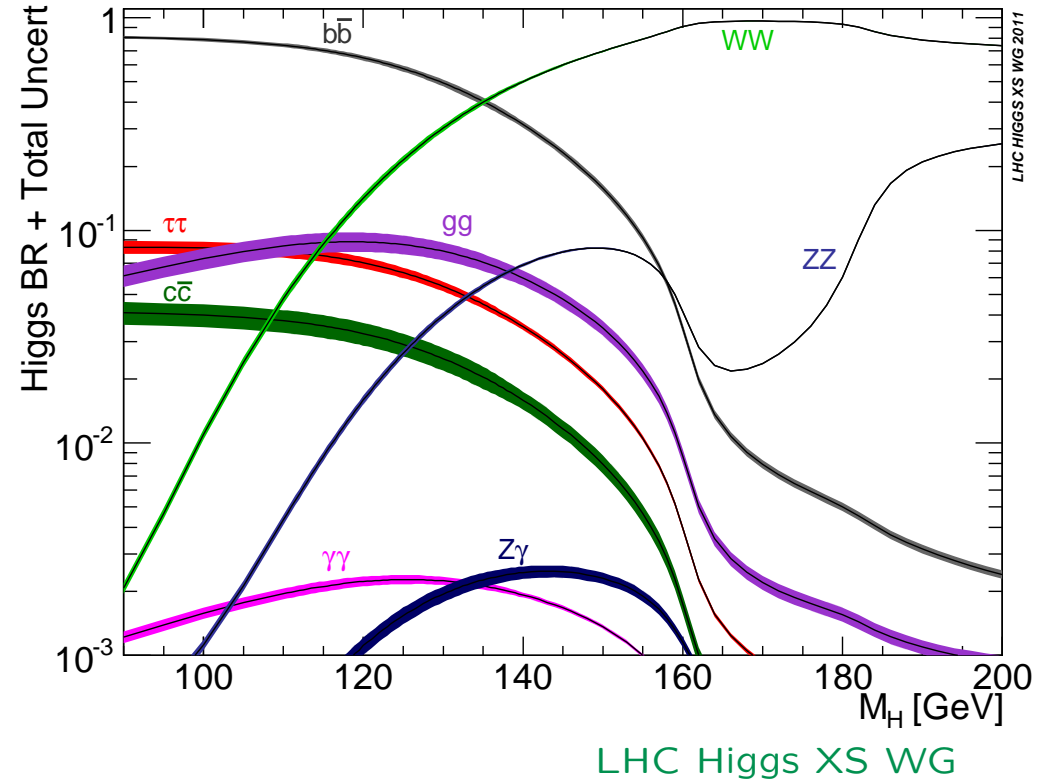
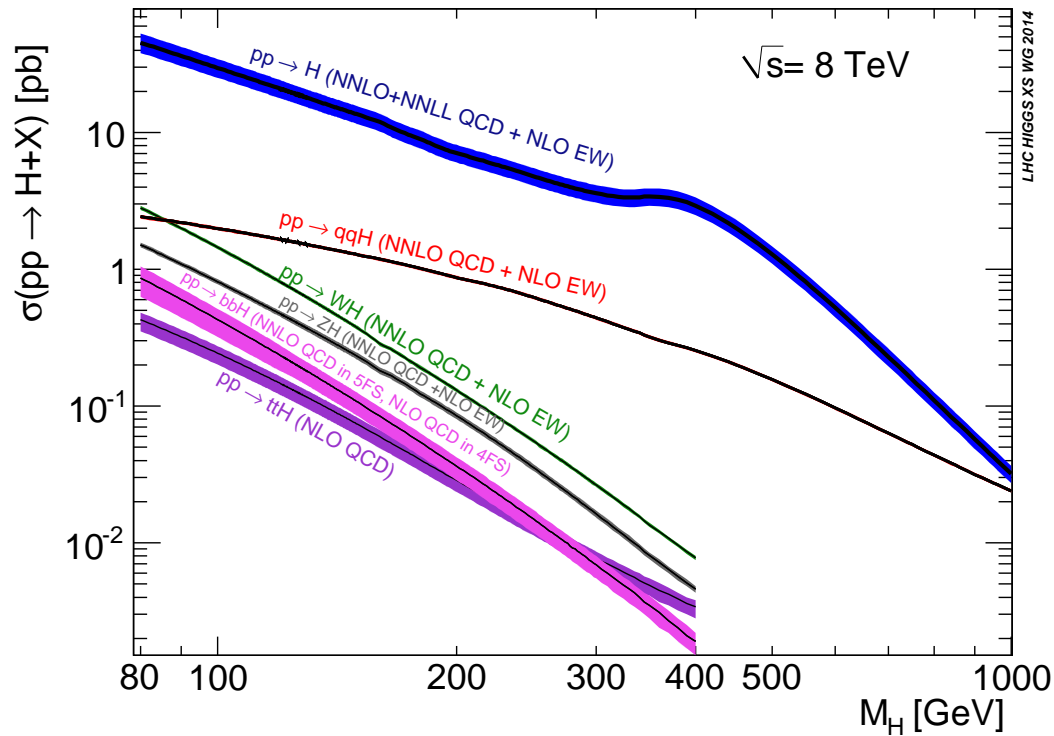
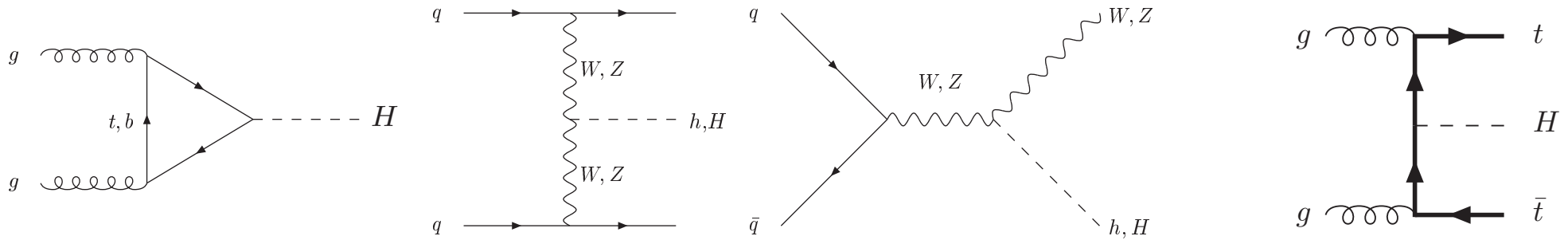
*PARAMETRICALLY ENHANCED  
CORRECTIONS IN SUPERSYMMETRY :  $\Delta_b$*

Michael Spira (PSI)

- I Introduction
- II  $\Delta_b$  Corrections
- III Higgs Production
- IV Conclusions

# I INTRODUCTION

## (i) Standard Model



- Discovery: LHC [Tevatron]

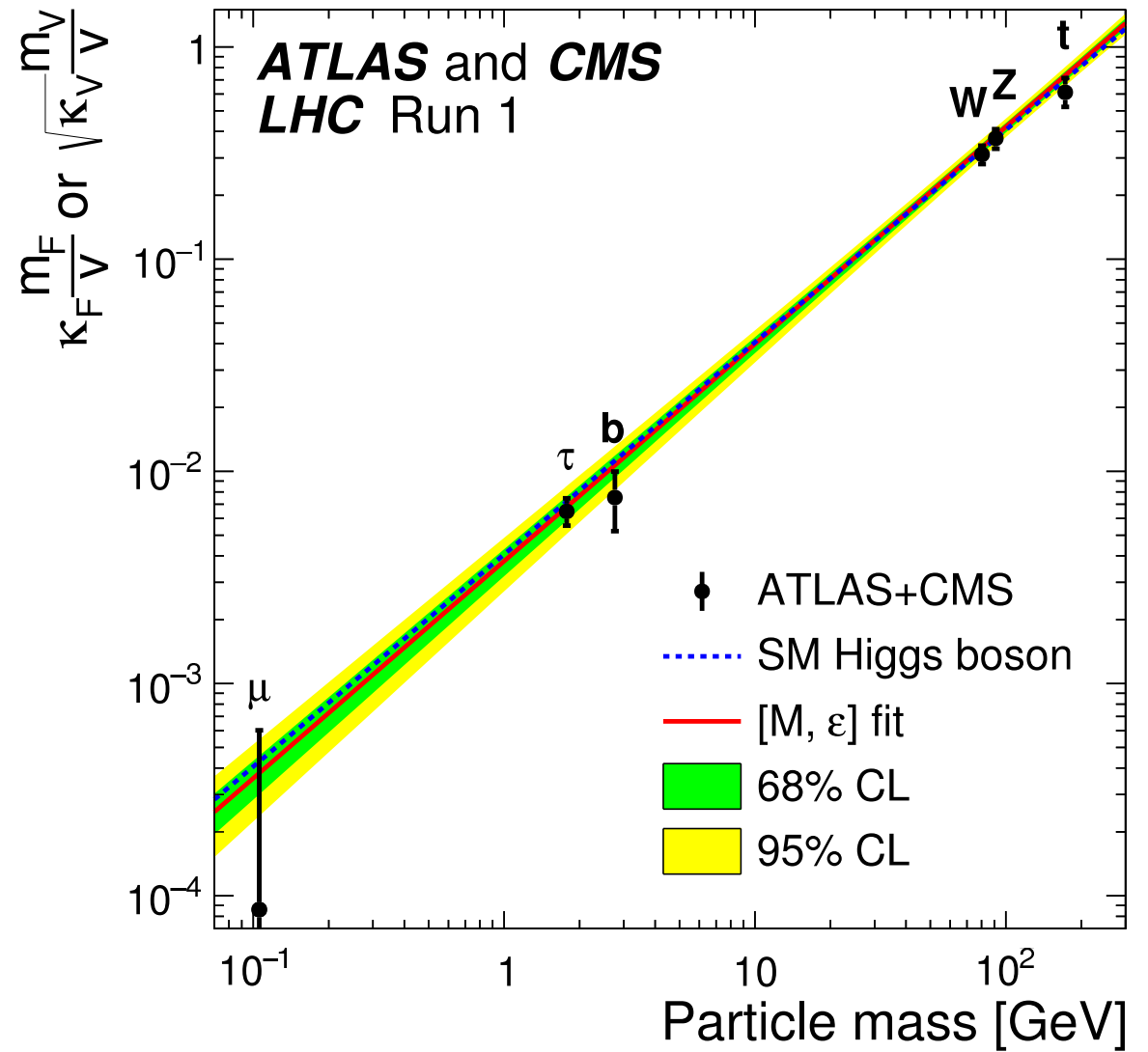
→ Higgs mass

couplings

spin

$CP$

$\lambda ?$



## (ii) MSSM

• 2 Higgs doublets  $\xrightarrow{\text{ESB}}$  5 Higgs bosons:  $h, H, A, H^\pm$

• LO: 2 input parameters:  $M_A, \text{tg}\beta = \frac{v_2}{v_1}$

• radiative corrections  $\propto m_t^4 \log \frac{m_{\tilde{t}_1} m_{\tilde{t}_2}}{m_t^2} \rightarrow \boxed{M_h \lesssim 135 \text{ GeV}}$

Haber  
Carena,...  
Heinemeyer,...  
Zhang  
Slavich,...  
...

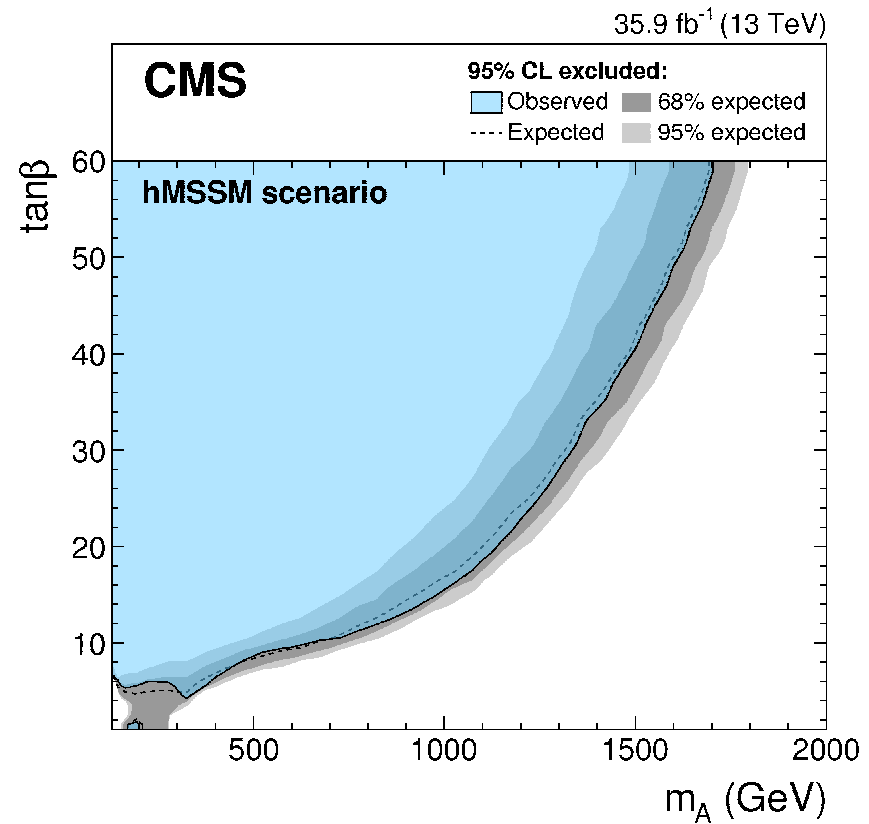
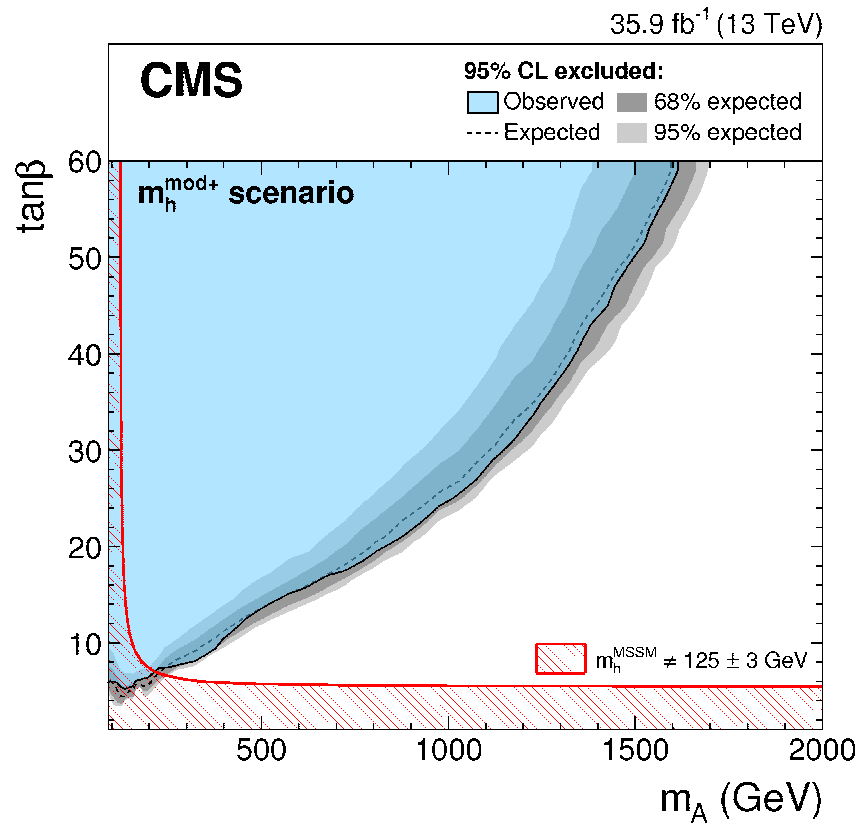
• Yukawa couplings:  $\text{tg}\beta \uparrow \Rightarrow g_u^\phi \downarrow \quad g_d^\phi \uparrow \quad g_V^\phi \downarrow$

• LHC:  $gg \rightarrow \phi$  dominant for  $\text{tg}\beta \lesssim 10$   
 $gg \rightarrow \phi b\bar{b}$  dominant for  $\text{tg}\beta \gtrsim 10$

$$gg \rightarrow b\bar{b}\phi^0, \quad gg \rightarrow \phi^0$$

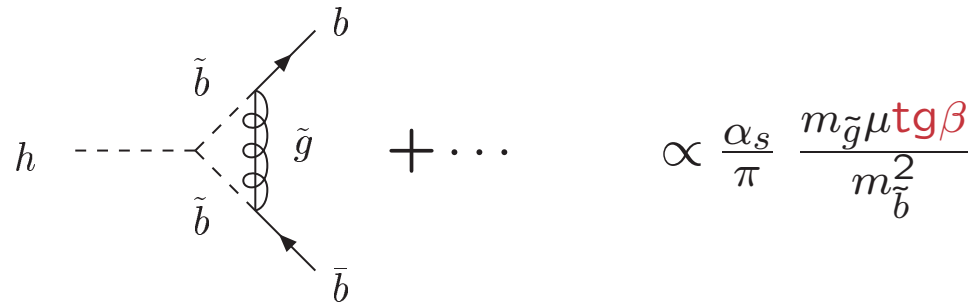


$$\phi^0 \rightarrow \tau^+\tau^-$$

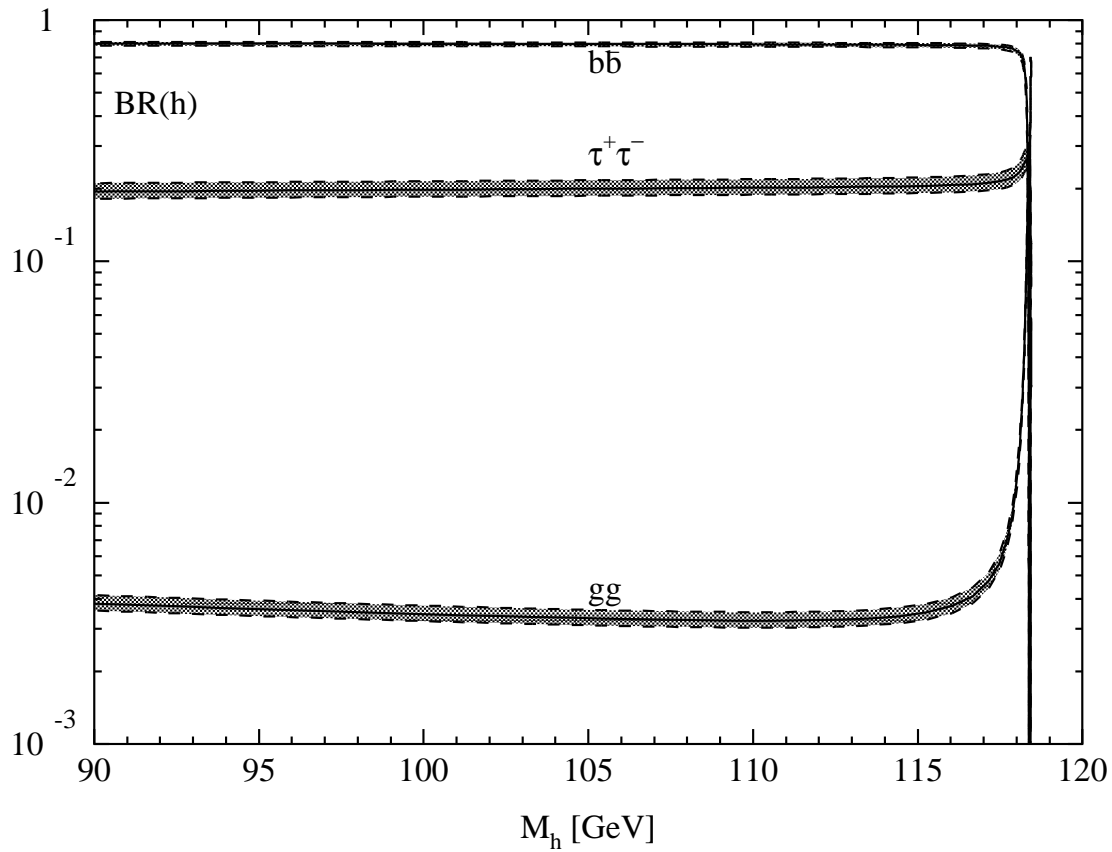


ATLAS: similar results

- large SUSY-QCD corrections to  $\phi^0 \rightarrow b\bar{b}$



Hall, ...  
 Carena, ...  
 Nierste, ...  
 Guasch, ...  
 etc.



Guasch, Häfliger, S.

## II $\Delta_b$ CORRECTIONS

### SUSY-QCD Corrections to $b\bar{b}\phi^0$

$[\Delta \lesssim 1\%]$

$$\begin{aligned} \mathcal{L}_{eff} &= -\lambda_b \bar{b}_R \left[ \phi_1^0 + \frac{\Delta_b}{\text{tg}\beta} \phi_2^{0*} \right] b_L + h.c. \quad \text{valid to all orders in } \Delta_b \\ &= -m_b \bar{b} \left[ 1 + i\gamma_5 \frac{G^0}{v} \right] b - \frac{m_b/v}{1 + \Delta_b} \bar{b} \left[ g_b^h \left( 1 - \frac{\Delta_b}{\text{tg}\alpha \text{tg}\beta} \right) h \right. \\ &\quad \left. + g_b^H \left( 1 + \Delta_b \frac{\text{tg}\alpha}{\text{tg}\beta} \right) H - g_b^A \left( 1 - \frac{\Delta_b}{\text{tg}^2\beta} \right) i\gamma_5 A \right] b \end{aligned}$$

$$\Delta_b = \Delta_b^{QCD(1)} + \Delta_b^{elw(1)}$$

$$\Delta_b^{QCD(1)} = \frac{2}{3} \frac{\alpha_s(\mu_R)}{\pi} M_{\tilde{g}} \mu \text{tg}\beta I(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, M_{\tilde{g}}^2)$$

$$\Delta_b^{elw(1)} = \frac{\lambda_t^2(\mu_R)}{(4\pi)^2} \mu A_t \text{tg}\beta I(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2, \mu^2)$$

$$I(a, b, c) = -\frac{ab \log \frac{a}{b} + bc \log \frac{b}{c} + ca \log \frac{c}{a}}{(a-b)(b-c)(c-a)}$$

Carena, Garcia, Nierste, Wagner  
Guasch, Häfliger, S.

$\Rightarrow$  resummed Yukawa couplings  $\tilde{g}_b^\Phi$

small  $\alpha_{eff}$  scenario [modified]

$$\text{tg}\beta = 30$$

$$M_{\tilde{Q}} = 800 \text{ GeV}$$

$$M_{\tilde{g}} = 1000 \text{ GeV} \quad \leftarrow$$

$$M_2 = 500 \text{ GeV}$$

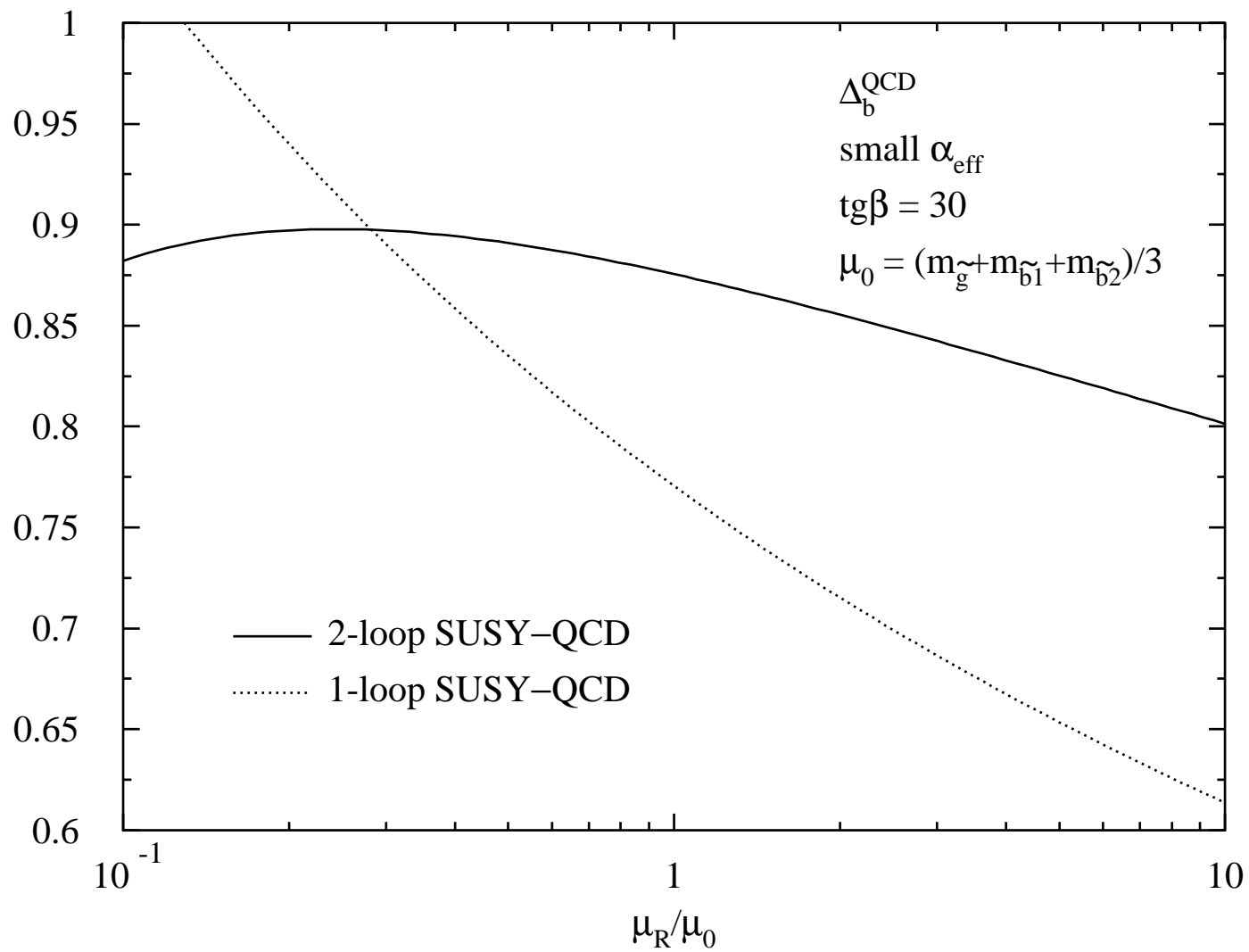
$$A_b = A_t = -1.133 \text{ TeV}$$

$$\mu = 2 \text{ TeV}$$

$$m_{\tilde{t}_1} = 679 \text{ GeV} \quad m_{\tilde{t}_2} = 935 \text{ GeV}$$

$$m_{\tilde{b}_1} = 601 \text{ GeV} \quad m_{\tilde{b}_2} = 961 \text{ GeV}$$

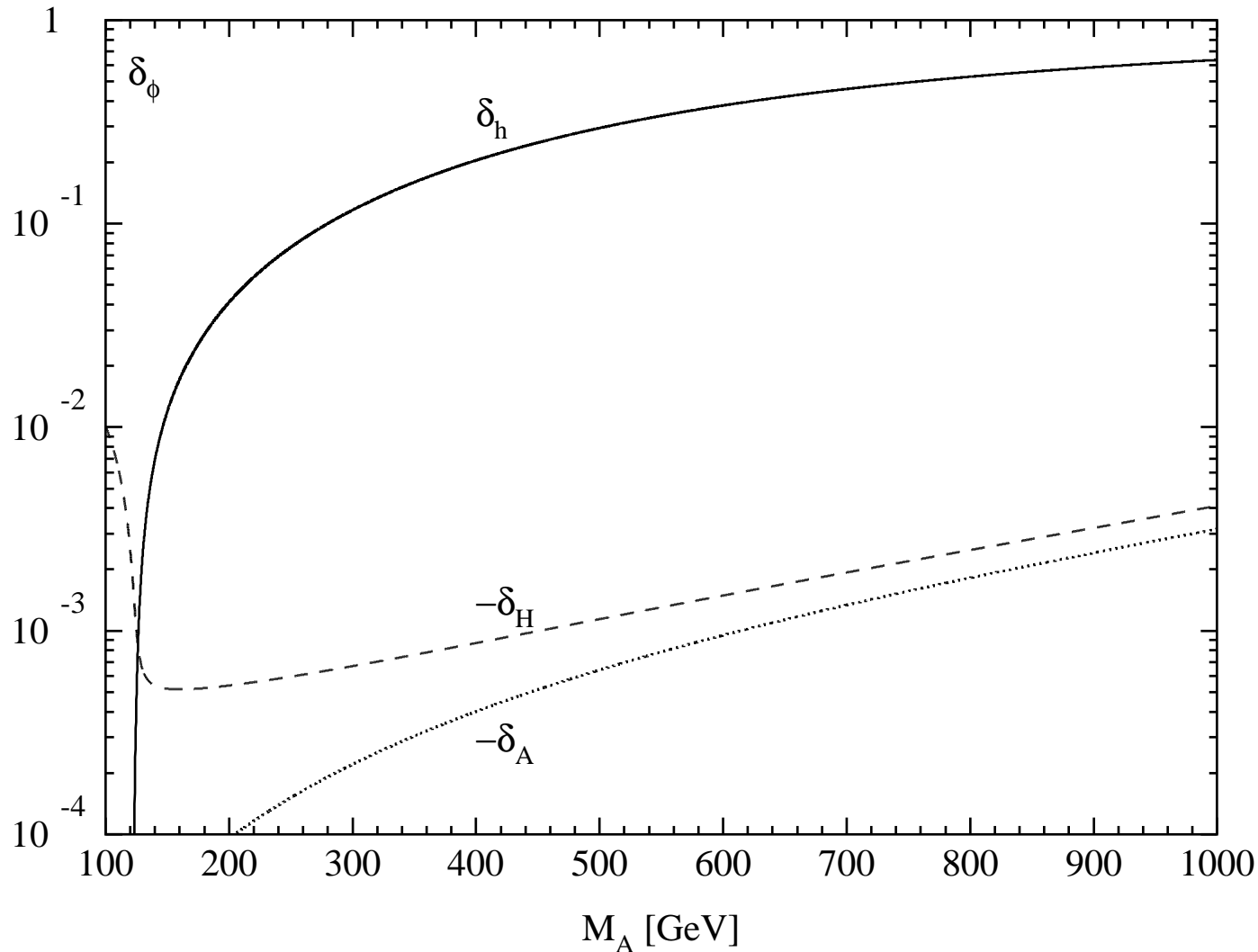




Noth, S.  
 (Mihaila, Reisser)

$$\Gamma[\Phi \rightarrow b\bar{b}] = \frac{3G_F M_\Phi \bar{m}_b^2(M_\Phi)}{4\sqrt{2}\pi} \Delta_{\text{QCD}} \tilde{g}_b^\Phi \left[ \tilde{g}_b^\Phi + g_b^\Phi \delta_{rem} \right]$$

$$M_A^2 \gg M_Z^2 : \text{tg}\alpha \rightarrow -\frac{1}{\text{tg}\beta} \quad \Rightarrow \quad \tilde{g}_b^h \rightarrow \frac{1}{1 + \Delta_b} \left( 1 - \frac{\Delta_b}{\text{tg}\alpha \text{tg}\beta} \right) \rightarrow 1$$



$$\delta_\phi = \frac{\delta_{rem}}{\delta_{SQCD}}$$

- extension to  $A_b$  terms:

$$\mathcal{L}_{eff} = -\lambda_b^0 \overline{b_R} \left[ (1 + \Delta_{b,1}) \phi_1^0 + \frac{\Delta_{b,2}}{\text{tg}\beta} \phi_2^{0*} \right] b_L + h.c.$$

$$\mathcal{L}_{eff} = -\lambda_b \overline{b_R} \left[ \phi_1^0 + \frac{\Delta_b}{\text{tg}\beta} \phi_2^{0*} \right] b_L + h.c.$$

$$\Rightarrow \Delta_b = \frac{\Delta_{b,2}}{1 + \Delta_{b,1}} \quad \text{Guasch, Häfliger, S. Ghezzi, Glaus, Müller, Schmidt, S.}$$

$$\Delta_{b,1} = -\frac{2}{3} \frac{\alpha_s(\mu_R)}{\pi} M_{\tilde{g}} A_b I(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, M_{\tilde{g}}^2) \rightarrow \text{NNLO}$$

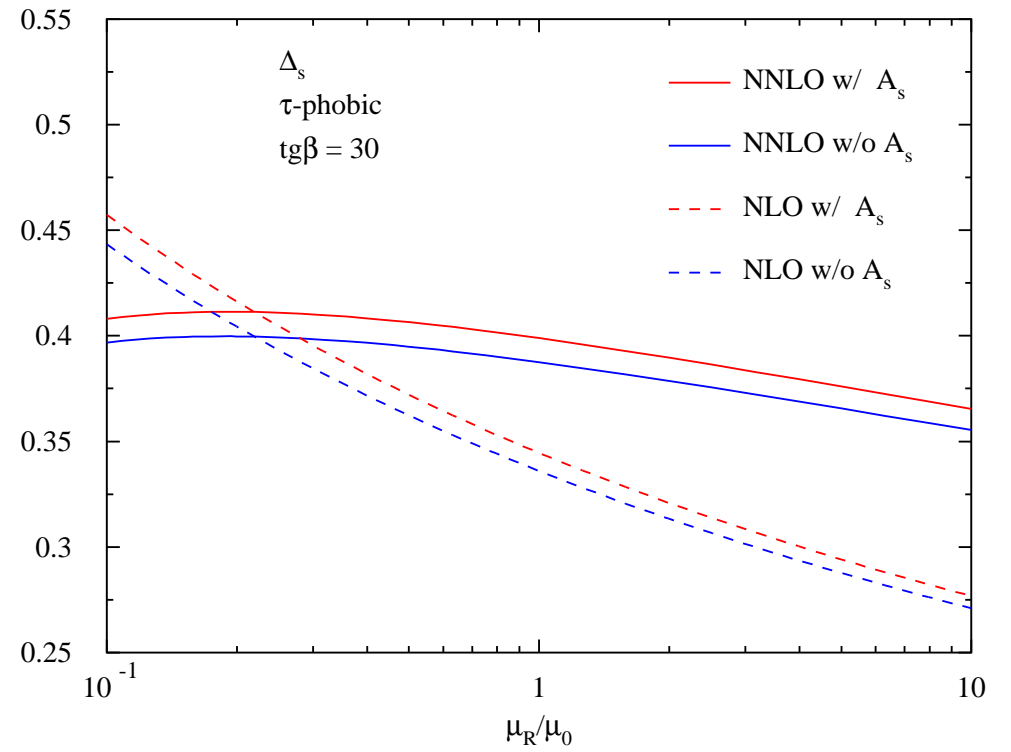
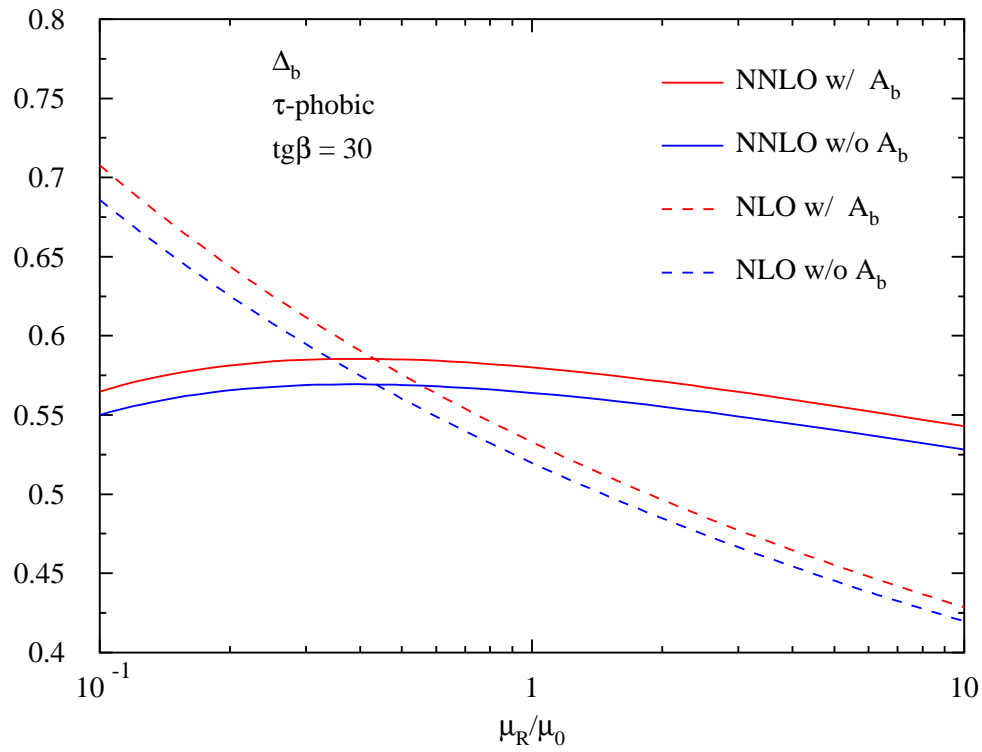
- strange Yukawa couplings:

$$\Delta_{s,1} = -\frac{2}{3} \frac{\alpha_s(\mu_R)}{\pi} M_{\tilde{g}} A_s I(m_{\tilde{s}_1}^2, m_{\tilde{s}_2}^2, M_{\tilde{g}}^2)$$

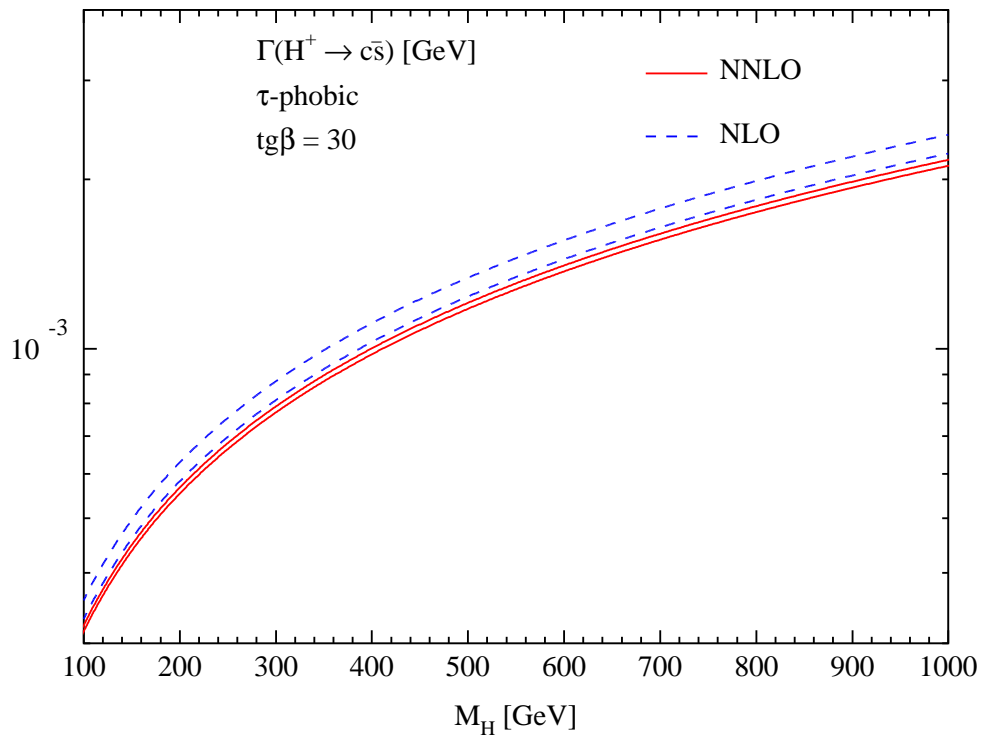
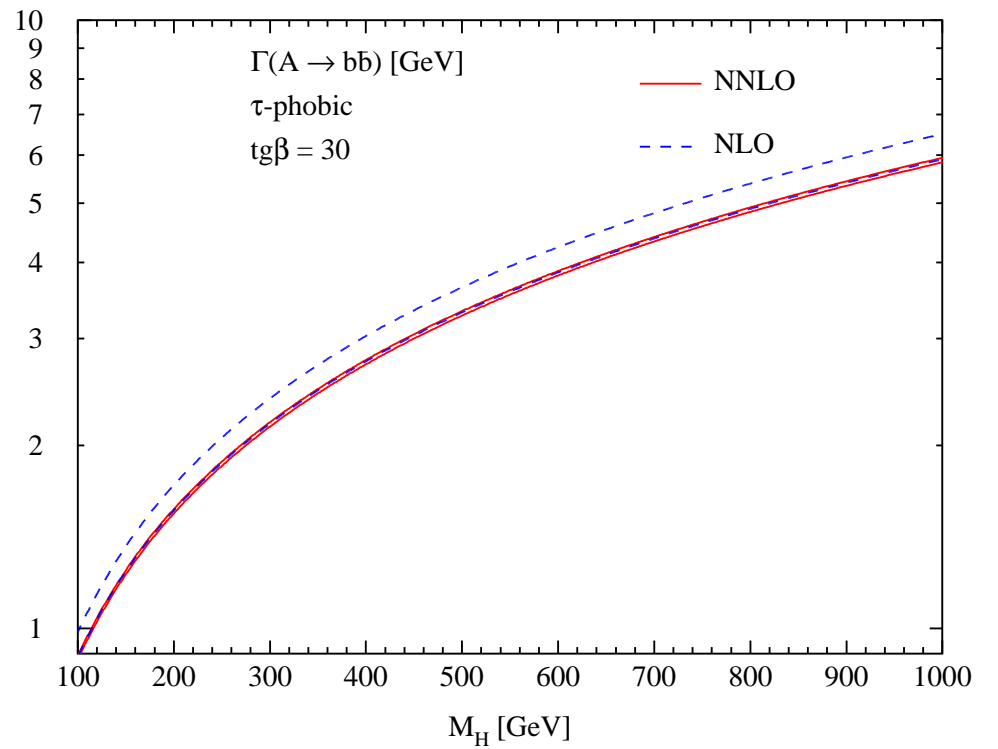
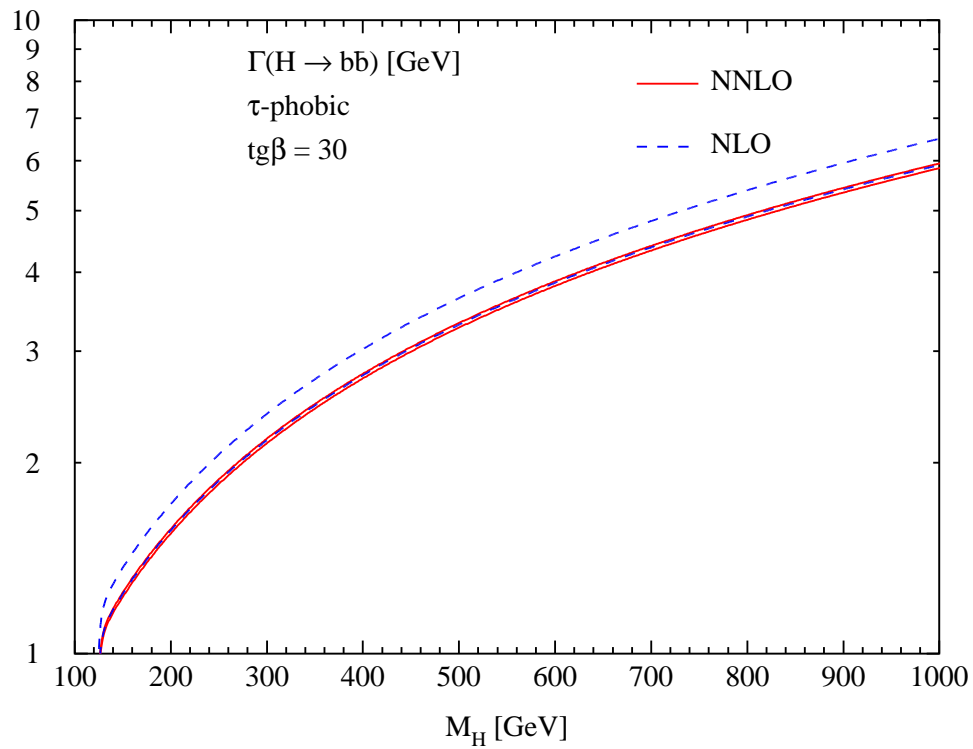
$$\Delta_{s,2} = \frac{2}{3} \frac{\alpha_s(\mu_R)}{\pi} M_{\tilde{g}} \mu \text{tg}\beta I(m_{\tilde{s}_1}^2, m_{\tilde{s}_2}^2, M_{\tilde{g}}^2)$$

$$\Delta_s = \frac{\Delta_{s,2}}{1 + \Delta_{s,1}} \rightarrow \text{NNLO}$$

Ghezzi, Glaus, Müller, Schmidt, S.



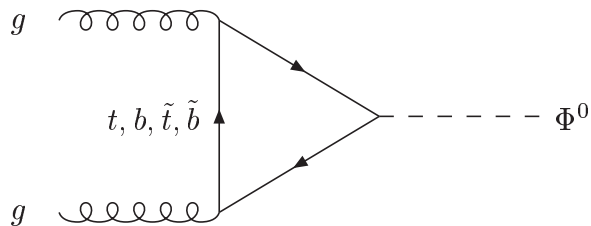
Ghezzi, Glaus, Müller, Schmidt, S.



Ghezzi, Glaus, Müller, Schmidt, S.

# III HIGGS BOSON PRODUCTION

## (i) $gg \rightarrow h/H/A$



Georgi,...

Gamberini,...

S., Djouadi, Graudenz, Zerwas

Dawson, Kauffman

- NLO QCD corrections:  $\sim 10 \dots 100\%$

- NNLO calculated for  $m_t \gg M_\phi \Rightarrow$  further increase by 20–30%

[top mass effects small in SM]

Harlander, Kilgore

Anastasiou, Melnikov

Ravindran, Smith, van Neerven

Marzani, Ball, Del Duca, Forte, Vicini

Harlander, Ozeren

Pak, Rogal, Steinhauser

- N<sup>3</sup>LO for  $m_t \gg M_\phi \Rightarrow$  scale stabilization

scale dependence:  $\Delta \lesssim 5\%$

Moch, Vogt

Ravindran

de Florian, Mazzitelli, Moch, Vogt

Anastasiou, Duhr, Dulat, Furlan, Gehrmann, Herzog, Mistlberger

Ball, Bonvini, Forte, Marzani, Ridolfi

- N<sup>3</sup>LL soft gluon resummation:  $\lesssim 2\%$

Catani, de Florian, Grazzini, Nason  
Ravindran  
Ahrens, Becher, Neubert, Yang  
Ball, Bonvini, Forte, Marzani, Ridolfi  
Bonvini, Marzani  
Schmidt, S.

- SM + 2HDM elw. corrections:  $\sim 5\%$

Aglietti, . . .  
Degrassi, Maltoni  
Actis, Passarino, Sturm, Uccirati  
Jenniches, Sturm, Uccirati

- QCD corrections to squark loops: 10–100%

Mühlleitner, S.  
Bonciani, Degrassi, Vicini

- impl. of  $gg \rightarrow \phi$  in POWHEG including mass effects @ NLO  
(QCD also valid for 2HDM and other Higgs extensions)

Bagnaschi, Degrassi, Slavich, Vicini

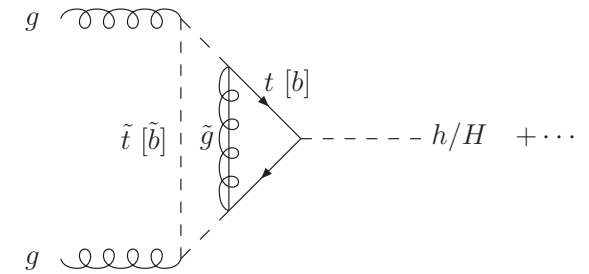
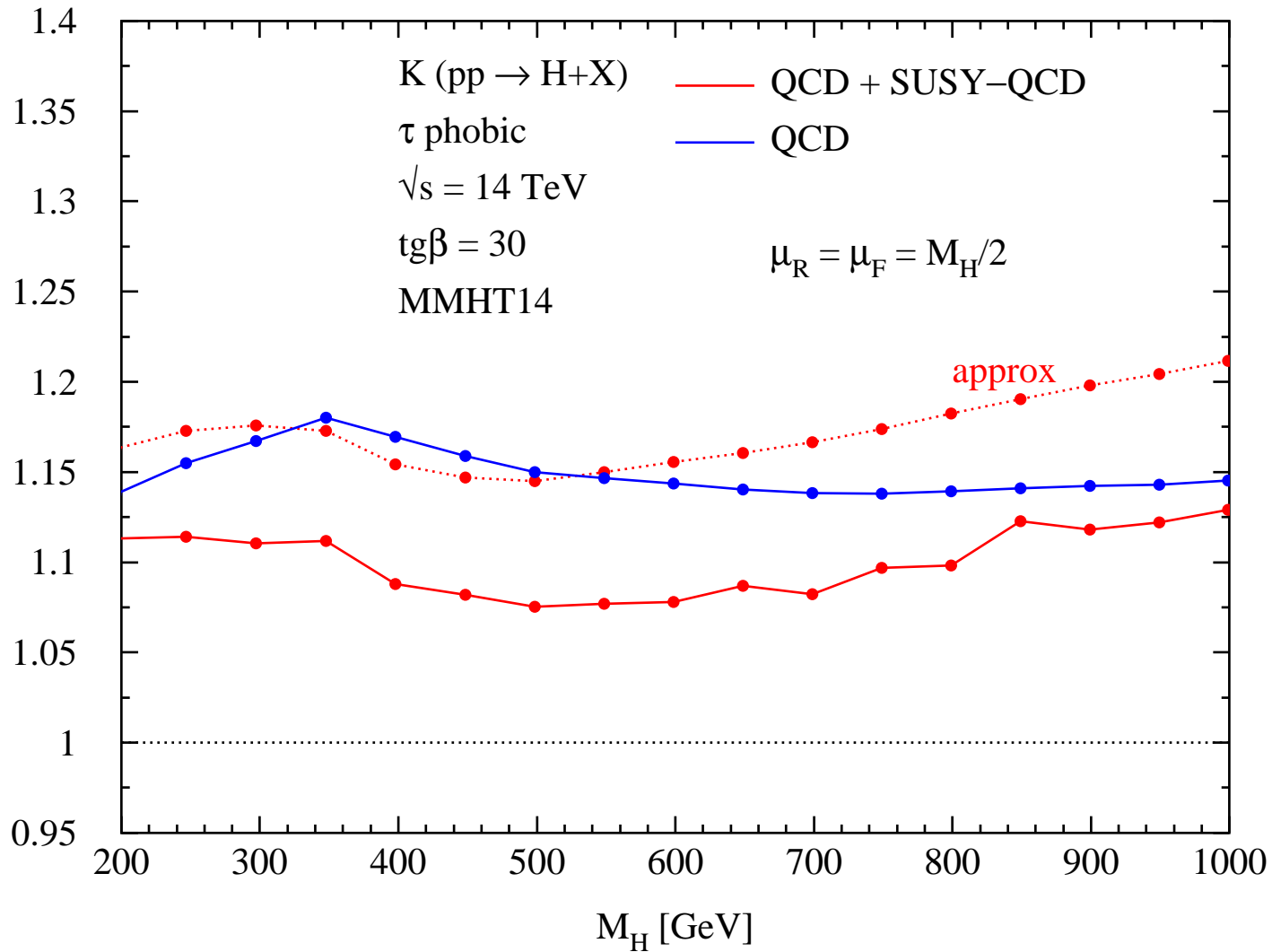
- SUSY-elw. corrections unknown

- genuine SUSY–QCD corrections: 10–100%  
[ $\leftarrow \Delta_b$  @ large  $\tan\beta$ ]

Harlander, Steinhauser, Hofmann  
Degrassi, Slavich  
Anastasiou, Beerli, Daleo  
Mühlleitner, Rzehak, S.

$$\sigma(gg \rightarrow \Phi) = \sigma_{LO}(g_t^\Phi, \tilde{g}_b^\Phi) \left[ 1 + \delta_{QCD} + \delta_{SQCD} \right]$$

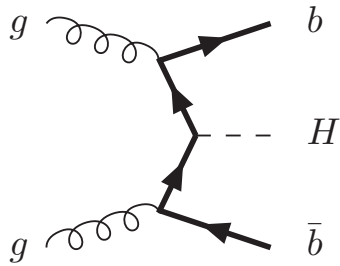
PRELIMINARY



Fritz, Mühlleitner, Rzehak, S.

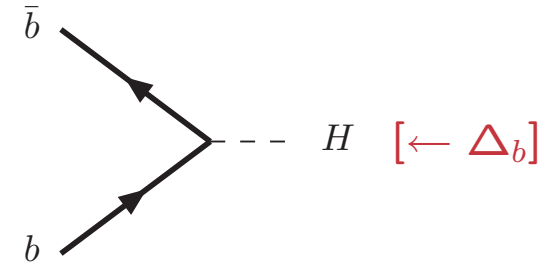


## (ii) $b\bar{b}$ +Higgs production



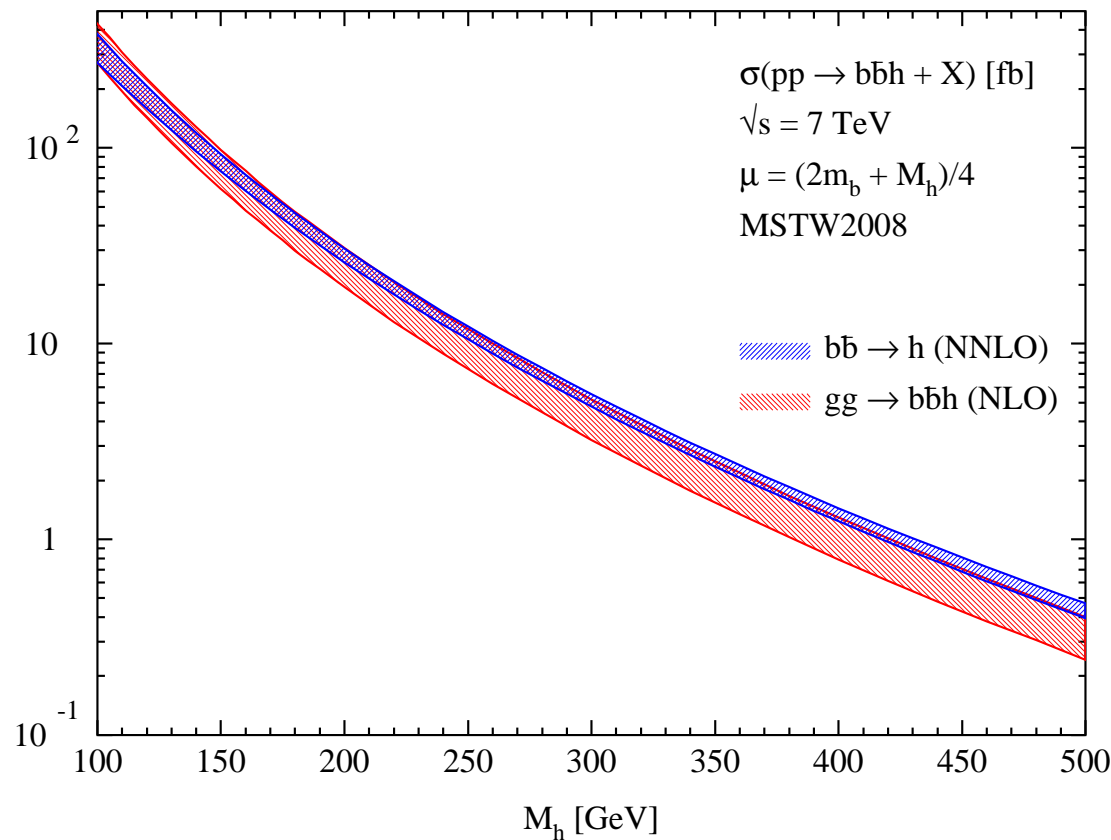
NLO

exact  $g \rightarrow b\bar{b}$  splitting & mass/off-shell effects  
no resummation of  $\log M_H^2/m_b^2$  terms



NNLO

massless/on-shell  $b$ 's, no  $p_{Tb}$   
resummation of  $\log M_H^2/m_b^2$  terms



Santander matching:

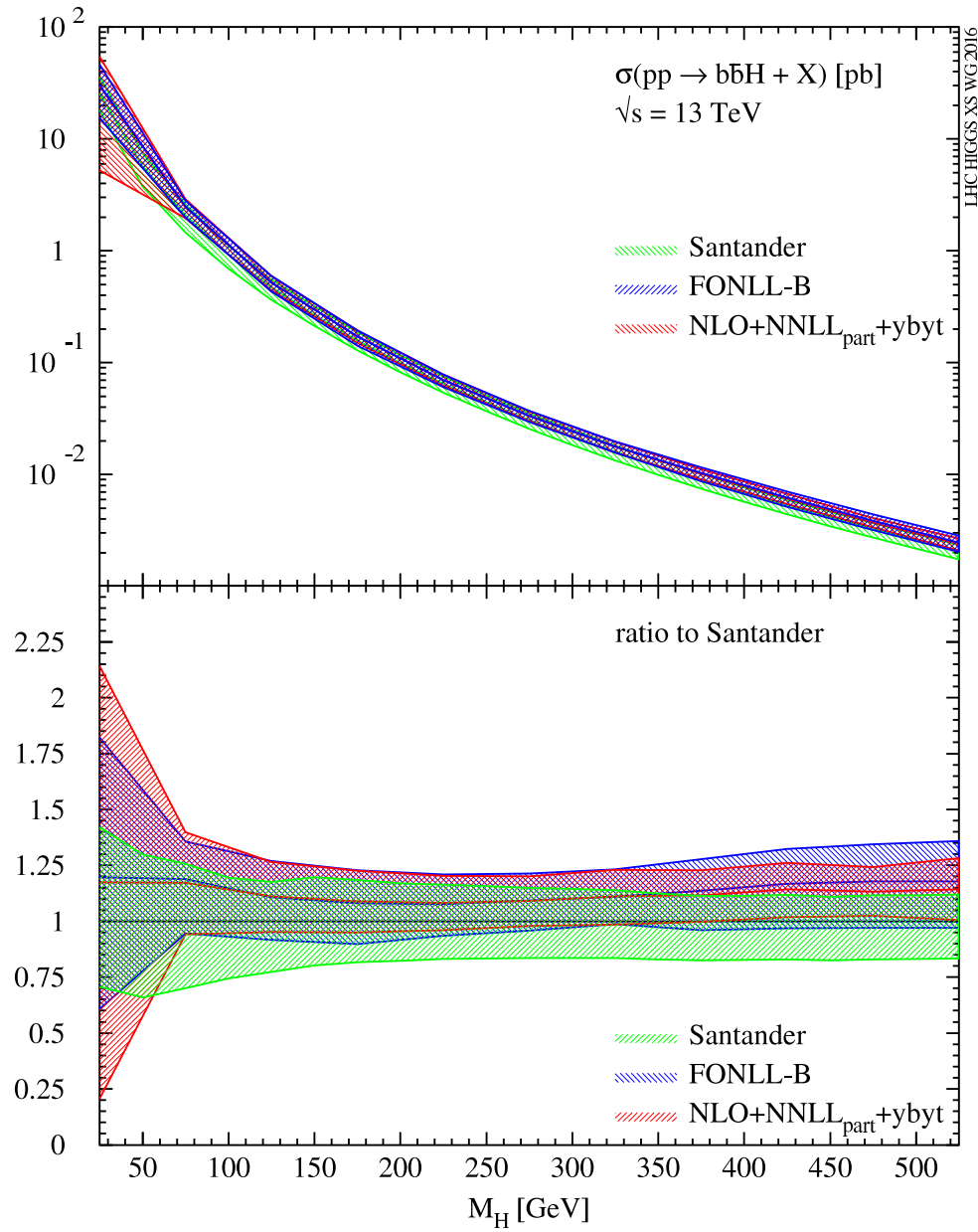
$$\sigma = \frac{\sigma^{4FS} + w\sigma^{5FS}}{1 + w}$$

$$w = \log \frac{M_H}{m_b} - 2$$

Harlander, Krämer, Schumacher

Dittmaier, Krämer, S.  
Dawson, Jackson, Reina, Wackerath  
Harlander, Kilgore

# matching



Bonvini, Papanastasiou, Tackmann

Forte, Napoletano, Ubiali

	$M_A$	$M_H$ [GeV]	$\delta_{QCD}^A$	$\delta_{SUSY}^A$	$\delta_{SUSYrem}^A$	$\delta_{QCD}^H$	$\delta_{SUSY}^H$	$\delta_{SUSYrem}^H$
7 TeV	100	113.9	0.23	-0.30	$0.4 \times 10^{-4}$	0.27	-0.38	$0.3 \times 10^{-4}$
	200	200	0.38	-0.30	$2.9 \times 10^{-4}$	0.39	-0.30	$5.8 \times 10^{-4}$
	300	300	0.46	-0.30	$6.7 \times 10^{-4}$	0.47	-0.30	$9.3 \times 10^{-4}$
	400	400	0.53	-0.30	$1.3 \times 10^{-3}$	0.53	-0.30	$1.5 \times 10^{-3}$
	500	500	0.57	-0.30	$2.0 \times 10^{-3}$	0.59	-0.30	$2.2 \times 10^{-3}$
14 TeV 14 TeV	100	113.9	0.14	-0.30	$0.4 \times 10^{-4}$	0.17	-0.38	$0.5 \times 10^{-4}$
	200	200	0.28	-0.30	$2.7 \times 10^{-4}$	0.29	-0.30	$5.7 \times 10^{-4}$
	300	300	0.37	-0.30	$6.5 \times 10^{-4}$	0.39	-0.30	$9.3 \times 10^{-4}$
	300	300	0.37	-0.30	$6.5 \times 10^{-4}$	0.39	-0.30	$9.3 \times 10^{-4}$
	400	400	0.45	-0.30	$1.2 \times 10^{-3}$	0.45	-0.30	$1.5 \times 10^{-3}$
	500	500	0.50	-0.30	$2.1 \times 10^{-3}$	0.49	-0.30	$2.3 \times 10^{-3}$

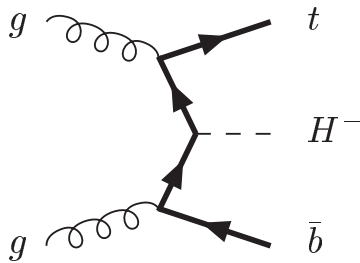
	$\text{tg}\beta$	$M_A$	$M_H$ [GeV]	$\delta_{SUSY}^A$	$\delta_{SUSYrem}^A$	$\delta_{SUSY}^H$	$\delta_{SUSYrem}^H$
7 TeV	3	200	209.7	-0.04	$2.1 \times 10^{-4}$	-0.04	$5.7 \times 10^{-4}$
	5	200	204.0	-0.06	$2.4 \times 10^{-4}$	-0.06	$5.3 \times 10^{-4}$
	7	200	202.1	-0.08	$2.5 \times 10^{-4}$	-0.09	$3.9 \times 10^{-4}$
	10	200	200.9	-0.12	$2.5 \times 10^{-4}$	-0.12	$3.8 \times 10^{-4}$
	20	200	200.1	-0.21	$2.6 \times 10^{-4}$	-0.21	$4.4 \times 10^{-4}$
	30	200	200.0	-0.30	$2.9 \times 10^{-4}$	-0.30	$5.8 \times 10^{-4}$
14 TeV	3	200	209.7	-0.04	$2.0 \times 10^{-4}$	-0.04	$7.2 \times 10^{-4}$
	5	200	204.0	-0.06	$2.2 \times 10^{-4}$	-0.06	$5.0 \times 10^{-4}$
	7	200	202.1	-0.08	$2.4 \times 10^{-4}$	-0.09	$4.4 \times 10^{-4}$
	10	200	200.9	-0.12	$2.5 \times 10^{-4}$	-0.12	$4.1 \times 10^{-4}$
	20	200	200.1	-0.21	$2.7 \times 10^{-4}$	-0.21	$4.4 \times 10^{-4}$
	30	200	200.0	-0.30	$2.7 \times 10^{-4}$	-0.30	$5.7 \times 10^{-4}$

SPS1b

(iii)  $pp \rightarrow t\bar{b}H^- + X$

- $M_{H^\pm} < m_t - m_b$ :  $\sigma_{t\bar{b}H^-} = \sigma_{t\bar{t}} \times BR(\bar{t} \rightarrow \bar{b}H^-)$
- $M_{H^\pm} \sim m_t - m_b$ : new NLO calculation
- $M_{H^\pm} > m_t - m_b$ :

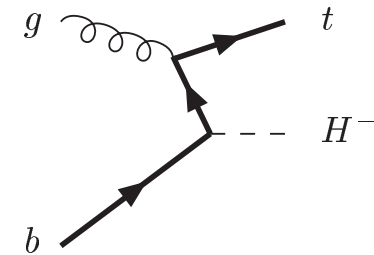
Degrande, Frederix, Wiesemann, Zaro



NLO

exact  $g \rightarrow b\bar{b}$  splitting & mass/off-shell effects  
no resummation of  $\log M_{H^\pm}^2/m_b^2$  terms

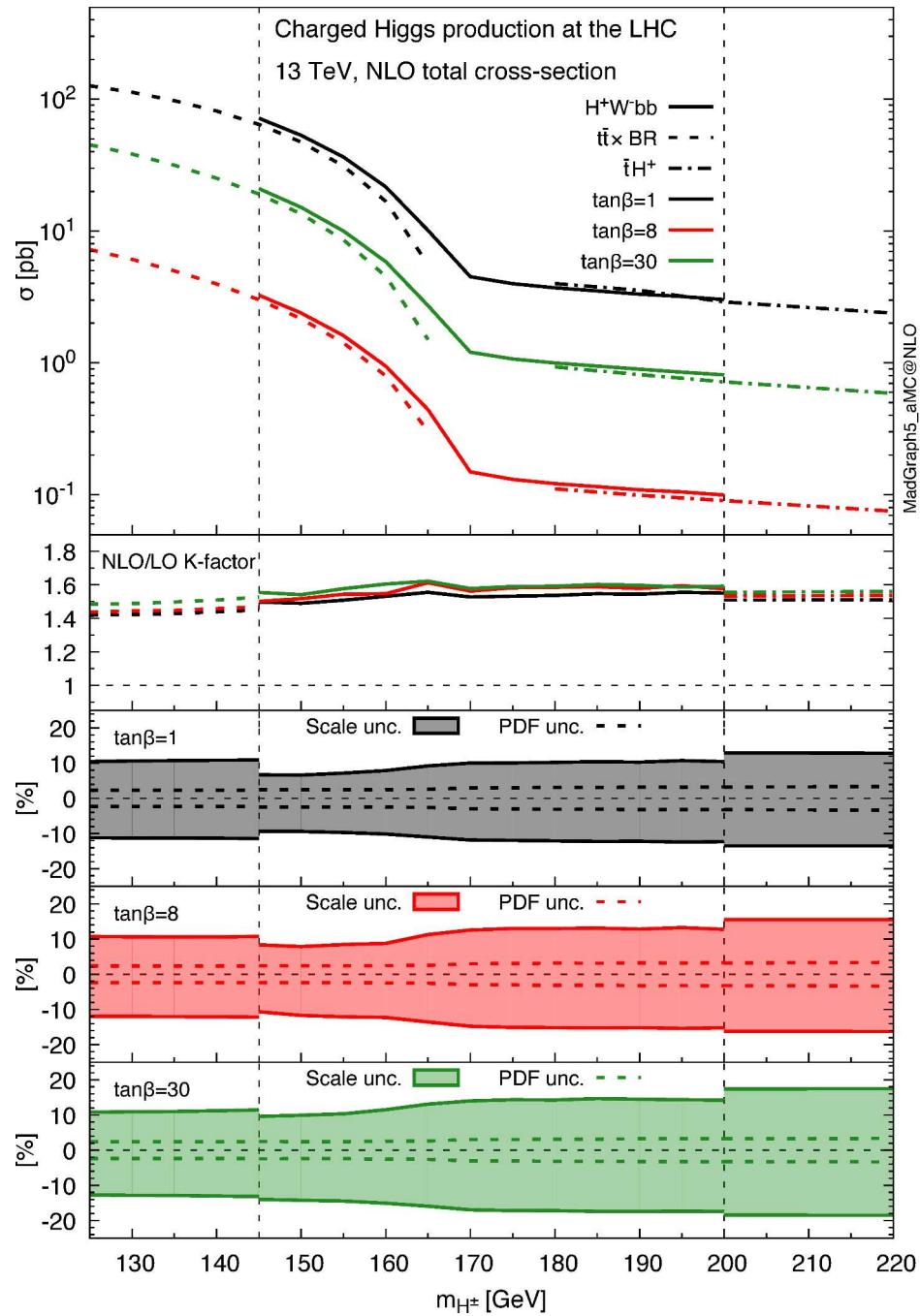
→ Santander matching



NLO

massless/on-shell  $b$ 's, no  $p_{Tb}$   
resummation of  $\log M_{H^\pm}^2/m_b^2$  terms

Dittmaier, Krämer, S., Walser  
Plehn  
Flechl, Klees, Krämer, Spira, Ubiali



Degrade, Frederix, Wiesemann, Zaro

- charged Higgs:  $\tilde{g}_b^{H^\pm} = \frac{\text{tg}\beta}{1 + \Delta_b} \left( 1 - \frac{\Delta_b}{\text{tg}^2\beta} \right)$

$$\sigma_{NLO} = \sigma_{LO} \Big|_{g_b^{H^\pm} \rightarrow \tilde{g}_b^{H^\pm}} \times \left\{ 1 + \delta_{QCD} + \delta_{SQCD}^{rem} \right\}$$

$\text{tg}\beta$	$\delta_{SUSY}^{rem} [\%]$
3	-5.7%
5	-7.9%
10	-4.8%
30	-0.13%

$\leftarrow g_t^{H^\pm}$

## IV CONCLUSIONS

- genuine SUSY–QCD corrections large @ large  $\tan\beta \rightarrow \Delta_b$
- small remainders beyond  $\Delta_b$  approximation in most cases
- analogous results for strange Yukawa coupling  $\rightarrow \Delta_s$

*BACKUP SLIDES*